# **High-Performance Computing with GPUs**

**Project: Accelerated MNIST Classification** 

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**Link to Github Repository** 

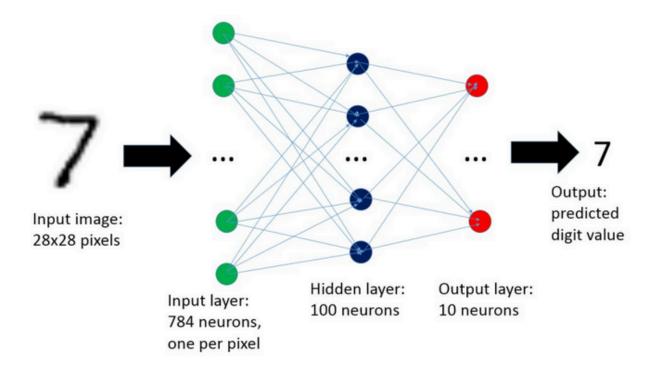
#### Introduction

MNIST digit classification, involving 28x28 grayscale images of handwritten digits (0–9), is a standard benchmark in machine learning. This project applies CUDA GPU programming to speed up the training and inference of a neural network on MNIST, showcasing how HPC techniques enhance computational performance in real-world AI tasks.

## Problem

The neural network takes each image as a flattened array of pixel intensity values and passes it through multiple layers of interconnected nodes. Through repeated exposure to training data, the network adjusts its configurations. Over time, the model "learns" to recognize the underlying patterns in the pixel data that correspond to each digit.

A demonstration of this is given below.



## Implementation Versions

V1: Baseline

**Neural Network Structure:** 

- Input layer: 784 nodes (28×28 pixels) each input.
- **Hidden layer**: 128 nodes with **ReLU** activation function.
- **Output layer**: 10 nodes with **Softmax** (representing digits 0–9).

Forward propagation multiplies input by weights  $\rightarrow$  adds bias  $\rightarrow$  applies ReLU  $\rightarrow$  feeds to output layer  $\rightarrow$  applies Softmax.

```
hidden = ReLU(W1 * input + b1)
output = Softmax(W2 * hidden + b2)
```

Backward propagation computes gradients by:

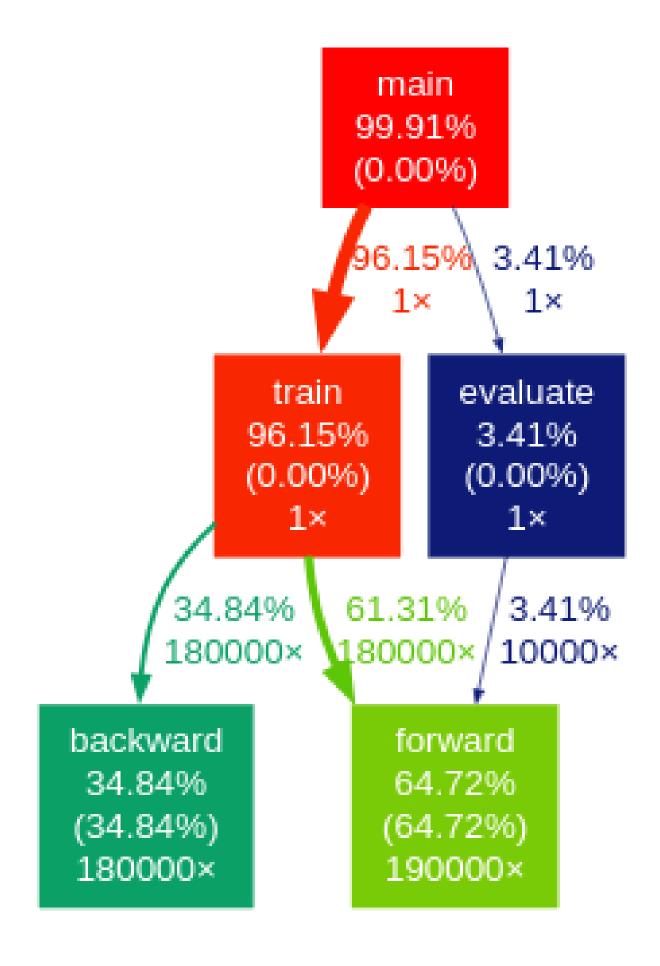
- Output error: output target
- Hidden error via chain rule and ReLU derivative

Updates weights and biases using **gradient descent**:

```
W2 -= LR * d_output * hidden^T
W1 -= LR * d_hidden * input^T
```

The training loop repeats the process for 3 epochs on all 60,000 training images, measures loss (cross-entropy) and accuracy per epoch.

The serial implementation takes an average of 77.101 second training time, with most of the computation focussed on forward and backward propagation functions.



### V2: Naive GPU Implementation

This implementation introduces CUDA. By integrating CUDA, we shift from the serial CPU-based implementation to a parallelized approach that can take advantage of the thousands of threads available on a GPU.

The serial implementation helped identify computational bottlenecks. These are now targeted for parallel execution to improve performance.

#### **CUDA** kernels

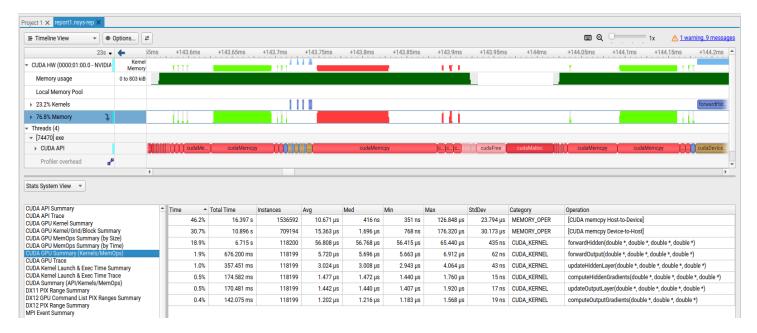
The forward propagation functions, (forwardHidden, forwardOutput) and the backward propagation functions (updateOutputLayer, updateHiddenLayer) have been implemented in the form of CUDA kernels.

#### Device-Side Memory Optimization

A key design decision in this version was to keep all weights and biases on the GPU (device memory) throughout training. By allocating them once at the beginning and updating them in-place on the GPU, we reduce memory transfer overhead and maintain consistency in computation.

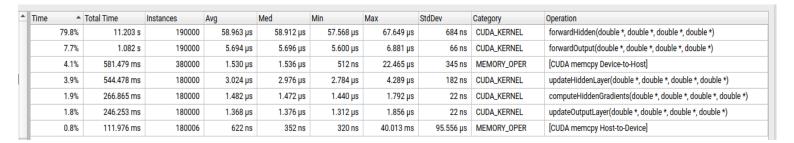
Additionally, the entire dataset is also copied once to the device at the start of training and remains there for the duration of the process. This ensures that we do not need to perform repeated cudaMemcpy() calls for each image, which would otherwise become a major bottleneck.

Mainly, this communicational optimization insight was given to us by using the profiling tool, which showed that most of our time was being spent in copying data to and fro between the device and the host.



**Profiler Results** 

The NVIDIA Nsight Systems Profiling tools gives us accurate measurements of time for each kernel and memory transfer. The optimized version, showing lesser memory transfers is shown below.



The speed-ups comparing every version to V1 (serial) can be found at the end here.

## V3: Optimized GPU Implementation

Since most of the memory transfer time has now been greatly reduced, we will now be aiming to make the kernels faster.

## Launch Configuration

The launch configurations on the naive implementation were set to use 1 block only which for obvious reasons did not yield the best results. We tried various combinations of multiple threads and blocks to see which one yields the best result

(in terms of time for each epoch). As a result of this hit and trial method, We concluded that with these combinations the time consumed was lowest.

```
forwardHidden<<<4, 32>>>
forwardOutput<<<1, 64>>>
computeHiddenGradients<<<16, 4>>>
updateOutputLayer<<<OUTPUT_SIZE, HIDDEN_SIZE>>>
updateHiddenLayer<<<HIDDEN_SIZE, INPUT_SIZE>>>
```

The code was also changed a bit to manage multiple blocks instead of just one.

Shared Memory Usage

To further improve performance, **shared memory** was introduced in performance-critical kernels to reduce redundant global memory access. The forwardHidden and forwardOutput kernels seem to be taking the most amount of time, and therefore we will be aiming to reduce the time it takes by using shared memory.

Once the launch configurations changed, and shared memory was implemented, the following times were noted on the profiler.

*	Time -	Total Time	Instances	Avg	Med	Min	Max	StdDev	Category	Operation	
	69.3%	6.607 s	190000	34.773 µs	32.994 µs	32.194 µs	48.707 µs	2.114 µs	CUDA_KERNEL	forwardHidden(double *, double *, double *, double *)	
	10.8%	1.031 s	190000	5.424 µs	5.152 µs	4.993 µs	6.241 µs	340 ns	CUDA_KERNEL	forwardOutput(double *, double *, double *, double *)	
	6.5%	618.806 ms	380000	1.628 µs	1.600 µs	480 ns	24.001 µs	271 ns	MEMORY_OPER	[CUDA memcpy Device-to-Host]	
	5.4%	519.306 ms	180000	2.885 µs	2.816 µs	2.304 µs	4.320 µs	209 ns	CUDA_KERNEL	updateHiddenLayer(double *, double *, double *, double *)	
	3.8%	358.952 ms	180000	1.994 µs	2.080 µs	1.824 µs	2.369 µs	112 ns	CUDA_KERNEL	computeHiddenGradients(double *, double *, double *, double *)	
	3.0%	286.495 ms	180000	1.591 µs	1.632 µs	1.408 µs	2.176 µs	53 ns	CUDA_KERNEL	updateOutputLayer(double *, double *, double *, double *)	
	1.2%	116.710 ms	180006	648 ns	416 ns	320 ns	39.812 ms	95.095 µs	MEMORY_OPER	[CUDA memcpy Host-to-Device]	

When we compare these times to the ones in the naive implementation, we see that the time is greatly reduced.

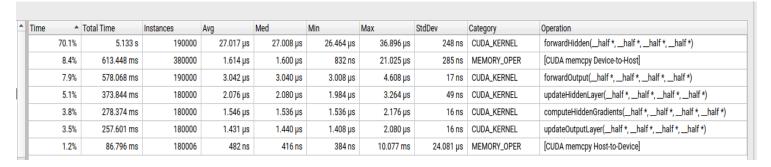
Note: We tried shared memory on the other two functions too but they did not seem to be affecting the performance a lot. Since accessing global memory was not a bottleneck in these kernels, using shared memory gave us little leverage.

Half-Precision (FP16) Data Type Usage

FP16 (half) uses 2 bytes (16 bits) per number instead of 8 bytes which we were previously using. This means for every calculation we are doing ( weights,

activations and gradients), the data is ¼ times smaller in size making the calculations quicker. This helps reduce bottlenecks caused by limited memory bandwidth.

Although we did have concerns about compromising the accuracy/precision of our model's predictions, no significant loss in accuracy was observed. It improved our time greatly.



#### Coalesced Memory Access

Memory being accessed in column-major format seemed to be taking more time, so we changed it and stored it in row-major format. This allowed performance improvement by almost 2 seconds per epoch.

All memory is accessed as contiguously as possible, meaning threads in a warp read memory addresses adjacent to each other. This makes sure that minimal bank conflicts occur in the shared memory.

## Pinned Memory Usage

Although we did try using pinned memory, the result was way worse than our previous versions, so we dumped that idea.

#### **Profiler Results**

The most optimized version reported the following times:

*	Time		Total Time	Instances	Avg	Med	Min	Max	StdDev	Category	Operation
		61.4%	3.269 s	190000	17.206 µs	17.184 µs	16.639 µs	19.872 µs	310 ns	CUDA_KERNEL	forwardHidden(half *,half *,half *,half *)
		9.9%	527.456 ms	380000	1.388 µs	1.535 µs	480 ns	20.160 µs	265 ns	MEMORY_OPER	[CUDA memcpy Device-to-Host]
		9.5%	504.786 ms	190000	2.656 µs	2.656 µs	2.623 µs	3.520 µs	38 ns	CUDA_KERNEL	forwardOutput(_half *, _half *, _half *, _half *)
П		5.4%	290.296 ms	180000	1.612 µs	1.600 µs	1.535 µs	1.920 µs	31 ns	CUDA_KERNEL	updateHiddenLayer(_half *, _half *, _half *, _half *)
		5.0%	264.852 ms	180006	1.471 µs	1.408 µs	320 ns	10.096 ms	24.052 µs	MEMORY_OPER	[CUDA memcpy Host-to-Device]
		4.6%	244.794 ms	180000	1.360 µs	1.344 µs	1.311 µs	1.696 µs	24 ns	CUDA_KERNEL	computeHiddenGradients(half *,half *,half *,half *)
		4.3%	227.049 ms	180000	1.261 µs	1.248 µs	1.215 µs	1.472 µs	23 ns	CUDA_KERNEL	updateOutputLayer(half *,half *,half *,half *)

The speed-ups comparing every version to V1 (serial) can be found at the end here.

#### V4: Tensor Core Utilization

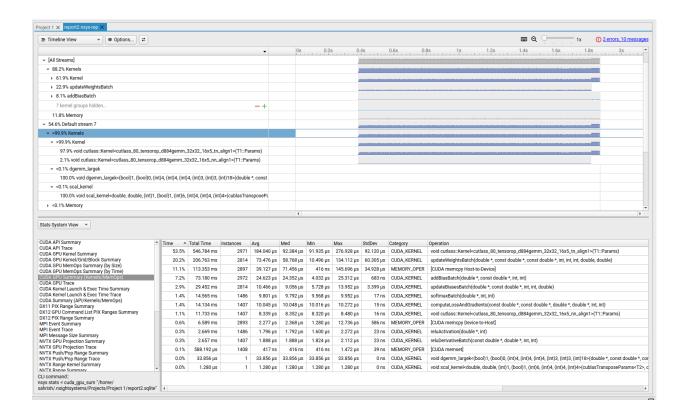
This version largely focused on batches and matrix multiplication. This led to the updation of the forward and back propagation in the following ways:

#### Forward Propagation

- 1. Input  $\rightarrow$  Hidden Layer:
  - Matrix Multiply: Uses cublasDgemm (cuBLAS) for W1 @ input\_batch.
  - Bias Add: Custom kernel addBiasBatch adds biases to all samples in the batch.
  - o Activation: Leaky ReLU applied via reluActivation kernel.
- 2. Hidden  $\rightarrow$  Output Layer:
  - Matrix Multiply: cublasDgemm for W2 @ hidden\_activations.
  - o Bias Add: Same as above.
  - Softmax: Batched softmax via softmaxBatch kernel for numerical stability.

#### **Backward Propagation**

- 1. Loss & Output Gradients:
  - Kernel: computeLossAndGradients computes cross-entropy loss and gradients (output - target) in one pass.
- 2. Hidden Gradients:
  - Matrix Multiply: cublasDgemm computes W2^T @ output\_gradients.
  - ReLU Derivative: reluDerivativeBatch applies gradients based on hidden layer activations.
- 3. Weight Updates:
  - Kernels: updateWeightsBatch (for W1/W2) and updateBiasesBatch (for b1/b2).



The speed-ups comparing every version to V1 (serial) can be found at the end here.

## Performance Analysis

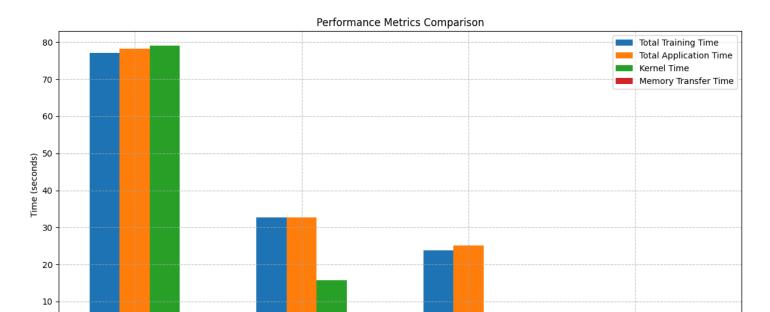
Note: The serial implementation does not include any hardware optimization instructions to the compiler. This means that the -o2 flag included in the original makefile has been removed so that the impact of GPU parallelization can be clearly demonstrated.

Although outputs have been generated in each version of code for calculating speed-ups, using the NVIDIA Nsight Systems profiling tool gives us better, more accurate measurements of time.

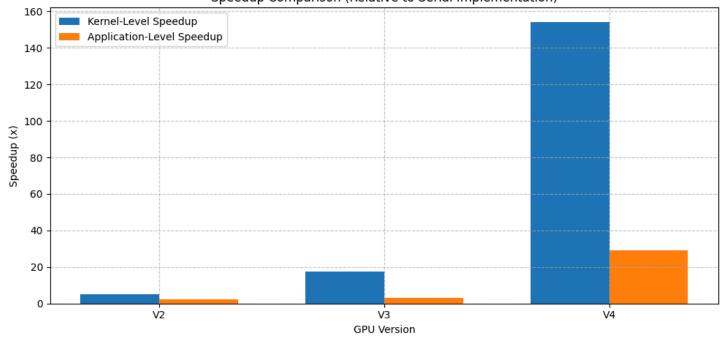
These timings have been reported for each version <u>above</u>, and used to calculate speed-ups below.

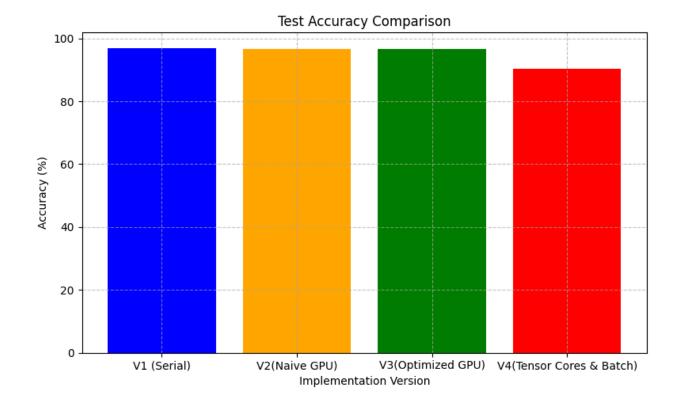
Number of Epochs	3							
Timing (s)	V1 (Serial)	V2(Naive GPU)	V3(Optimized GPU)	V4(Tensor Cores)				
Total Training Time	77.101	32.671	23.841	1.396				
Total Application Time (train + evaluate)	78.311	32.763	25.1168	2.699				
Kernel Time (forward + back prop)	79.009	15.744381	4.556925	0.512				
Memory Transfer Time	-	0.693455	0.792308	0.18				
Kernel + Memory Transfer	79.097	16.437836	5.349233	0.692				
Test Accuracy (%)	97	96.72	96.55	90.29				
Speed Up (Kernel-Level)		5.018234759	17.33822698	154.3144531				
Speed Up (Application-Level)		2.39022678	3.117873296	29.0148203				

The results are presented in tabular format below.



Speedup Comparison (Relative to Serial Implementation)





## Conclusion

This project showcased how GPU acceleration using CUDA can significantly improve neural network training times for MNIST classification. By progressively optimizing memory access, kernel configuration, and precision, we reduced training time from 77 seconds to just 1.4 seconds. Although minor accuracy trade-offs occurred, the performance gains were substantial. Overall, the project highlights the power of parallel computing in real-world machine learning tasks.