

Recurrent Neural Networks (RNN)

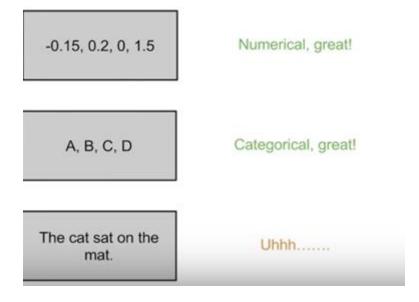
R. Venkatesh Babu, IISc







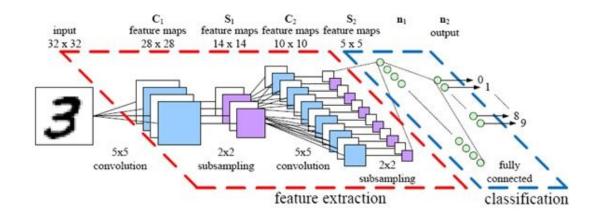
Data/Output Paradigms







CNN Revisited

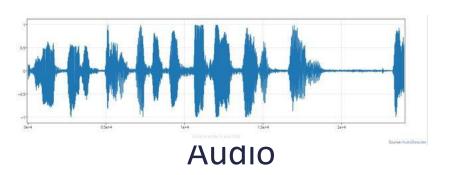


- Data is fed "in one shot", not in parts (mostly)
 - ► E.g. Image of "3" above is not processed row-by-row
- Captures "spatial context"
- State-less
- What if data is inherently "sequential" (composed of sequential 'parts')?
 - ► Need to capture "sequential context"



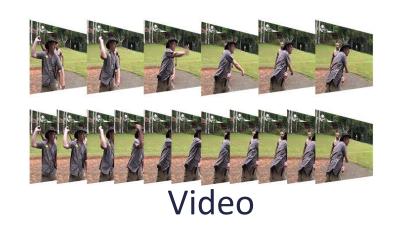


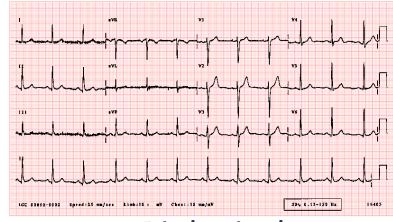
Sequential data



O Nachiketa, after pondering well the pleasures that are or seem to he delightful, you have renounced them all. You have not taken the road abounding in wealth, where many men sink. (*Kathopanishad*, II:3)

Text



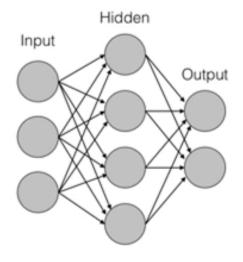


Biological

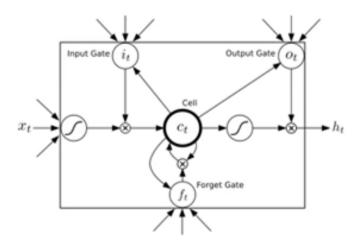




What are RNNs for?



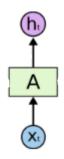
- Independence
- Fixed Length



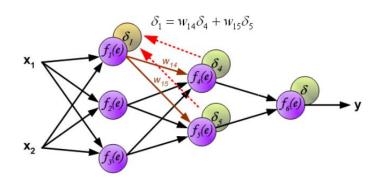
- Temporal dependencies
- · Variable sequence length





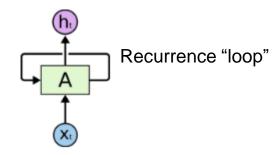


Error derivatives w.r.t weights in kth layer = f(Error derivatives from (k+1)th layer)

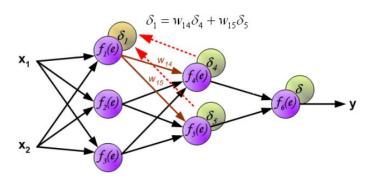






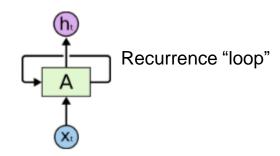


Error derivatives w.r.t weights in kth layer = f(Error derivatives from (k+1)th layer)



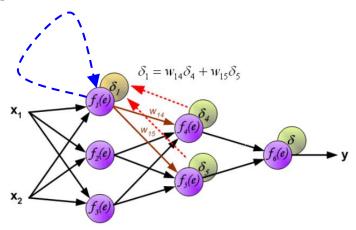






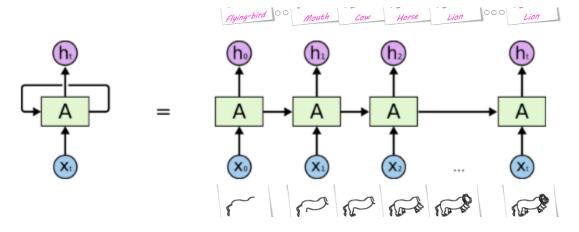
Error derivatives w.r.t weights in kth layer = f(Error derivatives from (k+1)th layer)

⇒ Error derivatives in terms of themselves ??!!!









- RNN unrolled → Not "that different" from a CNN (feed-forward connections)
- But crucial differences exist!





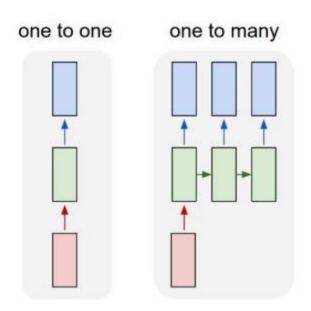
Recurrent Networks offer a lot of flexibility:

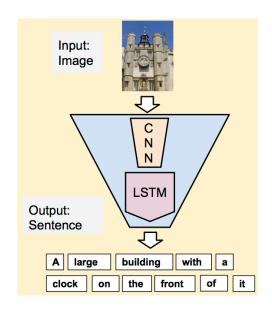
Vanilla Neural Networks





Recurrent Networks offer a lot of flexibility:





e.g. Image Captioning image -> sequence of words

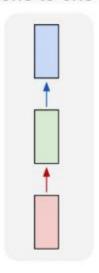


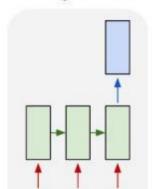


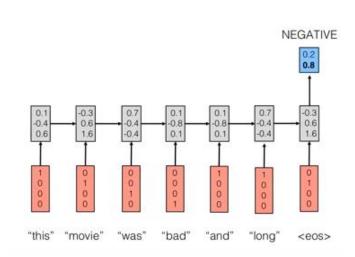
Recurrent Networks offer a lot of flexibility:

many to one









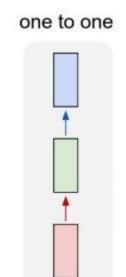


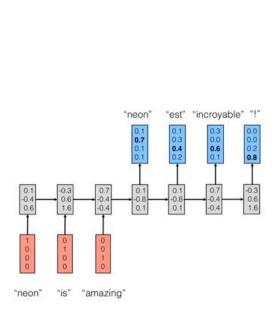
e.g. Sentiment Classification sequence of words -> sentiment

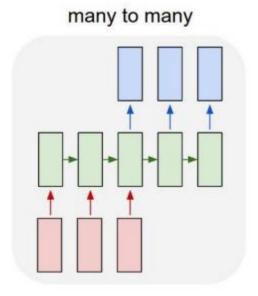




Recurrent Networks offer a lot of flexibility:





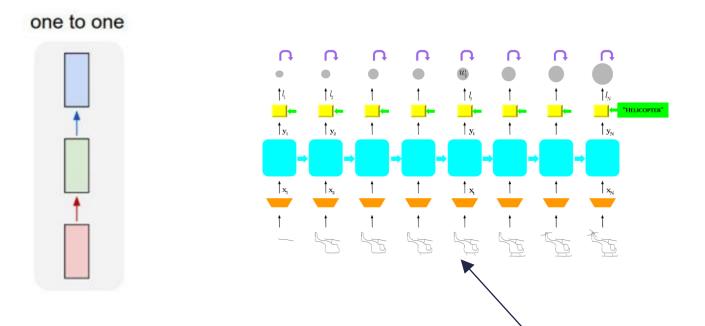


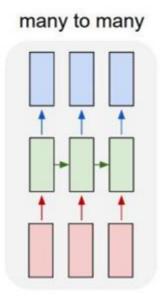
e.g. Machine Translation seq of words -> seq of words





Recurrent Networks offer a lot of flexibility:



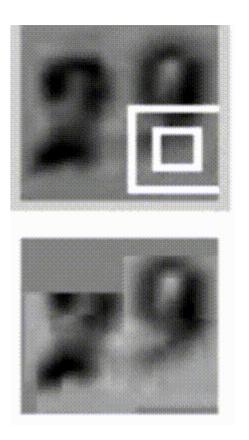


E.g. On-line freehand sketch recognition Seq of strokes -> Seq of "guesses"





Paradigm: Sequential "processing"



Reading house numbers

Input/Output may be "fixed", but processing can be sequential!

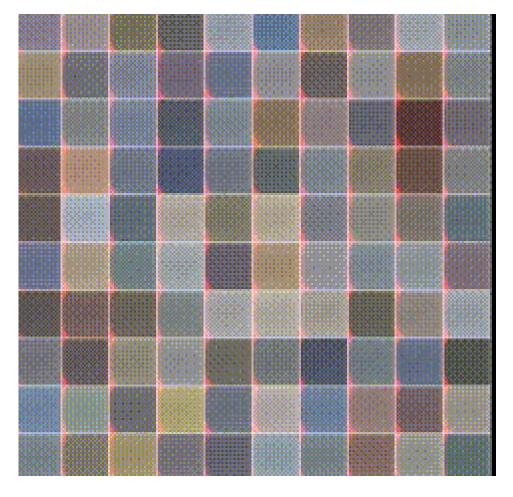
Multiple Object Recognition with Visual Attention, Ba et al.





Paradigm: Sequential "processing"

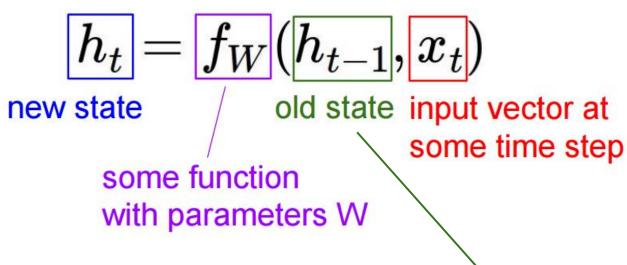
DRAW: A Recurrent Neural Network For Image Generation, Gregor et al.

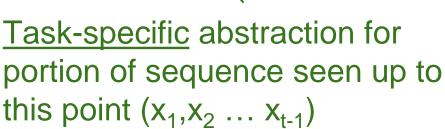






We can process a sequence of vectors **x** by applying a recurrence formula at every time step:







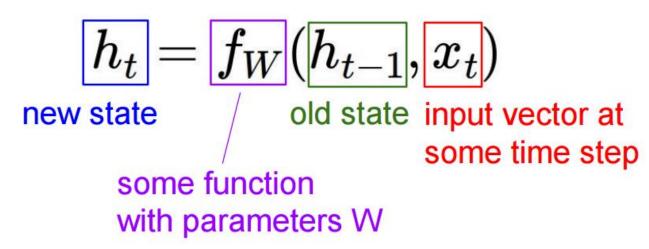
y

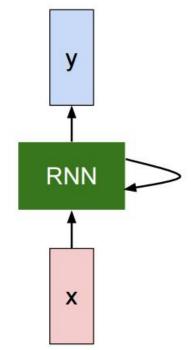
RNN

X



We can process a sequence of vectors **x** by applying a recurrence formula at every time step:

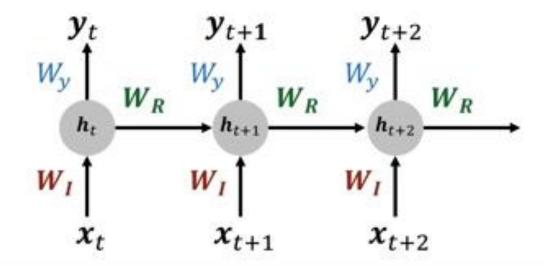




Notice: the same function and the same set of parameters are used at every time step.







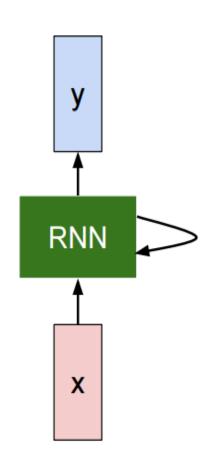
3 sets of parameters - W_I,W_y,W_R (shared for each time-step)





(Vanilla) Recurrent Neural Network

The state consists of a single "hidden" vector h:



$$h_t = f_W(h_{t-1}, x_t)$$

$$h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t)$$

$$y_t = W_{hy} h_t$$



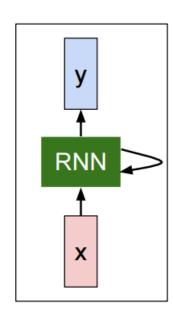


Character-level language model example

Vocabulary: [h,e,l,o]

Example training sequence: "hello"





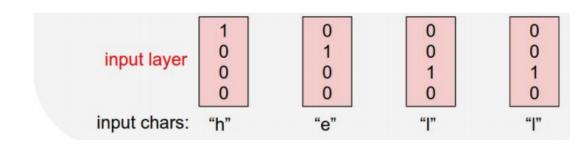




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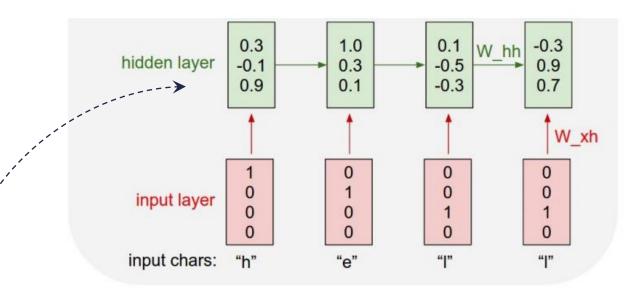


Character-level language model example

$$h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t)$$

Vocabulary: [h,e,l,o]

Example training sequence: "hello"



 $h_t \rightarrow$ abstraction of current input upto step t



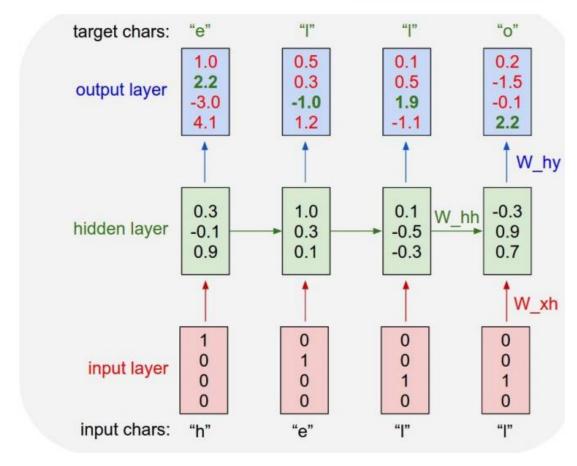


 $y_t = W_{hy} h_t$

Character-level language model example

Vocabulary: [h,e,l,o]

Example training sequence: "hello"



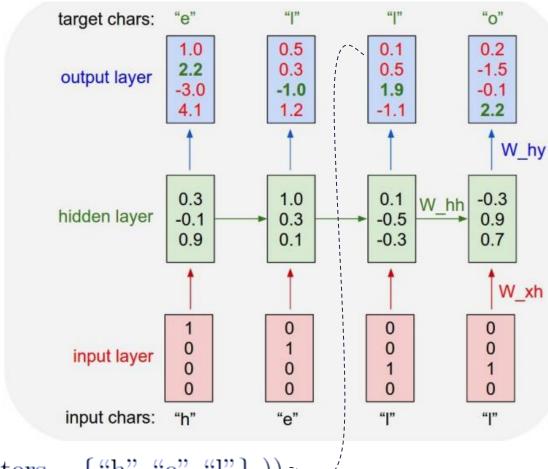




Character-level language model example

Vocabulary: [h,e,l,o]

Example training sequence: "hello"



$$p(\text{next letter} = \text{"l"}|\text{previous letters} = \{\text{"h"}, \text{"e"}, \text{"l"}\}))$$





Sonnet 116 - Let me not ...

by William Shakespeare

Let me not to the marriage of true minds
 Admit impediments. Love is not love

Which alters when it alteration finds,
 Or bends with the remover to remove:

O no! it is an ever-fixed mark
 That looks on tempests and is never shaken;

It is the star to every wandering bark,
 Whose worth's unknown, although his height be taken.

Love's not Time's fool, though rosy lips and cheeks
 Within his bending sickle's compass come:

Love alters not with his brief hours and weeks,
 But bears it out even to the edge of doom.

If this be error and upon me proved,
 I never writ, nor no man ever loved.





at first:

tyntd-iafhatawiaoihrdemot lytdws e ,tfti, astai f ogoh eoase rrranbyne 'nhthnee e plia tklrgd t o idoe ns,smtt h ne etie h,hregtrs nigtike,aoaenns lng

train more

"Tmont thithey" fomesscerliund Keushey. Thom here sheulke, anmerenith ol sivh I lalterthend Bleipile shuwy fil on aseterlome coaniogennc Phe lism thond hon at. MeiDimorotion in ther thize."

train more

Aftair fall unsuch that the hall for Prince Velzonski's that me of her hearly, and behs to so arwage fiving were to it beloge, pavu say falling misfort how, and Gogition is so overelical and ofter.

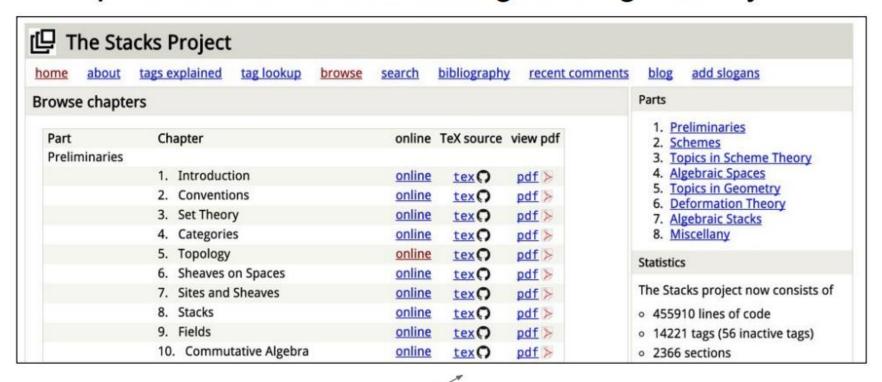
train more

"Why do what that day," replied Natasha, and wishing to himself the fact the princess, Princess Mary was easier, fed in had oftened him. Pierre aking his soul came to the packs and drove up his father-in-law women.





open source textbook on algebraic geometry



Latex source





Proof. Omitted.

Lemma 0.1. Let C be a set of the construction.

Let C be a gerber covering. Let F be a quasi-coherent sheaves of O-modules. We have to show that

$$\mathcal{O}_{\mathcal{O}_X} = \mathcal{O}_X(\mathcal{L})$$

Proof. This is an algebraic space with the composition of sheaves F on $X_{\acute{e}tale}$ we have

$$\mathcal{O}_X(\mathcal{F}) = \{morph_1 \times_{\mathcal{O}_X} (\mathcal{G}, \mathcal{F})\}$$

where G defines an isomorphism $F \to F$ of O-modules.

Lemma 0.2. This is an integer Z is injective.

Lemma 0.3. Let S be a scheme. Let X be a scheme and X is an affine open covering. Let $U \subset X$ be a canonical and locally of finite type. Let X be a scheme. Let X be a scheme which is equal to the formal complex.

The following to the construction of the lemma follows.

Let X be a scheme. Let X be a scheme covering. Let

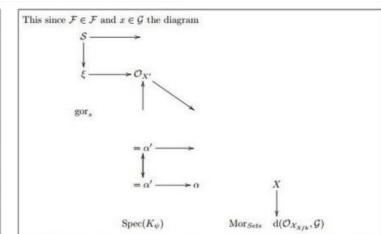
$$b: X \to Y' \to Y \to Y \to Y' \times_X Y \to X.$$

be a morphism of algebraic spaces over S and Y.

Proof. Let X be a nonzero scheme of X. Let X be an algebraic space. Let \mathcal{F} be a quasi-coherent sheaf of \mathcal{O}_X -modules. The following are equivalent

- F is an algebraic space over S.
- (2) If X is an affine open covering.

Consider a common structure on X and X the functor $\mathcal{O}_X(U)$ which is locally of finite type.



is a limit. Then G is a finite type and assume S is a flat and F and G is a finite type f_* . This is of finite type diagrams, and

- the composition of G is a regular sequence,
- O_{X'} is a sheaf of rings.

Proof. We have see that $X = \operatorname{Spec}(R)$ and \mathcal{F} is a finite type representable by algebraic space. The property \mathcal{F} is a finite morphism of algebraic stacks. Then the cohomology of X is an open neighbourhood of U.

Proof. This is clear that G is a finite presentation, see Lemmas ??.

A reduced above we conclude that U is an open covering of C. The functor F is a "field

$$\mathcal{O}_{X,x} \longrightarrow \mathcal{F}_{\overline{x}} -1(\mathcal{O}_{X_{\ell tale}}) \longrightarrow \mathcal{O}_{X_{\ell}}^{-1}\mathcal{O}_{X_{\lambda}}(\mathcal{O}_{X_{n}}^{\overline{v}})$$

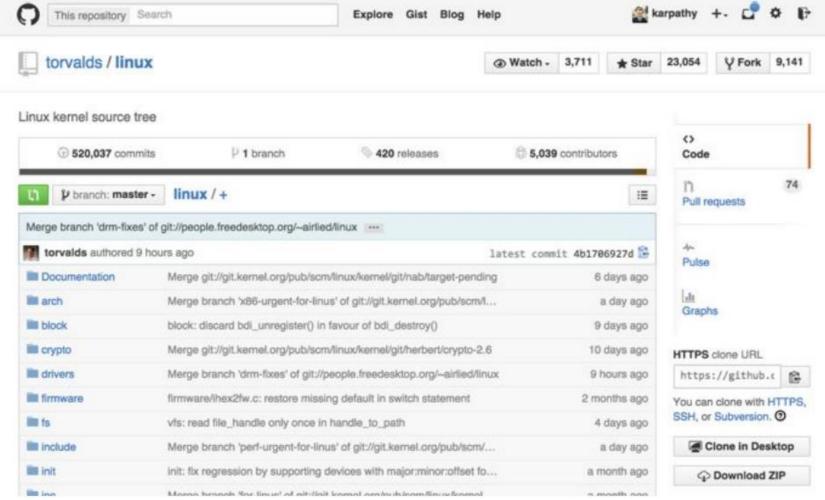
is an isomorphism of covering of O_{X_i} . If F is the unique element of F such that X is an isomorphism.

The property \mathcal{F} is a disjoint union of Proposition ?? and we can filtered set of presentations of a scheme \mathcal{O}_X -algebra with \mathcal{F} are opens of finite type over S. If \mathcal{F} is a scheme theoretic image points.

If \mathcal{F} is a finite direct sum $\mathcal{O}_{X_{\lambda}}$ is a closed immersion, see Lemma ??. This is a sequence of \mathcal{F} is a similar morphism.











```
static void do command(struct seg file *m, void *v)
 int column = 32 << (cmd[2] & 0x80);
 if (state)
    cmd = (int)(int state ^ (in 8(&ch->ch flags) & Cmd) ? 2 : 1);
  else
    seg = 1;
  for (i = 0; i < 16; i++) {
   if (k & (1 << 1))
     pipe = (in use & UMXTHREAD UNCCA) +
        ((count & 0x0000000ffffffff8) & 0x000000f) << 8;
    if (count == 0)
      sub(pid, ppc md.kexec handle, 0x20000000);
   pipe set bytes(i, 0);
  /* Free our user pages pointer to place camera if all dash */
  subsystem info = &of changes[PAGE SIZE];
 rek_controls(offset, idx, &soffset);
 /* Now we want to deliberately put it to device */
 control check polarity(&context, val, 0);
  for (i = 0; i < COUNTER; i++)
    seq puts(s, "policy ");
```

Generated C code

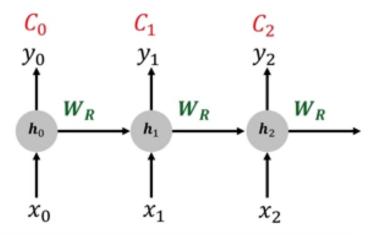
S





Training RNNs - Backpropagation through time

$$\mathbf{h}^{(t)} = g_h(W_I \mathbf{x}^{(t)} + W_R \mathbf{h}^{(t-1)} + \mathbf{b}_h)$$
$$\mathbf{y}^{(t)} = g_y(W_y \mathbf{h}^{(t)} + \mathbf{b}_y)$$



$$\frac{\partial C}{\partial W_R} = \sum_{t=1}^{T} \frac{\partial C_t}{\partial W_R}$$

$$\frac{\partial C_t}{\partial W_R} = \sum_{k=1}^{t} \frac{\partial C_t}{\partial y_t} \frac{\partial y_t}{\partial h_t} \frac{\partial h_t}{\partial h_k} \frac{\partial h_k}{\partial W_R}$$

$$\frac{\partial h_t}{\partial h_k} = \prod_{i=k+1}^t \frac{\partial h_i}{\partial h_{i-1}} = \prod_{i=k+1}^t W_R^T \operatorname{diag}(g_h'(W_I x^{(i)} + W_R h^{(i-1)} + b_h))$$

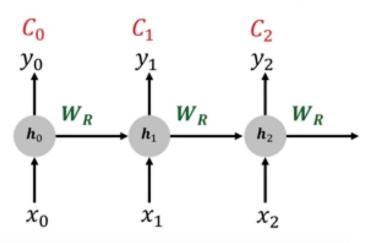
- (Potentially) multiple, intermediate costs C₀,C₁,C₂
- Shared weights W_R





Training RNNs - BPTT, Vanishing gradients

$$\mathbf{h}^{(t)} = g_h(W_I \mathbf{x}^{(t)} + W_R \mathbf{h}^{(t-1)} + \mathbf{b}_h)$$
$$\mathbf{y}^{(t)} = g_y(W_y \mathbf{h}^{(t)} + \mathbf{b}_y)$$



$$\frac{\partial C}{\partial W_R} = \sum_{t=1}^T \frac{\partial C_t}{\partial W_R}$$

$$\frac{\partial C_t}{\partial W_R} = \sum_{k=1}^t \frac{\partial C_t}{\partial y_t} \frac{\partial y_t}{\partial h_t} \frac{\partial h_t}{\partial h_k} \frac{\partial h_k}{\partial W_R}$$

$$\frac{\partial h_t}{\partial h_k} = \prod_{i=k+1}^t \frac{\partial h_i}{\partial h_{i-1}} = \prod_{i=k+1}^t W_R^T \operatorname{diag}(g_h'(W_I x^{(i)} + W_R h^{(i-1)} + b_h))$$

$$\left\| \frac{\partial h_i}{\partial h_{i-1}} \right\| \leq \|W_R^T\| \left\| \operatorname{diag}(g_h'(W_I x^{(i)} + W_R h^{(i-1)} + b_h)) \right\| \leq \gamma_{W_R} \gamma_{g_h}$$

(Pascanu, et al., On the difficulty of training Recurrent Neural Networks.)

Vanishing gradients!





Training RNNs

Choice of al. Ch

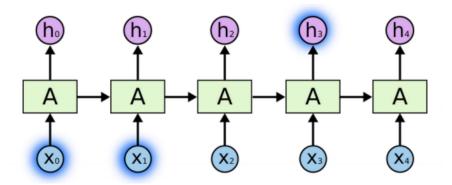
- |W_R| << 1 → Vanishing gradients
- |W_R| >> 1 → Vanishing gradients
- |W_R| 'close to 1' is ideal





Fundamental issues with RNNs

- RNNs connect previous information to the present task
 - Previous video frames may help understand present frame
- Sometimes we need only look at recent previous information to predict
 - To predict the last word of "The clouds are in the sky" we don't need any further context. It is obvious that the word is "sky"



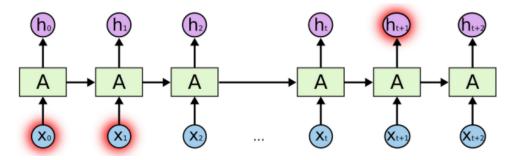




Fundamental issues with RNNs

Problem of Long-term dependency

- There are cases where we need more context
- To predict the last word in the sentence "I grew up in France….I speak fluent French"
- Using only recent information suggests that the last word is the name of a language. But more distant past indicates that it is French
- It is possible that the gap between the relevant information and where it is needed is very large







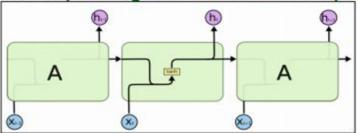


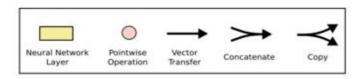






- Explicitly designed to avoid the long-term dependency problem
- RNNs have the form of a repeating chain structure
 - The repeating module has a simple structure such as tanh

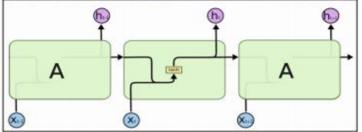


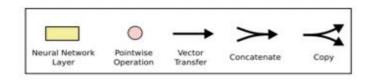




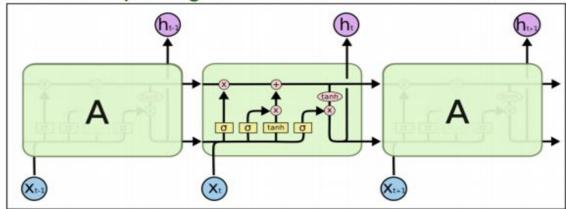


- Explicitly designed to avoid the long-term dependency problem
- RNNs have the form of a repeating chain structure
 - The repeating module has a simple structure such as tanh





- LSTMs also have a chain structure
 - but the repeating module has a different structure







LSTM

Core idea behind LSTM

- The key to LSTM is the cell state, C_t , the horizontal line running through the top of the diagram
- Like a conveyor belt
 - Runs through entire chain with minor interactions
 - LSTM does have the ability to
 remove/add information to cell state regulated by structures called gates





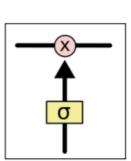
LSTM

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- Like a conveyor belt
 - Runs through entire chain with minor interactions
 - LSTM does have the ability to
 remove/add information to cell state regulated by structures called gates
- Gates are an optional way to let information through
- Consist of a sigmoid and a multiplication operation
- Sigmoid outputs a value between 0 and 1
 - 0 means let nothing through
 - 1 means let eveything through

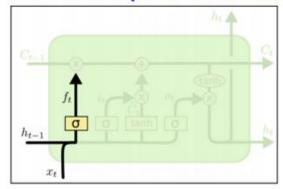








- Example of language model: predict next word based on previous ones
 - Cell state may include the gender of the present subject
- First step: information to throw away from cell state



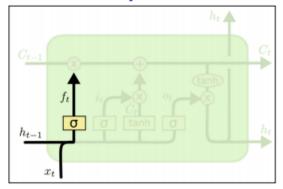
Called forget gate layer

It looks at h_{t-1} and x_t and outputs a number between 0 and 1 for each member of C_{t-1} for whether to forget

$$f_t = \sigma\left(W_f \cdot [h_{t-1}, x_t] + b_f\right)$$



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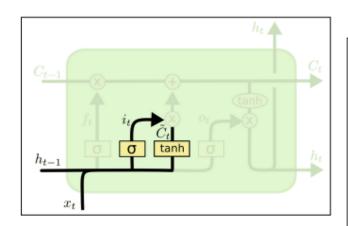
In language model

consider trying to predict the next word based on all previous ones.
The cell state may include the gender of the present subject so that the proper pronouns can be used.
When we see a new subject we want to forget old subject.





 Next step is to decide as to what new information we're going to store in the cell state



This has two parts:

first a sigmoid layer called *Input gate layer*: decides which values we will update Next a \tanh layer creates a vector of new candidate values \tilde{C}_{t} that could be added to the state.

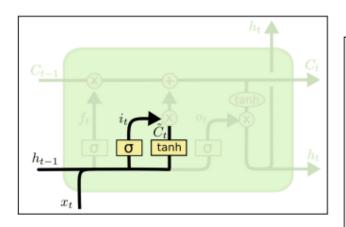
In the third step we will combine these two to create an update to the state

$$i_t = \sigma \left(W_i \cdot [h_{t-1}, x_t] + b_i \right)$$
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$





 Next step is to decide as to what new information we're going to store in the cell state



In the Language model, we'd want to add the gender of the new subject to the cell state, to replace the old One we are forgetting

This has two parts:

first a sigmoid layer called *Input gate layer*: decides which values we will update Next a \tanh layer creates a vector of new candidate values \tilde{C}_t that could be added to the state.

In the third step we will combine these two to create an update to the state

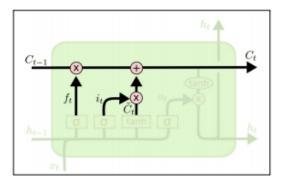
$$i_t = \sigma \left(W_i \cdot [h_{t-1}, x_t] + b_i \right)$$

$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$





- It's now time to update old cell state C_{t-1} into new cell state C_t
 - The previous step decided what we need to do
 - · We just need to do it



We multiply the old state by f_t , forgetting the things we decided to forget earlier.

Then we add $i_t * \tilde{C}_t$

This is the new candidate values, scaled by how much we decided to update each state value

In the Language model, this is where we'd actually drop the information about the old subject's gender and add the new information, as we decided in previous steps

$$C_t = f_t * C_{t-1} + i_t * \tilde{C}_t$$

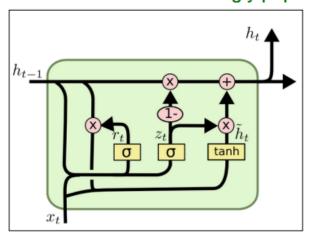




GRU: a LSTM variant

Gated Recurrent Unit (GRU)

- A dramatic variant of LSTM
 - It combines the forget and input gates into a single update gate
 - It also merges the cell state and hidden state, and makes some other changes
 - The resulting model is simpler than LSTM models
 - Has become increasingly popular



$$z_{t} = \sigma (W_{z} \cdot [h_{t-1}, x_{t}])$$

$$r_{t} = \sigma (W_{r} \cdot [h_{t-1}, x_{t}])$$

$$\tilde{h}_{t} = \tanh (W \cdot [r_{t} * h_{t-1}, x_{t}])$$

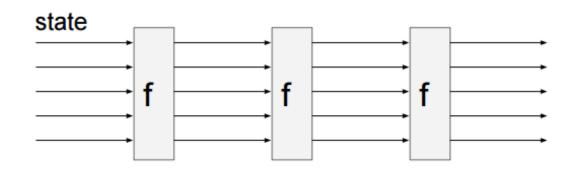
$$h_{t} = (1 - z_{t}) * h_{t-1} + z_{t} * \tilde{h}_{t}$$

13

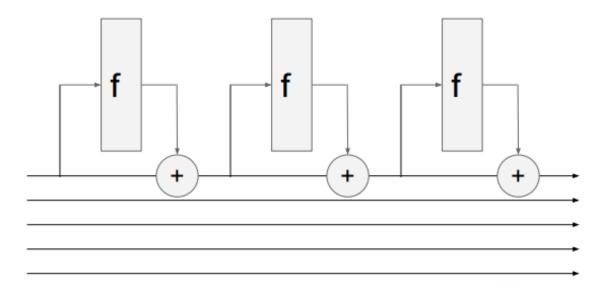




RNN

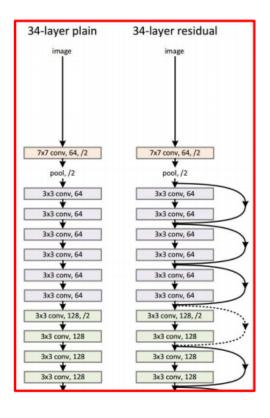


LSTM (ignoring forget gates)



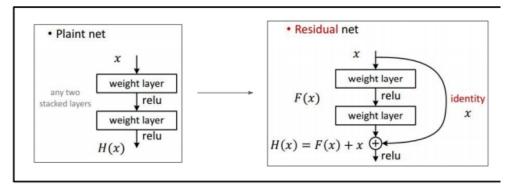






Recall: "PlainNets" vs. ResNets

ResNet is to PlainNet what LSTM is to RNN, kind of.

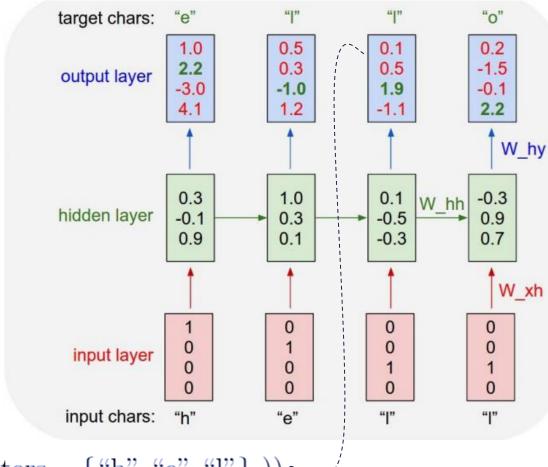




Character-level language model example

Vocabulary: [h,e,l,o]

Example training sequence: "hello"



$$p(\text{next letter} = \text{"l"}|\text{previous letters} = \{\text{"h"}, \text{"e"}, \text{"l"}\}))$$





Searching for interpretable cells

```
"You mean to imply that I have nothing to eat out of.... On the contrary, I can supply you with everything even if you want to give dinner parties," warmly replied Chichagov, who tried by every word he spoke to prove his own rectitude and therefore imagined Kutuzov to be animated by the same desire.

Kutuzov, shrugging his shoulders, replied with his subtle penetrating smile: "I meant merely to say what I said."
```

quote detection cell





Searching for interpretable cells

```
Cell sensitive to position in line:
```

```
The sole importance of the crossing of the Berezina lies in the fact that it plainly and indubitably proved the fallacy of all the plans for cutting off the enemy's retreat and the soundness of the only possible line of action--the one Kutuzov and the general mass of the army demanded--namely, simply to follow the enemy up. The French crowd fled at a continually increasing speed and all its energy was directed to reaching its goal. It fled like a wounded animal and it was impossible to block its path. This was shown not so much by the arrangements it made for crossing as by what took place at the bridges. When the bridges broke down, unarmed soldiers, people from Moscow and women with children who were with the French transport, all--carried on by vis inertiae--pressed forward into boats and into the ice-covered water and did not, surrender.
```

line length tracking cell





Searching for interpretable cells

```
audit_dupe
                   quote/comment cell
```





Getting started (code ...)

- Karpathy char-rnn: https://gist.github.com/karpathy/d4dee566867f8291f086
- TensorFlow
 - http://r2rt.com/recurrent-neural-networks-in-tensorflow-i.html
 - ► http://www.wildml.com/2015/09/recurrent-neural-networks-tutorial-part-1-introduction-to-rnns/
 - https://danijar.com/introduction-to-recurrent-networks-intensorflow/
 - http://monik.in/a-noobs-guide-to-implementing-rnn-lstm-usingtensorflow/
- Lasagne
 - https://github.com/craffel/Lasagnetutorial/blob/master/examples/tutorial.ipynb

