

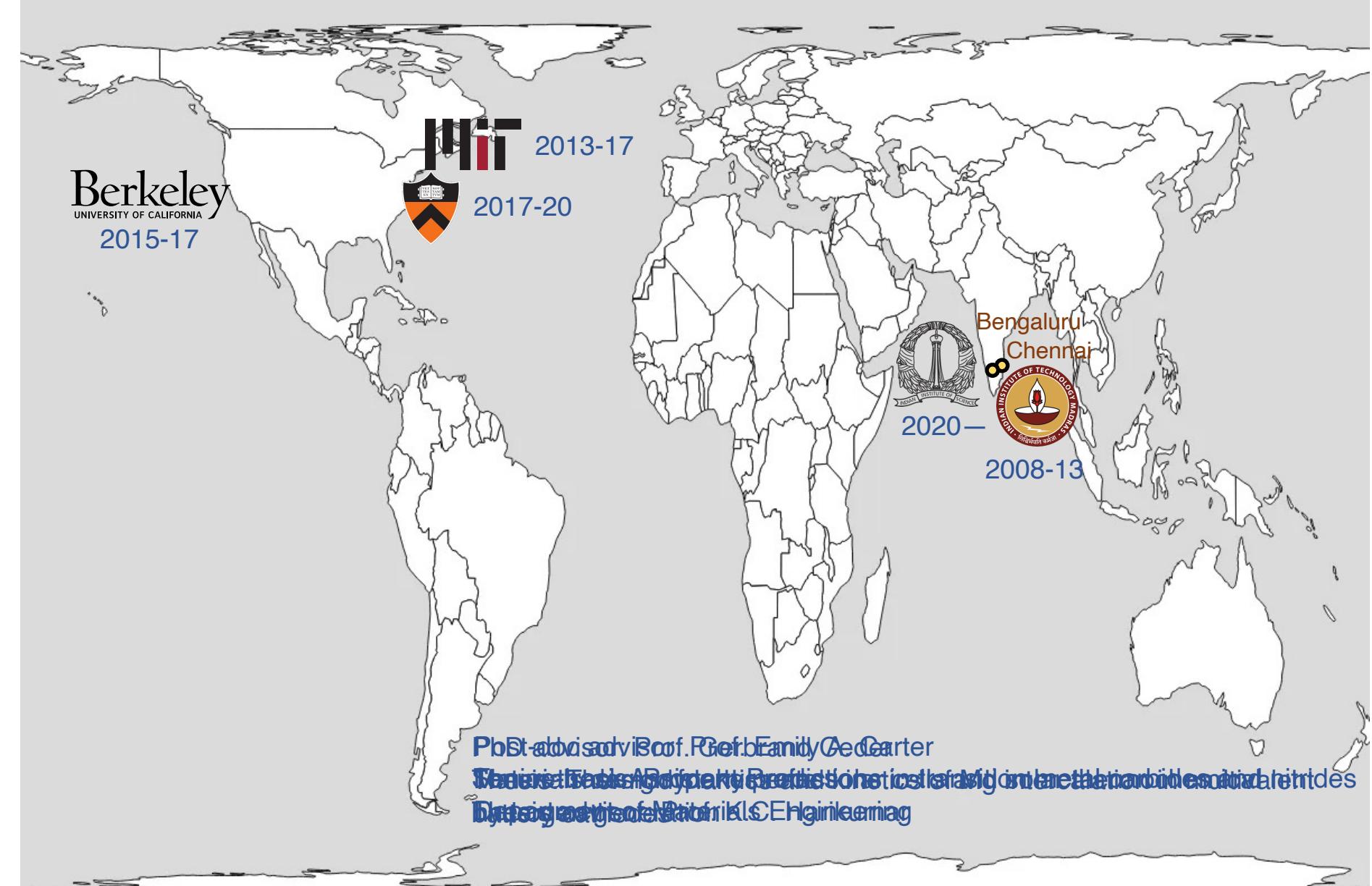
Theory-guided materials design for energy applications

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Scientific journey so far...



Climate change is here

ipcc

REPORTS

SYNTHESIS REPORT

WORKING GROUPS

ACTIVITIES

NEWS

CALENDAR

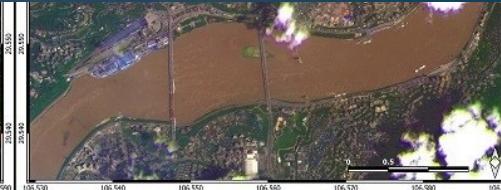
AR6 Synthesis Report: Climate Change 2022

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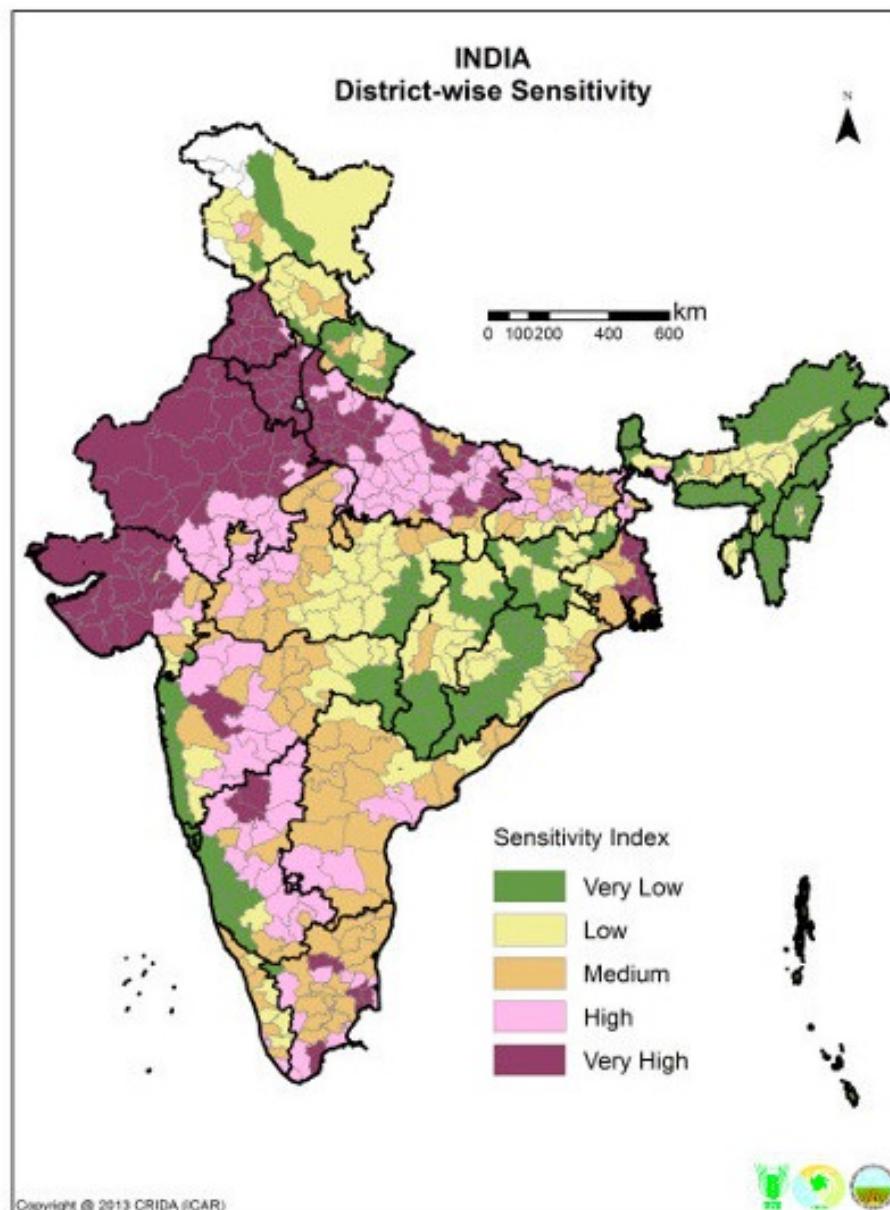
[CORE WRITING TEAM](#)

Code Red

Wildfire →
Fire clouds



Climate change's impact on India



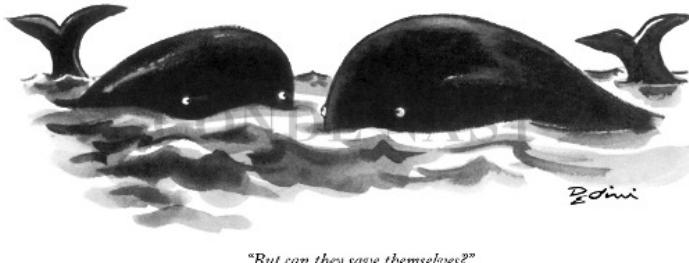
<https://www.financialexpress.com/india-news/water-scarcity-to-cost-growth-spark-conflict-migration-world-bank/248179/>



<https://www.indiatoday.in/science/story/india-may-suffer-devastating-climate-change-impact-in-80-years-study-1685987-2020-06-05>

Non-fossil-fuel options for mitigating climate change

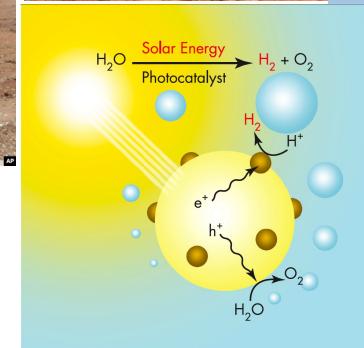
"With great power comes great responsibility problem"
- Uncle Ben Zen



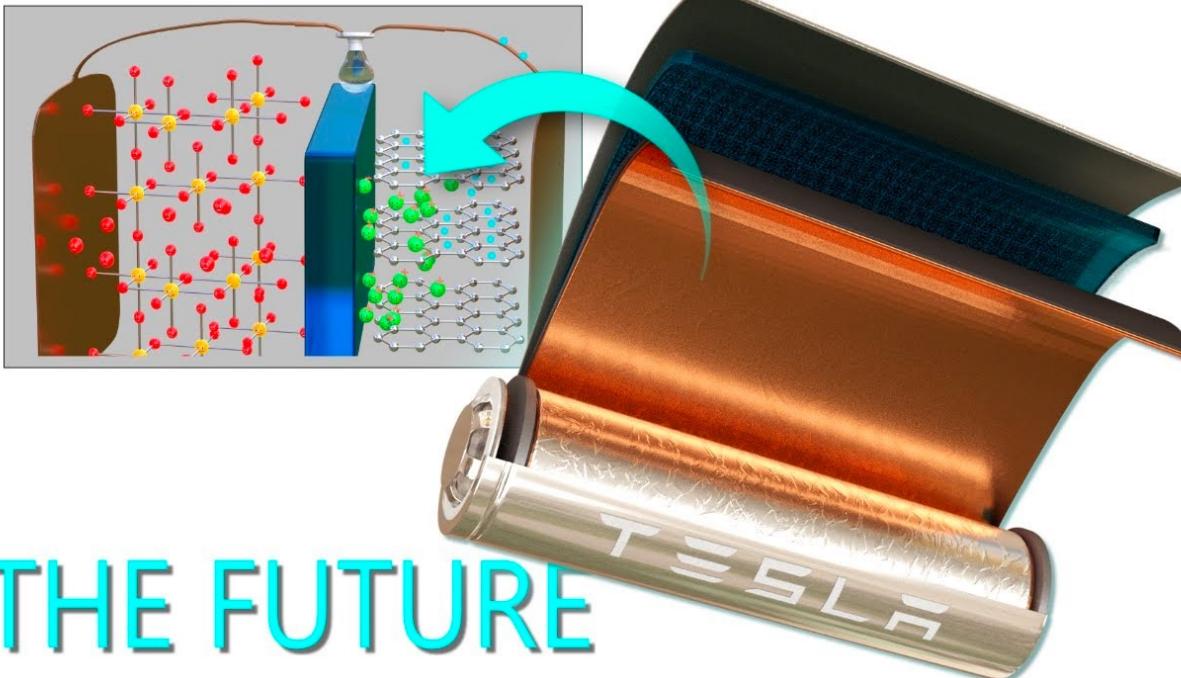
ROCKET MAN & PULLWINKER



+Tidal, biofuels, etc.



Non-fossil-fuel options for mitigating climate change



When the sun doesn't
shine or the wind doesn't
blow

THE FUTURE

Materials form the performance-bottlenecks of most renewable energy devices: **how do we understand and improve the material bottlenecks?**

- Look at what material properties govern energy devices first
- How can we improve the amount of energy stored (i.e., energy density) in a battery?
- How can we get better photovoltaics (solar cells)?

Energy technologies and how materials influence them

Solar Cells and Batteries

How does the modern Li-ion battery work?

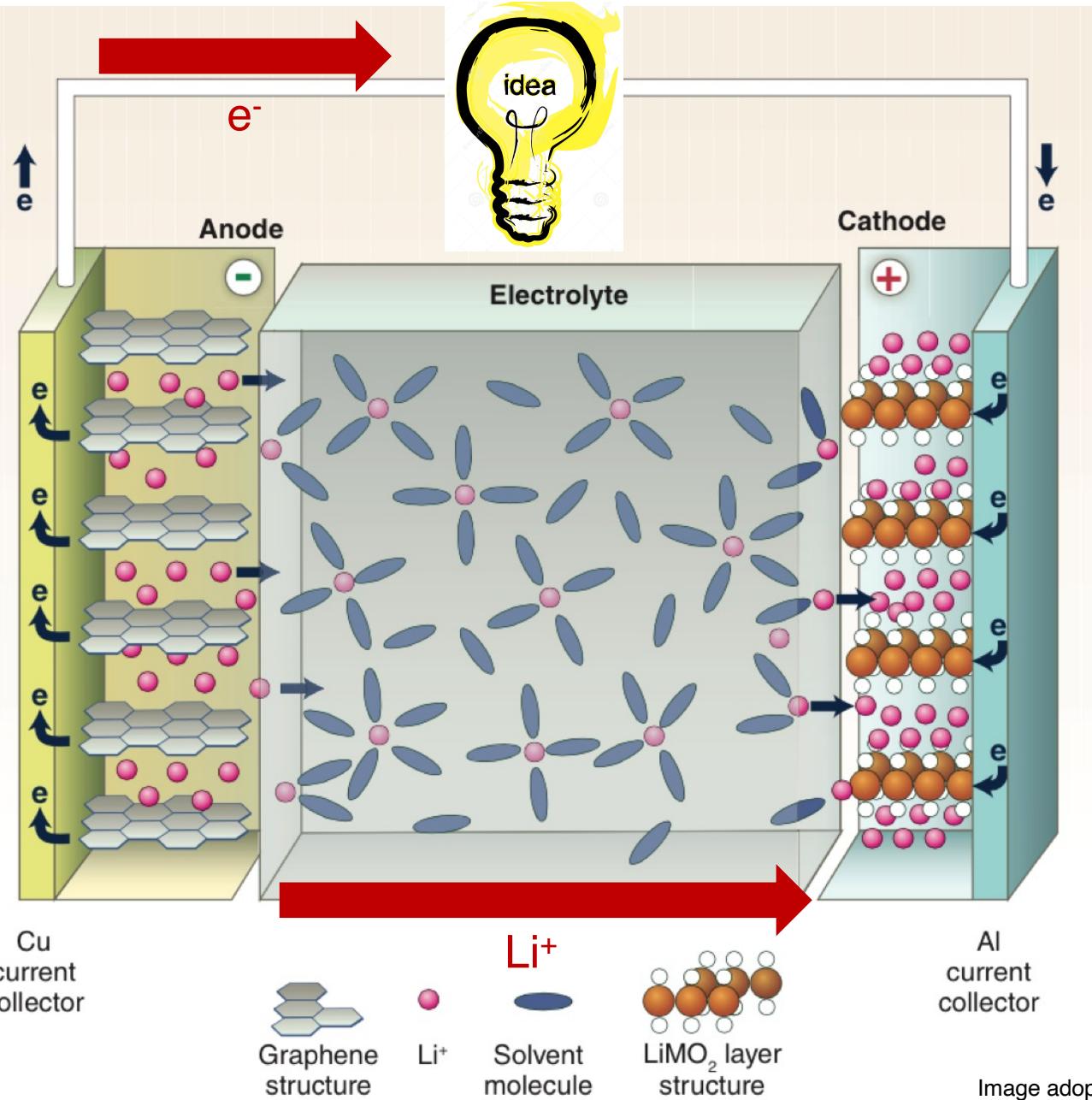
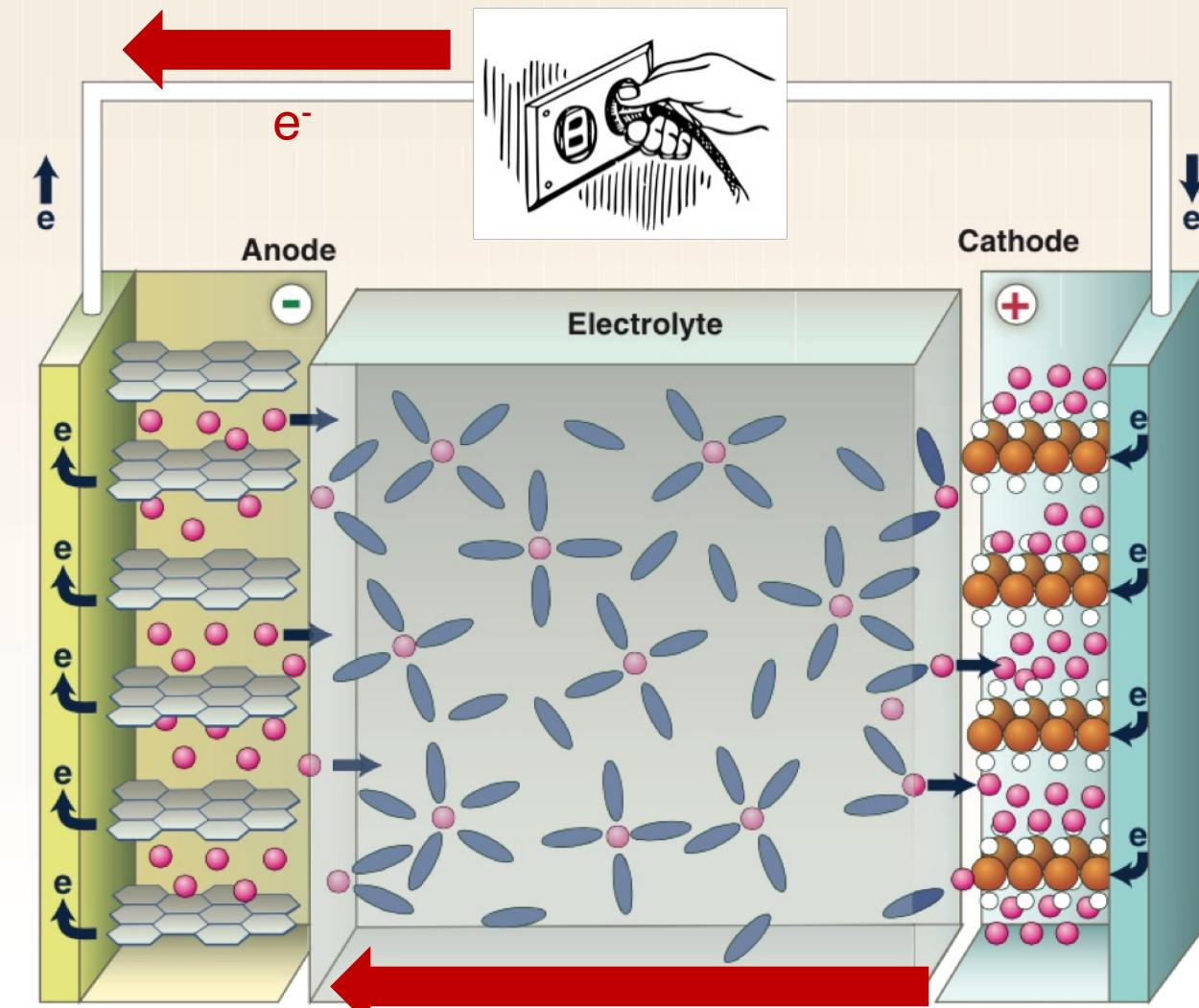
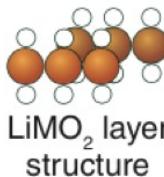
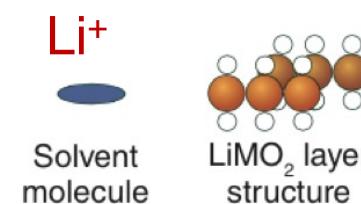
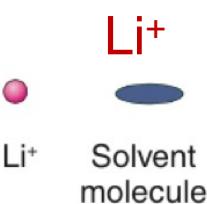
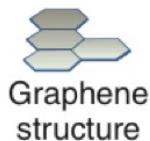


Image adopted from B. Dunn et al., Science 2011

How does the modern Li-ion battery work?



Cu
current
collector



Al
current
collector

Voltage (V): Potential to do work

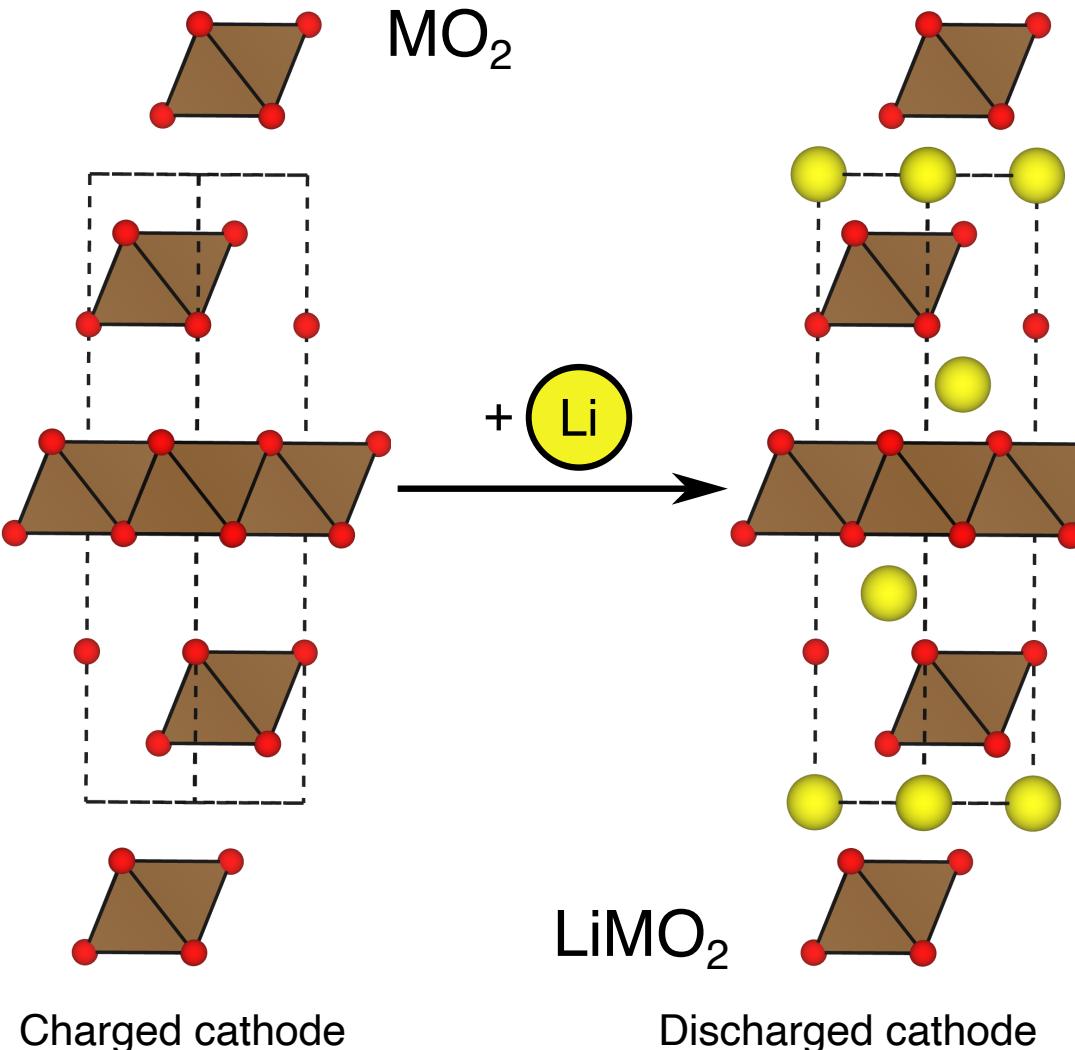
Capacity (mAh): Amount of charge stored

Voltage*capacity: Energy stored

Rate (C): How fast can a battery be charged and discharged?

All performance metrics of a battery system are **material dependent**: anode, cathode, and electrolyte

Voltage, capacity, and rate



$$\Delta G_{\text{intercalation}} = G_{\text{LiMO}_2} - G_{\text{MO}_2} - G_{\text{Li}}$$

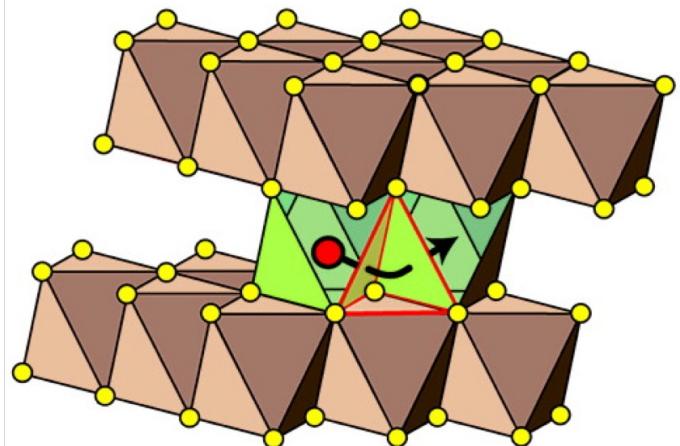
Nernst Equation

$$V = - \frac{\Delta G_{\text{intercalation}}}{nF}$$

(Do similar process for anode, take V difference!)

1 Li moved = 1 electron stored

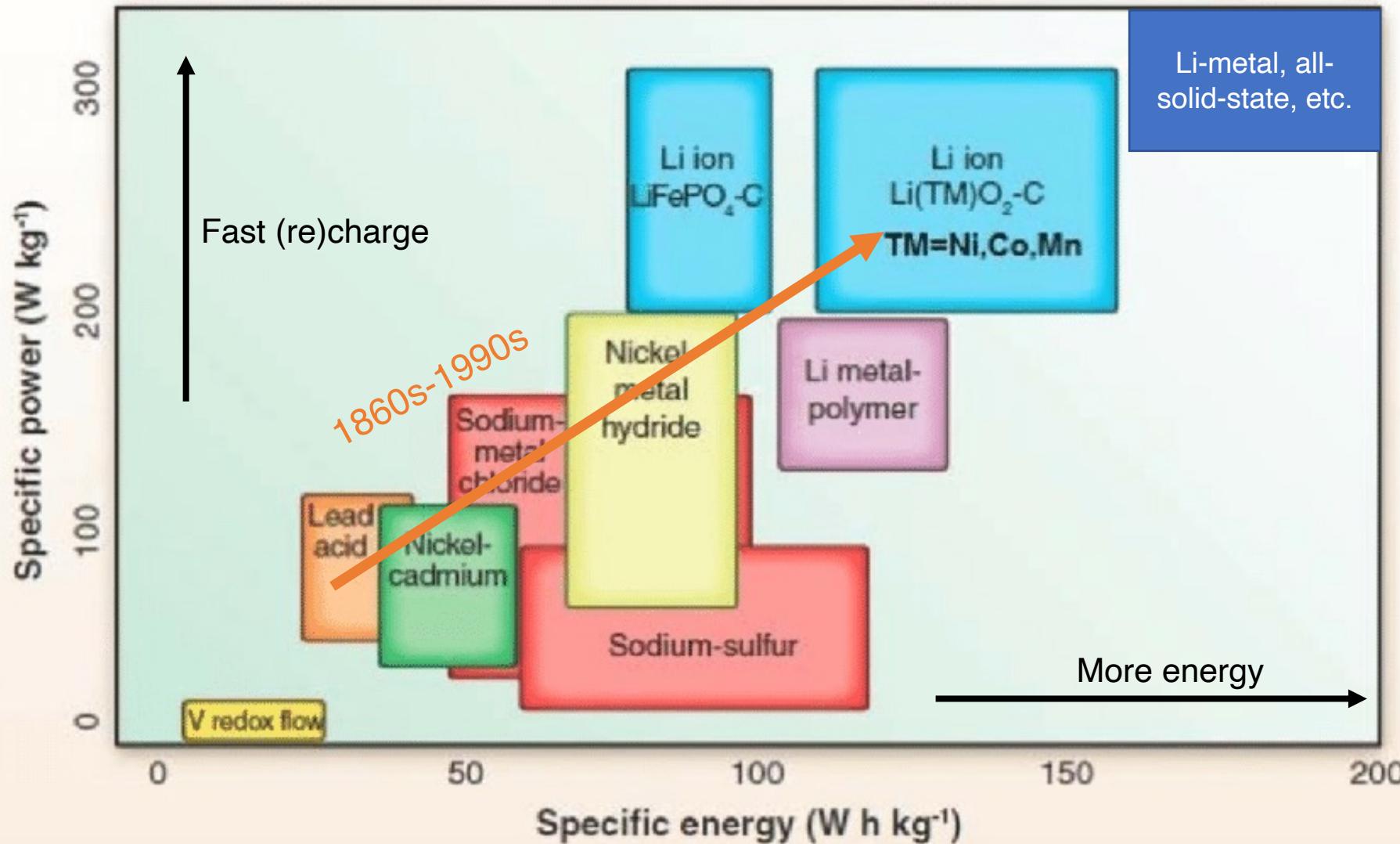
$$\text{Capacity} \propto \frac{\# \text{ Li moved}}{\# \text{ 'Framework' atoms}}$$



Rate: how fast can Li move (or diffuse) within electrode?

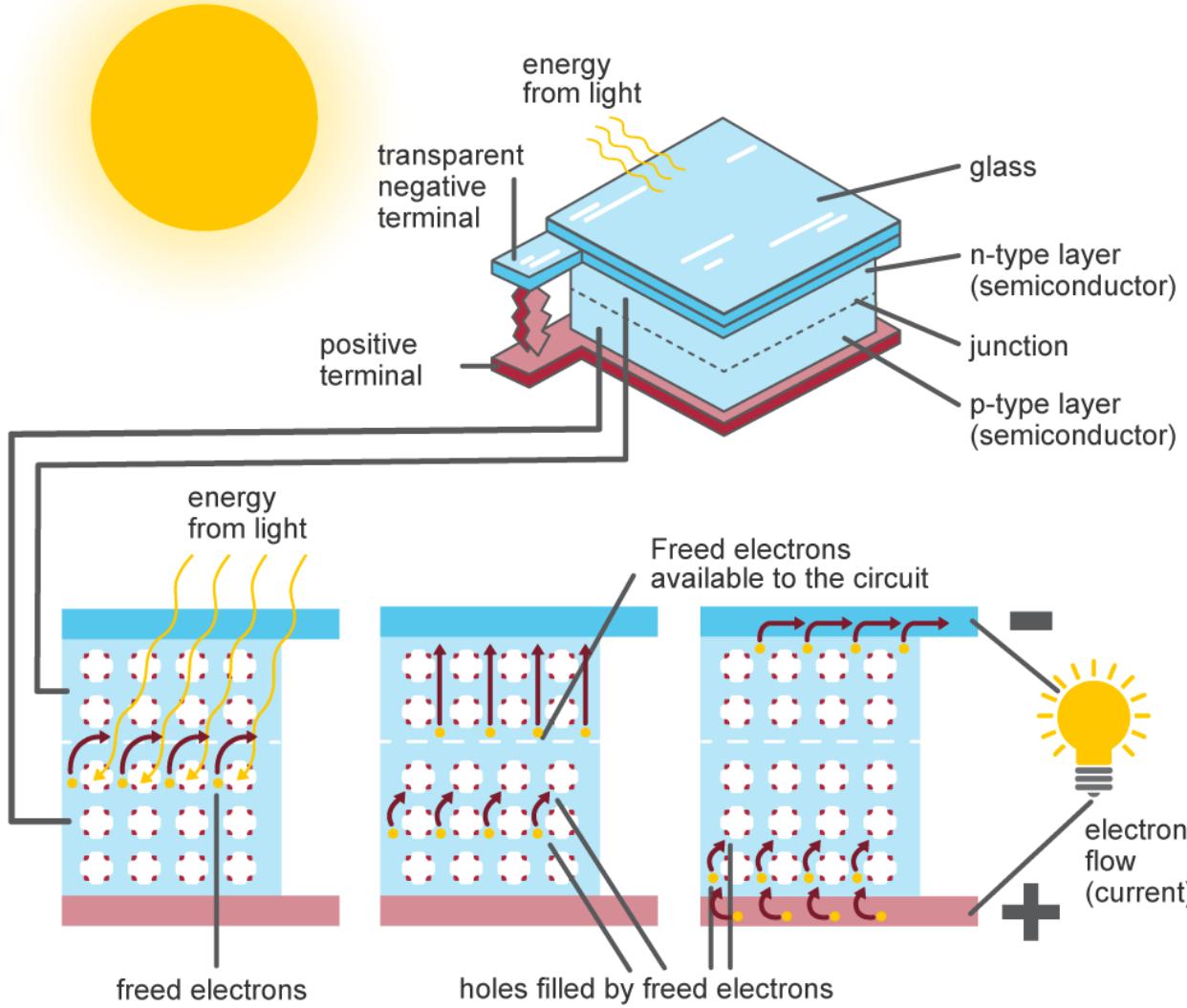
$$\text{Rate} \propto \exp\left(-\frac{E_m}{RT}\right)$$

We have made significant progress in batteries: but tremendous space left

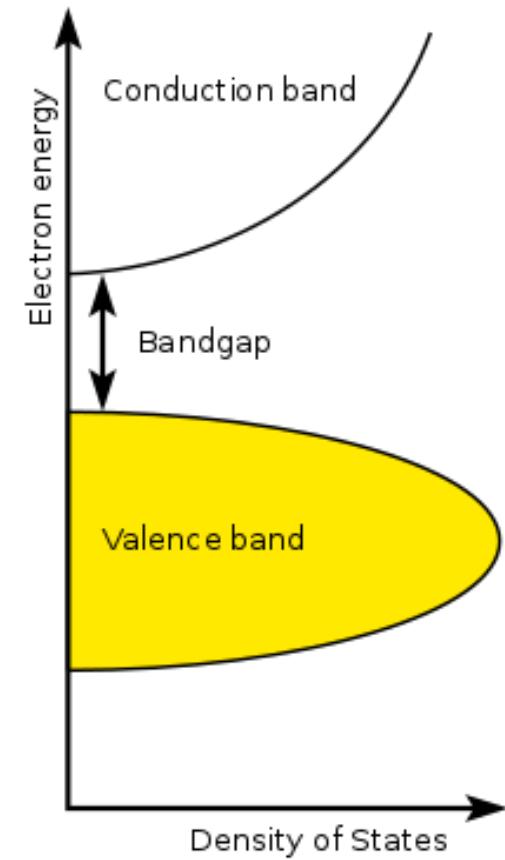


So how does a solar cell work?

Inside a photovoltaic cell

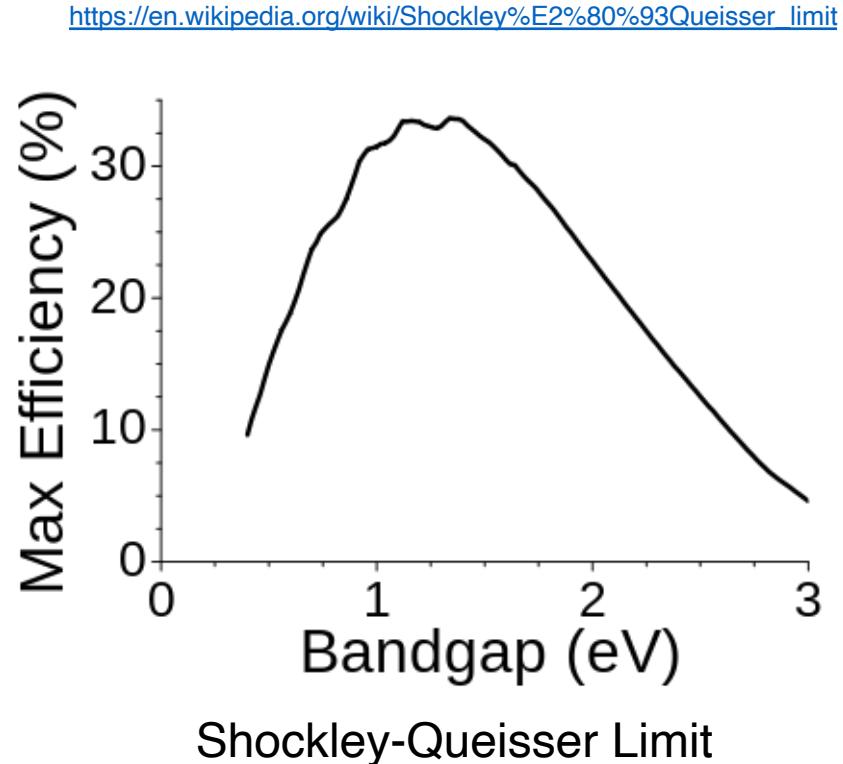
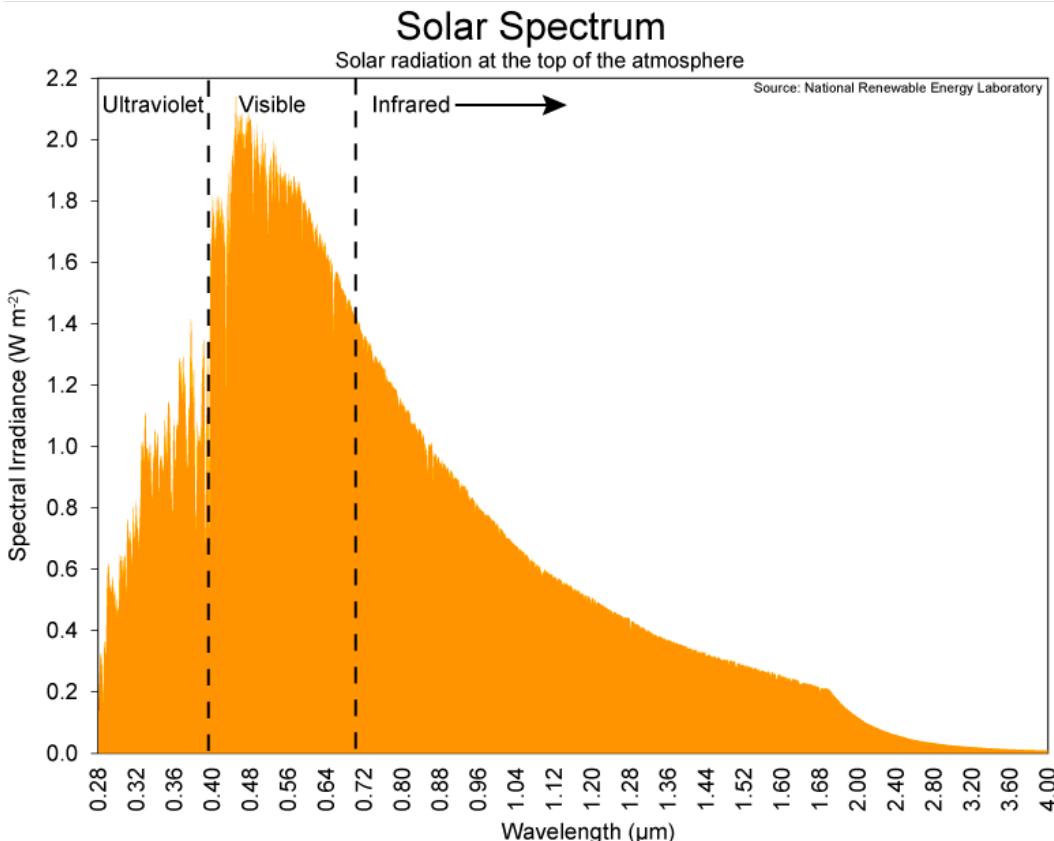


Voltage (V_{oc}) \propto Band gap
Current (I_{sc}) \propto # of states



"Curvature" of electronic bands
→ "mobility" of free carriers → do carriers escape into external circuit?

The band-gap trade-off



<http://sites.gsu.edu/geog1112/global-surface-temperature/>

Solar spectrum: peaks at certain frequencies/wavelengths

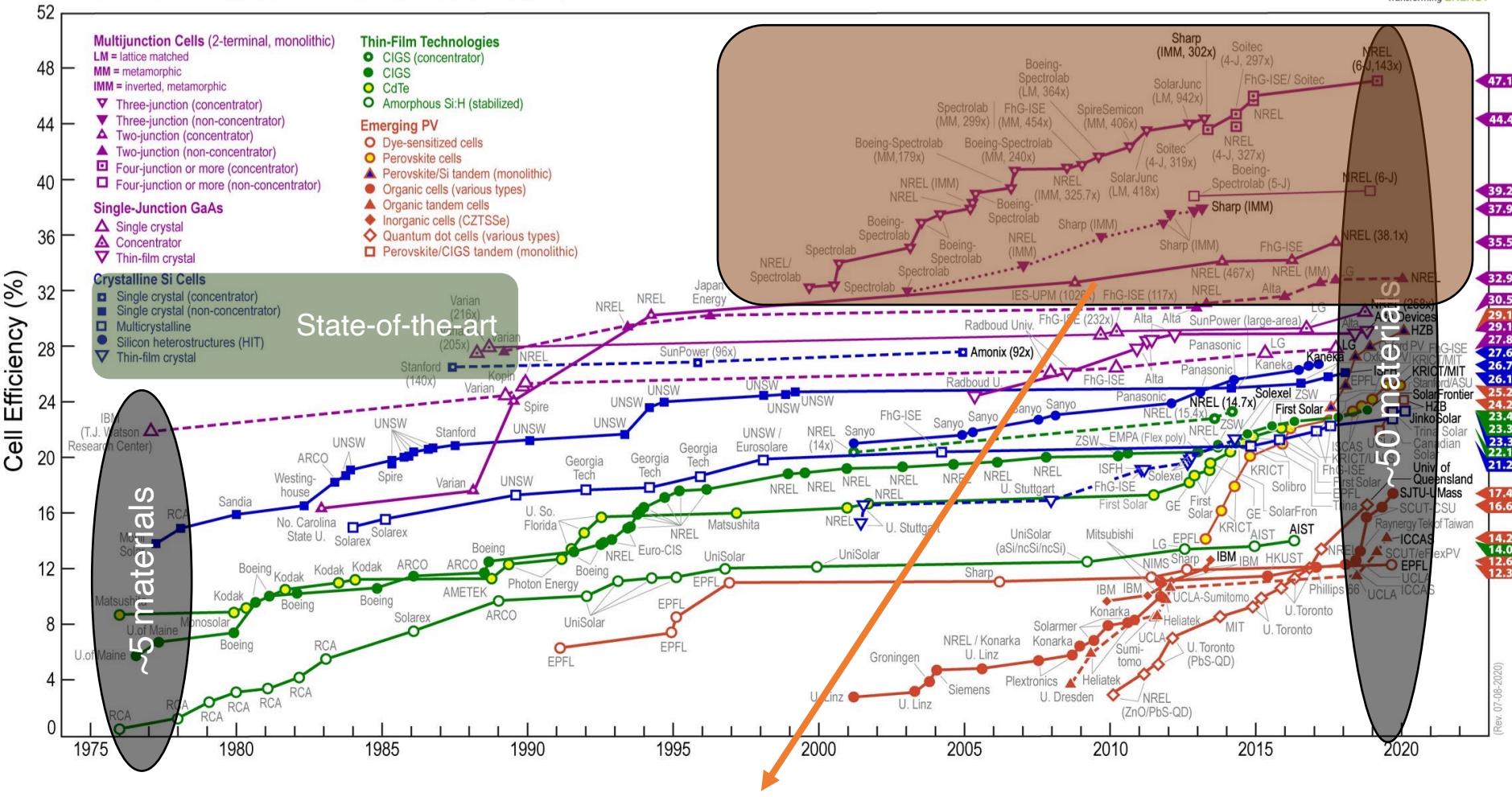
Band gap of semiconductor: needs to match this peak frequency (**1.3-1.5 eV**)

Analogous to Carnot efficiency for a “simple”, single *p-n* junction semiconductor

Several improvements in designing photovoltaics: still a long way to go

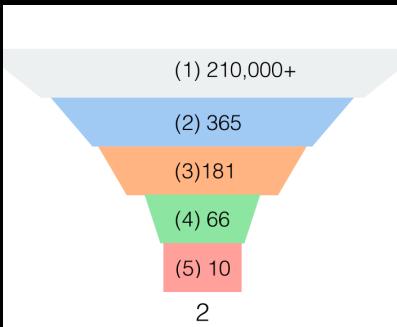
Best Research-Cell Efficiencies

NREL
Transforming ENERGY

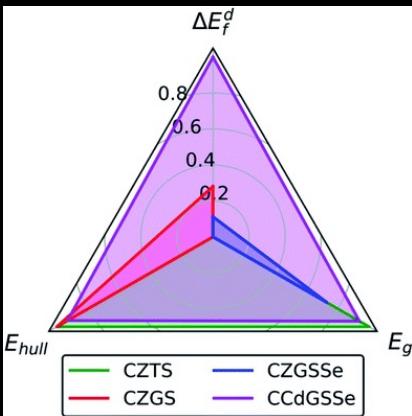


Going beyond the Shockley-Queisser limit via innovative device designs

Objectives

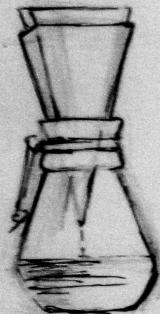


How to design better materials (electrodes)
for beyond-Li, multivalent batteries?



How to design better (defect-resistant)
photovoltaics?

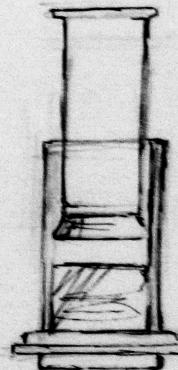
BREW METHODS



CHEMEX



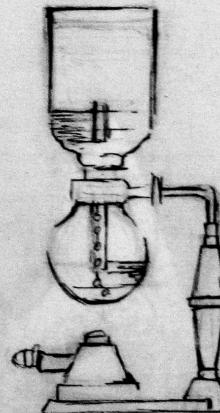
FLAT BOTTOM
POUR OVER FILTER



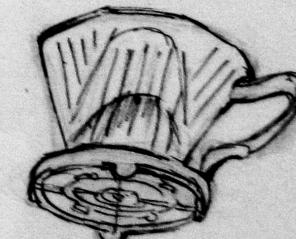
AEROPRESS



FRENCH PRESS



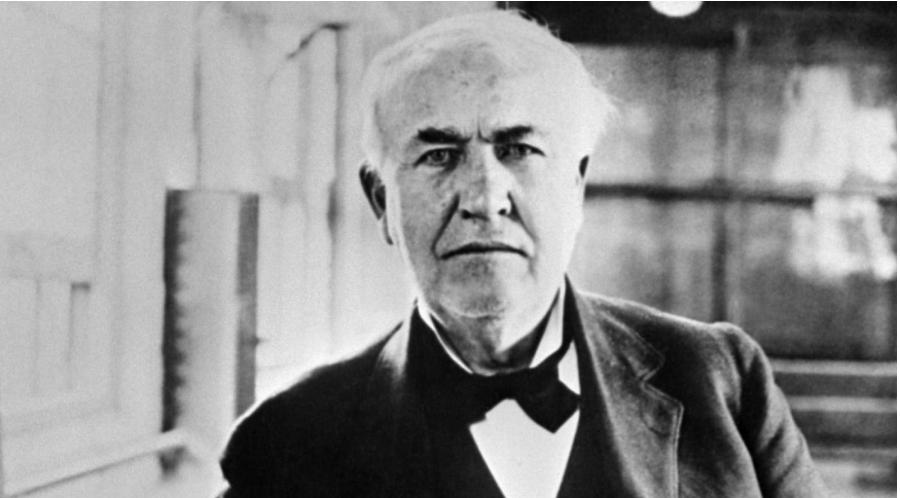
SYPHON



CLEVER DRIPPER

Methods detour (and stability)

Methods: Edison vs. Iron Man



Trial and error of candidates in a lab

Simulate and identify candidates
(on a transparent touch screen preferably)



Density functional theory:
(Approximately) predict
material properties

Machine learning: learn
from predictions to make
better predictions



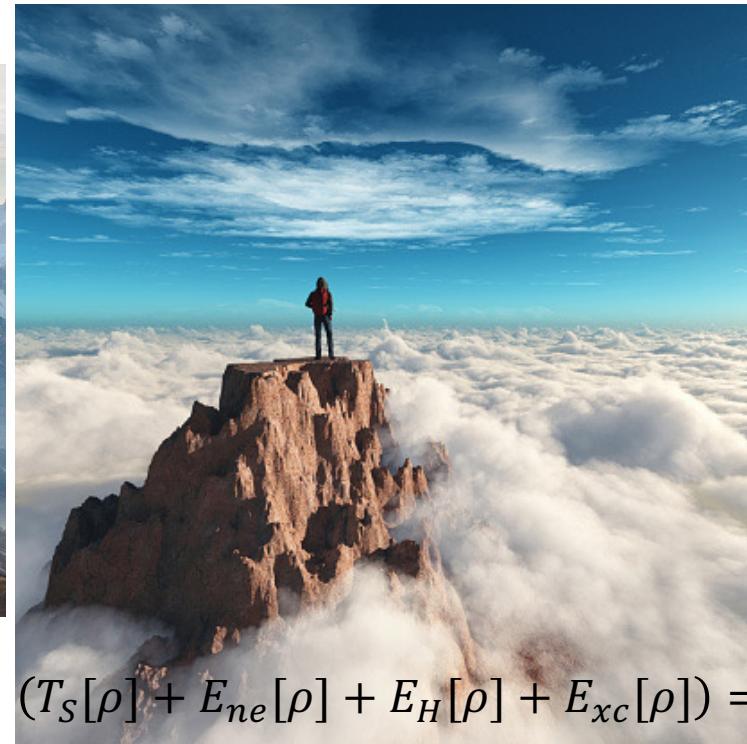
What is density functional theory (DFT)?



$$\left(\frac{p^2}{2m_e} + V(r) \right) \psi(r) = E\psi(r)$$

(kinetic energy+potential energy)*
(many-body-wavefunction)=
Total energy of system*
(many-body-wavefunction)

Analytical solution unknown for multi-electron system
Computational cost of numerical solution: $O(N^7-N^{10})$



$$(T_S[\rho] + E_{ne}[\rho] + E_H[\rho] + E_{xc}[\rho]) = E[\rho(r)]$$

(kinetic+nucleus-electron+electron-electron+
exchange-correlation) at given density
= Energy of system(at given density)

Electron density = Probability of finding electron

Computational cost of numerical solution: $\sim O(N^3)$

Variational principle $\rightarrow 0$ K!
Total energy=Internal energy~Gibbs energy

Use DFT: predict material properties

$$H\psi = E\psi \longrightarrow \text{Total energy at } 0 \text{ K} \approx \text{Gibbs energy} \rightarrow \text{Thermodynamics}$$



Density of states + Band structure \rightarrow Band gap

Energy to displace atoms \rightarrow Phonon/vibrational

Barriers for atomic migration \rightarrow Kinetics

Energy of defective structures \rightarrow Defect thermodynamics

Density functional theory^{1,2}: approximate electronic interactions into a non-interacting mean-field

- Approximation: exchange-correlation (XC) functional

DFT toolkit choice: Vienna ab initio simulation package
(<https://www.vasp.at/>)

XC functionals: Jacob's ladder of increasing accuracy

- Choice: strongly constrained appropriately normed (SCAN)³
- Or Hubbard U corrected generalized gradient approximation (GGA+ U)⁴



Structural input: databases

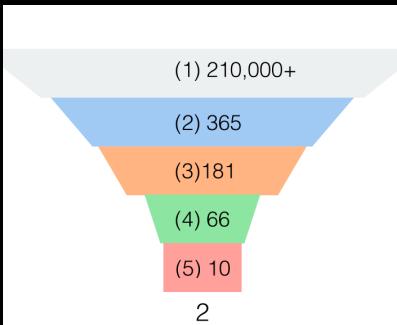
3. Sun et al., *Phys. Rev. Lett.* 2015, 115, 036402
Figure (above): Car, *Nat. Chem.* 2016, 8, 820

1. Hohenberg and Kohn, *Phys. Rev.* 1964, 136, B864

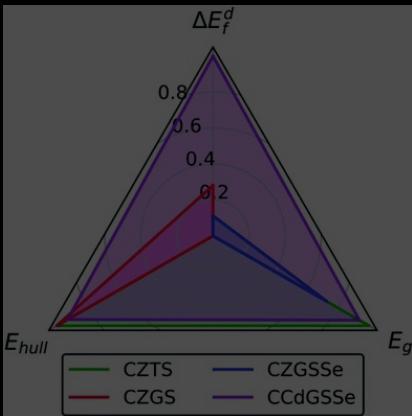
2. Kohn and Sham, *Phys. Rev.* 1965, 140, A1133

4. Perdew et al., *Phys. Rev. Lett.* 1996, 77, 3865

Objectives



How to design better materials (electrodes) for beyond-Li, multivalent batteries?

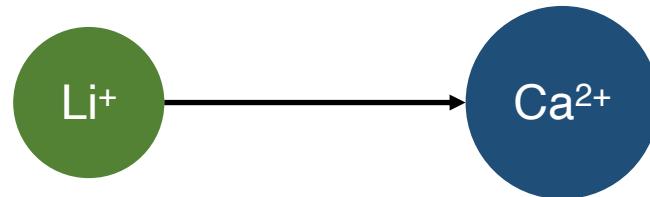


How to design better (defect-resistant) photovoltaics?

Why Multivalent or Ca batteries?

Next generation of electric devices will benefit from higher energy density storage systems

- Multi-valent == More electrons (Ca^{2+} , Mg^{2+} , Al^{3+} , etc.)
- Li-ion technology approaching fundamental limits
 - Safety, supply-chain constraints; limits on achievable energy densities
- Smaller batteries useful for portable electronics
- Lighter batteries favorable for electric vehicles

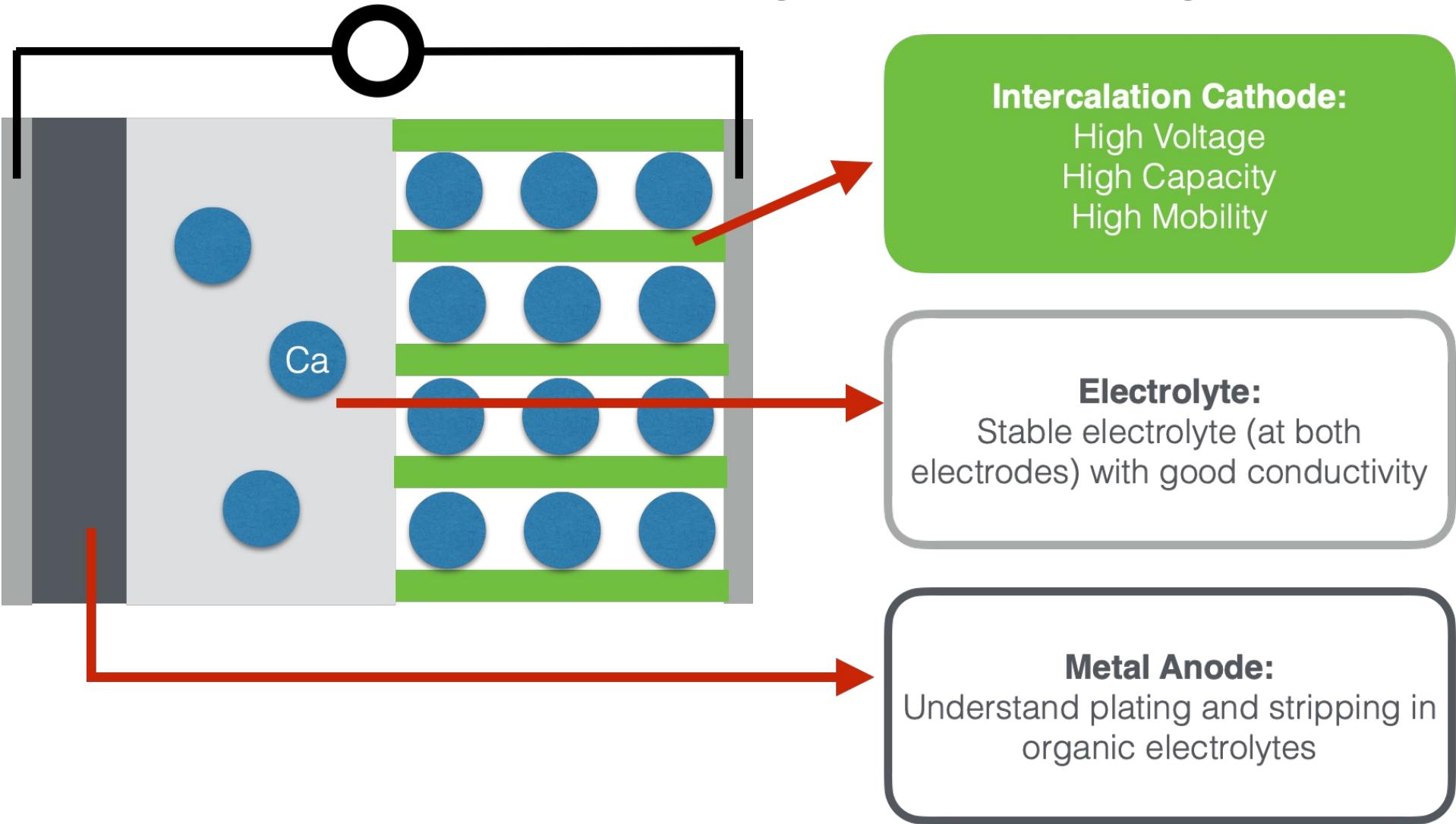


Why Ca?

- Superior volumetric capacity for Ca metal ($\sim 2077 \text{ Ah/l}$) than Li in graphite ($\sim 800 \text{ Ah/l}$)
- Ca is safer than Li, less constrained geopolitically

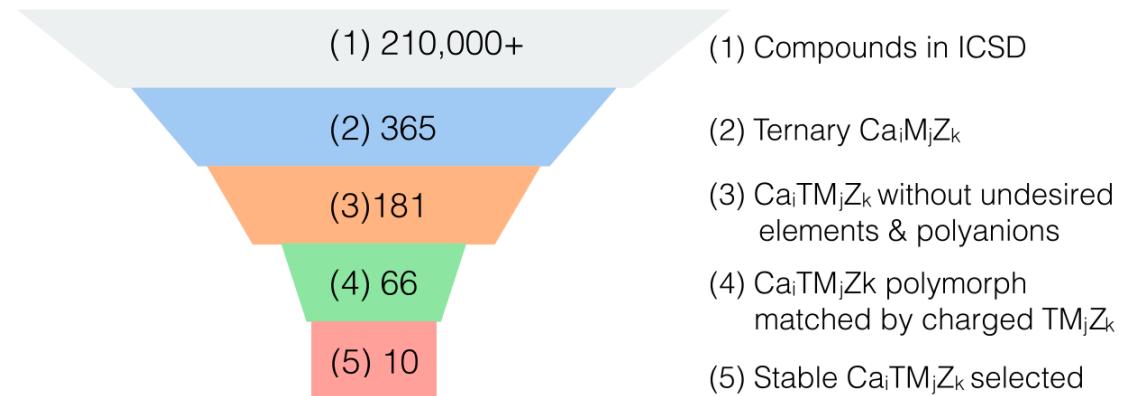
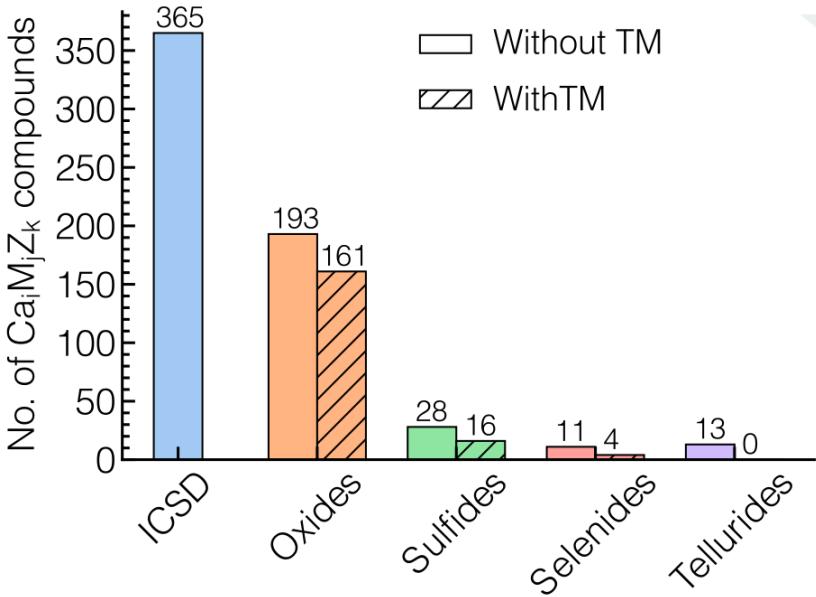


Ca cathode design challenge



Find new cathode materials that can yield **facile Ca diffusion**, reasonable voltage and capacity, and be thermodynamically stable

Let's look at ternary Ca-compounds



Inorganic crystal structure database (ICSD¹): has **> 210,000** compounds

- Only **365** are ternary compounds containing Ca
 - Compounds of composition $\text{Ca}_i\text{M}_j\text{Z}_k$; M, Z = elements other than Ca
- Let M = TM (i.e., transition metal) and Z = O, S, Se, or Te
 - Results in **181** unique compounds
- Charge-neutral charged compound (TM_jZ_k) available for $\text{Ca}_i\text{TM}_j\text{Z}_k$?
 - CaMn_2O_4 - Mn_2O_4 is ok, CaVO_3 - VO_3 not ok
 - 66** unique structures
- Either of $\text{Ca}_i\text{TM}_j\text{Z}_k$ or TM_jZ_k thermodynamically (meta)stable?
 - Decomposition energy ≤ 30 meV/atom (based on Materials Project²)
 - 10** unique compounds → evaluate mobility

Final candidates!

1. <https://icsd.products.fiz-karlsruhe.de/>
2. <https://materialsproject.org/>

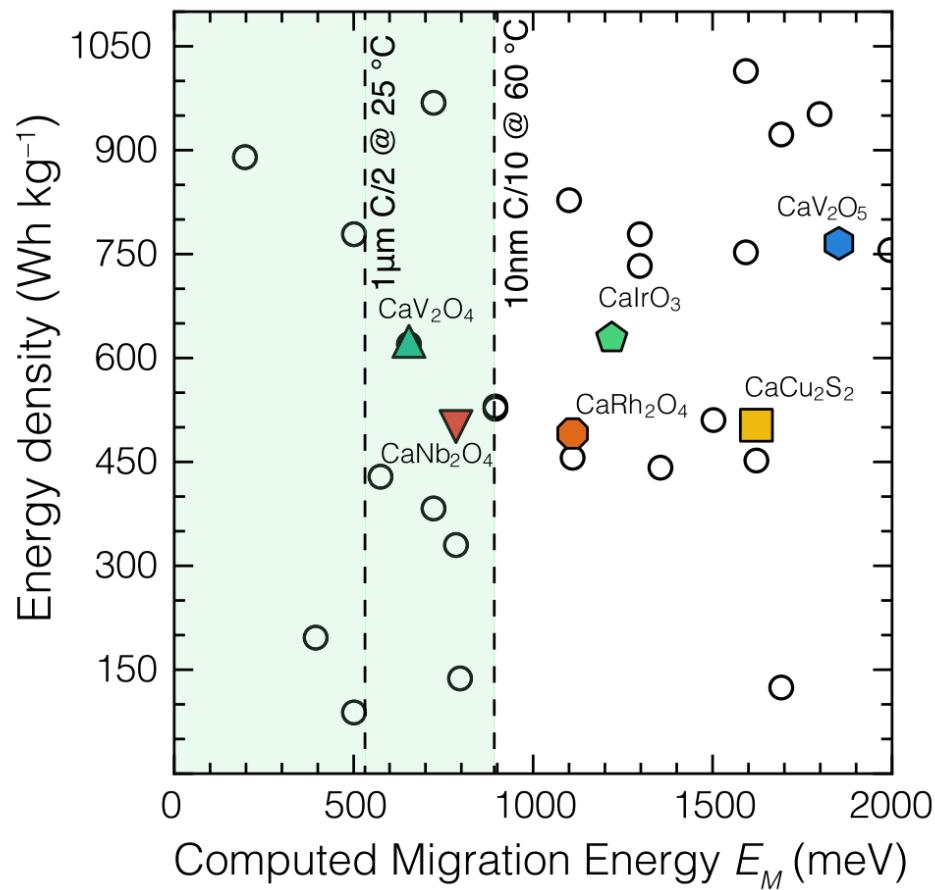
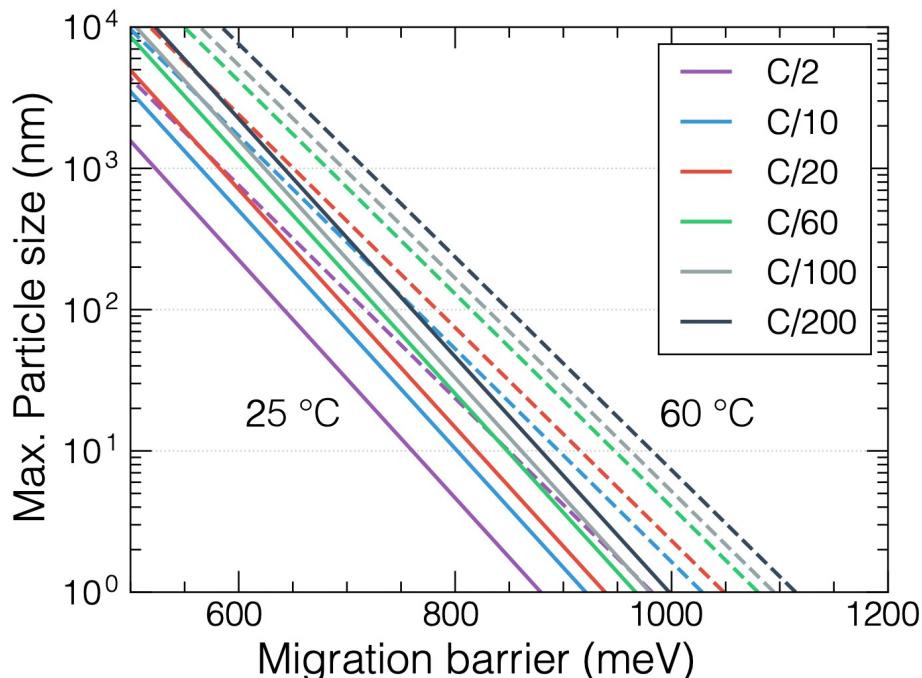
Ca diffusivity: nudged elastic band

$$D \approx \frac{x^2}{t}$$

Electrode particle size
Diffusion time (rate of operation)

$$D = v a^2 f g x_D \exp\left(-\frac{E_m}{k_B T}\right)$$

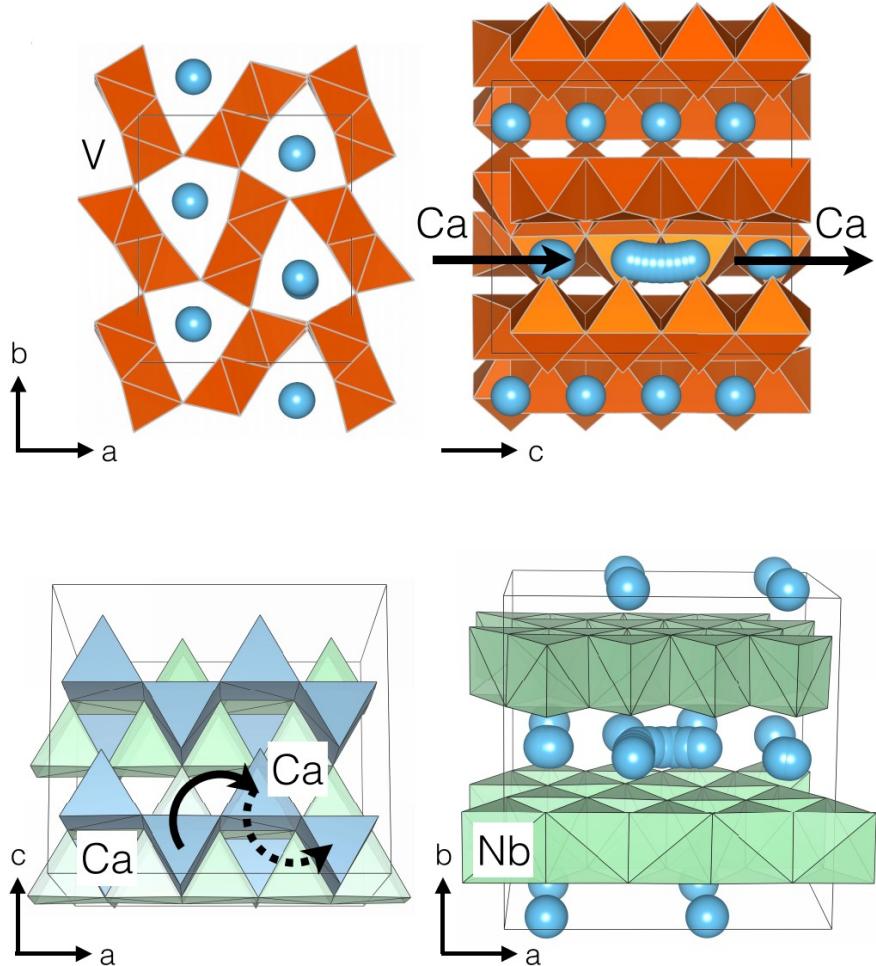
Diffusivity mainly governed by barrier
Required diffusivity \rightarrow maximum of E_m
Variables: size, time, and temperature



Max. tolerable barrier ~ 980 meV

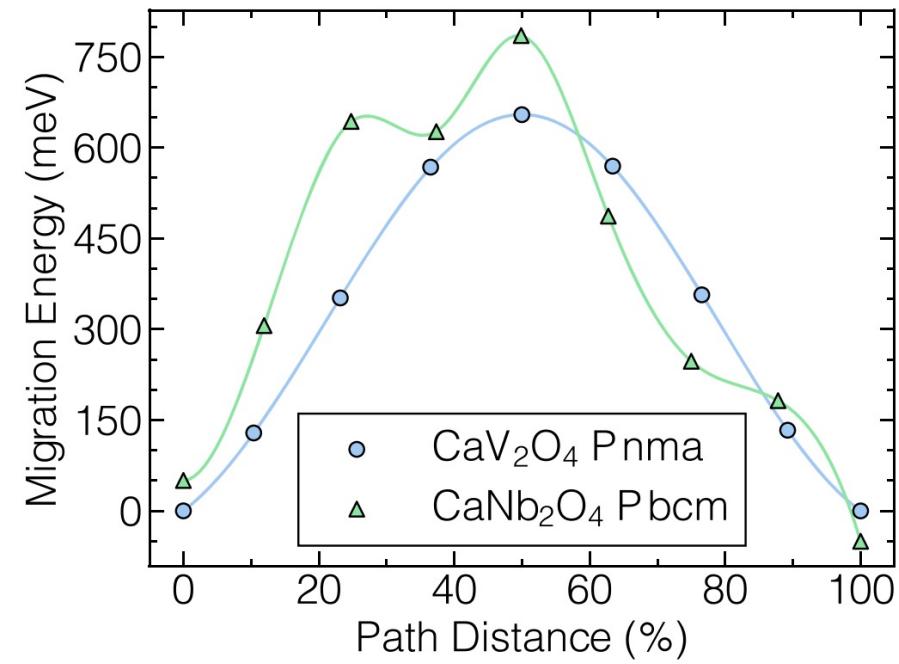
- 2 candidates display reasonable E_m
- CaV₂O₄: 654 meV
 - CaNb₂O₄: 785 meV

Migration pathways of candidates



$\text{CaV}_2\text{O}_4: 8 \rightarrow 3 \rightarrow 8$

$\text{CaNb}_2\text{O}_4: 6 \rightarrow 4 \rightarrow 6 \rightarrow 4 \rightarrow 6$

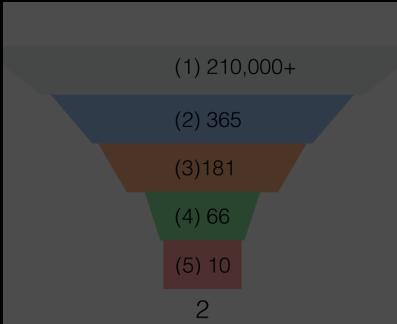


2 promising candidates!

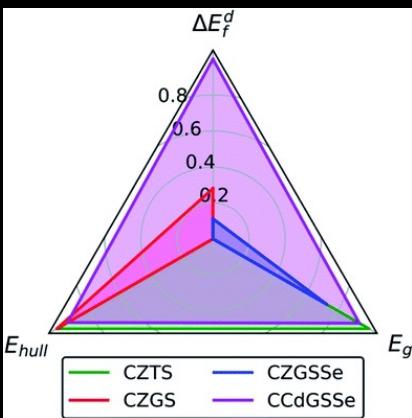
Summary

- Ca (or multivalent) batteries form an important type of high-energy-density, beyond-Li systems
 - Chief challenge is to find (positive) electrodes with facile Ca-diffusion
- Screening through ICSD for redox-active, charge-neutral and thermodynamically (meta)stable ternary Ca oxides/chalcogenides yielded 10 possible candidates
 - Evaluated using density functional theory calculations
- 2 promising candidates: CaV_2O_4 and CaNb_2O_4

Objectives

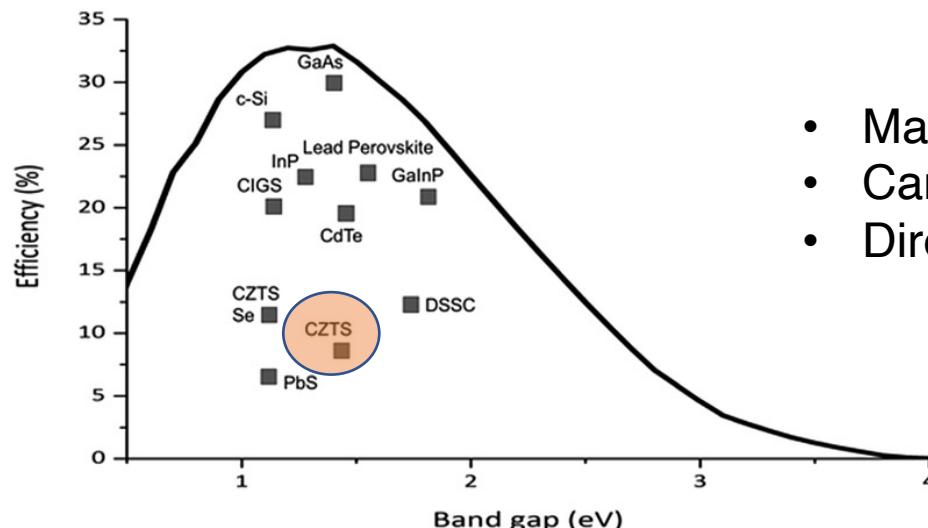


How to design better materials (electrodes) for beyond-Li, multivalent batteries?



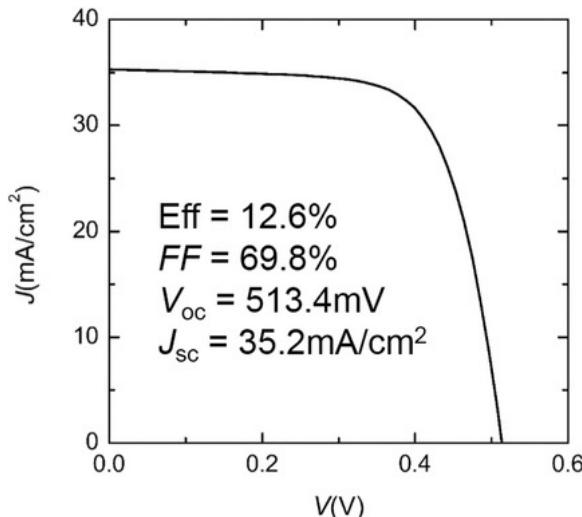
How to design better (defect-resistant) photovoltaics?

$\text{Cu}_2\text{ZnSnS}_4$ (CZTS) is a promising candidate for beyond-Si solar cells



- Made of abundant elements
- Can be synthesized through wet chemistry
- Direct band gap, 1.4-1.6 eV

Mathews et al., *Chem. Sci.* **8**, 4177 (2017)



Wang et al., *Adv. Energy Mater.* **4**, 1301465 (2014)

Often suffers from low efficiencies (~12%)

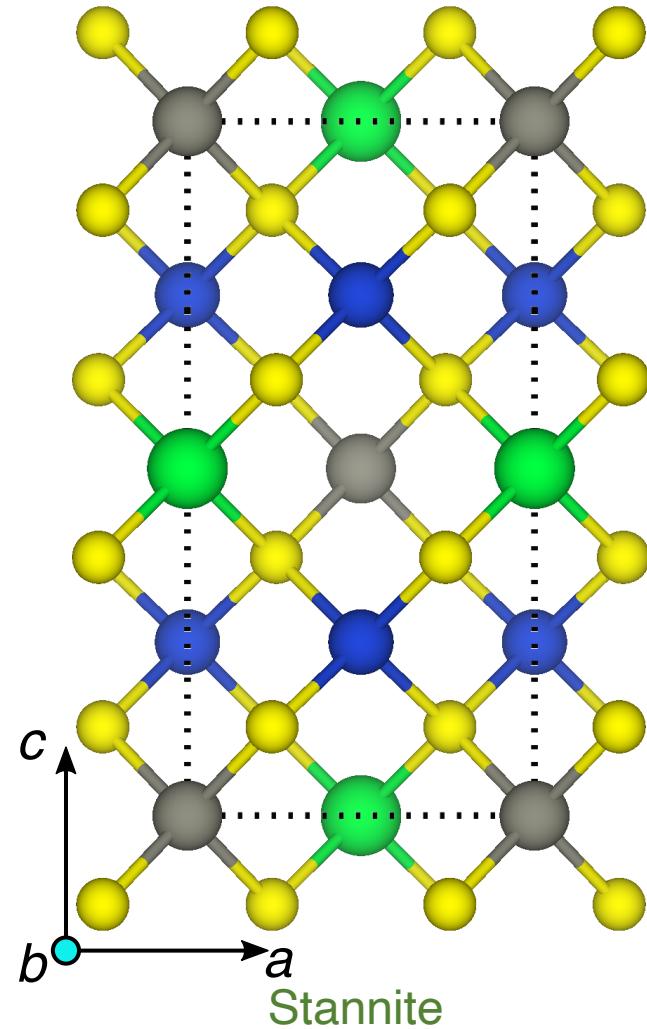
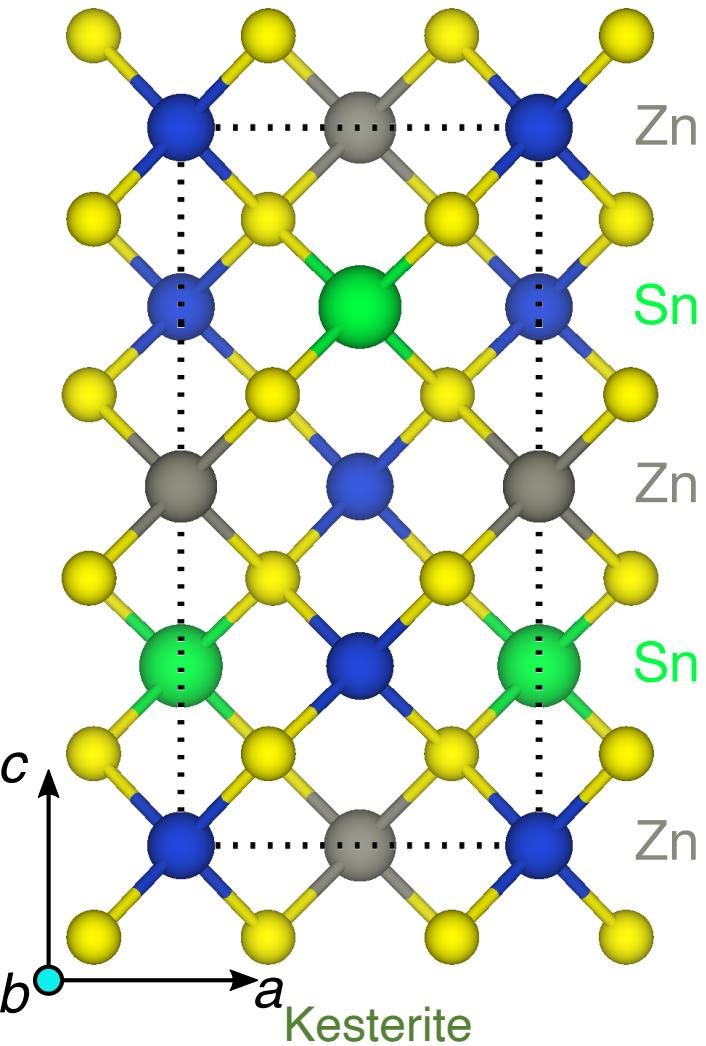
- Si is > 20%
- Due to disorder in Cu-Zn sub-lattice

Se frequently added to tune band gap

High temperature annealing to improve crystal size

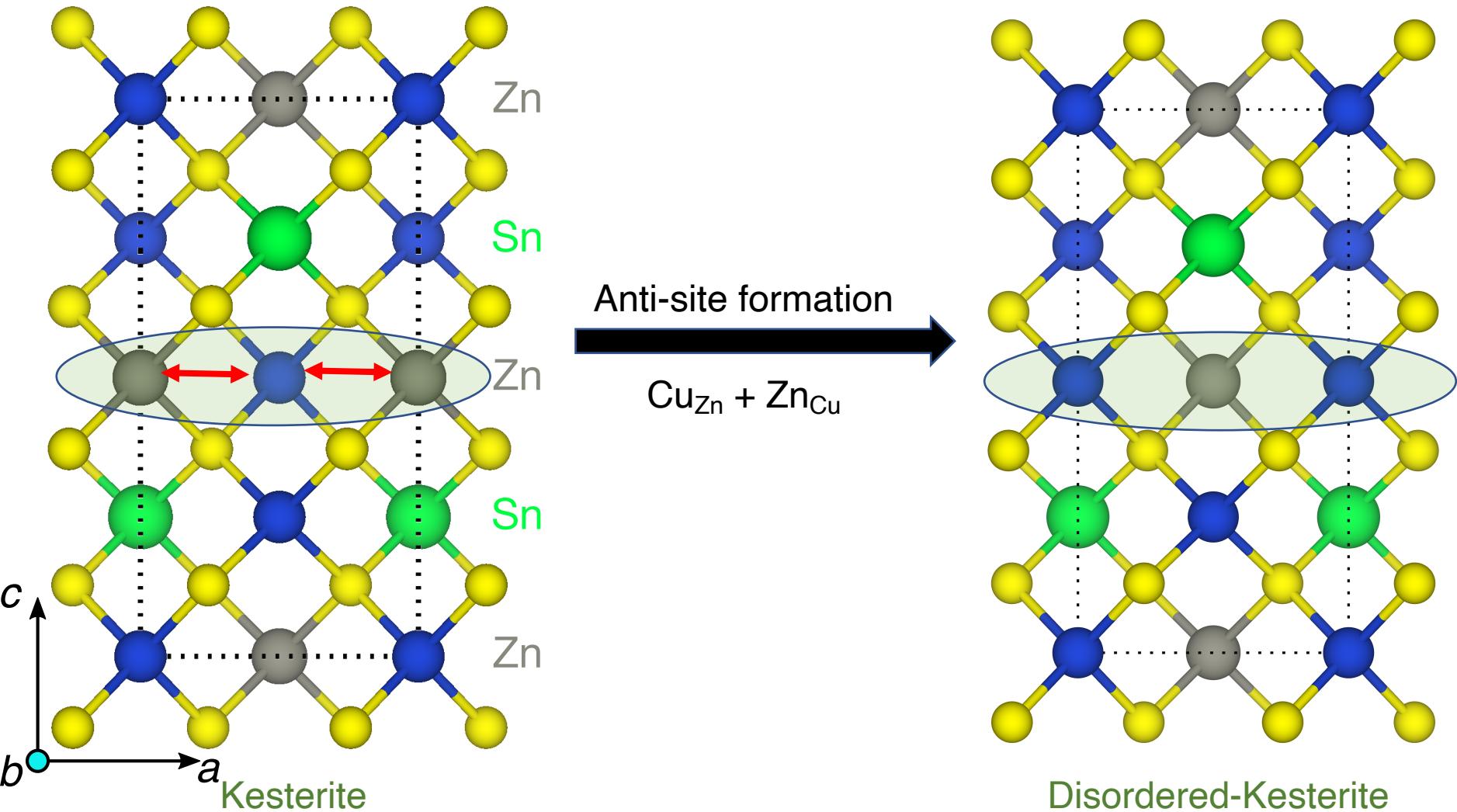
- Often leads to elemental loss and defect production

Disorder \equiv Antisites \equiv Defects



Cu-Zn: similar atomic radii
Kesterite-Stannite near degeneracy (~ 3 kJ/mol)

Disorder \equiv Antisites \equiv Defects



Cu-Zn: similar atomic radii

Kesterite-Stannite near degeneracy (~ 3 kJ/mol)

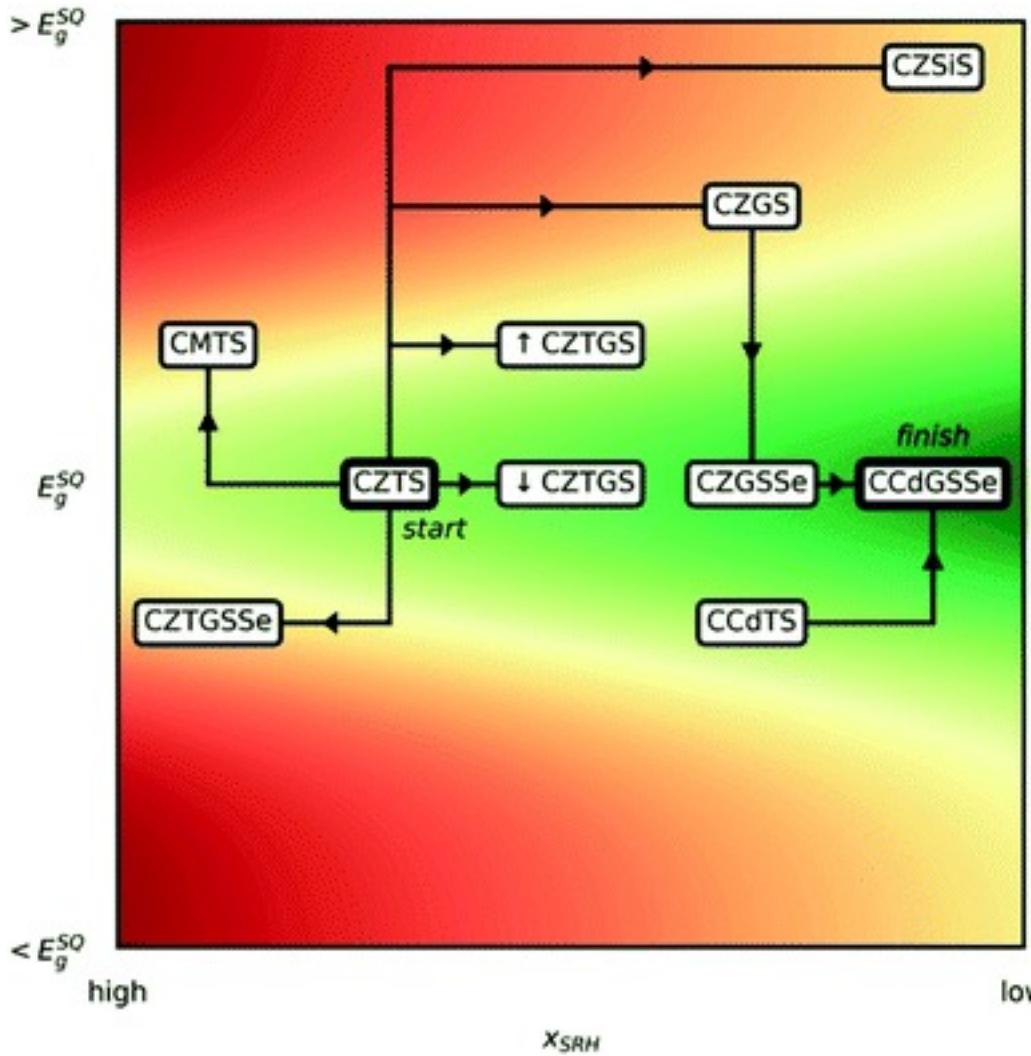
Other defects:

$\text{Sn}_{\text{Zn}} + 2\text{Cu}_{\text{Zn}}$ (electron traps)

V_{Cu} (reduce band edge fluctuations)

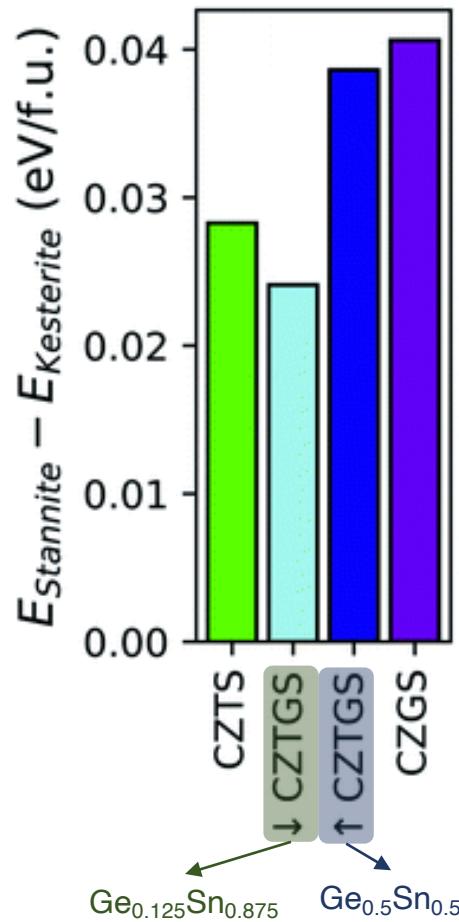
Objectives and roadmap

- Optimal band gap (1.3-1.5 eV)
- Thermodynamic stability (less than 25 meV/atom decomposition energy at 0 K)
- High defect formation energy for $\text{Cu}_{\text{Zn}} + \text{ZnCu}$ and $\text{Sn}_{\text{Zn}} + 2\text{Cu}_{\text{Zn}}$ (at least higher than CZTS)
- Low defect formation energy for V_{Cu}

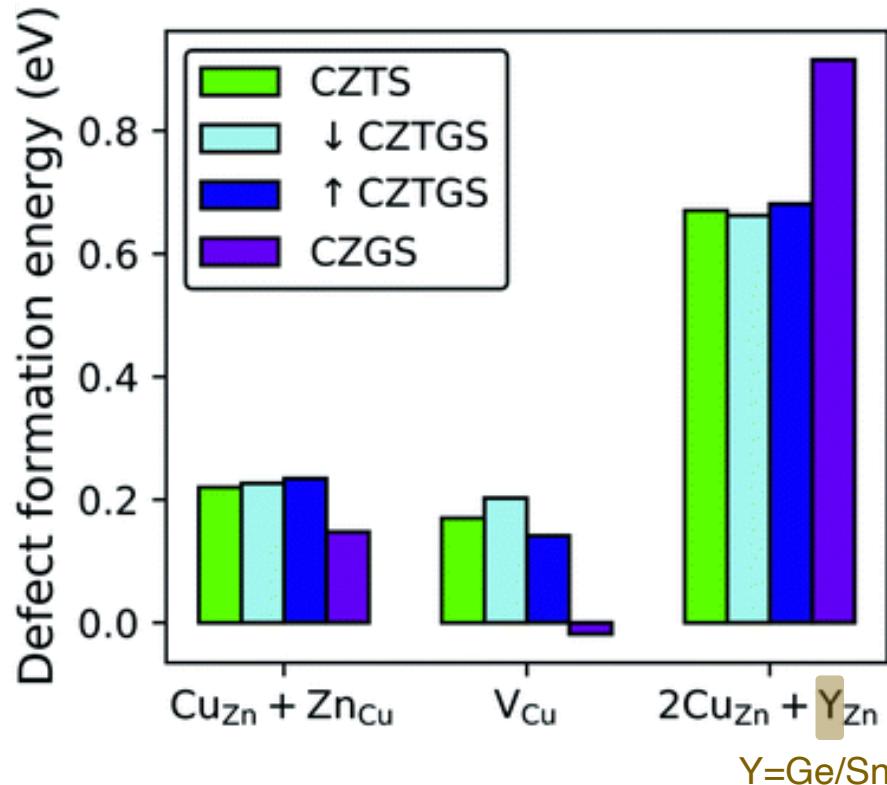


Elements explored (apart from CZTS):
M=Mg, G=Ge, Si=Si, Se=Se, Cd=Cd

Ge: suppresses Sn_{Zn} but increases band gap

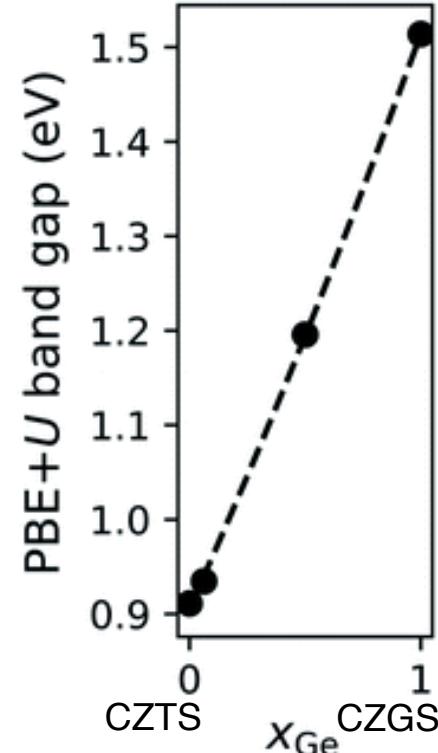


Stabilizes kesterite
Stability: Good



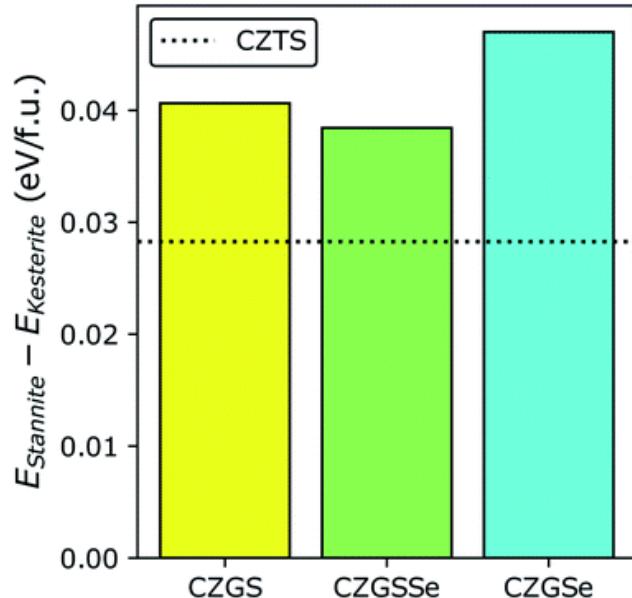
- Ge suppresses $\text{Cu}_{\text{Zn}}+\text{Zn}_{\text{Cu}}$ only at intermediate concentrations
- Largely favors V_{Cu} formation
- Suppresses $\text{Sn}_{\text{Zn}}+2\text{Cu}_{\text{Zn}}$ only at large concentrations

Defect thermodynamics: Not great



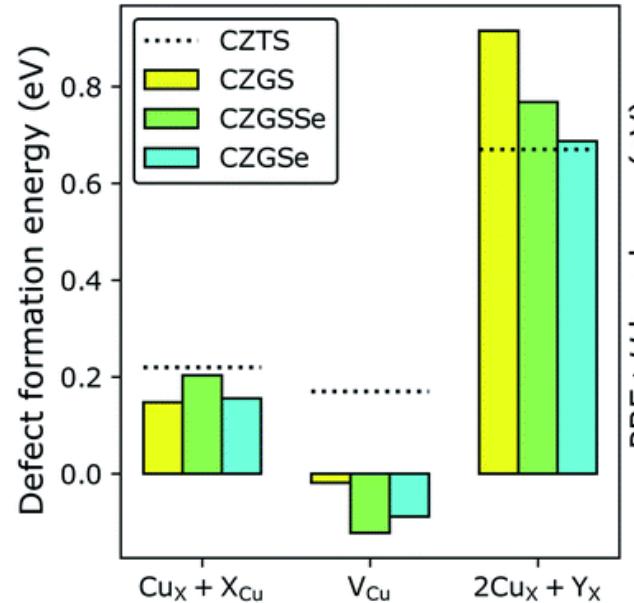
Increases band gap
Theory: 1.5 eV
Experiments: 2.1 eV
Band gap: Bad

Ge+Se: defects form more readily



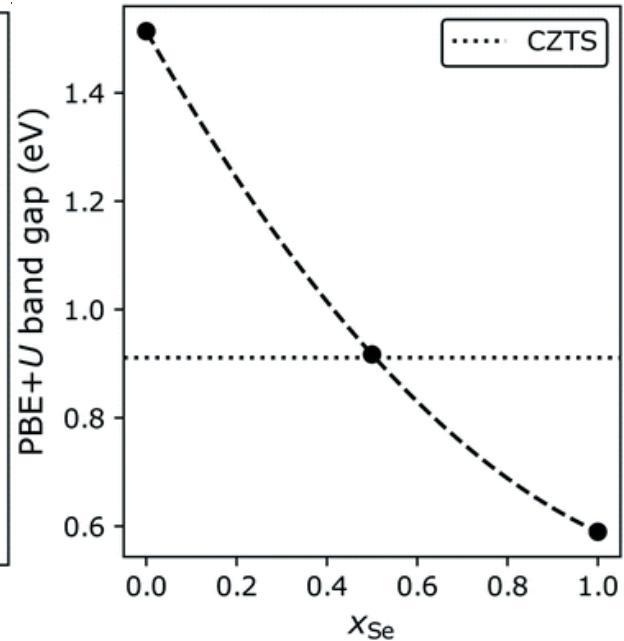
Stabilizes kesterite better than CZTS/CZGS

Stability: Good



- $\text{Cu}_{\text{Zn}} + \text{Zn}_{\text{Cu}}$: more favored than CZTS
- V_{Cu} : more favored than CZTS
- $\text{Sn}_{\text{Zn}} + 2\text{Cu}_{\text{Zn}}$: similar to CZTS

Defect thermodynamics: Bad

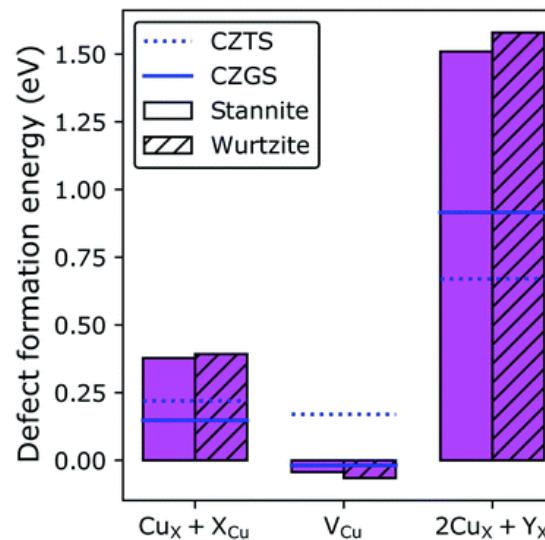
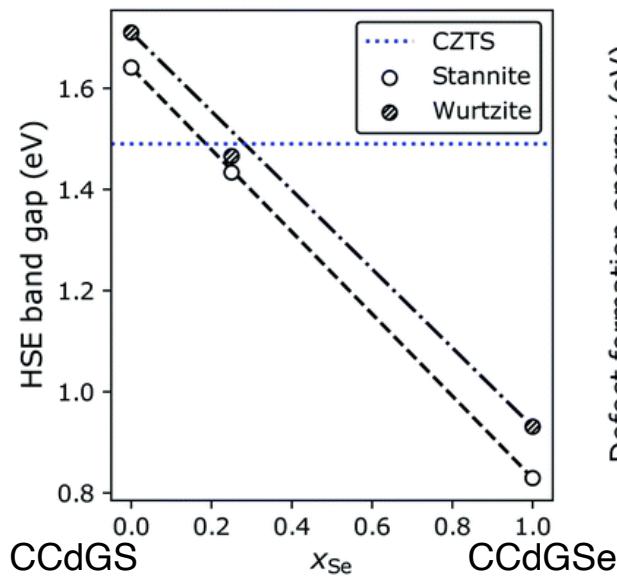
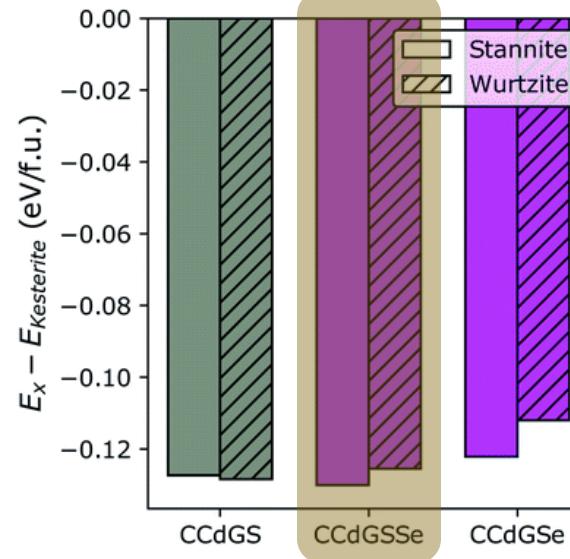
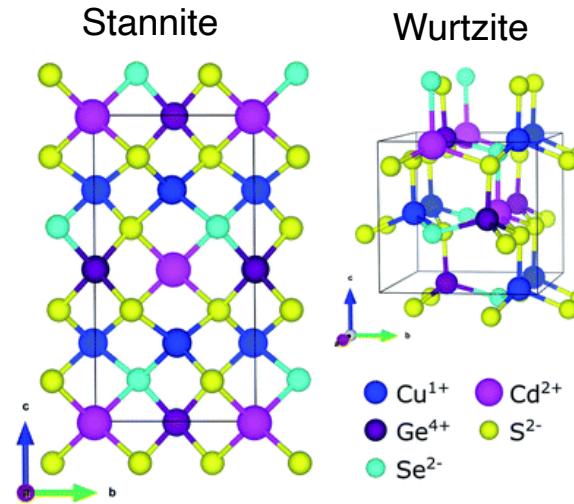


Predicted band gap: similar to CZTS

Band gap: Excellent

Overall, Ge or Ge+Se addition does not provide better photovoltaic candidate than CZTS
Any other dopants or substituent elements?

Ge+Cd+Se: optimal composition, new photovoltaic candidate



- Stable polymorph of $\text{Cu}_2\text{CdGeS}_3\text{Se}$: stannite, not kesterite
- Wurtzite's stability similar to stannite
Stannite/Wurtzite could still be beneficial

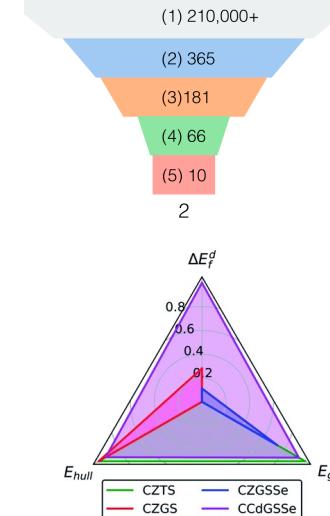
Stability: Ok

- $\text{Cu}_{\text{Zn}}+\text{Zn}_{\text{Cu}}$ and $\text{Sn}_{\text{Zn}}+2\text{Cu}_{\text{Zn}}$: better suppressed than CZTS/CZGS
- V_{Cu} formation: more favored than CZTS

Defect formation: Excellent

- Predicted band gap: similar to predicted gap for CZTS
- HSE functional: typically agrees with experiments for $\text{S}^{2-}/\text{Se}^{2-}$

Band gap: Excellent



Conclusions and Acknowledgments

- Removing material bottlenecks is important for improving performance of energy devices
 - Need better batteries (Ca vs. Li)
 - Need better photovoltaics (sulfides vs. silicon)
- Ca-containing ternary compounds from ICSD screened
 - Screening criteria: redox-activity, charge-neutrality, and thermodynamic stability
 - 2 possible candidates: CaV_2O_4 and CaNb_2O_4
- Computational search for chalcogenide semiconductors that exhibit optimal band gap with higher defect formation energy for detrimental defects and better structural stability
 - Optimal candidate is $\text{Cu}_2\text{CdGeS}_3\text{Se}$ (CCdGSSe)

Ca-batteries:

“Searching ternary oxides and chalcogenides as positive electrodes for calcium batteries”, W. Lu, J. Wang, G.S. Gautam, and P. Canepa, **Chem. Mater.** **2021**, *33*, 5809-5821

Photovoltaics:

“Optimizing kesterite solar cells from $\text{Cu}_2\text{ZnSnS}_4$ to $\text{Cu}_2\text{CdGe}(\text{S},\text{Se})_4$ ”, R.B. Wexler, G.S. Gautam, and E.A. Carter, **J. Mater. Chem. A** **2021**, *9*, 9882-9897



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