Assignment 4

1. Heart Start produces automated external defibrillators (AEDs) in each of two different plants (A and B). The unit production costs and monthly production capacity of the two plants are indicated in the table below. The AEDs are sold through three wholesalers. The shipping cost from each plant to the warehouse of each wholesaler along with the monthly demand from each wholesaler are also indicated in the table. How many AEDs should be produced in each plant, and how should they be distributed to each of the three wholesaler warehouses so as to minimize the combined cost of production and shipping?

	Unit Shipping Cost			Unit	Monthly
	Warehouse 1	Warehouse 2	Warehouse 3	– Production	Production
				Cost	Capacity
Plant A	\$22	\$14	\$30	\$600	100
Plant B	\$16	\$20	\$24	\$625	120
Monthly Demand	80	60	70		

Solution:

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/*Assigning variables to the given data */
/* Plant A Warehouse 1 = X1 */
/* Plant A Warehouse 2 = X2 */
/* Plant A Warehouse 3 = X3 */
/* Plant B Warehouse 1 = X4 */
/* Plant B Warehouse 2 = X5 */
/* Plant B Warehouse 3 = X6 */
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/* As demand and supply are not equal, to solve in transportation method we are adding **2 dummy** variables in order to match the demand and supply*/

Min M = 622 X1 + 614 X2 + 630 X3 + 641 X4 + 645 X5 + 649 X6 + 0 X7 + 0 X8;

2. **Oil Distribution** Texxon Oil Distributors, Inc., has three active oil wells in a west Texas oil field. Well 1 has a capacity of 93 thousand barrels per day (TBD), Well 2 can produce 88 TBD, and Well 3 can produce 95 TBD. The company has five refineries along the Gulf Coast, all of which have been operating at stable demand levels. In addition, three pump stations have been built to move the oil along the pipelines from the wells to the refineries. Oil can flow from any one of the wells to any of the pump stations, and from any one of the pump stations to any of the refineries, and Texxon is looking for a minimum cost schedule. The refineries' requirements are as follows.

Refinery	R1	R2	R3	R4	R5
Requirement (TBD)	30	57	48	91	48

The company's cost accounting system recognizes charges by the segment of pipeline that is used. These daily costs are given in the tables below, in dollars per thou- sand barrels.

То		Pump A		Pump B	Pun	Pump C		
	Well 1 1.52		2	1.60 1.		.40		
From	Well 2	1.70		Well 2 1.70		1.63	1.	.55
	Well 3	1.45		1.57	1.	1.30		
То		R1	R2	R3	R4	R5		
	Pump A	5.15	5.69	6.13	5.63	5.80		
From	Pump B	5.12	5.47	6.05	6.12	5.71		
	Pump C	5.32	6.16	6.25	6.17	5.87		

I. What is the minimum cost of providing oil to the refineries? Which wells are used to capacity in the optimal schedule? Formulation of the problem is enough.

Solution:

Formulating from the given:

	Pump A	Pump B	Pump C	Capacity-TBD
Well 1	1.52	1.60	1.40	93
Well 2	1.70	1.63	1.55	88
Well 3	1.45	1.57	1.30	95
R1	5.15	5.12	5.32	30
R2	5.69	5.47	6.16	57
R3	6.13	6.05	6.25	48
R4	5.63	6.12	6.17	91
R5	5.80	5.71	5.87	58

Pumps = (P_A, P_B, P_C) ; Wells = (w_{1, W_2, W_3}) ; Refineries = (R_{1,R_2,R_3,R_4,R_5})

$$\begin{aligned} \text{Min, M} &= 1.52 \text{ P}_{AW1} + 1.60 \text{ P}_{BW1} + 1.40 \text{ P}_{CW1} + 1.70 \text{ P}_{AW2} + 1.63 \text{ P}_{BW2} + 1.55 \text{ P}_{CW2} + 1.45 \text{ P}_{AW3} + 1.57 \text{ P}_{BW3} + \\ &1.30 \text{ P}_{CW3} + 5.15 \text{ P}_{AR1} + 5.12 \text{ P}_{BR1} + 5.32 \text{ P}_{CR1} + 5.69 \text{ P}_{AR2} + 5.47 \text{ P}_{BR2} + 6.16 \text{ P}_{CR2} + 6.13 \text{ P}_{AR3} + 6.05 \text{ P}_{BR3} + \\ &6.25 \text{ P}_{CR3} + 5.63 \text{ P}_{AR4} + 6.12 \text{ P}_{BR4} + 6.17 \text{ P}_{CR4} + 5.80 \text{ P}_{AR5} + 5.71 \text{ P}_{BR5} + 5.87 \text{ P}_{CR5} \end{aligned}$$

Well Constraints – Supply

$$P_{AW1} + P_{BW1} + P_{CW1} = 93$$

$$P_{AW2} + P_{BW2} + P_{CW2} = 88$$

$$P_{AW3} + P_{BW3} + P_{CW3} = 95$$

Refinery Constraints – Demand

$$P_{AR1} + P_{BR1} + P_{CR1} = 30$$

$$P_{AR2} + P_{BR2} + P_{CR2} = 57$$

$$P_{AR3} + P_{BR3} + P_{CR3} = 48$$

$$P_{AR4} + P_{BR4} + P_{CR4} = 91$$

$$P_{AR5} + P_{BR5} + P_{CR5} = 48$$

$$P_{ARD} + P_{BRD} + P_{CRD} = 2$$

/* As demand and supply are not equal, we added **dummy variables** in order to match the demand and supply*/

$$P_{AW1} + P_{BW1} + P_{CW1} = P_{AR1} + P_{AR2} + P_{AR3} + P_{AR4} + P_{AR5} + P_{ARD}$$

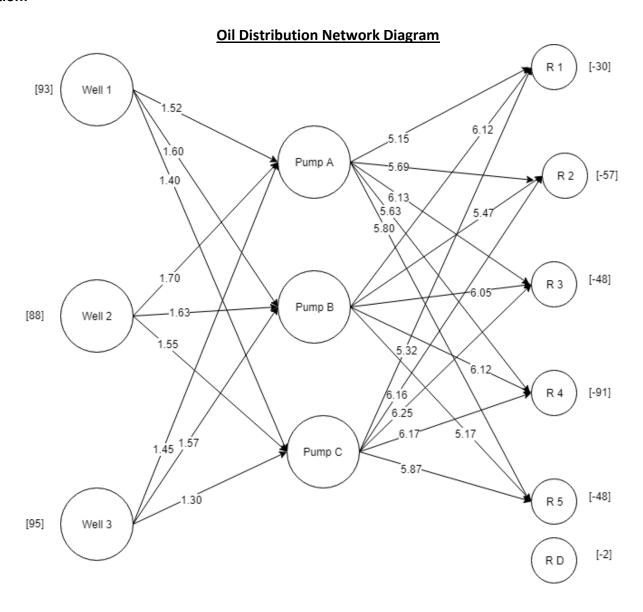
$$P_{AW2} + P_{BW2} + P_{CW2} = P_{BR1} + P_{BR2} + P_{BR3} + P_{BR4} + P_{BR5} + P_{BRD}$$

$$P_{AW3} + P_{CW3} + P_{CW3} = P_{CR1} + P_{CR2} + P_{CR3} + P_{CR4} + P_{CR5} + P_{CRD}$$

Where, $P_{WR} \ge 0$; $P_{UMPS} = (P_A, P_B, P_C)$; $P_{UMPS} = (P_A, P_C)$; $P_{$

II. Show the network diagram corresponding to the solution in (a). That is, label each of the arcs in the solution and verify that the flows are consistent with the given information

Solution:



Optimal Solution Network Diagram

Solving the above equations in R we found that Well 3 is the optimal schedule.

