

Hands-on 11

(a) Use the aggregate method in the aggregate method we consider the total cost across all the insertions and calculate the average cost per insertion.

when inserting the i^{th} element, if a resize operation is not needed - the existing happens cost $O(1)$ as it involves copying the existing elements to the new table of size $2k$ (k is no. of resizes performed).

$$\text{Total cost} = O(n) \cdot k \Rightarrow O(n \log n)$$

$$\text{cost per insertion} = O(\log n)$$

$$\text{Runtime per insertion} = O(\log n)$$

$$\text{Total time is } O(n) \times \log(n+1)$$

(b) Accounting method.

In this method, we assign each insertion a higher amortized cost the store credits that pay for future resizing costs.

Pseudo code -

for $i=1$ to n

if table is full

newtable = create new table

with size then copy elements from old table to new table

table = new table

insert element i into table

initial charge = 0

for $i = 1$ to n

charge $+= 2$

if table doubled in size from
into $2m$

credits $+= m$

total charge = $2 * n = O(n)$

total credits = $m + 2m - \frac{n}{2} * m = O(n)$

Amortized cost per insertion

= total / n

= $O(n/n)$

= $O(1)$

Runtime per insertion $O(1)$

Total time $O(n)$