

69. Sqrt(x)

Hint



Easy



7.2K

4.3K



Companies

Given a non-negative integer x , return the square root of x rounded down to the nearest integer. The returned integer should be **non-negative** as well.

You **must not** use any built-in exponent function or operator.

- For example, do not use `pow(x, 0.5)` in c++ or `x ** 0.5` in python.

Example 1:

Input: $x = 4$

Output: 2

Explanation: The square root of 4 is 2, so we return 2.

Example 2:

Input: $x = 8$

Output: 2

Explanation: The square root of 8 is 2.82842..., and since we round it down to the nearest integer, 2 is returned.

Constraints:

- $0 \leq x \leq 2^{31} - 1$

Accepted 1.6M

Submissions 4.2M

Acceptance Rate 37.8%

Brute force: Start checking from 1 to x and at every step check if $i^2 == x$ or not.

```
for (i: 1 to x)
{
    if ( $i * i == x$ ) return i
    else if ( $i * i > x$ ) return -1
}
```

Optimized approach: Using Binary Search

As we are checking on sorted integers from 1 to x , instead of linear search we can use binary search.

```
l = 1
r = x

while (l <= r)
{
    m = (l + r) / 2
    m = x / m

    if (m * m == x) return m
    else if (m * m < x) l = m + 1
    else r = m - 1
}

return r
```

Diagram illustrating the binary search logic for finding the integer square root of x :

- Initial values: $l = 1$, $r = x$
- While loop condition: $l \leq r$
- Inside the loop:
 - Calculate $m = \frac{l+r}{2}$ (circled in green)
 - Calculate $m = x/m$ (indicated by an arrow from the circled formula)
 - Check if $m * m == x$. If true, return m .
 - Else if $m * m < x$, update $l = m + 1$ (indicated by an arrow from the condition).
 - Else $r = m - 1$ (indicated by an arrow from the condition).
- After the loop, return r .

In both the above approaches the logic is correct but calculating $m * m$ for large input x we get integer overflow. To avoid that we can either use

- ① unsigned long long int l, m, r
(or)
- ② calculate m using different formula

$$m = l + \frac{r-l}{2}$$

$$= l + \frac{(r-l)}{2}$$

and instead of checking $m * m == x$
check if $m == x/m$
and
 $m < x/m$

$$T(n) = O(\log n)$$

Takeaway:

dealing with overflow using simple techniques on mathematical expressions

note: To check if x is a perfect square or not
→ A perfect square is formed by adding consecutive odd numbers.

$$\text{i.e. } 1 + 3 = 4$$

$$1 + 3 + 5 = 9$$

$$1 + 3 + 5 + 7 = 16$$

$$1 + 3 + 5 + 7 + 9 = 25$$

$$1+3+5+7+9=25$$

⋮

So

$a = 1$

while ($a < x$)

{

$a = a + (a+2)$

if ($a == x$) return true

}

return false