

Development of an Algorithm Improving Label Arrangements in Offset Printing

Geun Soo Jang^a, Taehyeong Kim^a, Ki Man Kong^c, Jeong Rye Park^a,
Jong-hyeon Seo^b, Sang-hyup Seo^{a,*}, Shin won Yoon^a

^a*Finance.Fishery.Manufacture Industrial Mathematics Center on Big Data, Pusan National University, Busan, 46241, Republic of Korea*

^b*Chubu University Academy of Emerging Science, Kasugai, 487-0027, Japan*

^c*World Komax Co., Ltd., 1505, Centum Jungang-Ro 48, Haeundae-Gu, Busan, 48059, Republic of Korea*

Abstract

One of the most classic problems in the manufacturing industry is inventory processing. There is a way to effectively reduce inventory by changing the array of the pieces on the printing plates in the offset printing. It is setting an upper limit of acceptable for each plate, and carrying out complete enumeration. This method dramatically reduces the operating time of the algorithm. The advantage of this method is that there is only change the arrangement of the pieces on the plates.

Keywords: Offset Printings, Combinations with Repetition, Label Arrangements, Inventory Managements

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1. Introduction

A combination with repetition is the number of cases, where k elements are selected from among different n elements allowing repetition [1]. It is indicated

*Corresponding author

Email addresses: sand621@naver.com (Geun Soo Jang), xogud7936@pusan.ac.kr (Taehyeong Kim), kennethkong@worldkomax.net (Ki Man Kong), parkjr@pusan.ac.kr (Jeong Rye Park), hyeonni94@gmail.com (Jong-hyeon Seo), saibie1677@gmail.com (Sang-hyup Seo), ysw0123@pusan.ac.kr (Shin won Yoon)

with the symbol ${}_nH_k$ and the following is established.

$${}_nH_k = {}_{n+k-1}C_k = \frac{(n+k-1)!}{(n-1)!k!} \quad (1)$$

5 For instance, the combination with repetition ${}_2H_4$ to select four elements from among two elements A and B comprises the following five cases.

- (1) [A, A, A, A] : a list consisting of four A's
- (2) [A, A, A, B] : a list consisting of three A's and one B
- (3) [A, A, B, B] : a list consisting of two each of A's and B's
- 10 (4) [A, B, B, B] : a list consisting of one A and three B's
- (5) [B, B, B, B] : a list consisting of four B's

Among the above cases, if we want to obtain three A's and nine B's, then we can choose $[A, B, B, B] \times 3$. Also, we consider the following as another case.

$$[A, A, B, B] \times 1 + [A, B, B, B] \times 1 + [B, B, B, B] \times 1 \quad (2)$$

In this case, we can get the three A's and nine B's. However, the former case
15 seems to be a 'Better' because there are three different lists in (2). Let us examine the other case.

$$[A, A, A, A] \times 1 + [B, B, B, B] \times 3 - [A] \times 1 - [B] \times 3 \quad (3)$$

$[A, B, B, B] \times 3$ also seems to be 'Better' because there is no loss. Under the following conditions, $[A, B, B, B] \times 3$ is the 'Best' method.

- (1) Minimize the number of list.
- 20 (2) Minimize the loss of lists.

Offset printing, also called offset lithography, or litho-offset, in commercial printing, widely used printing technique in which the inked image on a printing plate is printed on a rubber cylinder and then transferred (i.e., offset) to paper or

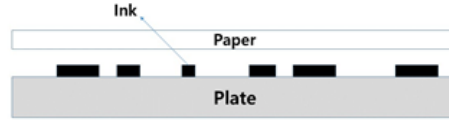


Figure 1: Offset Printing

other material. The rubber cylinder gives great flexibility, permitting printing
 25 on wood, cloth, metal, leather, and rough paper (see Figure 1) [2].

Offset printing is one of the most common ways of creating printed materials. A few of its common applications include: newspapers, magazines, brochures, stationery, and books. Compared to other printing methods, offset printing is best suited for economically producing large volumes of high quality prints in a
 30 manner that requires little maintenance [3]. To improve printing process, there were many researches in [4, 5, 6]. As an other improving, how to make the initial plates is an important issue. Above example means that what is the best arrangement in such print method.

In the past, production was based on ordering of products from companies
 35 and predictions of consumption. However, as the internet market has become popular, the production systems have been changed by consumers. Now, many factories produce only products ordered by consumers.

World Komax is a company that produces labels using the offset printing. The labels refer to stickers containing bar-codes attached to garments or shoes
 40 as follows (see Figure 2). Each bar-code in the label contains fixed information such as product names and colors, and variable information such as the date of manufacture.

Since the program of World Komax is not suitable for small quantity batch productions, the number of labels loss increased compared to the past.

45 Section 2 of this paper will describe the process of label printing using offsets. The modeling of the problem will be carried out in Section 3, and examples to help the understanding of the problem will be prepared in Section 4. The final results of the algorithm will be described in Section 5.



Figure 2: Sneaker Review : Nike Air Huarache (<http://visla.kr/?p=18146>)

2. Offset label printing process

2.1. Label printing process

Prior to describing the label printing process, we define the following terms first.

- * **Plate** : A printing plate for the offset printing (see Figure 3)
- * **Loss** : The number of labels printed in excess of the order-quantity

The offset label printing process is as follows. At first, we receive orders from customers. The order includes many types of labels and order-quantities by type (see Figure 4). Thereafter, offset printing plates are made. Many types of labels are placed on each plate so that many labels are printed at one printing. After the plates are made, we produce more labels than order-quantities using each plate. Then, the sheets are cut to the sizes of labels. As the final process, the labels are collected by type.



Figure 3: Plate and Label

2.2. Major points for cost saving

The constraint conditions and major points that will be considered in this paper for cost saving are as follows. First, one type of label should be placed on only one plate. This is to prevent different types of labels from being mixed when

- Let I be a set of products.
- For each product $i \in I$, let b_i be the number of order.
- 90 • Let $\mathbf{b} = (b_i | i \in I)$ be a vector of order-quantities.
- k is the total number of labels that can be placed in one Plate.
- π is a partition of I such that $1 \leq |P| \leq k$ for any $P \in \pi$.
- Let Γ_π be a set of matrix $A \in \text{Mat}_{\pi \times I}(\mathbf{Z})$ satisfy the following:
 - For all $(P, i) \in \pi \times I$, $A_{P,i} \geq 0$, and $A_{P,i} = 0$ if and only if $i \notin P$.
 - 95 - For each $P \in \pi$, $\sum_{i \in P} A_{P,i} = k$

Using the above notation,

$$\left\lceil \max \left\{ \frac{b_i}{A_{P,i}} \mid i \in P \right\} \right\rceil \quad (4)$$

is the number of printing of Plate P , where $\lceil \cdot \rceil$ means the ceiling. Assume that α is the cost to produce one Plate, and β is the cost of the loss of one label. Then, our goals is to obtain the following

$$\min_{\pi} \{ \alpha |\pi| + \beta E_{A,b} | A \in \Gamma_\pi \} \quad (5)$$

100 where

$$E_{A,b} = \sum_{P \in \pi} \sum_{i \in I} \left(\left\lceil \max \left\{ \frac{b_i}{A_{P,i}} \mid i \in P \right\} \right\rceil \cdot A_{P,i} - b_i \right) \quad (6)$$

means the total number of losses of labels.

Naturally, the complete enumeration using combinations with repetition is the surest way. However, this method has a problem that it takes too much time. For instance, when $n = 65$ and $k = 24$, the combination with repetition
 65 ${}_{65}H_{24}$ comprises about 2.36×10^{21} cases. Then, the calculation of the cases takes more than 658 hours, that is, more than 27 days using a super computer that can calculate 10^{15} partitions per second. Given that there are limits of the time from the date of receipt of orders to the delivery date, this is a very long computation time.

110 In this algorithm, this problem was solved by introducing any positive integers as thresholds. Thresholds mean the allowed amount of losses occurring in each plate. Adopting a partition that does not exceed the threshold will dramatically reduce the time taken.

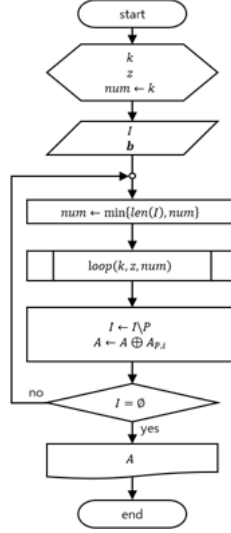


Figure 5: The Main Flowchart

Based on the foregoing, the flowchart of the algorithm can be set forth as follows. This algorithm outputs matrix A containing the label of each product when I and \mathbf{b} have been inputted for z , k , num (see Figure 5).

Meanwhile, in the case of the $loop(k, z, num)$ function, the flowchart in Figure 6 should be followed. First, the $Part(k, num)$ function finds partitions using the combination with repetition $num H_k$ and indicated in the form of a list. We set the result as $Part_list$. An appropriate P that has num pieces of products is selected from I and the loss is obtained using $Part_list$ and the printing number.

If the loss exceeds the threshold z , another $Part_list$ will be selected and the foregoing will be repeated while adjusting num until the threshold is not exceeded. As a result of this process, $A_{P,i}$ whose loss does not exceed the threshold is obtained.

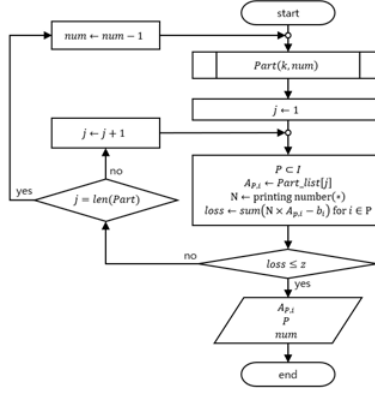


Figure 6: The Flowchart of Loop

4. Examples

This example was described to help the understanding of the problem. In this section, we assume that k is equal to 4.

Example 1. Let $I = \{A, B, C\}$ and $\mathbf{b} = (50, 30, 20)$.

130 We consider $\pi = \{\{A, B\}, \{C\}\}$ is a partition for the order-quantity vector \mathbf{b} . Without loss of generality, assume that $P_1 = \{A, B\}, P_2 = \{C\}$. Since $k = 4$, the matrix A can be found as follows.

$$A = \begin{pmatrix} 2 & 2 & 0 \\ 0 & 0 & 4 \end{pmatrix} \quad (7)$$

In this case, the printing numbers (4) of P_1 and P_2 are as follows, respectively.

$$\left\lceil \max \left\{ \frac{b_i}{A_{P_1,i}} \mid i \in P_1 \right\} \right\rceil = \left\lceil \max \left\{ \frac{50}{2}, \frac{30}{2} \right\} \right\rceil = 25 \quad (8)$$

and

$$\left\lceil \max \left\{ \frac{b_i}{A_{P_2,i}} \mid i \in P_2 \right\} \right\rceil = \left\lceil \max \left\{ \frac{20}{4} \right\} \right\rceil = 5. \quad (9)$$

135 We can see the Figure 7 for more details.

It can be seen that the total number of Loss $E_{A,\mathbf{b}}$ is 20.

Now, we consider a new partition $\pi = \{\{A, B, C\}\}$. In this case, $A =$

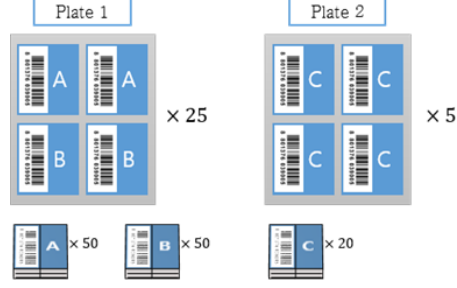


Figure 7:

(2 1 1), and printing number (4) is

$$\left\lceil \max \left\{ \frac{b_i}{A_{P,i}} \mid i \in P \right\} \right\rceil = \left\lceil \max \left\{ \frac{50}{2}, \frac{30}{1}, \frac{20}{1} \right\} \right\rceil = 30. \quad (10)$$

In addition, it can be easily seen that the total number of Loss $E_{A,\mathbf{b}}$ is 20 (see
 140 Figure 8). The array shown in Figure 8 is a more efficient because its Loss is
 the same but its number of Plates is smaller.

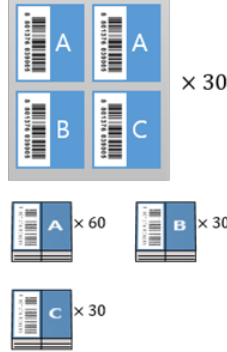


Figure 8:

Example 2. Assume that $I = \{A, B\}$, and the order-quantity vector $\mathbf{b} =$
 (50, 20).

We consider $\pi = \{\{A, B\}\}$ is a partition for the quantity vector \mathbf{b} . Since
 145 $k = 4$, the matrix $A = (2 2)$, and the printing number (4) is

$$\left\lceil \max \left\{ \frac{b_i}{A_{P,i}} \mid i \in P \right\} \right\rceil = \left\lceil \max \left\{ \frac{50}{2}, \frac{20}{2} \right\} \right\rceil = 25. \quad (11)$$

The total number of Loss $E_{A,\mathbf{b}}$ is 30 (see Figure 9).

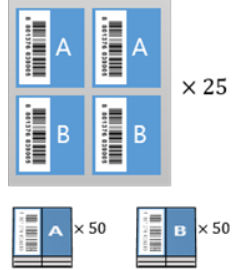


Figure 9:

For the same partition π , the matrix $A = \begin{pmatrix} 3 & 1 \end{pmatrix}$ can be considered. In this case, the printing number (4) is

$$\left\lceil \max \left\{ \frac{b_i}{A_{P,i}} \mid i \in P \right\} \right\rceil = \left\lceil \max \left\{ \frac{50}{3}, \frac{20}{1} \right\} \right\rceil = 20. \quad (12)$$

and the total number of Loss $E_{A,\mathbf{b}}$ is 10 (see Figure 10). The array shown in
 150 Figure 10 is more efficient because its number of Plate is the same but fewer losses occur.

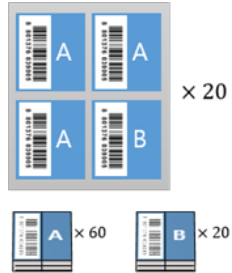


Figure 10:

5. Result

Each sorting report includes the number of losses corresponding to one plate. Using this, the total cost can be calculated by replacing each plate with loss.
 155 We used 82 sorting report samples. The algorithm can be improved for every

sample data. The total cost was reduced by from minimum -6.85%(sample no. 15) to maximum 27.5%(sample no. 74) (see Figure 11).

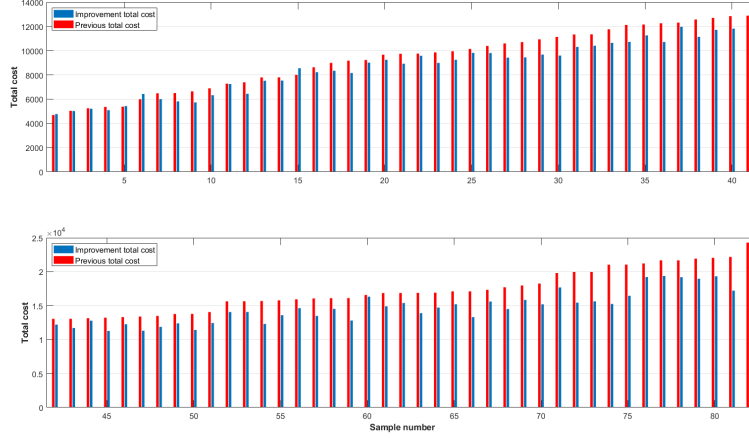


Figure 11: Comparing the Results

We used the *paired t-test*[7] to verify the efficiency of the algorithm. The paired t-test is one of the two sample t-test, and it is a test that verifies whether the two groups are different. The two populations are as follows.

- population1: total cost before applying the algorithm
- population2: total cost after applying the algorithm
- sample1: sample of 82 items from population1
- sample2: sample of 82 items from population2

In order to proceed with the two-sample t-test, the two groups have to satisfy the normality and homoscedasticity. We choose 82 sample data from the two populations, which can be satisfied the normality by the *central limit theorem* [8]. In addition, we identified the homoscedasticity of the two samples through the *var.test* of R. R is a programming language and free software environment for statistical computing and graphic.

The null hypothesis (H_0) of var.test is that ‘the variances of the two groups are equal’, and the alternative hypothesis (H_1) is that ‘the variances of the two groups are different’. If the p -value is below the significance level, the null hypothesis (H_0) will be rejected and if the p -value is not lower than the significance level, the alternative hypothesis (H_1) will be rejected. The result of var.test with the significance level to 0.05 is as follows (see Figure 12).

```
> var.test(sample1,sample2)

F test to compare two variances

data: sample1 and sample2
F = 1.5552, num df = 81, denom df = 81, p-value = 0.04847
alternative hypothesis: true ratio of variances is not equal to 1
95 percent confidence interval:
 1.002998 2.411501
sample estimates:
ratio of variances
 1.555227
```

Figure 12: var.test of R

Since the p -value is not lower than the significance level(0.05), the alternative hypothesis (H_1) is rejected and the null hypothesis (H_0) is accepted. We say that the variances of the two groups can be equal.

Since the two groups satisfy normality and homoscedasticity, we verified whether the difference between the two groups is significant through paired t-test. In this test, the null hypothesis (H_0) is ‘the total cost will be the same after applying the algorithm.’ and the alternative hypothesis (H_1) is ‘the total cost will be reduced after applying algorithm.’ The result of the paired t-test with the significance level to 0.05 is as follows (see Figure 13).

```
> t.test(sample1,sample2, paired=TRUE)

Paired t-test

data: sample1 and sample2
t = 10.766, df = 81, p-value < 2.2e-16
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 1240.884 1803.531
sample estimates:
mean of the differences
 1522.207
```

Figure 13: t.test of R

Since the p -value is below the significance level(0.05), the null hypothesis (H_0) is rejected and the alternative hypothesis (H_1) is accepted. We say that the difference between the two groups can be significant.

Finally, we check the efficiency over the number of products which is the size of I (cf. Section 3). We see that the efficiency increases as the number of products increases in Figure 14. For each 82 samples, we calculated the efficiency as the follow formula.

$$\text{Efficiency} = \left[1 - \frac{\text{Improvement Total Cost}}{\text{Previous Total Cost}} \right] \times 100 \quad (13)$$

The result of the linear fitting shows that the efficiency and the number of products have a positive correlation. Thus, we see that the improved algorithms have better results in many number of products. This suggests that the algorithm fits well into small quantity batch productions.

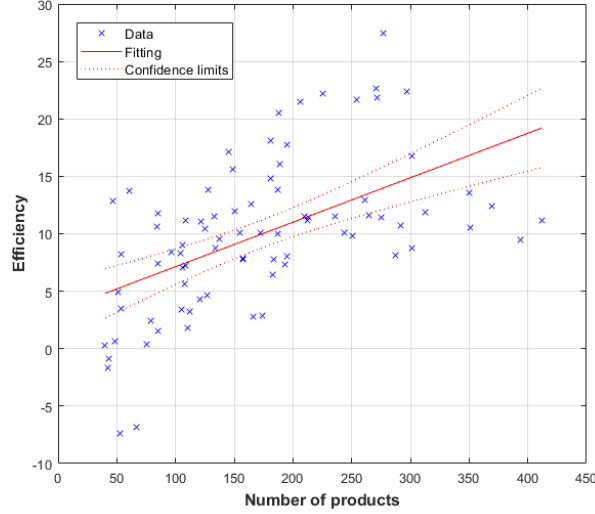


Figure 14: The linear fitting for the efficiency over the number of products

Notice. Please note that the detailed idea of the algorithm cannot be described for confidentiality of the company.

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