

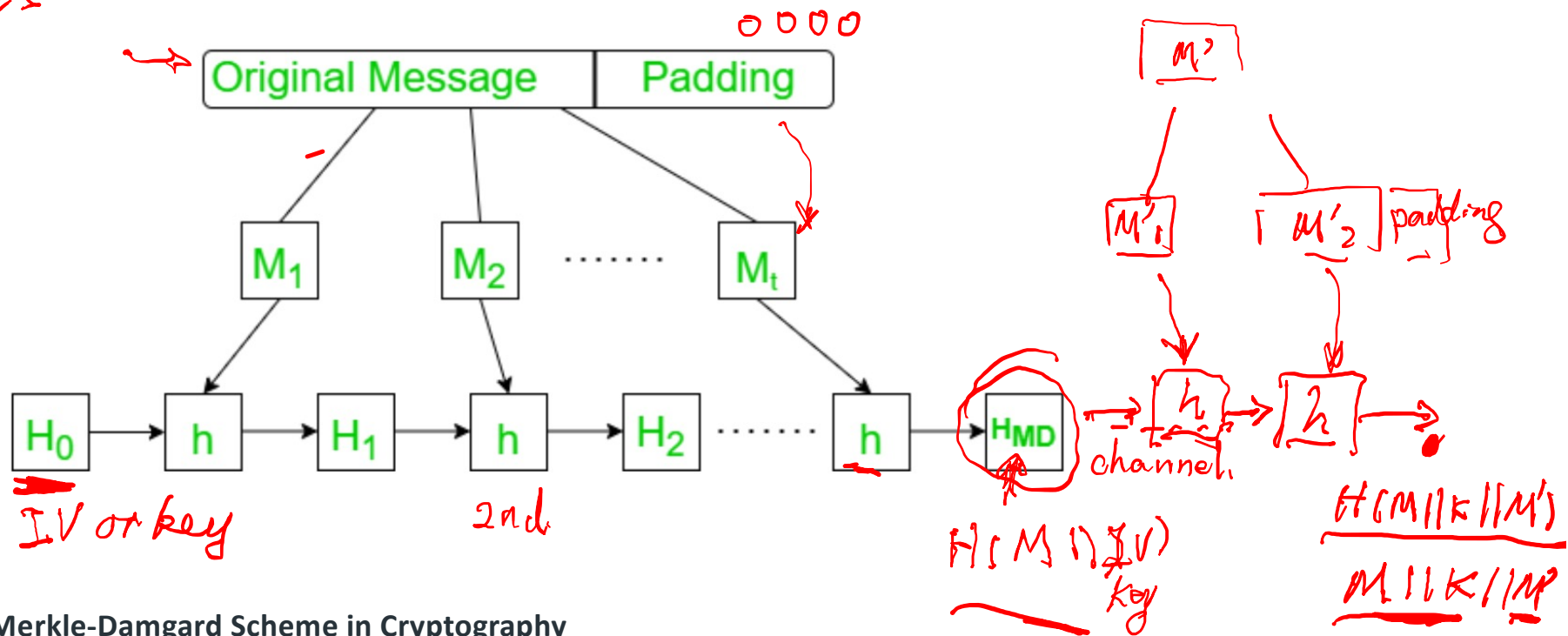
# Length Extension Attacks

- **Length extension attack:** Given  $H(x)$  and the length of  $x$ , but not  $x$ , an attacker can create  $H(x || m)$  for any  $m$  of the attacker's choosing.   
Handwritten notes:  $H(x || m) || x || m$  and  $b || x$  above the expression.
- [Length extension attack - Wikipedia](#)
- SHA-256 (256-bit version of SHA-2) is vulnerable
- SHA-3 is not vulnerable

# Merkle-Damgard Scheme

★ implementation of hash function matters

SFA-256



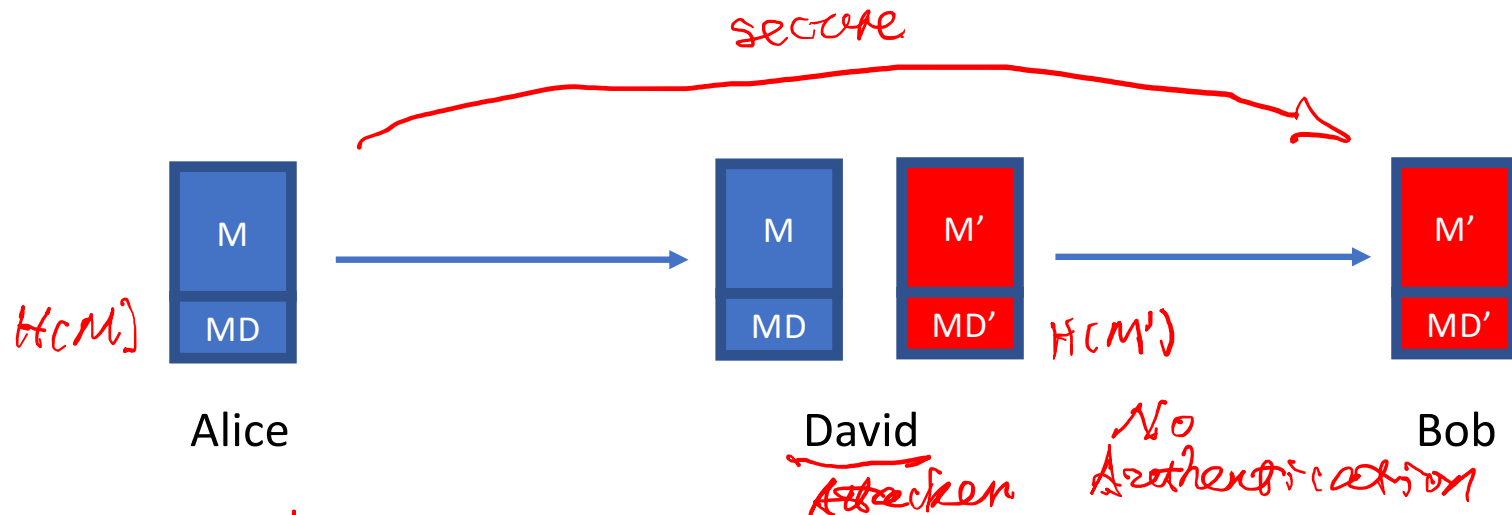
Merkle-Damgard Scheme in Cryptography

<https://www.geeksforgeeks.org/computer-networks/merkle-damgard-scheme-in-cryptography/>

# Do hashes provide integrity?

- It depends on your threat model
- Scenario
  - Alice and Bob want to communicate over an insecure channel
  - David might tamper with messages
- Idea: Use cryptographic hashes
  - Alice sends her message with a cryptographic hash over the channel
  - Bob receives the message and computes a hash on the message
  - Bob checks that the hash he computed matches the hash sent by Alice
- Threat model: David can modify the message *and the hash*
  - No integrity!

# Man-in-the-middle attack



Solutions: 1. MAC  
2. Digital Signature

# Do hashes provide integrity?

- It depends on your threat model
- If the attacker can modify the hash, hashes don't provide integrity
- Main issue: Hashes are *unkeyed* functions
  - There is no secret key being used as input, so any attacker can compute a hash on any value

# Solutions

- A message digest created using a secret **symmetric key** is known as a Message Authentication Code (MAC), because it can provide assurance that the message has not been modified
- The sender can also generate a message digest and then sign the digest using the private key of an **asymmetric key** pair, forming a digital signature. The signature must then be verified by the receiver through comparing it with a locally generated digest

# Hashes: Summary

- Map arbitrary large input to fixed-length output
- Output is deterministic
- Security properties
  - One way: Given an output  $y$ , it is infeasible to find any input  $x$  such that  $H(x) = y$ . →
  - Second preimage resistant: Given an input  $x$ , it is infeasible to find another input  $x' \neq x$  such that  $H(x) = H(x')$ . weak collision 5th
  - Collision resistant: It is infeasible to find any pair of inputs  $x' \neq x$  such that  $H(x) = H(x')$ . strong collision 6th find  $x'$
  - Randomized output
- Some hashes are vulnerable to length extension attacks implementation
- Hashes don't provide integrity (unless you can publish the hash securely)

Message Authentication Code

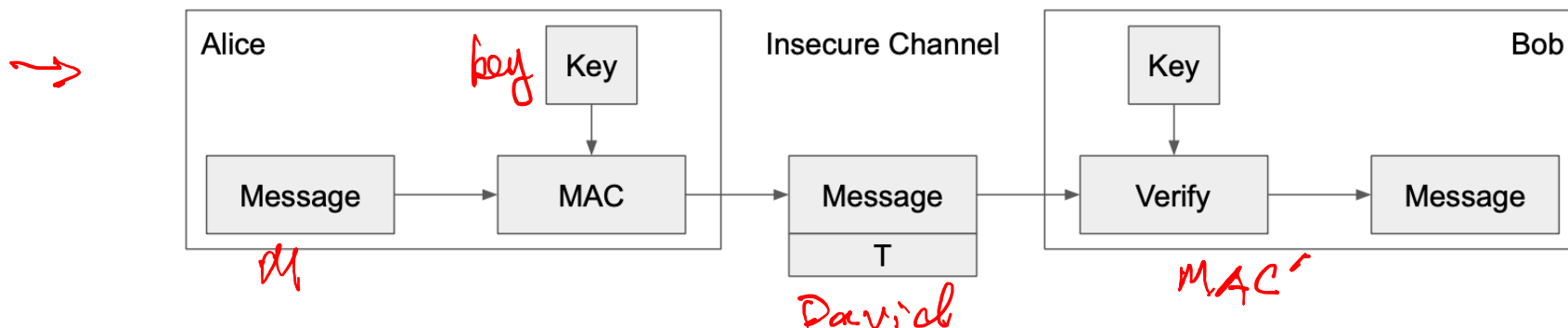


# Message authentication code (MAC)

- generated by an algorithm that creates a small fixed-sized block
  - depending on both message and some key  $\leftarrow$  *pre-shared secret*
  - not be reversible  $\rightarrow$  *h( )*
  - $\text{MAC}_M = F(K_{AB}, M)$   $\downarrow$  *symmetric*
- appended to message as a signature
- receiver performs same computation on message and checks it matches the MAC  $\rightarrow$  *key  $\rightarrow$  sender & receiver*
- provides assurance that message is unaltered and comes from sender
  - $\downarrow$  *Authentication*
  - $\downarrow$  *integrity*
  - $\downarrow$  *validates IP of origin  
non-repudiation of origin*

# MACs: Usage

- Alice wants to send  $M$  to Bob, but doesn't want David to tamper with it
- Alice sends  $M$  and  $T = \text{MAC}(K, M)$  to Bob
- Bob receives  $M$  and  $T$
- Bob computes  $\text{MAC}(K, M)$  and checks that it matches  $T$
- If the MACs match, Bob is confident the message has not been tampered with (integrity)



# MACs: Definition

- Two parts:

→ •  $\text{KeyGen}() \rightarrow K$ : Generate a key  $K$

→ •  $\text{MAC}(K, M) \rightarrow T$ : Generate a tag  $T$  for the message  $M$  using key  $K$

→ hash • Inputs: A secret key and an arbitrary-length message

→ HMAC • Output: A fixed-length tag on the message

- Properties

- **Correctness:** Determinism

- Note: Some more complicated MAC schemes have an additional  $\text{Verify}(K, M, T)$  function that don't require determinism, but this is out of scope

- **Efficiency:** Computing a MAC should be efficient

- **Security:** existentially unforgeable under chosen plaintext attack

Attacker  $M \rightarrow C$   
goal to derive



# Randomized MAC (Non-Deterministic)

