

Reference:

<https://www.geeksforgeeks.org/types-of-asymptotic-notations-in-complexity-analysis-of-algorithms/?ref=lbp>

<https://medium.com/@teamtechsis/big-o-notation-explained-in-plain-english-983b0f7227aa>

## Asymptotic Notations in Complexity Analysis

### Theta Notation ( $\Theta$ -Notation)

Theta notation encloses the function from above and below.

Since it represents **the upper and the lower bound** of the running time of an algorithm, it is used for analyzing **the average-case complexity** of an algorithm.

Amortized analysis

### Big-O Notation (O-notation)

Big-O notation represents **the upper bound** of the running time of an algorithm.

Therefore, it gives **the worst-case complexity** of an algorithm.

### Omega Notation ( $\Omega$ -Notation)

Omega notation represents **the lower bound** of the running time of an algorithm.

Thus, it provides **the best case complexity** of an algorithm.

## Calculate Asymptotic Time Complexity

$O(1) < O(\log n) < O(n) < O(n \log n) < O(n^2) < O(n^3) < O(2^n) < O(n!) < O(n^n)$

### Constant coefficients

Constant coefficients **are typically omitted** because they do not affect the growth rate of an algorithm as the input size increases.

### Exponential

In Big-O notation, we only consider the term with **the highest growth rate** as  $n$  increases because it dominates the overall performance for large input sizes.

$O(n^3 + n^2 + n) \rightarrow O(n^3)$

$O((\log n)^2 + \log n) \rightarrow O((\log n)^2)$

$O(n + n \log n) \rightarrow O(n \log n)$

### Recursive Time Complexity

#### Number of Recursive Calls per Function Call

If each call makes **one recursive call**, it's usually  **$O(n)$**  (e.g., Fibonacci with memoization, linked list traversal).

If each call makes **two recursive calls**, it's often  **$O(2^n)$**  (e.g., naive Fibonacci).

If each call makes  **$n$  recursive calls**, it can be  **$O(n!)$**  (e.g., generating all permutations).

#### Depth of Recursion (Base Case Matters!)

If the recursion depth **increases by 1 per call**, it typically leads to  **$O(n)$** .

If it halves each time (like binary search), it results in  **$O(\log n)$** .

#### Additional Work in Each Recursive Call

If extra work (e.g., copying an array) takes  **$O(n)$**  per call, and there are  **$2^n$  calls**, the total complexity could be  **$O(n \times 2^n)$** .

### $O(1)$ — Constant Time

```
int a = 15;
int b = 25;
int minVal = (a < b) ? a : b; // Finding the minimum
```

### $O(n)$ — Linear Time

Unknown growth

0, 1, 2, ..., x.

```
public static int linearSearch(int[] arr, int target) {
    for (int i = 0; i < arr.length; i++) {
        if (arr[i] == target) {
            return i; // Target found
        }
    }
    return -1; // Target not found
}
```

### $O(\log(n))$ — Logarithmic Time

Unknown growth

n, n/2, n/4, ..., x(x≤1)

```
public static int logBase2(int n) {
    int result = 0;
    while (n > 1) {
        n /= 2;
        result++;
    }
    return result;
}

public static int binarySearch(int[] arr, int target, int left, int right) {
    if (left > right) {
        return -1; // Target not found
    }

    int mid = left + (right - left) / 2;

    if (arr[mid] == target) {
        return mid; // Target found
    }

    if (arr[mid] < target) {
        return binarySearch(arr, target, mid + 1, right); // Search in the right half
    } else {
        return binarySearch(arr, target, left, mid - 1); // Search in the left half
    }
}
```

### $O(n \log(n))$ — Log-linear Time

```
public static void heapSort(int[] arr) {
    int n = arr.length;

    // Build heap (rearrange array)
    for (int i = n / 2 - 1; i >= 0; i--) {
        heapify(arr, n, i);
    }

    // One by one extract an element from heap
    for (int i = n - 1; i >= 0; i--) {
        // Move current root to end
        int temp = arr[0];
```

```

        arr[0] = arr[i];
        arr[i] = temp;

        // Call max heapify on the reduced heap
        heapify(arr, i, 0);
    }
}

public static void heapify(int[] arr, int n, int i) {
    int largest = i; // Initialize largest as root
    int left = 2 * i + 1; // left = 2*i + 1
    int right = 2 * i + 2; // right = 2*i + 2

    // If left child is larger than root
    if (left < n && arr[left] > arr[largest]) {
        largest = left;
    }

    // If right child is larger than largest so far
    if (right < n && arr[right] > arr[largest]) {
        largest = right;
    }

    // If largest is not root
    if (largest != i) {
        int swap = arr[i];
        arr[i] = arr[largest];
        arr[largest] = swap;

        // Recursively heapify the affected sub-tree
        heapify(arr, n, largest);
    }
}

```

#### $O(n^2)$ — Quadratic Time

```

public static void bubbleSort(int[] arr) {
    int n = arr.length;
    boolean swapped;
    for (int i = 0; i < n - 1; i++) {
        swapped = false;
        for (int j = 0; j < n - 1 - i; j++) {
            if (arr[j] > arr[j + 1]) {
                // Swap arr[j] and arr[j + 1]
                int temp = arr[j];
                arr[j] = arr[j + 1];
                arr[j + 1] = temp;
                swapped = true;
            }
        }
        // If no elements were swapped in inner loop, then the array is sorted
        if (!swapped) {
            break;
        }
    }
}

```

#### $O(n^3)$ — Cubic Time

#### $O(2^n)$ — Exponential Time

```

public static int fibonacci(int n) {
    if (n <= 1) {
        return n;
    }
    return fibonacci(n - 1) + fibonacci(n - 2);
}

```

#### $O(n!)$ — Factorial Time

```

public static void generatePermutations(String str, String prefix) {
    if (str.length() == 0) {

```

```

        System.out.println(prefix);
    } else {
        for (int i = 0; i < str.length(); i++) {
            String rem = str.substring(0, i) + str.substring(i + 1);
            generatePermutations(rem, prefix + str.charAt(i));
        }
    }
}

```

## Calculate Asymptotic Space Complexity

The space complexity is the measurement of total space required by an algorithm to execute properly.

It also includes memory required by input variables.

Basically, it's the sum of **auxiliary space** and the **memory used by input variables**.

Space complexity = Auxiliary space + Memory used by input variables

**O(n)**

```

public static int factorial(int n) {
    if (n == 0 || n == 1) {
        return 1;
    }
    return n * factorial(n - 1);
}

```

In this recursive factorial calculation, **each recursive call consumes space on the call stack**.

**The depth of the call stack** is proportional to the input value of 'n'.

```

public void depthFirstSearch(int[] nums, int target, int index, int sum){
    if(index>=nums.length) {
        if(sum==target)this.targetSum++;
        return;
    }
    depthFirstSearch(nums, target, index+1, sum+nums[index]);
    depthFirstSearch(nums, target, index+1, sum-nums[index]);
}

```

At each level of recursion, we're essentially making two function calls.

However, these calls don't happen simultaneously.

Once one call finishes, the other starts, **and the previous call's stack frame is released**.

Therefore, the maximum depth of the recursion stack is equal to the number of elements in the nums array, which is n.

So, the correct space complexity is O(n).

**O(1)**

```

public static int binarySearch(int[] arr, int target) {
    int left = 0;
    int right = arr.length - 1;

    while (left <= right) {
        int mid = left + (right - left) / 2;
        if (arr[mid] == target) {
            return mid;
        } else if (arr[mid] < target) {
            left = mid + 1;
        } else {
            right = mid - 1;
        }
    }
    return -1;
}

```

The space complexity of binary search is O(1) because **it only uses a few variables to keep track of indices** and does not require additional space that grows with the size of the input array.

## Recommendation Algorithms

Collaborative Filtering:

Use similarities between users or items to make recommendations. This can be user-based, item-based, or a hybrid

approach.

Content-Based Filtering:

Recommend items based on their features and the user's interests. Match item attributes with user preferences.

Hybrid Methods:

Combine multiple recommendation strategies to leverage the strengths of each and address their limitations.

Model-Based Approaches:

Apply **machine learning models** (e.g., matrix factorization, deep learning) to predict user preferences and make recommendations.

Deep Learning:

Utilize **neural networks** for complex recommendation tasks, such as sequence modeling and feature extraction.

## Algorithms / Math

### Calculation

#### Addition and Subtraction

$$7+3 = 10$$

1 2 3 4 5 6 7 [8 9 10]

$$7-3 = 4$$

[1 2 3] 4 5 6 7

1 2 3 4 [5 6 7]

### Calculate sums

$$1 + 2 + 3 + \dots + n = \frac{n \times (n + 1)}{2}$$

$$1^2 + 2^2 + 3^2 + \dots + n^2 = \frac{n \times (n + 1) \times (2n + 1)}{6} = \frac{(n^3 + 2n^2 + 2n)}{6}$$

1 3 6 10 15 21

$$a[2]-a[1] + a[3]-a[2] + a[4]-a[3] \dots + a[n]-a[n-1] = 2+3+4+\dots+n$$

$$a[n]-a[1] = (n+2)(n-1)/2$$

$$a[n] = (n^2+n)/2$$

$$S_n = [ n*(n+1)*(2n+1)/6 + (1+n)n/2 ] / 2 = [ n*(n+1)*(2n+1) + (1+n)*3n ] / 12$$
$$= (n+1)*(2n^2+4n) / 12 = [ 2n^3+4n^2+2n^2+4n ] / 6 = (n^3 + 2n^2 + 2n)/6$$

## Exponent

$$2^0 + 2^1 + 2^2 + \dots + 2^n = 2^{n+1} - 1$$

## Fibonacci sequence

0, 1, 1, 2, 3, 5, 8, 13, 21, 34, ...

Formula

The Fibonacci sequence can be defined by the following recurrence relation:

$$F(n) = F(n - 1) + F(n - 2)$$

## Quadratic Formula

$$ax^2 + bx + c = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

## Harmonic Series

$$H_n = \sum_{k=1}^n \frac{1}{k} = 1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \dots + \frac{1}{n} \approx \ln(n) + \gamma$$

$$H_n = \sum_{k=1}^n \frac{n}{k} = n + \frac{n}{2} + \frac{n}{3} + \frac{n}{4} + \dots + \frac{n}{n} \approx n \times (\ln(n) + \gamma)$$

Where  $H_n$  represents the  $n$ -th harmonic number. The series is known to grow without bound, although it does so very slowly.

As  $n$  increases, the harmonic series approaches infinity, but at a rate slower than logarithmic growth.

For large  $n$ , the harmonic series can be approximated as:

$$H_n \approx \ln(n) + \gamma$$

Where  $\ln(n)$  is the natural logarithm of  $n$  and  $\gamma$  is the Euler-Mascheroni constant (approximately 0.57721).

## Probability

### Select $m$ balls from $n$ balls

Order doesn't matter (Combinations)

$$C(n, m) = \frac{n!}{m! \times (n - m)!}$$

Select 3 balls from 7 balls: (All cases / Cases after removing order)

$$C(7, 3) = \frac{7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1}{3 \times 2 \times 1 \times (7 - 3)!} = \frac{7 \times 6 \times 5 \times 4}{4!} = \frac{7 \times 6 \times 5}{3!}$$

○○○ ○○○○ (7 × 6 × 5) / (3 × 2 × 1) The number of permutations needs to be divided by the number of permutations itself.

Order matters (Permutations)

$$P(n, m) = \frac{n!}{(n - m)!}$$

$$P(7, 3) = \frac{7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1}{(7 - 3)!} = \frac{7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1}{4!}$$

○○○ ○○○○ (7 × 6 × 5)

Probability Combination Formula

$$C(n, m) = C(n - 1, m - 1) + C(n - 1, m)$$

$$C(n, m) = C(n, n - m)$$

## Binomial Theorem

$$\sum_{k=0}^n C(n, k) \times a^{n-k} \times b^k = (a + b)^n$$

The variable k represents the index of summation and ranges from 0 (inclusive) to n (inclusive).

$$\sum_{k=1}^n k \times C(n, k) = 1 \times C(n, 1) + 2 \times C(n, 2) + \dots + n \times C(n, n) = n \times 2^{n-1}$$

$$\sum_{k=0}^n C(n, k) = C(n, 0) + C(n, 1) + C(n, 2) + \dots + C(n, n) = (1 + 1)^n$$

$$\Rightarrow C(n, k) < 2^n$$

$$C(n, m) = C(n, n - m)$$

Since  $C\left(n, \frac{n}{2}\right)$  is the largest coefficient, we can approximate the sum  $\sum_{k=0}^n C(n, k)$  by repeating  $C\left(n, \frac{n}{2}\right)$ , which would overestimate the total sum  $(1 + 1)^n$ ,

$$C\left(n, \frac{n}{2}\right) + C\left(n, \frac{n}{2}\right) + C\left(n, \frac{n}{2}\right) + \dots + C\left(n, \frac{n}{2}\right) > (1 + 1)^n$$

There are a total of n+1 elements, The equation is:

$$C\left(n, \frac{n}{2}\right) > \frac{2^n}{n + 1}$$

So it follows that:

$$\frac{2^n}{n + 1} < C\left(n, \frac{n}{2}\right) < 2^n$$

## Formulas

## Bit Operations

$$a \oplus b \oplus b = a$$

## The mode

In statistics, the **mode** is the value that appears most frequently in a data set.

It is a measure of central tendency, like the mean and median, but it specifically identifies the most common value.

If no value repeats, the data set has **no mode**.

For example:

In the data set [1, 2, 2, 3, 4], the mode is 2 because it appears most frequently.

In the data set [1, 1, 2, 3, 3], the modes are 1 and 3 (bimodal) because both appear with equal highest frequency.

## 指数

$$\log_2 3 = \log_{10} 3 / \log_{10} 2$$

## 角度

$$\sin(\pi + \alpha) = -\sin \alpha,$$

$$\cos(\pi + \alpha) = -\cos \alpha,$$

$$\sin(\pi - \alpha) = \sin \alpha,$$

$$\cos(\pi - \alpha) = -\cos \alpha,$$

$$\sin(\pi/2 + \alpha) = \cos \alpha,$$

$$\cos(\pi/2 + \alpha) = -\sin \alpha,$$

$$\cos 2\theta = (\cos \theta)^2 - (\sin \theta)^2$$

$$\sin 2\theta = 2 \sin \theta \cos \theta$$

$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta \quad (\cos \text{ 符号变反})$$

$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta \quad (\sin \text{ 符号不变})$$

$$\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$$

$$\sin \alpha \cos \beta = [\sin(\alpha + \beta) + \sin(\alpha - \beta)] \quad (\text{不同变相同 } \sin, \sin \text{ 在前})$$

$$\cos \alpha \sin \beta = [\sin(\alpha + \beta) - \sin(\alpha - \beta)]$$

$$\cos \alpha \cos \beta = [\cos(\alpha + \beta) + \cos(\alpha - \beta)] \quad (\text{相同变相同 } \cos, \cos \text{ 在前})$$

$$\sin \alpha \sin \beta = -[\cos(\alpha + \beta) - \cos(\alpha - \beta)]$$

## 拆分分母

合并：通过常数项分离，表达式除以分离表达式 求出其他表达式

分解：分母表达式为 0 的 s 值待入其他表达式的积/分母表达式为 0 的 s 值待入其他表达式的和

$$\frac{s+4}{s(s+1)(s+2)} = 2 \frac{1}{s} - 3 \frac{1}{s+1} + \frac{1}{s+2}$$

## 对数

$$x = \log_a M \quad (a^x = M)$$

$$\log_a(MN) = \log_a M + \log_a N$$

$$\log_a(M/N) = \log_a M - \log_a N$$

$$\log_a M^n = n \log_a M$$

$$\log_a b = \log_c b / \log_c a \quad \text{换底公式}$$

## Differentiation

Differentiation is the process of finding the derivative of a function. It's the action of taking the derivative.

The derivative of a function measures how the function's output changes as its input changes.

Mathematically, the derivative of a function f(x) is defined as:

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

This represents the **instantaneous rate of change** or the **slope of the tangent line** at a specific point on the function's curve.

The derivative tells us the slope of a function at any given point.

Example: If  $y = x^2$ , then  $y' = 2x$ , which gives the slope at any x.

$$(uv)' = u' * v + u * v' \quad \text{【微分求导, 积分反求导】}$$



$$\left(\frac{u}{v}\right)' = u' \cdot \frac{1}{v} + u \cdot \frac{v'}{v^2} = \frac{u' \cdot v + u \cdot v'}{v^2}$$

$$y = c \quad y' = 0 \quad (\text{constant})$$

$$y = x \quad y' = 1$$

$$y = x^\mu \quad y' = \mu x^{\mu-1}$$

$$y = \frac{1}{x} \quad y' = -\frac{1}{x^2}$$

$$y = \sqrt{x} \quad y' = \frac{1}{2\sqrt{x}}$$

$$y = a^x \quad y' = a^x \times \ln a$$

$$y = e^x \quad y' = e^x$$

$$y = \log_a x \quad y' = \frac{\log_a e}{x}$$

$$y = \ln x \quad y' = \frac{1}{x}$$

$$y = \sin x \quad y' = \cos x$$

$$y = \cos x \quad y' = -\sin x$$

$$y = \tan x \quad y' = \sec^2 x = \frac{1}{\cos^2 x}$$

## 积分

反求导  $f'(x) = \frac{d}{dx} f(x)$   $f'(x) = f'(x)$

与 x 轴围成的面积  $S = \int_a^b f(x) dx$   $f(x)$  函数内,  $x=a$  到  $x=b$  范围的面积

线面积分  $\int_L f(dL) dL$   $\int_S f(ds) ds$   $\int_V f(dv) dv$  ( $dL$   $ds$   $dv$  都为最小单位点)

$u \cdot v = \int u \cdot v' + \int u' \cdot v$   $\int u \cdot v' = u \cdot v - \int u' \cdot v$  // 去掉  $\int \sin x$   $\rightarrow \int \sin x = -\cos x$   $\rightarrow \int \cos x = \sin x$   $\rightarrow \int \sin x = -\cos x$   $\rightarrow \int \cos x = \sin x$  (代入上步化去积分)

## 复数

$z = x + yi$  [代数式] =  $r(\cos\theta + i \sin\theta)$  [三角式] =  $r e^{i\theta}$  [指数式] 【 $\text{Re}(z)$  指实部,  $\text{Im}(z)$  指虚部,  $\theta$  为与 x 轴的逆时针夹角 数学中  $i$  表示虚部, 物理用  $j$ 】

共轭复数  $z = x + yi$   $\bar{z} = x - yi$   $\cos\theta = (e^{i\theta} + e^{-i\theta})/2$   $\sin\theta = (e^{i\theta} - e^{-i\theta})/2i$

复数开方  $\sqrt[n]{z} = |z|^{\frac{1}{n}} (\cos \frac{\theta + 2k\pi}{n} + i \sin \frac{\theta + 2k\pi}{n})$  【 $\theta = \arg(z)$ 】

幅角主值  $\arg(z) = \theta$

幅角  $\text{Arg}(z) = \theta + 2k\pi, k=0, \pm 1, \pm 2, \dots$

$\text{Arg}(xy) = \text{Arg}(x) + \text{Arg}(y)$   $\text{Arg}(x/y) = \text{Arg}(x) - \text{Arg}(y)$

xy 方程 互换 复数方程  $x = (z + \bar{z})/2$   $y = (z - \bar{z})/2i$  //  $2x + 3y = 1$   $\rightarrow (3 + 2i)z + (-3 + 2i)\bar{z} - 2i = 0$

$z = x + yi$   $\bar{z} = x - yi$  //  $\text{Re}[2 + \bar{z}] = 4$   $\rightarrow \text{Re}[2 + x - yi] = 4$   $x = 2$

分离 xy 方程  $x = t + 1$   $y = t^2 + 1$   $\rightarrow z = t + 1 + i(t^2 + 1)$

$z = (t + 2) + i(t + 1)$   $\rightarrow x = t + 2$   $y = t + 1$

映射下的象 求  $z = 1 + i$  在映射  $w = z^2$  下的象  $\rightarrow w = 2i$

$\arg(w) = \arg(w) * \arg(z) / \theta$  求  $0 < \arg(z) < \pi/2$  在映射  $w = z^2$  下的象  $\rightarrow$  设  $z = r e^{i\theta}$   $w = r^2 e^{i2\theta}$   $\arg(w) = 2\theta$

$\arg(w) = 2\arg(z)$   $0 < \arg(w) < \pi$

$z = x + yi$   $w = u + vi$  求  $2(x^2 + y^2) + 3x - 4y + 1 = 0$  在映射  $w = 1/z$  下的象  $x + yi = 1/(u + vi)$  -

$\rightarrow x = u/(u^2 + v^2)$   $y = -v/(u^2 + v^2)$   $\rightarrow u^2 + v^2 + 3u + 4v + 2 = 0$

复数的三角函数  $\sin z = (e^{iz} - e^{-iz})/2i$   $\cos z = (e^{iz} + e^{-iz})/2$  【复数的  $\sin z$   $\cos z$  取值范围为  $(-\infty, \infty)$ 】

复数的对数函数  $\ln z = \ln|z| + i \arg(z) + 2k\pi i$   $k=0, \pm 1, \pm 2, \dots$  【 $\ln(e^z) = z$ 】

$\ln z = \ln|z| + i \arg(z)$

已知  $e^{iz} - 2e^{-iz} = 0$  求  $z$  式子转化成  $e^{2z} = \dots$  等号两边同时取  $\ln$

复数的幂函数

$$z^{\frac{m}{n}} = r^{\frac{m}{n}} \left[ \cos \frac{m(\theta + 2k\pi)}{n} + i \sin \frac{m(\theta + 2k\pi)}{n} \right] \quad k=0, \pm 1, \pm 2, \dots$$

$$z^a = e^{a \ln z} \quad (\text{复数指数, 指数为负数时变正数分之一})$$

复数作为指数

$$e^z = e^{x(\cos y + i \sin y)} \quad x \text{ 为 } \operatorname{Re} \quad y \text{ 为 } \operatorname{Im} = \theta \quad [|e^z| = e^x \quad e^z \text{ 的模为 } e^x, \quad e^z \text{ 是周期函数}]$$

复数方程求导

$$f(z) = u(x, y) + v(x, y)i \quad f'(z) = u'_x + v'_x i$$

解析 $\rightarrow$ 可导 $\rightarrow$ 连续 $\rightarrow$ 有极限

连续是解析的必要不充分条件 (解析 $\leftarrow$ 连续) 有极限是可导的必要不充分条件

判断函数在哪个可导与解析

在满足  $u'_x = v'_y \quad u'_y = -v'_x$  处可导 【当解的结果为  $x=x \quad y=y$  在  $(x, y)$  内解析 其他结果则处处不解析】

$$// \quad f(z) = (x-y)^2 + 2(x+y)i \quad \text{在何处可导数, 何处解析} \quad u = (x-y)^2 \quad v = 2(x+y) \quad \rightarrow \quad 2x-2y=2 \quad -2x+2y=-2$$

$\rightarrow x-y-1=0$  在直线  $x-y-1=0$  处可导, 处处不解析

证明函数为调和函数

$$u''_{xx} \quad u''_{xy} \quad u''_{yx} \quad u''_{yy} \text{ 都连续 (xy 所有值都能取 } 1/x \quad \ln x \text{ 为不连续)} \quad u''_{xx} + u''_{yy} = 0$$

$$// \text{ 证明 } u(x, y) = y^3 - 3x^2y \text{ 为调和函数} \quad u''_{xx} = -6y \quad u''_{xy} = -6x \quad u''_{yx} = -6x \quad u''_{yy} = 6y \quad u''_{xx} + u''_{yy} = -$$

$$6y + 6y = 0$$

共轭调和函数

$$v(x, y) = \int u'_x dy + \int [-u'_y - (\int u'_x dy)'_x] dx + C$$

解析函数

$$f(x) = u(x, 0) + iv(x, 0) \text{ 再将结果的 } x \text{ 全换成 } z \quad // u(x, y) = y^3 - 3x^2y \text{ 为调和函数, 其共轭函数 } v(x, y) = -3xy^2 + x^3 + C$$

$$u(x, 0) = 0 \quad v(x, 0) = x^3 + C \quad f(x) = ix^3 + iC \rightarrow f(z) = iz^3 + iC$$

卷积

$$// \text{ 已知 } f(t) = u(t) \quad g(t) = \sin t, \quad 0 \leq t \leq \pi/2 \quad 0, \text{ 其他} \quad \text{求 } f(t) * g(t)$$

$$m \text{ 替换 } t, \quad f(t)g(t) \text{ 任选一个计算 } f(t-m) \text{ 的值} \quad f(t-m) = 1 \quad m < t, \quad 0 > m > t$$

$$\text{画出区间, 计算 } t \text{ 取不同值时 } f(t-m) * g(m) \text{ 的不同取值} \quad f(t-m) * g(m) = \sin m, \quad 0 \leq m \leq \pi/2$$

$$\text{计算上步各种情况下的 } \int_{-\infty}^{\infty} f(t-m) * g(m) \text{ 的值}$$

$$\text{傅里叶变换} \quad F[f(t)] = \int_{-\infty}^{\infty} f(t) e^{-i\omega t} dt \quad (\omega \text{ 视为常量})$$

$$\text{性质: } F[tf(t)] = jF'(\omega)$$

$$F[f(t) = 0, t < 0 \quad Ce^{-at}, t \geq 0] = \frac{C}{a + j\omega} \quad F[f(t) = Ce^{at}, t < 0 \quad Ce^{-at}, t \geq 0] = \frac{2Ca}{a^2 + \omega^2} \quad F[f(t) = C, |t| \leq a/2 \quad 0, \text{其他}] = \frac{2C}{a} \sin\left(\frac{a\omega}{2}\right)$$

$$F[\delta(t+a)] = e^{j\omega a} F[\delta(t)]$$

傅里叶积分表达式

$$f(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} f(\omega) e^{-i\omega t} d\omega = \frac{1}{2\pi} \int_{-\infty}^{\infty} f(\omega) \cos \omega t d\omega + \frac{j}{2\pi} \int_{-\infty}^{\infty} f(\omega) \sin \omega t d\omega$$

积分内奇函数部分直接去掉, 偶函数部分下限变为 0, 系数乘 2

去掉结果取值范围中  $\leq, \geq$  里的等于号, 单独列出等于时的情况等于时, 结果为左右侧取值之和的一半

傅里叶逆变换

$$F[f(\omega)] = 2\pi f(t) \quad // \quad F[xx] = xx\omega \quad F[xx\omega] = 2\pi * xx$$

$$\text{积分} \quad \oint_{|z|=1.5} \frac{e^z}{z(z-1)} dz \quad z \neq 0, 1 \quad \text{在 } z \text{ 圈里的点为奇点 } z \neq 0, 1 \quad (\text{没有奇点 } \oint_{|z|=xx} = 0)$$

$$\text{一个奇点} \quad \oint_C \frac{f(z)}{z-a} dz = 2\pi i f(a) \quad \oint_C \frac{f(z)}{(z-a)^{n+1}} dz = \frac{2\pi i}{n!} f^{(n)}(a) \quad \text{将奇点式子放在分母, 求出对应奇点 } a \text{ 的结果} \quad [f^{(n)}(a) \text{ 为求 } n$$

次导数】

$$// \quad \oint_C \frac{e^z}{z(z-1)} dz = \oint_C \frac{e^z}{z-1} dz \quad f(z) = \frac{e^z}{z}$$

多个奇点 将每个奇点式子放在分母, 求出对应奇点  $a$  的结果

$$\text{拉普拉斯变换} \quad F(s) = \int_0^{\infty} f(t) e^{-st} dt \quad (s \text{ 视为常量})$$

$$\text{周期函数} \quad F(s) = \int_0^T f(t) e^{-st} dt \quad \text{根据原函数式子拆解成积分相加}$$

$$L[\cos at] = \frac{s}{s^2 + a^2} \quad L[\sin at] = \frac{a}{s^2 + a^2}$$

$$L[e^{\mp at}] = \frac{1}{s \mp a} \quad L[\delta(t)] = 1 \quad L[\delta'(t)] = s \quad L[te^{-t}] = \frac{1}{(s+1)^2} \quad L[t^a] = \frac{a!}{s^{a+1}}$$

$$L[(-1)^n t^n f(t)] = F^{(n)}(s) \quad e^{\pm at} f(t) = F(s \pm a)$$

求微分方程  $y'' + 2y' + y = te^{-t}$  满足  $y(0)=1$  和  $y'(0)=-2$  的解

$$\text{对等号两边同时进行拉式变换} \quad y \rightarrow Y(s) \quad y' = sY(s) - y(0) \quad y'' = s^2 Y(s) - sy(0) - y'(0) \quad y''' = s^3 Y(s) - s^2 y(0) - sy'(0) - y''(0)$$

$$\text{求出 } Y(s) \quad \text{求出 } Y(s) \text{ 拉式逆变换 } y(t)$$

欧拉公式

$$e^{i\theta} = \cos \theta + i \sin \theta$$

傅里叶级数

$$f(x) = C + \sum_{n=1}^{\infty} \left[ a_n \cos\left(\frac{2n\pi}{T} x\right) + b_n \sin\left(\frac{2n\pi}{T} x\right) \right] \quad (\text{奇函数 } a_n = 0 \quad \text{偶函数 } b_n = 0) \quad \text{【任何一个周期 } T \text{ 函数 都可以表示为}$$

## 周期 $T/n$ $f(x)$ 的形式】

基  $\{1, \cos(\frac{2\pi n}{T}x), \sin(\frac{2\pi n}{T}x)\}$   $f(x)$  相当于向量  $(C, a_n, b_n)$

频谱图: 横轴=每个  $\sin/\cos$   $x$  的系数  $0 < \dots < 3 < \dots < 4/\pi \sin(3x)$  (常数项对应基 1 向量  $C$  横轴 0)

纵轴=常数项和每个  $\sin/\cos$  的幅值  $2 < \dots < 4/\pi \sin(3x)$

偶函数频谱图要左右对应 //  $f(x) = 2 + 4/\pi \sin(3x)$  基 =  $(1, \sin(3x))$  向量 =  $(2, 4/\pi)$

柯西积分公式  $\oint_C \frac{f(z)}{z-z_0} dz = 2\pi i f(z_0)$  【 $f(z)$  沿封闭曲线  $C$  积分,  $z_0$  为曲线内一点】

留数定理  $\text{Res}[f(z), z_0] = \frac{1}{2\pi i} \oint_C f(z) dz = \lim_{z \rightarrow z_0} (z - z_0) f(z)$  【 $(z - z_0) f(z)$  不一定为 0】

计算  $\oint_{|z|=3} \frac{ze^z}{z-1} dz = 2\pi i \{ \text{Res}[f(z), x_1] + \text{Res}[f(z), x_2] \}$  【 $x_1, x_2$  为在  $|z| < 3$  范围内的极点 (不论级数)】

泰勒级数  $f(z) = \sum_{n=0}^{\infty} \frac{f^{(n)}(z_0)}{n!} (z - z_0)^n$  ( $n=0, \pm 1, \pm 2, \dots$ ) 【 $f(z)$  在  $z_0$  处的泰勒展开式,  $f^{(n)}(z_0)$  为  $z = z_0$  时,  $f(z)$  的  $n$  阶导数】

洛朗级数  $f(z) = \sum_{n=-\infty}^{+\infty} c_n (z - z_0)^n$   $c_n = \frac{1}{2\pi i} \oint_C \frac{f(\varepsilon)}{(\varepsilon - z_0)^{n+1}} d\varepsilon$  ( $n=0, \pm 1, \pm 2, \dots$ ) 【 $f(z)$  在圆环域  $R_1 < |z - z_0| < R_2$  处的泰勒展开式】

$\frac{1}{1-u} = \sum_{n=0}^{+\infty} u^n$  【 $A < z < B$ : 化为自变量只有  $z$  的 E 综合式】

## 函数

奇函数: 关于原点对称 (奇\*奇=偶 奇/偶=偶 偶\*偶=偶 偶/偶=偶 奇\*偶=奇)

偶函数: 关于 Y 轴对称

分解分数式子 设  $\frac{a}{x+1} + \frac{b}{x+2} = \frac{4x+5}{(x+1)(x+2)}$

## 方程

一元二次方程  $ax^2 + bx + c = 0$   $\Delta = b^2 - 4ac$   $\Delta \geq 0$  两根为实数  $x_1 = [-b + \sqrt{\Delta}]/2a$   $x_2 = [-b - \sqrt{\Delta}]/2a$

$\Delta < 0$  两根为复数  $x_1 = -b/2a + [\sqrt{-\Delta}/2a]j$   $x_2 = -b/2a - [\sqrt{-\Delta}/2a]j$

## 矩阵

相乘 一矩阵  $a$  行 \* 二矩阵  $b$  列 的和 == 新矩阵 第  $a$  行第  $b$  列的值

## 概率

$A_{35} = 5 \cdot 4 \cdot 3$  (取出的 3 个有顺序)  $C_{35} = 5 \cdot 4 \cdot 3 / 3! \cdot 2! \cdot 1!$  (取出的 3 个没有顺序) 【 $C_{26} \cdot C_{26}/2!$   $C_{35} = A_{35}/3!$  除去自身阶乘的情况】

## 概念

范围  $\text{for}(i=1; i \leq 5; i++)$  1-5 包含 6 个数,

$\text{for}(i=0; i < 5; i++)$  0-4 包含 5 个数, 减法计算不会包括首数或尾数, 加法计算不会包括首数

极限  $\lim f(x) = \lim f'(x)$

导数  $\frac{\delta y}{\delta x}$   $y$  视作不变量,  $x$  求导数 (其他部分都为常数)

函数解析 如果函数  $f(z)$  在  $z_0$  以及  $z_0$  的邻域内处处可导 那称  $f(z)$  在  $z_0$  解析, 如果  $f(z)$  在区域  $D$  内每一点可导, 那称  $f(z)$  在  $D$  内解析

幂级数 在  $x=a$  点处展开成幂级数, 也就是展开为  $(x-a)$  的幂级数

$m$  阶零点  $f(x)$  在  $x=a$  处的函数值、一阶导数值、.....、 $m-1$  阶导数为 0,, 但是  $m$  阶导数非 0

$m$  阶极点  $m$  阶函数  $f(x)$  在  $x=a$  处极限为  $\infty$  (分母为 0) 【判断 2 为几级极点: 用  $(z-2)$  的  $m$  次幂乘原函数, 结果在  $z \rightarrow 0$  的时 极限为常数, 则为  $m$  级极点】

奇点 可去奇点  $f(z)$  在  $a$  附近有界, 称  $a$  为  $f$  的可去奇点

极点 ( $a$  是  $1/f$  的可去奇点):  $f(z)$  在  $a$  处的极限为  $\infty$ , 称  $a$  为  $f$  的极点

本性奇点:

极限不存在

xy 方程化为复数  $z\bar{z}$  方程  $2x+3y=1$  ( $z=x+yi$   $\bar{z}=x-yi$ )  $\implies (3+2i)z+(-3+2i)\bar{z}-2i=0$

复数方程化为 xy 方程  $\operatorname{Re}(2+\bar{z})=4 \implies \operatorname{Re}(2+x-yi)=4 \implies x=2$

$f(z)=x^2+2xy+ay^2+i(y^2+bxy-x^2)$  在复平面处处解析  $\implies \frac{\delta \operatorname{Re}}{\delta x} = \frac{\delta \operatorname{Im}}{\delta y} \quad \frac{\delta \operatorname{Im}}{\delta x} = -\frac{\delta \operatorname{Re}}{\delta y}$  ( $v=bx^2y-y^3$   $v$  对  $y$  求导  $= bx^2-3y^2$ )

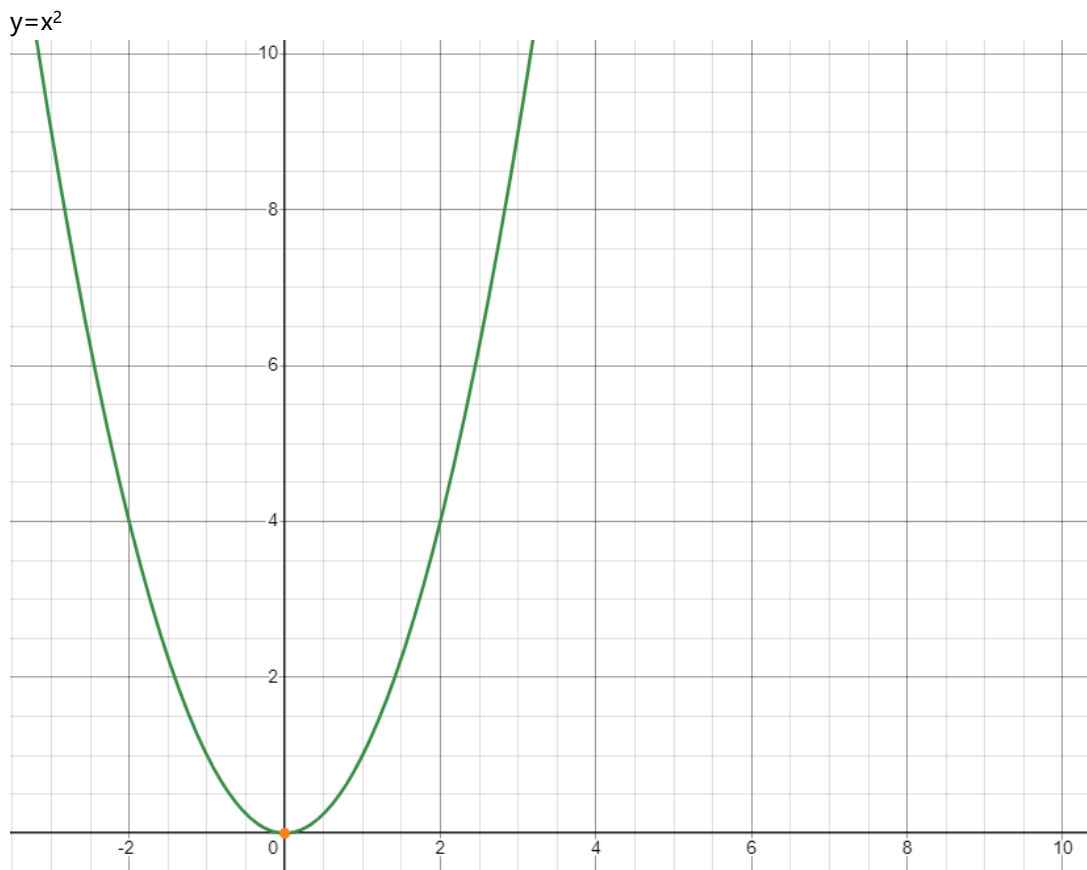
$\langle x \rangle$  表示  $\geq x$  的最小整数 //  $\langle 1, 1 \rangle = 2, \langle -1, 1 \rangle = -1$

## 单位

光年 (ly)  $1\text{ly} = 94605 \times 10^8 \text{ km}$   $1\text{ER} = \text{一个地球}$   $1\text{SR} = \text{一个太阳}$   $1\text{AU} = \text{太阳到地球的直线距离}$  可观测宇宙  
46,500,000,000ly

## Function Graph

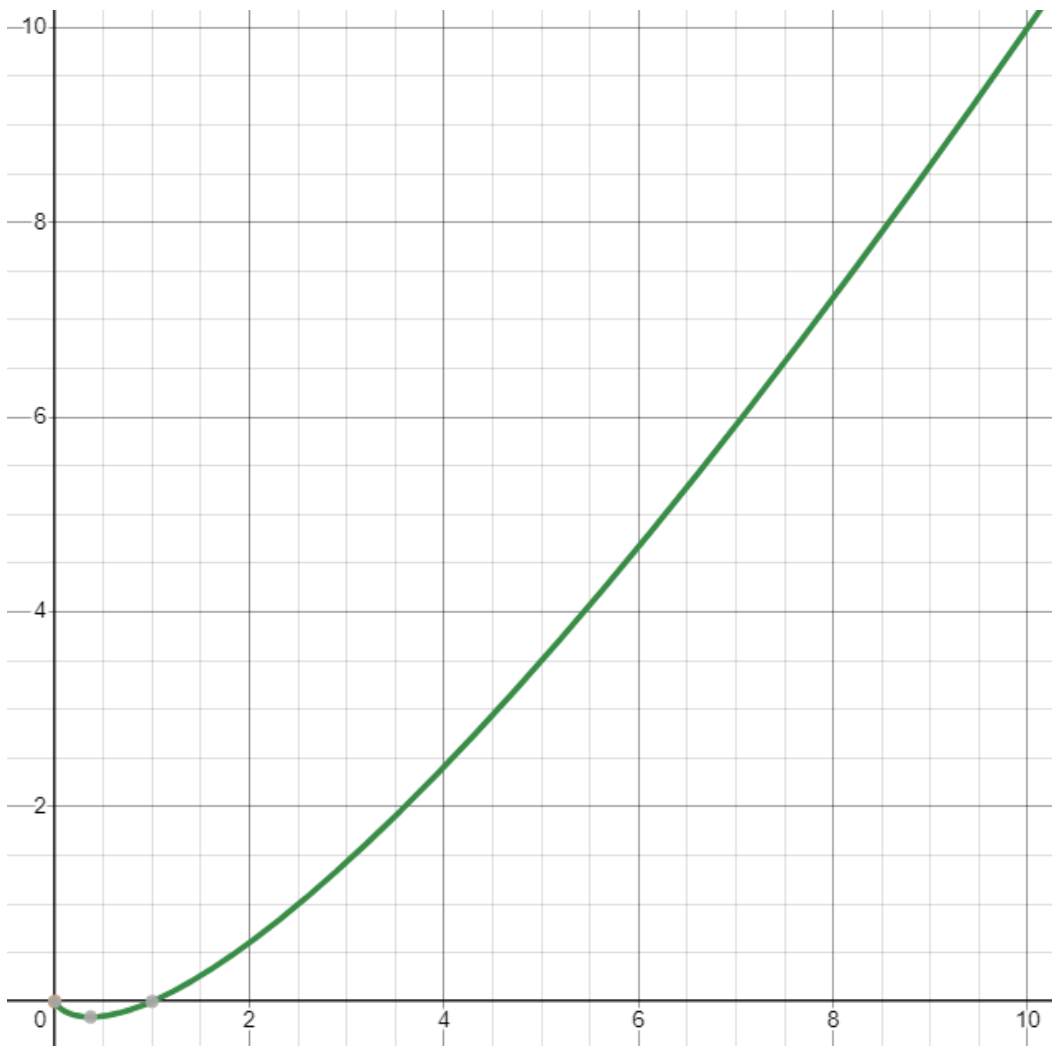
### Quadratic function



### Log-Linear

The default base of log is e (2.718281828459).

$y=x\log(x)$



## Algorithms / Data Structure

Reference:

<https://www.geeksforgeeks.org/introduction-to-data-structures/>

<https://builtin.com/software-engineering-perspectives/tree-traversal>

### Common data structures

## String in Data Structure

## Array Data Structure

### Set

```
Set<Integer>[] g = new Set[n + 1]; // Array of Set objects
```

### Bitmap

In Java, a bitmap is a data structure used to efficiently store and manage a set of binary flags (0s and 1s) or boolean values.

It's often used for tasks like:

#### Bit Flags

Storing and manipulating individual flags or states.

#### Set Representation

Representing a set of elements where the presence or absence of each element can be checked quickly.

Using an `int` array instead of a `byte` array for the bitmap is a common practice because of the convenience of manipulating bits within the `int` type, which is generally 32 bits in size.

#### Bit Manipulation Convenience:

An `int` is 32 bits long, so you can manage 32 bits with a single `int` variable. This aligns well with bit manipulation operations (shifting and bitwise operations).

Using an `int` array allows you to easily access and modify any bit within the 32-bit chunk by calculating the appropriate index and offset.

#### Performance:

Operations on `int` types are generally faster than on `byte` types due to word size alignment in most processors. Modern processors handle 32-bit integers more efficiently.

Bitwise operations like shifting and bitwise OR (`|`) are more straightforward and performant when working with `int` compared to `byte`.

### Bloom filter

A Bloom filter is a probabilistic data structure used to test whether an element is a member of a set.

It's highly space-efficient but allows for false positive matches (incorrectly indicating that an element is in the set) while never generating false negatives (correctly indicating that an element is not in the set if it indeed is not).

This trade-off makes Bloom filters suitable for applications where space efficiency is critical and occasional false positives are tolerable.

#### How a Bloom Filter Works

##### Initialization:

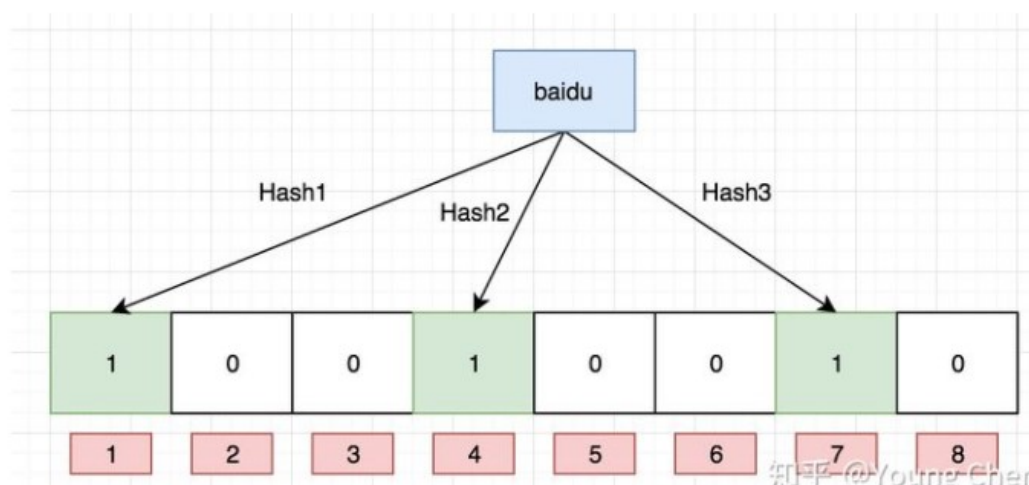
A Bloom filter starts with an array of bits, all set to 0. This array is of a fixed size, say `m` bits.

##### Hash Functions:

The filter uses `k` different hash functions. Each hash function takes an input and produces a hash value which corresponds to a position in the bit array.

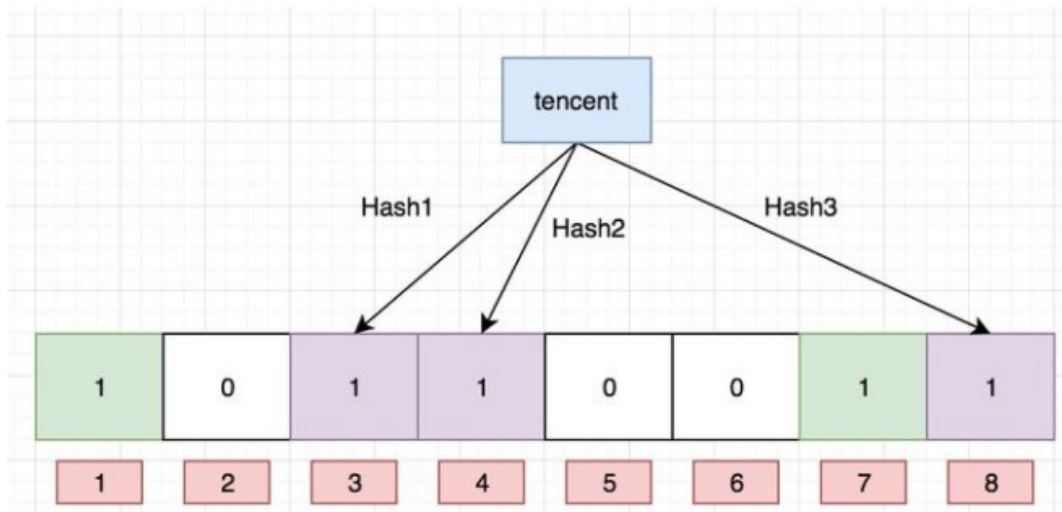
##### Adding an Element:

To add an element to the Bloom filter, the element is passed through each of the `k` hash functions, producing `k` positions in the bit array. The bits at these positions are set to 1.



##### Checking Membership:

To check if an element is in the set, the element is passed through the same `k` hash functions to get `k` positions. If all the bits at these positions are 1, the element is considered to be in the set. If any of these bits are 0, the element is definitely not in the set.



## Linked List Data Structure

### Rule

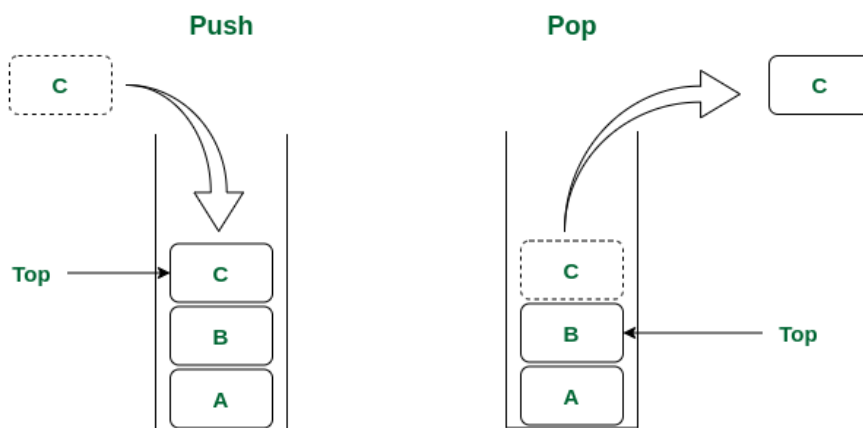
Create a new Node instead of operating the original node (Beneficial for handling node order).

## Stack Data Structure

Stack is a linear data structure which follows a particular order in which the operations are performed.

The order may be LIFO (Last In First Out) or FILO (First In Last Out).

In stack, all insertion and deletion are permitted at only one end of the list.

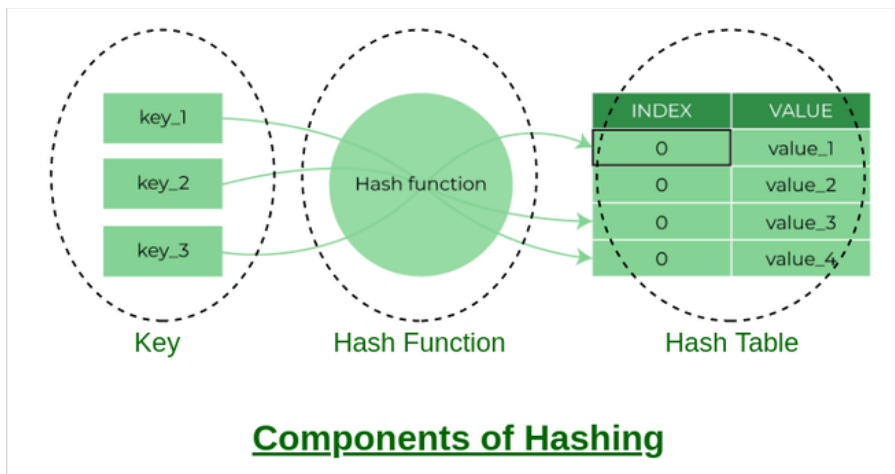


## Stack Data Structure

## Queue Data Structure

See `java.util.Queue`

## Hashing in Data Structure



## Advanced Data Structure

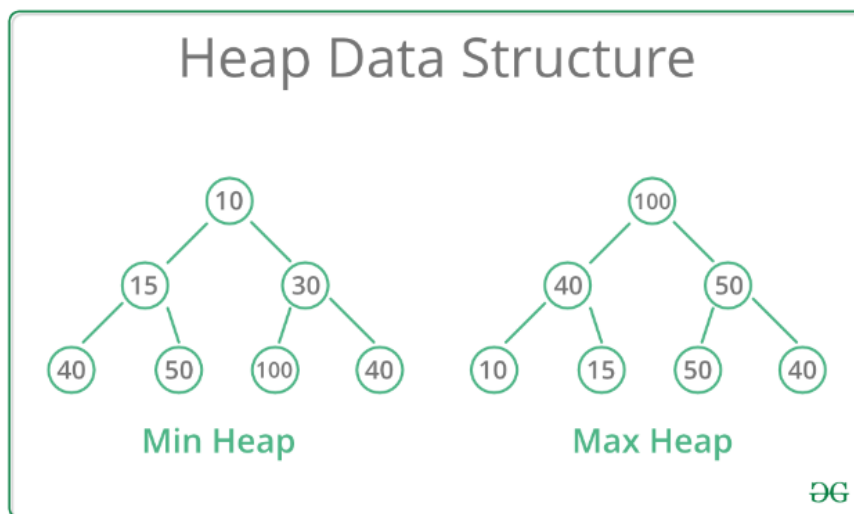
### Heap Data Structure

What is Heap Data Structure

A Heap is a **complete binary tree data structure** that satisfies the heap property:

for every node, the value of its children is **less than or equal to its own value**.

Heaps are usually used to implement priority queues, where the smallest (or largest) element is always at the root of the tree.



#### Max Heap

The root node **contains the maximum value**, and the values decrease as you move down the tree.

#### Min Heap

The root node **contains the minimum value**, and the values increase as you move down the tree.

## Tree Data Structure

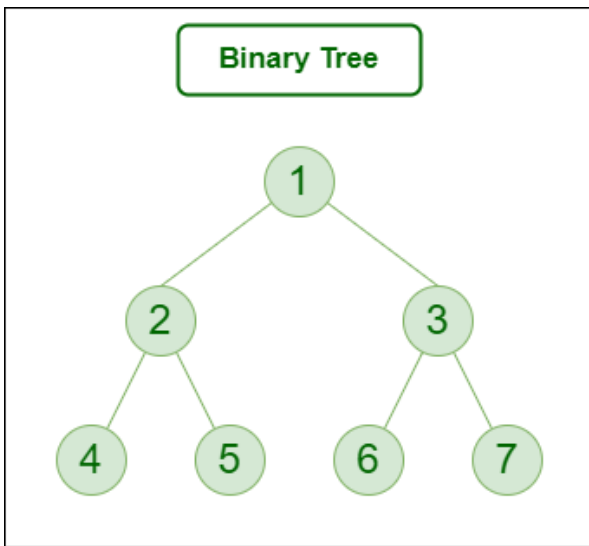
Based on the number of children

### Binary Tree

A binary Tree is defined as a Tree data structure with **at most 2 children**.

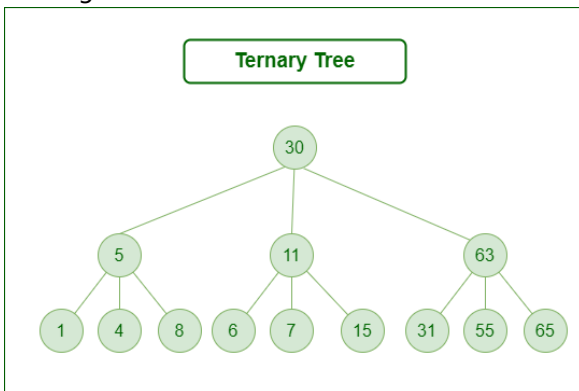
Since each element in a binary tree can have only 2 children, we typically name them the left and right child.



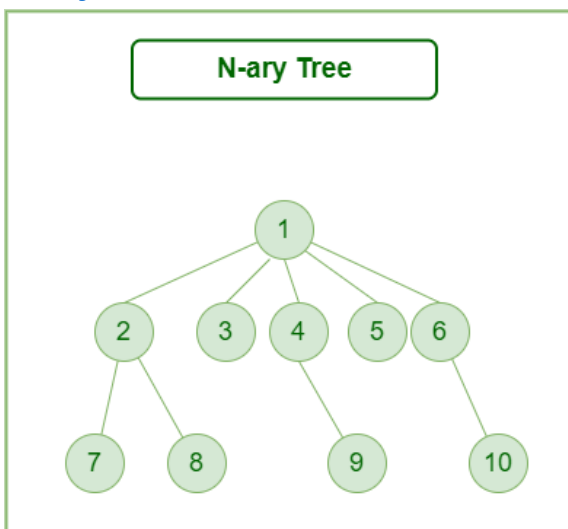


## Ternary Tree

A Ternary Tree is a tree data structure in which each node has **at most three child nodes**, usually distinguished as "left", "mid" and "right".



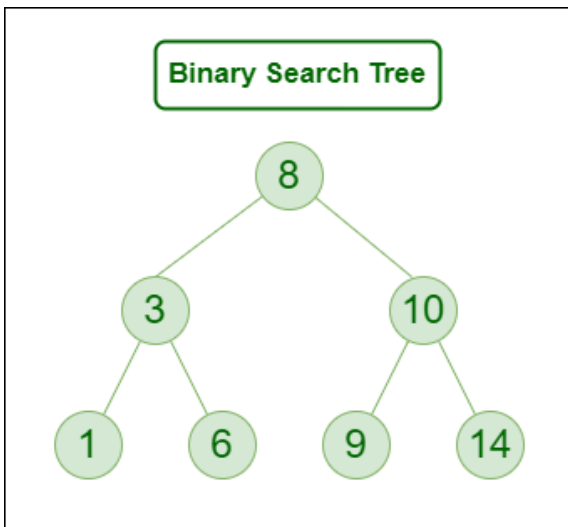
## N-ary Tree (Generic Tree)



Generic trees are a collection of nodes where each node is a data structure that consists of **records and a list of references to its children** (duplicate references are not allowed). Unlike the linked list, each node stores the address of multiple nodes.

Based on the nodes' values

## Binary Search Tree



#### Node Structure

Each node in a BST has a maximum of two children, referred to as the left and right child.

Leaf nodes are nodes without child nodes.

#### Ordering Property:

The left subtree of a node contains only nodes with keys less than the node's key.

The right subtree of a node contains only nodes with keys greater than the node's key.

Both the left and right subtrees must also be binary search trees.

## Binary Indexed Tree or Fenwick Tree

A Binary Indexed Tree (BIT), also known as a **Fenwick Tree**, is a data structure used for efficiently performing operations on prefix sums of a list of numbers.

It is particularly useful for scenarios where you need to frequently update values in an array and calculate prefix sums or ranges.

#### How It Works

A BIT is implemented using a 1-based array, where `tree[i]` stores cumulative sums for certain indices based on the least significant bit (LSB) of `i`.

The LSB determines the range of indices contributing to a given `tree[i]`.

For `tree[40]` (binary: 0010 1000):

Step 1:

```

tree[40] += val
i & -i = 0010 1000 & 1101 1000 = 0000 1000
i = i + (i & -i) = 0010 1000 + 0000 1000 = 0011 0000 = 48

```

Step 2:

```

tree[48] += val
i & -i = 0011 0000 & 1101 0000 = 0001 0000
i = i + (i & -i) = 0011 0000 + 0001 0000 = 0100 0000 = 64

```

Step 3:

```

tree[64] += val
...

```

The inserted value will be added at index 40, 48, 64, ... `n`.

For `tree[6]` (binary: 110):

The LSB is 2, so `tree[6]` stores the sum of indices [5, 6].

#### Usage

```

class BinaryIndexedTree {

```

```

private final int[] tree;

// Constructor: Initialize the BIT for n elements
public BinaryIndexedTree(int n) {
    tree = new int[n + 1]; // 1-based indexing
}

// Update: Add value to index i
public void update(int i, int val) {
    while (i < tree.length) {
        tree[i] += val;
        i += i & -i; // Move to the next affected index
    }
}

// Query: Compute prefix sum up to index i
public int prefixSum(int i) {
    int sum = 0;
    while (i > 0) {
        sum += tree[i];
        i &= i-1; // Move to the parent index
    }
    return sum;
}

// Range Query: Sum between indices [left, right]
public int rangePrefixSum(int left, int right) {
    return prefixSum(right) - prefixSum(left - 1);
}
}

```

Time Complexity:

update:  $O(\log n)$

prefixSum:  $O(\log n)$

rangePrefixSum:  $O(\log n)$

Space Complexity:  $O(n)$

## AVL Tree (Adelson-Velsky and Landis tree)

AVL tree is a self-balancing Binary Search Tree (BST) where the difference between heights of left and right subtrees for any node cannot be more than one.

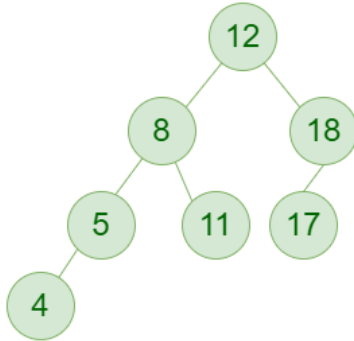
### Self-balancing Binary Search Tree

A self-balancing binary search tree (BST) is a type of binary search tree that automatically maintains its height (or balance) after insertions and deletions.

This ensures that the tree remains balanced, providing efficient performance for search, insertion, and deletion operations.

The balance of the tree is crucial for maintaining logarithmic time complexity for these operations, typically  $O(\log n)$ , where  $n$  is the number of nodes in the tree.

### AVL Tree



## Red-Black Tree

A red-black tree is a kind of self-balancing binary search tree where each node has an extra bit, and that bit is often interpreted as the color (red or black). These colors are used to ensure that the tree remains balanced during insertions and deletions.

Although the balance of the tree is not perfect, it is good enough to reduce the searching time and maintain it around  $O(\log n)$  time, where  $n$  is the total number of elements in the tree.

Rules That Every Red-Black Tree Follows:

Node Color

Each node is either red or black.

Root Property

The root is always black.

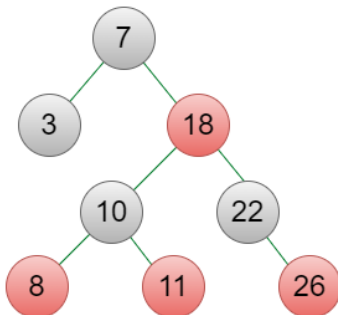
Leaf Property

Every leaf (NULL node) is black.

Red Property

If a red node has children, then the children are always black (no two red nodes can be adjacent).

### Red- Black Tree



## B-Tree

A B-tree is a **self-balancing tree data structure** that maintains sorted data and allows for efficient insertion, deletion, and search operations. It is widely used in databases and file systems.

In a B-tree, data entries or pointers can be stored **in both internal nodes and leaf nodes**, unlike the B+ tree where data pointers are exclusively stored in leaf nodes.

This distinction significantly affects the structure: B-tree leaf nodes may contain actual data entries or serve as placeholders for keys.

### Key Characteristics

- **Balanced Tree**  
All leaf nodes are **at the same depth**, ensuring that the tree remains balanced.
- **Variable Number of Children**  
Each node can have a variable number of children within a predefined range. This range is defined by a minimum degree  $t$ .
- **Efficient Operations**  
Ensures logarithmic time complexity for search, insertion, and deletion operations.

### Properties

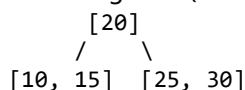
- **Degree  $t$**   
The minimum degree of the B-tree. Each node, except the root, must have at least  $t-1$  keys and at most  $2t-1$  keys. The root must have at least one key.
- **Keys in Nodes**  
All keys in a node are sorted **in non-decreasing order**. Keys **in the left subtree** of a node are less than the node's keys, and keys **in the right subtree** are greater.
- **Height**  
The height of a B-tree with  $n$  keys and minimum degree  $t$  is at most  $\log_t(n+1)$ .

### B-tree Operations

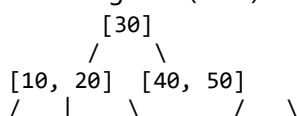
- **Search**  
Begins at the root and recursively traverses down the tree. At each node, a binary search is performed on the keys to determine the path to the next node.
- **Insertion:**
  - 1) New keys are always inserted at the leaf nodes.
  - 2) If a node becomes full (i.e., it has  $2t-1$  keys), it is **split into two nodes**, and **the middle key is promoted to the parent node**.
- **Deletion:**
  - 1) Keys are deleted from the leaf nodes.
  - 2) If a key is deleted from an internal node, it is replaced by its predecessor or successor key, and the predecessor or successor is then deleted.
  - 3) If a node has fewer than  $t-1$  keys, it **is merged or keys are redistributed from its siblings**.

Example:

B-tree of Degree 2 ( $t = 2$ )

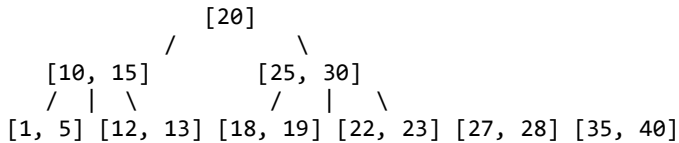


B-tree of Degree 2 ( $t = 2$ ) with More Levels



[5] [15] [25] [35, 37] [45, 47, 49]

B-tree of Degree 3 ( $t = 3$ ) with More Levels



## B+ Tree

B+ tree eliminates the drawback B-tree used for indexing **by storing data pointers only at the leaf nodes of the tree**.

Thus, the structure of leaf nodes of a B+ tree is quite different from the structure of internal nodes of the B tree.

Key Characteristics:

- **Balanced Tree**  
All leaf nodes are at the same depth, ensuring balance throughout the tree.
- **Variable Number of Children**  
Each node, except the root, can have a variable number of children within a predefined range.
- **Sequential Access and Range Queries**  
B+ trees store data pointers only in leaf nodes, organized in a linked list structure.  
This design facilitates **efficient range queries and sequential access**, which are common in database operations like **range scans** and **queries** involving ordered data retrieval.

Properties:

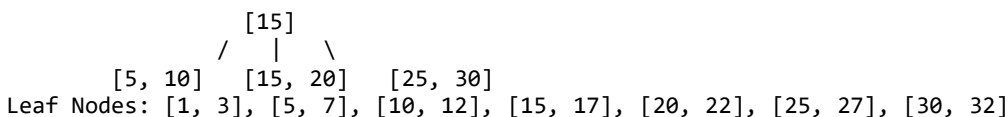
- **Order  $m$**   
The  $m$  is **the maximum number of children** for internal nodes and **the maximum number of data entries** (or pointers) for leaf nodes.  
Each non-root internal node, and each leaf node (except possibly the root), must have at least  $m/2$  entries.
- **Keys in Nodes**  
Sorted in non-decreasing order within each node. Internal nodes guide searches, and leaf nodes facilitate range queries.
- **Height**  
With  $n$  data entries and order  $m$ , the height is at most  $\log_{\lceil m/2 \rceil}(n+1)$ .

B+ Tree Operations:

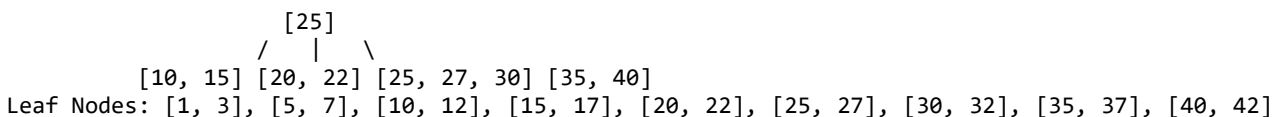
- **Search:**  
Begins at the root and follows keys down the tree to locate the desired data entry.
- **Insertion**  
New entries are always **inserted into leaf nodes**. If a leaf node becomes full, it splits, and **the middle key is promoted to the parent node**.
- **Deletion**  
Removes entries from leaf nodes. If a leaf node falls below a minimum occupancy, it **may merge with a sibling or redistribute entries**.

Example:

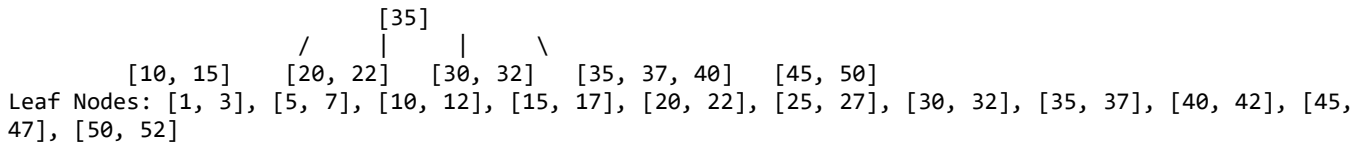
B+ Tree with Order  $m=3$



B+ Tree with Order  $m=4$



B+ Tree with Order m=5



## Prefix Tree

A Prefix Tree, also known as a Trie (pronounced "try"), is a specialized tree-like data structure that is used to efficiently store and retrieve keys in a dataset of strings.

The name "Trie" comes from the word "retrieval." This data structure is particularly useful for tasks that involve searching for words or prefixes,

such as autocomplete systems, spell checkers, and IP routing.

```
import java.util.HashMap;
import java.util.Map;

public class PrefixTree {
    // Stores the word at the end node, optional for some implementations
    private String word;
    private Map<Character, PrefixTree> children;
    private boolean isWord;

    public PrefixTree() {
        this.children = new HashMap<>();
        this.isWord = false;
        this.word = null;
    }

    // Method to insert a word into the Prefix Tree
    public void insert(String word) {
        //The "this" object is the original PrefixTree object used at the beginning of each word.
        PrefixTree node = this;
        // Put all characters into the prefix tree sequentially
        for (char c : word.toCharArray()) {
            node.children.putIfAbsent(c, new PrefixTree());
            node = node.children.get(c);
        }
        node.isWord = true;
        node.word = word;
    }

    // Method to search for a word in the Prefix Tree
    public boolean search(String word) {
        PrefixTree node = this;
        for (char c : word.toCharArray()) {
            node = node.children.get(c);
            if (node == null) {
                return false;
            }
        }
        return node.isWord;
    }

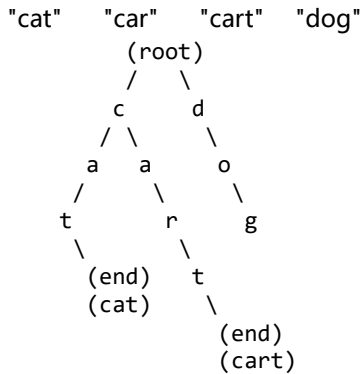
    // Method to check if any word in the Prefix Tree starts with the given prefix
    public boolean startsWith(String prefix) {
        PrefixTree node = this;
        for (char c : prefix.toCharArray()) {
            node = node.children.get(c);
            if (node == null) {
                return false;
            }
        }
        return true;
    }
}
```

```

public static void main(String[] args) {
    PrefixTree trie = new PrefixTree();
    trie.insert("apple");
    System.out.println(trie.search("apple"));    // Output: true
    System.out.println(trie.search("app"));      // Output: false
    System.out.println(trie.startsWith("app")); // Output: true
    trie.insert("app");
    System.out.println(trie.search("app"));      // Output: true
}

```

### Example



## Skip Lists

A Probabilistic Alternative to Balanced Trees

### Usage

```

import java.util.*;

class SkipList {
    static final int MAX_LEVEL = 16;
    private final Node head;
    private final Random random;
    private int level;

    // Node class for SkipList
    static class Node {
        int value;
        Node[] next;

        Node(int value, int level) {
            this.value = value;
            this.next = new Node[level];
        }
    }

    // Constructor
    public SkipList() {
        this.head = new Node(-1, MAX_LEVEL);
        this.random = new Random();
        this.level = 1;
    }

    // Generate random level for a new node
    private int randomLevel() {
        int lvl = 1;
        while (random.nextFloat() < 0.5 && lvl < MAX_LEVEL) {
            lvl++;
        }
        return lvl;
    }

    // Insert a value into the skip list

```



```

public void insert(int value) {
    Node current = head;
    Node[] update = new Node[MAX_LEVEL];
    Arrays.fill(update, head);

    // Find the insertion point
    for (int i = level - 1; i >= 0; i--) {
        while (current.next[i] != null && current.next[i].value < value) {
            current = current.next[i];
        }
        update[i] = current;
    }

    int newLevel = randomLevel();
    if (newLevel > level) {
        for (int i = level; i < newLevel; i++) {
            update[i] = head;
        }
        level = newLevel;
    }

    // Insert the new node
    Node newNode = new Node(value, newLevel);
    for (int i = 0; i < newLevel; i++) {
        newNode.next[i] = update[i].next[i];
        update[i].next[i] = newNode;
    }
}

// Search for a value in the skip list
public boolean search(int value) {
    Node current = head;

    for (int i = level - 1; i >= 0; i--) {
        while (current.next[i] != null && current.next[i].value < value) {
            current = current.next[i];
        }
    }

    current = current.next[0];
    return current != null && current.value == value;
}

// Delete a value from the skip list
public void delete(int value) {
    Node current = head;
    Node[] update = new Node[MAX_LEVEL];
    Arrays.fill(update, head);

    // Find the node to delete
    for (int i = level - 1; i >= 0; i--) {
        while (current.next[i] != null && current.next[i].value < value) {
            current = current.next[i];
        }
        update[i] = current;
    }

    current = current.next[0];
    if (current != null && current.value == value) {
        for (int i = 0; i < level; i++) {
            if (update[i].next[i] != current) break;
            update[i].next[i] = current.next[i];
        }

        while (level > 1 && head.next[level - 1] == null) {
            level--;
        }
    }
}

```

```

    }

    // Print the skip list
    public void print() {
        for (int i = 0; i < level; i++) {
            Node current = head.next[i];
            System.out.print("Level " + i + ": ");
            while (current != null) {
                System.out.print(current.value + " ");
                current = current.next[i];
            }
            System.out.println();
        }
    }

    // Main method for testing
    public static void main(String[] args) {
        SkipList skipList = new SkipList();

        skipList.insert(3);
        skipList.insert(6);
        skipList.insert(7);
        skipList.insert(9);
        skipList.insert(12);
        skipList.insert(19);
        skipList.insert(17);
        skipList.insert(26);
        skipList.insert(21);
        skipList.insert(25);

        System.out.println("Skip List after insertion:");
        skipList.print();

        System.out.println("Search for 19: " + skipList.search(19));
        System.out.println("Search for 15: " + skipList.search(15));

        skipList.delete(19);
        System.out.println("Skip List after deleting 19:");
        skipList.print();
    }
}

```

## Graph Data Structure

Based on Data Structure

## Disjoint Set Union (DSU) or Union-Find

It is a data structure that efficiently manages and **manipulates partitions of a set into disjoint subsets**. It supports two main operations:

Based on Graph Type

## Directed Graph

A graph in **which every edge has a direction**, indicating a one-way relationship between nodes.

For example, if there is an edge from node A to node B, it means you can travel from A to B, but not necessarily from B to A.

### Base Ring Tree

A special kind of graph that consists of **a single cycle (ring)** and several trees attached to it.

The "base ring" is the cycle part, and the trees (树) are connected to the nodes of this cycle.

It is often used in graph theory problems because it represents a common structure in many scenarios, combining cyclic and acyclic components.

## Pseudotree and Pseudoforest

What is "pseudotree" and "pseudoforest", What graph type does they belong?

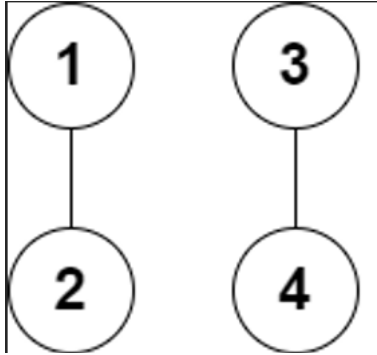
## Undirected Graph

Edges **do not have a direction**, indicating a two-way relationship.

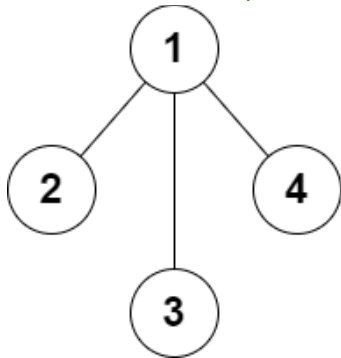
Nodes **can exist without any edges**. These nodes are called isolated nodes or isolated vertices. For example:

Example: A friendship in a social network is typically modeled as an undirected edge.

There are 4 nodes with odd degrees; we can connect **two different pairs of them** to ensure all 4 nodes have even degrees.



There are **no two distinct pairs** among them that can be connected.



## Weighted Graph

Edges have weights, representing some cost or distance.

Example: A road map where edges represent roads, and weights represent distances.

## Unweighted Graph

All edges are treated equally with no weights.

Example: A simple network of computers connected without specific costs.

## Cyclic Graph

Contains at least one cycle (a path where the start and end nodes are the same).

Example: Feedback loops in a control system.

## Acyclic Graph

Contains no cycles.

Example: A task dependency graph in a project (DAG: Directed Acyclic Graph).

## Disconnected Graph

In a disconnected graph, some nodes might not have any edges at all, leaving them isolated.

### Matrix Data Structure

A matrix represents a collection of numbers arranged in an order of rows and columns.

It is necessary to enclose the elements of a matrix in parentheses or brackets.

A matrix with 9 elements is shown below.

Col →	0	1	2	
Row ↓	0	5	10	20
1	25	30	35	
2	1	3	4	

### Algorithms / Core

## Backtracking

Double backtracking

Power Set LCCI

## Bitmap

## Breadth-first Search

## Conditional Logic

## Depth-first search

Basic code structure

```
public int depthFirstSearch(int[] nums, int target){  
    depthFirstSearch(nums, target);  
}
```

## Diff

Prefix sum

Each element in a sequence represents the cumulative sum of all previous elements up to that point.

## Dynamic Programming

Preparation

Compute all potential DP results at each index for subsequent reference.

## Greedy

A greedy algorithm is an approach to solving problems by making the locally optimal choice at each step with the hope that this leads to a globally optimal solution.

It works by breaking down a problem into smaller sub-problems, solving each sub-problem by choosing the best option available at the moment, without reconsidering previous decisions.

## HashTable

Value

The index is more suitable as a count information rather than the number of numbers.

## Heap

## Linked List

## Math

## Queue

## Recursion

Simplify for loops

If you find that you need a lot of for iterations, try using unbounded recursion.

Private and public vo data

```
public Vo dfs(TreeNode root, int start, Vo vo)
```

The vo object remains private to each path when a new vo instance is passed to subsequent recursions.

Avoid modifying the parent vo object during the process (e.g. vo.pathLen++).

The vo object is shared across all paths when the original vo instance is passed to subsequent recursions.

Return Value

At the final recursion level, verify how the returned data has changed.

Amount of Time for Binary Tree to Be Infected

## Set

## Sliding Window

Group

Exclusion

Follow the traversal, move the right boundary, and exclude elements at the left boundary.

Association

Check a far point associated with the sliding window.

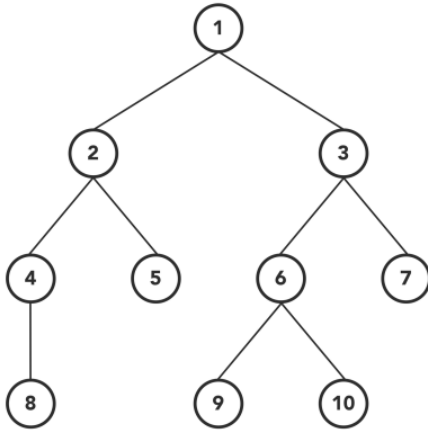
## Sorting

## Skip List

## Traversal

Preorder traversal

Visits **the current node** before visiting any nodes inside left or right subtrees.  
(root nodes > left nodes > right nodes)

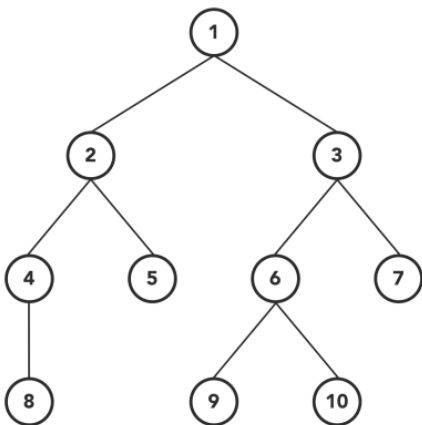


#### Usage

```
private void preorder(TreeNode root, List<Integer> list){  
    if(root != null){  
        list.add(root.val);  
        preorder(root.left,list);  
        preorder(root.right,list);  
    }  
}
```

#### Inorder traversal

Visits **all nodes inside the left subtree**, then visits **the current node** before visiting **any node within the right subtree**.  
(left nodes > root nodes > right nodes)



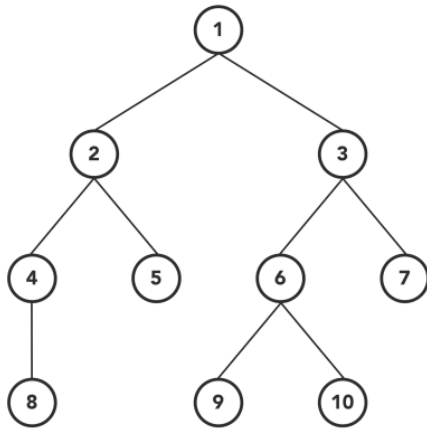
#### Usage

```
private void inorder(TreeNode root, List<Integer> list){  
    if(root != null){  
        inorder(root.left,list);  
        list.add(root.val);  
        inorder(root.right,list);  
    }  
}
```

#### Postorder traversal

(left nodes > right nodes > root nodes)

Visits **the current node** after visiting **all the nodes of left and right subtrees**.

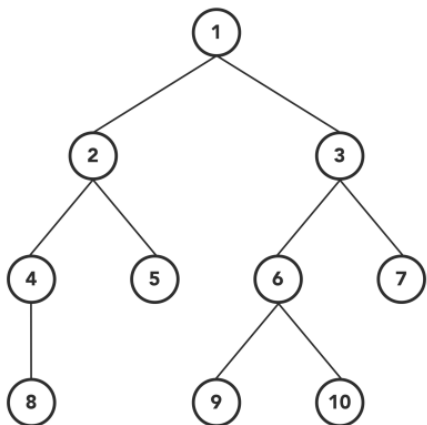


Usage

```
private void postorder(TreeNode root, List<Integer> list){  
    if(root != null){  
        postorder(root.left,list);  
        postorder(root.right,list);  
        list.add(root.val);  
    }  
}
```

Level order traversal

Visits nodes **level-by-level** and **in left-to-right** fashion at the same level.



## Algorithms / Questions

Backtrack

### Scenarios

Calculate the current return value:

When each branch needs to access shared data, based on **the shared data**. (e.g. this object, shared array)

When each branch needs its own private data, based on **the last returned data**.

Whenever possible, **return 0** instead of null, as 0 is useful for numerical calculations during backtracking.

Too many return values:

Encapsulate the return values into a **single object** to be returned by the method.

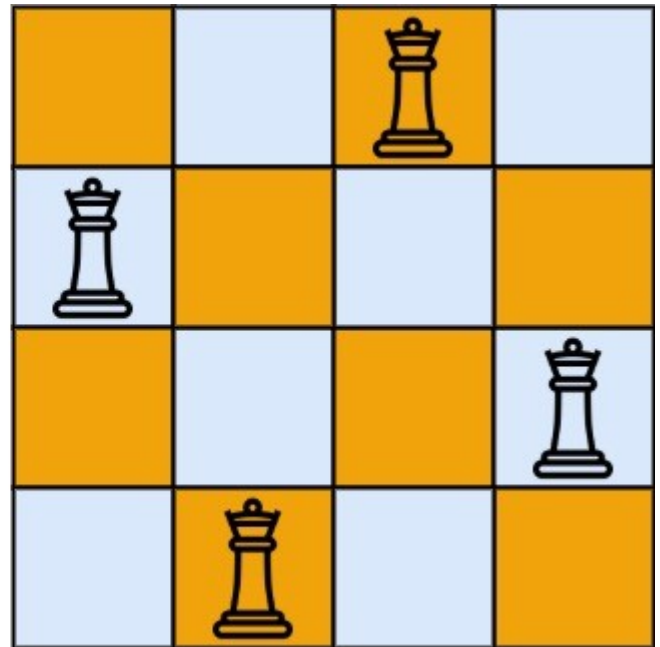
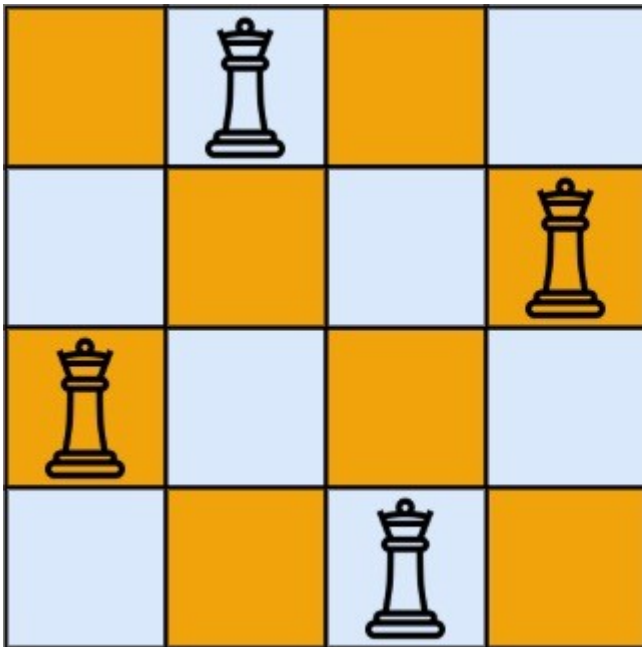
### N-Queens

The **n-queens** puzzle is the problem of placing **n** queens on an **n x n** chessboard such that no two queens attack each other.

Given an integer **n**, return *all distinct solutions to the n-queens puzzle*. You may return the answer in **any order**.

Each solution contains a distinct board configuration of the n-queens' placement, where '**Q**' and '**.**' both indicate a queen and an empty space, respectively.

#### Example 1:



**Input:** n = 4

**Output:** [".Q...", "...Q", "Q...", "...Q."], [".Q.", "Q...", "...Q", ".Q."]]

**Explanation:** There exist two distinct solutions to the 4-queens puzzle as shown above

#### Example 2:

**Input:** n = 1

**Output:** [".Q"]

#### Constraints:

- 1 <= n <= 9

### Previous Solution

```
package com.citi.ccb.cashmgmt;
```

```
import java.util.ArrayList;  
import java.util.Arrays;  
import java.util.List;
```

```
class Solution {  
    List<List<String>> results=new ArrayList<>();  
  
    public List<List<String>> solveNQueens(int n) {  
        //A. place a chess on the first line;
```



```

    for(int x=0; x<n; x++){
        int [][] board = new int[n][n];
        //B. the current grid is valid by default.
        dfs(board, x, 0, n, 1);
    }
    return results;
}

```

```

private List<String> buildBoardStringList(int[][] board, int n) {
    List<String> result=new ArrayList<>();
    //A. horizontal direction.
    for (int y = 0; y < n; y++) {
        StringBuilder currentString=new StringBuilder();
        for (int x = 0; x < n; x++) {
            if(board[x][y]==1)currentString.append('Q');
            else currentString.append('.');
        }
        result.add(currentString.toString());
    }
    return result;
}

```

```

// x x x 0
// 0 x x x
// x x 0 x
// x 0 x x

```

```

// (3, 3) (2, 4) (4, 2)

```

```

private void dfs(int [][] board, int x, int y, int n, int sum){
    //A. place a chess on the current grid(x, y).
    board[x][y] = 1;
    //A. end condition.
    if(sum==n){
        //A. collect results.
        results.add(buildBoardStringList(board, n));
        return;
    }

```

```

    //A. check if there is any valid grid.

```

```

    boolean original=true;

```

```

    for(int i=0; i<n; i++){

```

```

        for (int j = 0; j < n; j++) {

```

```

            //B. check if the current coordinate(i, j) of the current chess is valid.

```

```

            if(!checkIfChessValid(board, x, y, i, j, n))continue;

```

```

            //B. place the current chess in the next call.

```

```

            // create a new board because there are multiple calls in the same level.

```

```

            //B. how to avoid operating on the same object with different execution paths during

```

recursion?

```

            dfs(original?board: Arrays.copyOf(board,board.length), i, j, n, sum+1);

```

```

            original=false;

```

```

        }

```

```

    }

```

```

    //A. reset the current grid.

```

```

    board[x][y] = 0 ;

```

```

}

```

```

private boolean checkIfChessValid(int [][] board, int x, int y, int i, int j, int n) {
    //A. check in the horizontal and oblique direction
    if(i==x || j==y || i-x == j-y || board[i][j]==1)return false;
    //A. check other grids
    for (int k = 0; k < n; k++) {
        for (int l = 0; l < n; l++) {
            if(board[k][l]==1){
                if(i==k || j==l || Math.abs(i-k) == Math.abs(j-l))return false;
            }
        }
    }
    return true;
}

```

```

}

//[      ["Q...", "...Q.", ".Q...", "...Q", "..Q.."],
//      [".Q...", "...Q.", "Q...", "..Q..", "....Q"],
//      ["..Q..", "Q...", "...Q.", ".Q...", "....Q"],
//      ["...Q.", "Q...", "...Q.", "...Q", ".Q..."],
//      ["....Q", "..Q..", "Q....", "...Q.", ".Q..."]]

```

## Standard Solution

```

class Solution {
    public List<List<String>> solveNQueens(int n) {
        List<List<String>> solutions = new ArrayList<List<String>>();
        int[] queens = new int[n]; // column indexes of queens corresponding to each row.
        Arrays.fill(queens, -1);
        Set<Integer> columns = new HashSet<Integer>(); // column indexes
        Set<Integer> diagonals1 = new HashSet<Integer>();
        Set<Integer> diagonals2 = new HashSet<Integer>();
        backtrack(solutions, queens, n, 0, columns, diagonals1, diagonals2);
        return solutions;
    }

    public void backtrack(List<List<String>> solutions, int[] queens, int n, int row, Set<Integer> columns,
        Set<Integer> diagonals1, Set<Integer> diagonals2) {
        if (row == n) {
            List<String> board = generateBoard(queens, n);
            solutions.add(board);
        } else {
            //A. travers columns.
            for (int i = 0; i < n; i++) {
                if (columns.contains(i)) {
                    continue;
                }
                int diagonal1 = row - i;
                if (diagonals1.contains(diagonal1)) {
                    continue;
                }
                int diagonal2 = row + i;
                if (diagonals2.contains(diagonal2)) {
                    continue;
                }
                // traverse downward
                // x 0 x x 2
                // x x x 0 4
                // 0 x x x 1
                // x x 0 x 3
                // queens: 2 4 1 3
                // columns: 2 4 1 3
                // diagonals1: -1 -3 2
                // diagonals2: 1 4 2
                queens[row] = i;
                columns.add(i);
                diagonals1.add(diagonal1);
                diagonals2.add(diagonal2);
                backtrack(solutions, queens, n, row + 1, columns, diagonals1, diagonals2);
                //A. Because these objects are reset after each call, conflicts in traversal paths do not
                occur.

                // The backtracking method can return to the original path and reuse the object,
                // without having to execute to the bottom like the ordinary dfs method.
                queens[row] = -1;
                columns.remove(i);
                diagonals1.remove(diagonal1);
                diagonals2.remove(diagonal2);
            }
        }
    }

    public List<String> generateBoard(int[] queens, int n) {
        List<String> board = new ArrayList<String>();
    }
}

```

```

    for (int i = 0; i < n; i++) {
        char[] row = new char[n];
        Arrays.fill(row, '.');
        row[queens[i]] = 'Q';
        board.add(new String(row));
    }
    return board;
}
}

```

## Word Search II

Given an  $m \times n$  board of characters and a list of strings **words**, return *all words on the board*.

Each word must be constructed from letters of sequentially adjacent cells, where **adjacent cells** are horizontally or vertically neighboring.

The same letter cell may not be used more than once in a word.

**Example 1:**

o	a	a	n
e	t	a	e
i	h	k	r
i	f	l	v

**Input:** board = [["o","a","a","n"],["e","t","a","e"],["i","h","k","r"],["i","f","l","v"]], words = ["oath","pea","eat","rain"]

**Output:** ["eat","oath"]

**Example 2:**

a	b
c	d

**Input:** board = [["a","b"],["c","d"]], words = ["abcb"]

**Output:** []

**Constraints:**

- $m == \text{board.length}$
- $n == \text{board}[i].\text{length}$
- $1 \leq m, n \leq 12$
- $\text{board}[i][j]$  is a lowercase English letter.
- $1 \leq \text{words.length} \leq 3 * 10^4$
- $1 \leq \text{words}[i].\text{length} \leq 10$
- $\text{words}[i]$  consists of lowercase English letters.
- All the strings of words are unique.

## Previous Solution

```
class Solution {
    private List<String> results=new ArrayList<>();
    public List<String> findWords(char[][] board, String[] words) {
        this.results=new ArrayList<>();
        int n =words.length;
        Map<Character, List<int[]>> firstLetterMap=new HashMap<>(); // {'a':[ [2,3], [3,4] ]}
        //A. initialize firstLetterMap
        for (String word : words) {
            firstLetterMap.put(word.charAt(0),new ArrayList<>());
        }
        //A. find the coordinate of the first letter for each word.
        // avoid repeated traversal.
        for (int i = 0; i < board.length; i++) {
            for (int j = 0; j < board[0].length; j++) {
                if(firstLetterMap.containsKey(board[i][j])){
                    List<int[]> ints = firstLetterMap.get(board[i][j]);
                    ints.add(new int[]{i,j});
                }
            }
        }
        //A. find a word from the first character id.
        for (String word : words) {
            List<int[]> coordinateList = firstLetterMap.get(word.charAt(0));
            for (int[] ints : coordinateList) {
                if(backtrack(board, word, ints[0], ints[1], 0, new int[board.length][board[0].length]))break;
            }
        }
        return this.results;
    }

    private boolean backtrack(char[][] board, String word, int row, int column, int ind, int[][] paths){
        //A. end condition.
        if(invalidCoordinate(row,column,board))return false;
        if(paths[row][column]==1)return false;
        if(ind>word.length())return false;
        boolean passed=word.charAt(ind)==board[row][column];
        if(passed && ind==word.length()-1){
            this.results.add(word);
            return true;
        }
        //A. check if the current letter is valid.
        if(passed){
            //A. mark the current grid.
            paths[row][column]=1;
            // a b c
            // a e d
            // a f g
            // eaabcdgfa
            //A. these paths can share the mark list because they only check for a single word.
            // This method is different from the NQueen problem because the NQueen problem stores different
            data for each call,
            // while the current method only changes the value of one grid to 1. Both methods will clean up
            stored data.
            boolean res= backtrack(board, word, row+1, column, ind+1, paths)

```

```

        ||backtrack(board, word, row-1, column, ind+1, paths)
        ||backtrack(board, word, row, column+1, ind+1, paths)
        ||backtrack(board, word, row, column-1, ind+1, paths);
    //A. There will be no conflicts caused by operating shared objects.
    // After calling these four backtracking methods, the grid will return to the original state at
the end condition.
    paths[row][column]=0;
    return res;
}
return false;

}

private boolean invalidCoordinate(int row, int column, char[][] board) {
    return row>=board.length||column>=board[0].length || row<0 || column<0;
}

}

```

## Standard Solution

```

class Solution {
    int[][] dirs = {{1, 0}, {-1, 0}, {0, 1}, {0, -1}};

    public List<String> findWords(char[][] board, String[] words) {
        Trie trie = new Trie();
        for (String word : words) {
            trie.insert(word);
        }

        Set<String> ans = new HashSet<String>();
        //A. traverse every grid on the board.
        for (int i = 0; i < board.length; ++i) {
            for (int j = 0; j < board[0].length; ++j) {
                backtrack(board, trie, i, j, ans);
            }
        }
        return new ArrayList<String>(ans);
    }

    public void backtrack(char[][] board, Trie now, int i1, int j1, Set<String> ans) {
        // End conditions.
        if (!now.children.containsKey(board[i1][j1])) {
            return;
        }
        char ch = board[i1][j1];
        now = now.children.get(ch);
        //A. found a matching word.
        if (!"".equals(now.word)) {
            ans.add(now.word);
        }
        //A. avoid recursing over the same grid.
        board[i1][j1] = '#';
        for (int[] dir : dirs) {
            int i2 = i1 + dir[0], j2 = j1 + dir[1];
            if (i2 >= 0 && i2 < board.length && j2 >= 0 && j2 < board[0].length) {
                //B. traverse in the top, bottom, left, right directions.
                backtrack(board, now, i2, j2, ans);
            }
        }
        //A. restore the value of the current grid.
        board[i1][j1] = ch;
    }
}

class Trie {
    String word;
    Map<Character, Trie> children;
    boolean isWord;
}

```

```

public Trie() {
    this.word = "";
    this.children = new HashMap<Character, Trie>();
}

public void insert(String word) {
    //A. The "this" object is the original Trie object used at the beginning of each word.
    Trie cur = this;
    //A. Traverse the characters in the word.
    for (int i = 0; i < word.length(); ++i) {
        char c = word.charAt(i);
        //B. Set the current character as a key.
        if (!cur.children.containsKey(c)) {
            cur.children.put(c, new Trie());
        }
        // "ABB"      "ABC"
        //      R
        //      A
        //      B
        //      B("ABB")  C("ABC")
        //B. set cur to the Trie created earlier with new.
        cur = cur.children.get(c);
    }
    cur.word = word;
}
}

```

### Step-By-Step Directions From a Binary Tree Node to Another

You are given the root of a **binary tree** with  $n$  nodes. Each node is uniquely assigned a value from 1 to  $n$ .

You are also given an integer `startValue` representing the value of the start node  $s$ , and a different integer `destValue` representing the value of the destination node  $t$ .

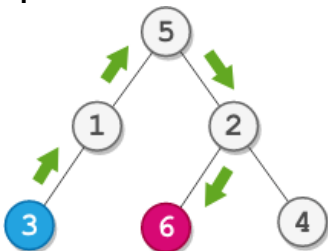
Find the **shortest path** starting from node  $s$  and ending at node  $t$ .

Generate step-by-step directions of such path as a string consisting of only the **uppercase** letters 'L', 'R', and 'U'. Each letter indicates a specific direction:

- 'L' means to go from a node to its **left child** node.
- 'R' means to go from a node to its **right child** node.
- 'U' means to go from a node to its **parent** node.

Return *the step-by-step directions of the **shortest path** from node  $s$  to node  $t$ .*

#### Example 1:



**Input:** root = [5,1,2,3,null,6,4], startValue = 3, destValue = 6

**Output:** "UURL"

**Explanation:** The shortest path is:  $3 \rightarrow 1 \rightarrow 5 \rightarrow 2 \rightarrow 6$ .

#### Example 2:



**Input:** root = [2,1], startValue = 2, destValue = 1

**Output:** "L"

**Explanation:** The shortest path is: 2 → 1.

**Constraints:**

- The number of nodes in the tree is n.
- $2 \leq n \leq 10^5$
- $1 \leq \text{Node.val} \leq n$
- All the values in the tree are **unique**.
- $1 \leq \text{startValue}, \text{destValue} \leq n$
- $\text{startValue} \neq \text{destValue}$

## Previous Solution

```
class Solution {
    public String getDirections(TreeNode root, int startValue, int destValue) {

    }

    public void preorderTree(TreeNode root, int startValue, int destValue, Character direction, StringBuilder sb){
        if(root!=null){
            if(root.val==startValue){

            }
            getDirections(root.left, startValue, destValue, 'L', sb);
            getDirections(root.right, startValue, destValue, 'R', sb);
        }
    }
}
```

## Standard Solution

```
class Solution {
    List<List<Character>> resultPath;
    List<Character> startPath;
    List<Character> endPath;

    public String getDirections(TreeNode root, int startValue, int destValue) {
        this.resultPath = new ArrayList<>();
        this.startPath = new ArrayList<>();
        this.endPath = new ArrayList<>();
        //A. find the nearest common ancestor node of two nodes.
        TreeNode commonRoot = findRoot(root, startValue, destValue);
        //A. find the path from start node to commonRoot.
        dfsStart(commonRoot, startValue);
        //A. find the path from commonRoot to end node.
        dfsDest(commonRoot, destValue);
        StringBuilder sb = new StringBuilder();
        //A. merge two pathes.
        for(List<Character> paths : resultPath){
            for(char path : paths) sb.append(path);
        }
        return sb.toString();
    }

    public TreeNode findRoot(TreeNode root, int startValue, int destValue){
        //A. Return nodes with null values, startValue, or destValue.
        if(root == null || root.val == startValue || root.val == destValue) return root;
        TreeNode left = findRoot(root.left, startValue, destValue);
        TreeNode right = findRoot(root.right, startValue, destValue);
        if(left == null) return right;
        if(right == null) return left;
        return root;
    }
}
```

```

public void dfsStart(TreeNode root, int startValue){
    if(root == null) return;
    //A. Found the start node, save the path.
    if(root.val == startValue){
        resultPath.add(new ArrayList<>(startPath));
        return;
    }
    startPath.add('U');
    dfsStart(root.left, startValue);
    startPath.remove(startPath.size()-1);

    startPath.add('U');
    dfsStart(root.right, startValue);
    startPath.remove(startPath.size()-1);
}

public void dfsDest(TreeNode root, int destValue){
    if(root == null) return;
    //A. Found the end node, save the path.
    if(root.val == destValue){
        resultPath.add(new ArrayList<>(endPath));
        return;
    }
    endPath.add('L');
    dfsDest(root.left, destValue);
    endPath.remove(endPath.size()-1);

    endPath.add('R');
    dfsDest(root.right, destValue);
    endPath.remove(endPath.size()-1);
}
}

```

## Bitmap

### Different Phone Numbers

Given a file containing a large number of phone numbers, each number is 8 digits, how can we count the number of different numbers? Memory limit 100M.

## Standard Solution

Using Integers:

Since an integer is 32 bits long, we can use each bit of an integer to represent a single phone number.

Thus, if we have 100,000,000 possible phone numbers, we need 100,000,000 bits.

This equates to  $100,000,000 / 32 = 3,125,000$  integers (each integer containing 32 bits).

Counting Unique Numbers:

Iterate through the bitmap array and use `Integer.bitCount()` to count the number of bits set to 1 in each int.

```

public class PhoneNumberCounter {
    public static void main(String[] args) {
        // Assuming we have a method that provides phone numbers from a file
        int[] phoneNumbers = getPhoneNumbersFromFile();

        // Total bits needed: 100 million (100,000,000)
        // Each int is 32 bits, so we need 100,000,000 / 32 = 3,125,000 ints
        int[] bitmap = new int[100_000_000 / 32 + 1];

        for (int number : phoneNumbers) {

```



```

        int arrayIndex = number / 32;
        int bitPosition = number % 32;
        bitmap[arrayIndex] |= (1 << bitPosition);
    }

    // Count the number of unique phone numbers
    int uniqueCount = 0;
    for (int i = 0; i < bitmap.length; i++) {
        uniqueCount += Integer.bitCount(bitmap[i]);
    }

    System.out.println("Unique phone numbers count: " + uniqueCount);
}

private static int[] getPhoneNumbersFromFile() {
    // Placeholder for actual file reading logic
    return new int[]{12345678, 87654321, 12345678, 23456789}; // example phone numbers
}
}

```

### Breadth-first Search

#### Word Ladder

A transformation sequence from word **beginWord** to word **endWord** using a dictionary **wordList** is a sequence of words **beginWord** -> **s1** -> **s2** -> ... -> **sk** such that:

- Every adjacent pair of words differs by a single letter.
- Every **si** for  $1 \leq i \leq k$  is in **wordList**. Note that **beginWord** does not need to be in **wordList**.
- **sk == endWord**

Given two words, **beginWord** and **endWord**, and a dictionary **wordList**, return the number of words in the shortest transformation sequence from **beginWord** to **endWord**, or 0 if no such sequence exists.

Example 1:

Input: **beginWord** = "hit", **endWord** = "cog", **wordList** = ["hot","dot","dog","lot","log","cog"]

Output: 5

Explanation: One shortest transformation sequence is "hit" -> "hot" -> "dot" -> "dog" -> "cog", which is 5 words long.

Example 2:

Input: **beginWord** = "hit", **endWord** = "cog", **wordList** = ["hot","dot","dog","lot","log"]

Output: 0

Explanation: The **endWord** "cog" is not in **wordList**, therefore there is no valid transformation sequence.

Constraints

- $1 \leq \text{beginWord.length} \leq 10$
- $\text{endWord.length} == \text{beginWord.length}$
- $1 \leq \text{wordList.length} \leq 5000$
- $\text{wordList}[i].\text{length} == \text{beginWord.length}$
- **beginWord**, **endWord**, and **wordList[i]** consist of lowercase English letters.
- **beginWord** != **endWord**
- All the words in **wordList** are unique.

## Previous Solution

```

class Solution {
    public int ladderLength(String beginWord, String endWord, List<String> wordList) {
        //A. public data
        int left=-1;
        int right=-1; // 1 <= wordList.length <= 5000
        int matchingLeft=-1;
    }
}

```

```

int matchingRight=-1;
String previousWord=null;
int invalidWordNum=0;
//A. traverse wordList
for(int i =-1; i<wordList.size(); previousWord=currentWord,i++){
    String currentWord=i==-1?beginWord:wordList.get(i);
    //C. check if currentWord is valid. 出现错误单词后需要与之前的单词逐个比较吗?
    if(left!=-1&&previousWord!=null&&!checkWorkList(previousWord,currentWord)){
        invalidWordNum++;
    }
    //B. found beginWord
    if(currentWord.equals(beginWord)){ // 细分状态 便于分析
        left=i;
        //C. The right word already exists, but left>right.
        //      A-right-B-left-C
        if(right!=-1&&left>right){
            right=-1;
        }
        //C. skip checking if valid
    }
    //B. found endWord
    } else if(currentWord.equals(endWord)){
        right=i;
        //C. The left word already exists, save the matching result.
        //      A-left-B-right-C
        if(left!=-1&&left<right){
            matchingLeft=left;
            matchingRight=right;
            left=-1;
            right=-1;
        }
    }
}

if(matchingLeft!=-1&&matchingRight!=-1)return matchingRight-matchingLeft;
else return 0;
}
private boolean checkWorkList(String var1, String var2){
    int sumSame=0;
    int sumDiff=0;
    for(int i=0; i<var1.length(); i++){
        if(var1.charAt(i)==var2.charAt(i))sumSame++;
        else sumDiff++;
    }
    return sumDiff==1&&sumSame==var1.length()-sumDiff;
}
}

```

## Standard Solution

```

class Solution {
    Map<String, Integer> wordId = new HashMap<String, Integer>(); // word and word index
    List<List<Integer>> edge = new ArrayList<List<Integer>>(); // The index corresponds to word index.
    int nodeNum = 0; // total number of nodes

    public int ladderLength(String beginWord, String endWord, List<String> wordList) {
        //A. populate object map
        for (String word : wordList) {
            addEdge(word);
        }
        addEdge(beginWord);
        //A. check if endWord exists
        if (!wordId.containsKey(endWord)) {
            return 0;
        }
        //A. public data
        int[] dis = new int[nodeNum]; // distance from begin word to current word
        Arrays.fill(dis, Integer.MAX_VALUE);
        int beginId = wordId.get(beginWord), endId = wordId.get(endWord);
    }
}

```

```

dis[beginId] = 0;

Queue<Integer> que = new LinkedList<Integer>(); // word id queue
que.offer(beginId);
//A. populate que
while (!que.isEmpty()) {
    // check if current word with index x is the endword
    int x = que.poll();
    if (x == endId) {
        return dis[endId] / 2 + 1;
    }
    // related word indexes
    for (int it : edge.get(x)) {
        if (dis[it] == Integer.MAX_VALUE) {
            dis[it] = dis[x] + 1;
            que.offer(it);
        }
    }
}
return 0;
}

public void addEdge(String word) {
    //A. add current word
    addWord(word);
    //A. public data
    int id1 = wordId.get(word);
    char[] array = word.toCharArray();
    int length = array.length;
    //A. traverse word characters and add matching word at the same time.
    for (int i = 0; i < length; ++i) {
        char tmp = array[i];
        array[i] = '*';
        //B. add a new word(e.g. "*og", "d*g", "do*").
        String newWord = new String(array);
        addWord(newWord);
        //B. add edges to each other(e.g. "dog" - [7,8,9], "*og" - [6]).
        int id2 = wordId.get(newWord);
        edge.get(id1).add(id2);
        edge.get(id2).add(id1);
        array[i] = tmp;
    }
}

public void addWord(String word) {
    if (!wordId.containsKey(word)) {
        wordId.put(word, nodeNum++);
        edge.add(new ArrayList<Integer>());
    }
}
}

```

## Depth-first search

### Getting Started

#### Writing basic code structure

```

public int depthFirstSearch(int[] nums, int target){
    depthFirstSearch(nums, target);
}

```

## Best Time to Buy and Sell Stock IV

You are given an integer array `prices` where `prices[i]` is the price of a given stock on the  $i^{\text{th}}$  day, and an integer `k`.

Find the maximum profit you can achieve. You may complete at most **k** transactions: i.e. you may buy at most **k** times and sell at most **k** times.

**Note:** You may not engage in multiple transactions simultaneously (i.e., you must sell the stock before you buy again).

#### Example 1:

**Input:** k = 2, prices = [2,4,1]

**Output:** 2

**Explanation:** Buy on day 1 (price = 2) and sell on day 2 (price = 4), profit = 4-2 = 2.

#### Example 2:

**Input:** k = 2, prices = [3,2,6,5,0,3]

**Output:** 7

**Explanation:** Buy on day 2 (price = 2) and sell on day 3 (price = 6), profit = 6-2 = 4. Then buy on day 5 (price = 0) and sell on day 6 (price = 3), profit = 3-0 = 3.

#### Constraints:

- $1 \leq k \leq 100$
- $1 \leq \text{prices.length} \leq 1000$
- $0 \leq \text{prices}[i] \leq 1000$

### Previous Solution

```
class Solution {
    public int maxProfit(int k, int[] prices) {
        int len=prices.length;
        if(len==1)return 0;
        int pivot= prices.length/2;
        int profit=0;
        int indList=IntStream.range(0, prices.length).toArray();
        //A. bubble sort.
        for(int i=0; i< len; i++){
            for(int j=i; j< len; j++){
                if(prices[i]>prices[j]){
                    int temp1=prices[i];
                    prices[i]=prices[j];
                    prices[j]=temp1;
                    int temp2=indList[i];
                    indList[i]=indList[j];
                    indList[j]=temp2;
                }
            }
        }
        //A. calculate profit.
        for(int left=0, right=len-1-left; left< k && left<len;){
            if(indList[right]==-1){
                right--;
                //?
                continue;
            }
            if(indList[left]<indList[right]){
                profit+= prices[right]-prices[left];
            }
        }
        return profit;
    }
}
```

### Standard Solution

```
class Solution {
    public int maxProfit(int k, int[] prices) {
```

```

if (prices.length == 0) {
    return 0;
}

int n = prices.length;
k = Math.min(k, n / 2);

// Input: k = 2, prices = [3,2,6,5,0,3]
// Output: 7
// buy action
// price index - number of transactions (add an extra column)
// -3 -3 -3 -3 -3 -3 // already bought here
// -2 S x x x x
// -2 x x x x x
// there are many prices we can choose from.
int[][] buy = new int[n][k + 1];

// sell action
// price index - number of transaction (add an extra column)
// 0 0 0 0 0 0
// 0 S 0 0 0 0
// 0 0 0 0 0 0
// there are many prices we can choose from.
int[][] sell = new int[n][k + 1];

buy[0][0] = -prices[0];
sell[0][0] = 0;
for (int i = 1; i <= k; ++i) {
    buy[0][i] = sell[0][i] = Integer.MIN_VALUE / 2;
}

for (int i = 1; i < n; ++i) {
    buy[i][0] = Math.max(buy[i - 1][0], sell[i - 1][0] - prices[i]);
    for (int j = 1; j <= k; ++j) {
        buy[i][j] = Math.max(
            sell[i - 1][j] - prices[i], // you didn't have a stock on hand earlier, execute a buy
            buy[i - 1][j] // you did have a stock on hand earlier, do nothing.
        );
        sell[i][j] = Math.max(
            sell[i - 1][j], // you didn't have a stock on hand earlier, do nothing.
            buy[i - 1][j - 1] + prices[i] // you did have a stock on hand earlier, execute a sell
        );
    }
}
return Arrays.stream(sell[n - 1]).max().getAsInt();
}

```

### Frog Jump

A frog is crossing a river. The river is divided into some number of units, and at each unit, there may or may not exist a stone. The frog can jump on a stone, but it must not jump into the water.

Given a list of **stones** positions (in units) in sorted **ascending order**, determine if the frog can cross the river by landing on the last stone.

Initially, the frog is on the first stone and assumes the first jump must be **1** unit.

If the frog's last jump was **k** units, its next jump must be either **k - 1**, **k**, or **k + 1** units. The frog can only jump in the forward direction.

#### Example 1:

**Input:** stones = [0,1,3,5,6,8,12,17]

**Output:** true

**Explanation:** The frog can jump to the last stone by jumping 1 unit to the 2nd stone, then 2 units to the 3rd stone, then 2 units to the 4th stone, then 3 units to the 6th stone, 4 units to the 7th stone, and 5 units to the 8th stone.

**Example 2:**

**Input:** stones = [0,1,2,3,4,8,9,11]

**Output:** false

**Explanation:** There is no way to jump to the last stone as the gap between the 5th and 6th stone is too large.

**Constraints:**

- $2 \leq \text{stones.length} \leq 2000$
- $0 \leq \text{stones}[i] \leq 2^{31} - 1$
- $\text{stones}[0] == 0$
- stones is sorted in a strictly increasing order.

## Previous Solution

```
class Solution {

    public boolean canCross(int[] stones) {
        return recursiveSearch(stones, 0, 1);
    }

    private boolean recursiveSearch(int[] stones, int currentStoneInd, int currentUnit){
        //A. create end conditions
        if(currentStoneInd==stones.length-1)return true;
        else if(currentStoneInd==-1)return false;
        int currentVal=stones[currentStoneInd];
        //A. search for the stone that the frog can reach.
        boolean exist=false;
        int matchingInd=-1;
        for(int i=currentStoneInd+1; i<stones.length; i++){
            int comparisonVal=stones[i];
            if(comparisonVal==currentVal+currentUnit){
                exist=true;
                matchingInd=i;
                break;
            }
            else if(comparisonVal>currentVal+currentUnit){
                exist=false;
                break;
            }
        }
        //A. create recursive conditions
        if(exist){
            return recursiveSearch(stones, matchingInd, currentUnit-1)
            ||recursiveSearch(stones, matchingInd, currentUnit)
            ||recursiveSearch(stones, matchingInd, currentUnit+1);
        }else{
            return false;
        }
    }

}
```

## Standard Solution

```
class Solution {
    private Boolean[][] rec;

    public boolean canCross(int[] stones) {
        int n = stones.length;
        rec = new Boolean[n][n];
```

```

        return dfs(stones, 0, 0);
    }

    private boolean dfs(int[] stones, int currentInd, int lastDis) {
        //A. create end conditions
        if (currentInd == stones.length - 1) return true;

        if (rec[currentInd][lastDis] != null) {
            return rec[currentInd][lastDis];
        }
        //A. Check for the presence of the stones at these three distance.
        for (int curDis = lastDis - 1; curDis <= lastDis + 1; curDis++) {
            if (curDis > 0) {
                int j = Arrays.binarySearch(stones, currentInd + 1, stones.length, curDis +
stones[currentInd]);
                if (j >= 0 && dfs(stones, j, curDis)) {
                    //B. store searching result to avoid repeating searching.
                    return rec[currentInd][lastDis] = true;
                }
            }
        }
        return rec[currentInd][lastDis] = false;
    }
}

```

### Making A Large Island

You are given an  $n \times n$  binary matrix grid. You are allowed to change at most one 0 to be 1.

Return the size of the largest island in **grid** after applying this operation.

An island is a 4-directionally connected group of 1s.

**Example 1:**

**Input:** grid = [[1,0],[0,1]]

**Output:** 3

**Explanation:** Change one 0 to 1 and connect two 1s, then we get an island with area = 3.

**Example 2:**

**Input:** grid = [[1,1],[1,0]]

**Output:** 4

**Explanation:** Change the 0 to 1 and make the island bigger, only one island with area = 4.

**Example 3:**

**Input:** grid = [[1,1],[1,1]]

**Output:** 4

**Explanation:** Can't change any 0 to 1, only one island with area = 4.

**Constraints:**

- $n == \text{grid.length}$
- $n == \text{grid}[i].\text{length}$
- $1 \leq n \leq 500$
- $\text{grid}[i][j]$  is either 0 or 1.

### Previous Solution

```

class Solution {
    private int value1Sum=0;
    private boolean hasZero=false;

    public int largestIsland(int[][] grid) {
        // constrains
        // n == grid.length
        // n == grid[i].length
        // 1 <= n <= 500
        // grid[i][j] is either 0 or 1.

        // 1 0 1 0 0
        // 0 0 0 0 0
        // 0 1 1 0 0
        // 0 0 0 0 0
    }
}

```

```

    int ilen=grid.length;
    int jlen=grid[0].length;
    //A. check if we can connect all grids with a value of 1.
    for(int i=0; i< ilen; i++){
        for(int j=0; j< jlen; j++){
            if(grid[i][j]==1)value1Sum++;
            if(grid[i][j]==0)hasZero=true;
        }
    }
    if(!hasZero)return value1Sum;
    if(this.value1Sum==0)return 1;
    boolean res=checkIfGridsConnected(grid, 0, 0, 0, false);
    return res?this.value1Sum+1:this.value1Sum;
}

private boolean checkIfGridsConnected(int[][] grid, int i, int j, int sum, boolean change0To1){
    //A. limiting case.
    // 1 0 1 0 0 ?   [j]
    // 0 0 0 0 0
    // 0 1 1 0 0
    // 0 0 0 0 0
    // ? ...
    // [i]
    if(i<0||i>=grid.length)return false;
    if(j<0||j>=grid[0].length)return false;
    if(sum == this.value1Sum+1)return true;
    if(sum < this.value1Sum && grid[i][j]==0 && change0To1)return false;
    if(sum < this.value1Sum && grid[i][j]==0 && !change0To1){
        grid[i][j]=1;
        change0To1=true;
        sum++;
    }
    if(grid[i][j]==1)sum++;
    //A. start checking.
    return checkIfGridsConnected(grid, i-1, j, sum, change0To1) // left
    || checkIfGridsConnected(grid, i, j-1, sum, change0To1) // top
    || checkIfGridsConnected(grid, i+1, j, sum, change0To1) // right
    || checkIfGridsConnected(grid, i, j+1, sum, change0To1); // bottom
}
}

// 0 0 0 0 0
// 1 1 0 0 0
// 0 0 0 0 0
// 0 0 0 0 0
// 0,0,0,0,0,0
// 0,1,1,1,1,0,0
// 0,1,0,0,1,0,0
// 1,0,1,0,1,0,0
// 0,1,0,0,1,0,0
// 0,1,0,0,1,0,0
// 0,1,1,1,1,0,0

```

## Standard Solution

```

class Solution {
    static int[] d = {0, -1, 0, 1, 0};

    public int largestIsland(int[][] grid) {
        int n = grid.length, res = 0;
        int[][] tag = new int[n][n];
        Map<Integer, Integer> area = new HashMap<Integer, Integer>();

        //A. traverse grid.
        for (int i = 0; i < n; i++) {
            for (int j = 0; j < n; j++) {
                if (grid[i][j] == 1 && tag[i][j] == 0) {
                    //B. Count the number of grids in the same area around the current grid.
                    int t = i * n + j + 1; // a custom unique tag
                    area.put(t, dfs(grid, i, j, tag, t));
                }
            }
        }
    }
}

```



```

        res = Math.max(res, area.get(t));
    }
}
}
//A. traverse grid for the second time.
for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
        //B. check if there is a new grid that can be connected to the surrounding area.
        if (grid[i][j] == 0) {
            int z = 1;
            Set<Integer> connected = new HashSet<Integer>();
            //A. traverse all directions(bottom, left, top, right).
            for (int k = 0; k < 4; k++) {
                int x = i + d[k], y = j + d[k + 1];
                if (!valid(n, x, y) || tag[x][y] == 0 || connected.contains(tag[x][y])) {
                    continue;
                }
                //C. plus the number of grids of the area detected in the current direction.
                z += area.get(tag[x][y]);
                connected.add(tag[x][y]);
            }
            res = Math.max(res, z);
        }
    }
}
return res;
}

/**
 * Count the number of grids in the same area around the current grid.
 */
public int dfs(int[][] grid, int x, int y, int[][] tag, int t) {
    int n = grid.length, res = 1;
    //A. set the same tag for grids in the same area.
    tag[x][y] = t;
    //A. traverse all directions(bottom, left, top, right).
    for (int i = 0; i < 4; i++) {
        int x1 = x + d[i], y1 = y + d[i + 1];
        //B. check if the current grid is a new island.
        if (valid(n, x1, y1) && grid[x1][y1] == 1 && tag[x1][y1] == 0) {
            res += dfs(grid, x1, y1, tag, t);
        }
    }
    return res;
}

public boolean valid(int n, int x, int y) {
    return x >= 0 && x < n && y >= 0 && y < n;
}
}

```

### Vertical Order Traversal of a Binary Tree

Given the **root** of a binary tree, calculate the **vertical order traversal** of the binary tree.

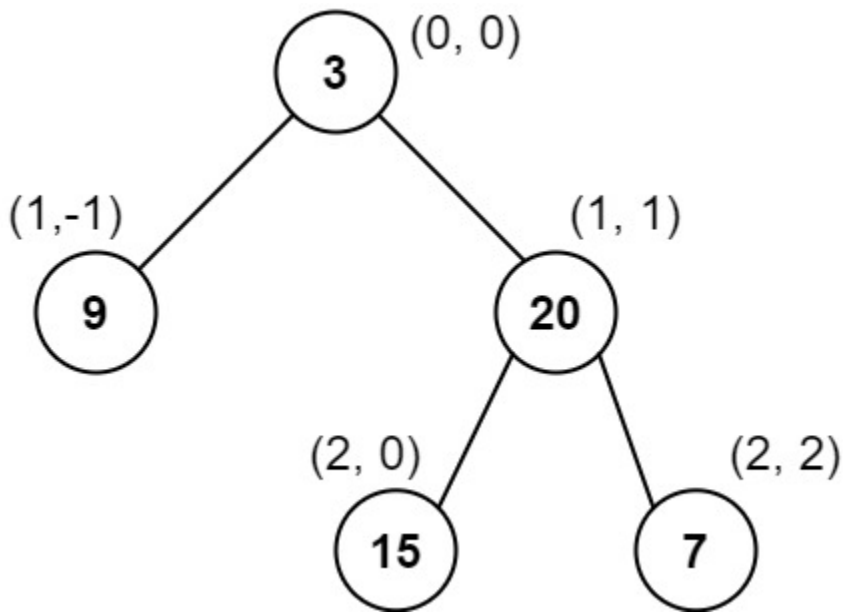
For each node at position (**row**, **col**), its left and right children will be at positions (**row + 1**, **col - 1**) and (**row + 1**, **col + 1**) respectively. The root of the tree is at (**0**, **0**).

The **vertical order traversal** of a binary tree is a list of top-to-bottom orderings for each column index starting from the leftmost column and ending on the rightmost column.

There may be multiple nodes in the same row and same column. In such a case, sort these nodes by their values.

Return *the vertical order traversal of the binary tree*.

Example 1:



**Input:** root = [3,9,20,null,null,15,7]

**Output:** [[9],[3,15],[20],[7]]

**Explanation:**

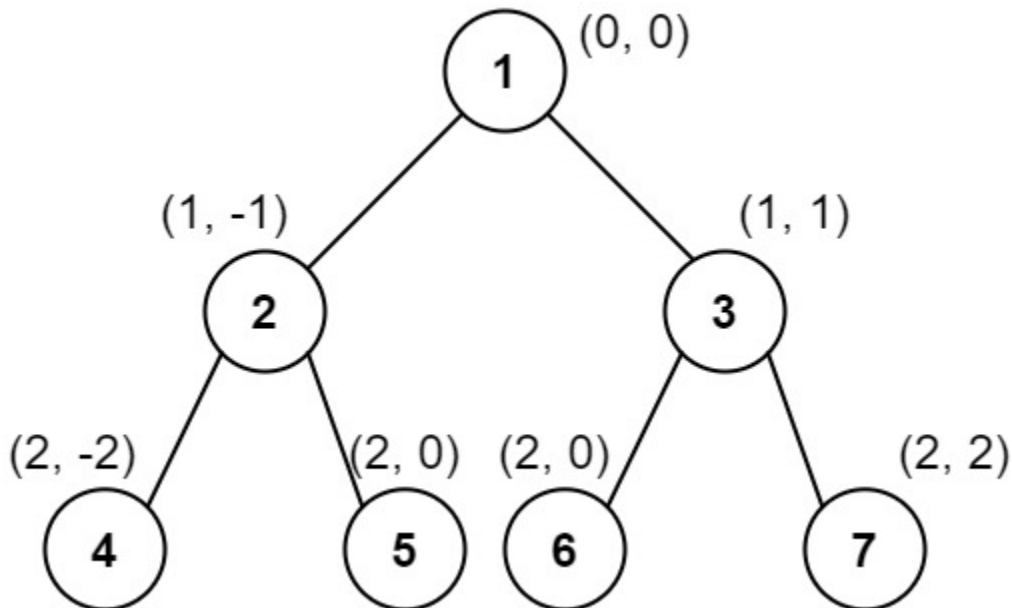
Column -1: Only node 9 is in this column.

Column 0: Nodes 3 and 15 are in this column in that order from top to bottom.

Column 1: Only node 20 is in this column.

Column 2: Only node 7 is in this column.

Example 2:



**Input:** root = [1,2,3,4,5,6,7]

**Output:** [[4],[2],[1,5,6],[3],[7]]

**Explanation:**

Column -2: Only node 4 is in this column.

Column -1: Only node 2 is in this column.

Column 0: Nodes 1, 5, and 6 are in this column.

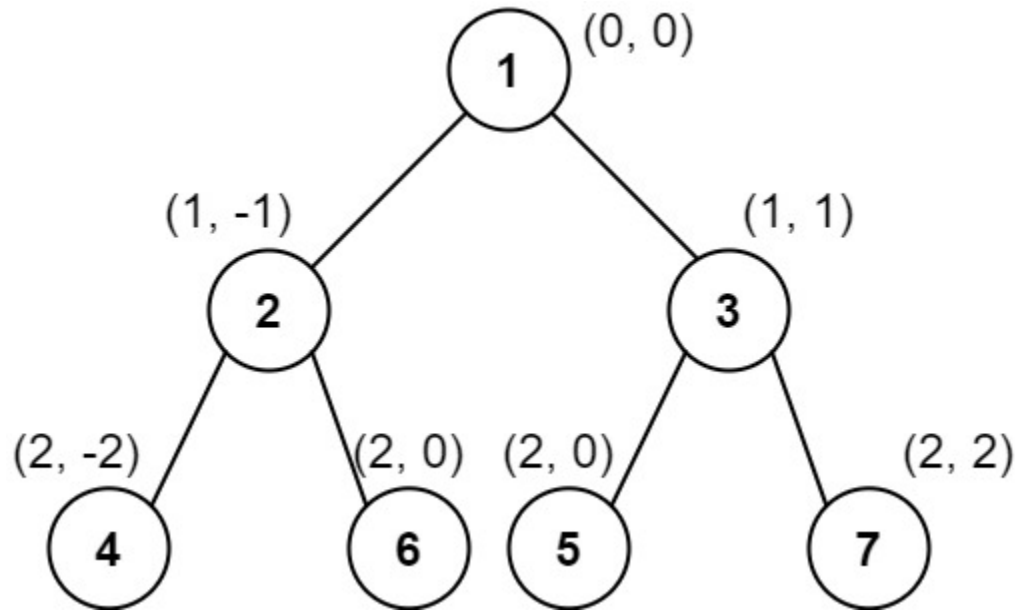
1 is at the top, so it comes first.

5 and 6 are at the same position (2, 0), so we order them by their value, 5 before 6.

Column 1: Only node 3 is in this column.

Column 2: Only node 7 is in this column.

Example 3:



**Input:** root = [1,2,3,4,6,5,7]

**Output:** [[4],[2],[1,5,6],[3],[7]]

**Explanation:**

This case is the exact same as example 2, but with nodes 5 and 6 swapped.

Note that the solution remains the same since 5 and 6 are in the same location and should be ordered by their values.

#### Constraints:

- The number of nodes in the tree is in the range [1, 1000].
- $0 \leq \text{Node.val} \leq 1000$

#### Previous Solution

```
/**
 * Definition for a binary tree node.
 * public class TreeNode {
 *     int val;
 *     TreeNode left;
 *     TreeNode right;
 *     TreeNode() {}
 *     TreeNode(int val) { this.val = val; }
 *     TreeNode(int val, TreeNode left, TreeNode right) {
 *         this.val = val;
 *         this.left = left;
 *         this.right = right;
 *     }
 * }
 */
class Solution {
    public List<List<Integer>> verticalTraversal(TreeNode root) {
        Map<Integer,List<Integer>> columnMap=new TreeMap(); // col - [ node.value ]
        //A. traverse root.
        sortTreeNode(columnMap, root, 0, 0);
        LinkedList<List<Integer>> result = new LinkedList<List<Integer>>(columnMap.values());
        return result;
    }
    private class WrappedNode{
```

```

int row;
int col;
TreeNode node;
public WrappedNode(TreeNode node, int row, int col){
    this.node=node;
    this.row=row;
    this.col=col;
}
}

private void sortTreeNodees(Map<Integer,List<Integer>> columnMap, TreeNode node, int row, int col){
    //A. end conditions.
    if(node==null)return;
    columnMap.compute(col, (key, val)->{
        if(val==null){
            List<Integer> arr=new LinkedList();
            arr.add(node.val);
            return arr;
        }else{
            val.add(node.val);
        }
        return val;
    });
    sortTreeNodees(columnMap, node.left, row+1, col-1);
    sortTreeNodees(columnMap, node.right, row+1, col+1);
}
}

```

## Standard Solution

```

class Solution {
    public List<List<Integer>> verticalTraversal(TreeNode root) {
        List<int[]> nodes = new ArrayList<int[]>(); // [ [col, row, node.val] ]
        //A. calculate the row and column index of each node.
        dfs(root, 0, 0, nodes);
        //A. ordering priority: col > row > node.val
        Collections.sort(nodes, new Comparator<int[]>() {
            public int compare(int[] tuple1, int[] tuple2) {
                if (tuple1[0] != tuple2[0]) {
                    return tuple1[0] - tuple2[0];
                } else if (tuple1[1] != tuple2[1]) {
                    return tuple1[1] - tuple2[1];
                } else {
                    return tuple1[2] - tuple2[2];
                }
            }
        });
        //A. collect results with the sorted nodes.
        List<List<Integer>> ans = new ArrayList<List<Integer>>();
        int size = 0;
        int lastcol = Integer.MIN_VALUE;
        for (int[] tuple : nodes) {
            int col = tuple[0], row = tuple[1], value = tuple[2];
            //B. create a new list for the new row.
            if (col != lastcol) {
                lastcol = col;
                ans.add(new ArrayList<Integer>());
                size++;
            }
            ans.get(size - 1).add(value);
        }
        return ans;
    }

    public void dfs(TreeNode node, int row, int col, List<int[]> nodes) {
        if (node == null) {
            return;
        }
    }
}

```

```

        nodes.add(new int[]{col, row, node.val});
        dfs(node.left, row + 1, col - 1, nodes);
        dfs(node.right, row + 1, col + 1, nodes);
    }
}

```

## Dynamic Programming

bottom-up manner

## Trapping Rain Water

Given  $n$  non-negative integers representing an elevation map where the width of each bar is 1, compute how much water it can trap after raining.

**Example 1:**



Input: height = [0,1,0,2,1,0,1,3,2,1,2,1]

Output: 6

Explanation: The above elevation map (black section) is represented by array [0,1,0,2,1,0,1,3,2,1,2,1]. In this case, 6 units of rain water (blue section) are being trapped.

**Example 2:**

Input: height = [4,2,0,3,2,5]

Output: 9

**Constraints:**

- $n == \text{height.length}$
- $1 \leq n \leq 2 \times 10^4$
- $0 \leq \text{height}[i] \leq 10^5$

## Previous Solution

```

class Solution {
    public int trap(int[] height) {
        //A. public data
        int maxHeight=0;
        int trappedRainWater=0;
        //A. traverse height list
        for(int i=0; i<height.length; i++){
            int currentHeight=height[i];
            //B. check if current height is equal or greater than the max height
            if(currentHeight>=maxHeight){
                //C. go back and collect rain water
                for(int j=i-1; j>0; j--){
                    int currentBackHeight=height[j];

```

```

        if(currentBackHeight==maxHeight)break;
        trappedRainWater+=maxHeight-currentBackHeight;
        System.out.println(""+j+" "+maxHeight+" "+currentBackHeight);
    }
    maxHeight=currentHeight;
}
}
return trappedRainWater;
}
}

```

## Standard Solution

```

class Solution {
    public int trap(int[] height) {
        int n = height.length;
        if (n == 0) {
            return 0;
        }

        int[] leftMax = new int[n];
        leftMax[0] = height[0];
        //A. traverse height list and populate leftMax list
        for (int i = 1; i < n; ++i) {
            //B. maximum value of adjacent values: get maximum value on the left or right side; fill the
            depression.
            leftMax[i] = Math.max(leftMax[i - 1], height[i]);
        }

        int[] rightMax = new int[n];
        rightMax[n - 1] = height[n - 1];
        //A. traverse height list and populate rightMax list
        for (int i = n - 2; i >= 0; --i) {
            rightMax[i] = Math.max(rightMax[i + 1], height[i]);
        }

        int ans = 0;
        //A. traverse height list and compute trapped rain water
        for (int i = 0; i < n; ++i) {
            ans += Math.min(leftMax[i], rightMax[i]) - height[i];
        }
        return ans;
    }
}

```

## Regular Expression Matching

Given an input string *s* and a pattern *p*, implement regular expression matching with support for '.' and '\*' where:

- '.' Matches any single character.
- '\*' Matches zero or more of the preceding element.

The matching should cover the **entire** input string (not partial).

Example 1:

Input: *s* = "aa", *p* = "a"

Output: false

Explanation: "a" does not match the entire string "aa".

Example 2:

Input: *s* = "aa", *p* = "a\*"

Output: true

Explanation: '\*' means zero or more of the preceding element, 'a'. Therefore, by repeating 'a' once, it becomes "aa".

Example 3:

Input: *s* = "ab", *p* = ".\*"

Output: true

Explanation: "." means "zero or more (\*) of any character (.)".

Constraints:

- $1 \leq s.length \leq 20$
- $1 \leq p.length \leq 20$
- s contains only lowercase English letters.
- p contains only lowercase English letters, '.', and '\*'.
- It is guaranteed for each appearance of the character '\*', there will be a previous valid character to match.

## Previous Solution

```
class Solution {
    public boolean isMatch(String s, String p) {
        //A. public variables
        char[] pCharArray=p.toCharArray();
        char[] sCharArray=s.toCharArray();
        Character lastSChar=null;
        Character lastPChar=null; // except '.' and '*'
        boolean isInSocialCharacters=false; // '.', '*'
        Integer characterType=null; // '.' -> 0 '*' -> 1 "." 2
        //A. traverse string p
        for(int i=0,j=0; i<pCharArray.length; i++,j++){
            char pi=pCharArray[i];
            Character prePi=null;
            Character nextPi=null;
            Character si=null;
            if(i+1<pCharArray.length)nextPi=pCharArray[i+1];
            boolean siExists=s.length>j;
            if(siExists)si=sCharArray[j]
            boolean isPassed=false;
            boolean isSpecialCharacters=pi=='*' || pi=='.';

            //B. "abc" => "abc"
            if(siExists&&pi==si)isPassed=true;
            //B. "abc" => "ab.", "ab.d"
            if(pi == '.' && nextPi!='*'
                && siExists ) isPassed=true;
            //B. "ab" => "ab*", "ab*d"
            if(isInSocialCharacters&&characterType!=null&&characterType==1
                &&!isSpecialCharacters
            ){
            }
            //B. "ab.*d"
            //B. "ab*d"

            //B. check whether the current char is passed
            if(!isPassed)return false;

            //B. tail public data
            if(pi=='.')characterType=0;
            if(pi=='*&&(prePi!=null&&prePi!='.'))characterType=1;
            if(pi=='*&&prePi!=null&&prePi!='.')characterType=2;
            if(isSpecialCharacters)isInSocialCharacters=true;
            lastPChar=isSpecialCharacters?lastPChar:pi;
            if(siExists &&!isInSocialCharacters )lastSChar=sCharArray[j];

        }
        return true;
    }
}
```

## Standard Solution

时间复杂度:  $O(mn)$ , 其中  $m$  和  $n$  分别是字符串  $s$  和  $p$  的长度。我们需要计算出所有的状态, 并且每个状态在进行转移时的时间复杂度为  $O(1)$ 。

空间复杂度:  $O(mn)$ , 即为存储所有状态使用的空间。

```
class Solution {
    public boolean isMatch(String s, String p) {
        int m = s.length();
        int n = p.length();

        boolean[][] f = new boolean[m + 1][n + 1];
        f[0][0] = true;
        //A. traverse string s.
        for (int i = 0; i <= m; ++i) {
            //B. traverse wildcard string p (starts from j-1).
            for (int j = 1; j <= n; ++j) {
                //C. compare the value at index i-1 with the value at index j-2.
                // match( "abcdefg", "abcdefg*" ) = match("abcdef", "abcdefg*") || match("abcdef",
                "abcdef") if( matchChar('g','g') ==true )
                // match( "abcdefg", "abcdefy*" ) = match("abcdefg", "abcdef")
                if( matchChar('g','y') ==false )
                    //C. fill the entire table: the result of f[i][j] needs to access the results of f[i-1][j],
                    f[i-1,j-2] and f[i,j-2],
                    // so The entire table needs to be filled in.
                    if (p.charAt(j - 1) == '*') {
                        //D. access previous matching results: access previous matching results through a single
                        matching result,
                        // gradually narrowing the matching scope
                        f[i][j] = f[i][j - 2];
                        if (matches(s, p, i, j - 1)) {
                            f[i][j] = f[i][j] || f[i - 1][j];
                        }
                    }
                    //C. compare the value at index i-1 with the value at index j-1.
                    // match( "abcd", "abc." ) = match( "abc", "abc" ) if( matchChar('d', '.') ==
                    true )
                    // match( "abcd", "ab*c*d" ) = match( "abc", "ab*c*" ) if( matchChar('d', 'd') ==
                    true )
                    // match( "abcd", "abcy" ) = false if( matchChar('d', 'y') ==
                    false)
                } else {
                    //D. skip index i=0.
                    if (matches(s, p, i, j)) {
                        f[i][j] = f[i - 1][j - 1];
                    }
                    //D. except for f[0][0], set f[i][j] to false by default.
                }
            }
        }
        return f[m][n];
    }

    /**
     * compare the character in the index i-1 of string s with the charcater in the index j-1 of string p.
     */
    public boolean matches(String s, String p, int i, int j) {
        if (i == 0) {
            return false;
        }
        if (p.charAt(j - 1) == '.') {
            return true;
        }
        return s.charAt(i - 1) == p.charAt(j - 1);
    }
}
```



You are given a 2D array of integers `envelopes` where `envelopes[i] = [wi, hi]` represents the width and the height of an envelope.

One envelope can fit into another if and only if **both the width and height of one envelope are greater than** the other envelope's width and height.

Return *the maximum number of envelopes you can Russian doll (i.e., put one inside the other)*.

**Note:** You cannot rotate an envelope.

#### Example 1:

**Input:** envelopes = [[5,4],[6,4],[6,7],[2,3]]

**Output:** 3

**Explanation:** The maximum number of envelopes you can Russian doll is 3 ([2,3] => [5,4] => [6,7]).

#### Example 2:

**Input:** envelopes = [[1,1],[1,1],[1,1]]

**Output:** 1

#### Constraints:

- 1 <= envelopes.length <= 10<sup>5</sup>
- envelopes[i].length == 2
- 1 <= w<sub>i</sub>, h<sub>i</sub> <= 10<sup>5</sup>

## Previous Solution

```
class Solution {
    public int maxEnvelopes(int[][] envelopes) {
        int [][]widthOrderEnvelopes=new int[envelopes.length][2];

        //A. sort envelopes by width
        for(int i=0;i<envelopes.length;i++){
            for(int j=0;j<envelopes.length;j++){
                if(envelopes[j][0]<envelopes[i][0]){
                    int[] temp=envelopes[j];
                    envelopes[j]=envelopes[i];
                    envelopes[i]=temp;
                }
            }
        }
        //A. How to filter out the most suitable heights?
        return 0;
    }
}
```

## Standard Solution

```
class Solution {
    public int maxEnvelopes(int[][] envelopes) {
        if (envelopes.length == 0) {
            return 0;
        }
        //A. sort envelopes by width.
        int n = envelopes.length;
        Arrays.sort(envelopes, new Comparator<int[]>() {
            public int compare(int[] e1, int[] e2) {
                if (e1[0] != e2[0]) {
                    return e1[0] - e2[0];
                } else {
                    return e2[1] - e1[1];
                }
            }
        });
    }
}
```

```

int[] f = new int[n];
Arrays.fill(f, 1);
int ans = 1;
//A. traverse the envelopes( j < i ).
for (int i = 1; i < n; ++i) {
    for (int j = 0; j < i; ++j) {
        //C. the height at index j is less than the height at index i.
        if (envelopes[j][1] < envelopes[i][1]) {
            //D. store the number of the envelop with smaller height at f[i].
            // height:          1 - 3 - 5 - 1 - 4
            // f[j]+1:           2   3   1   3
            // max(f[i],f[j]+1)                                x
            f[i] = Math.max(f[i], f[j] + 1);
        }
    }
    //B. return the maximum level in the current range.
    ans = Math.max(ans, f[i]);
}
return ans;
}
}

```

### Super Egg Drop

You are given  $k$  identical eggs and you have access to a building with  $n$  floors labeled from 1 to  $n$ .

You know that there exists a floor  $f$  where  $0 \leq f \leq n$  such that any egg dropped at a floor **higher** than  $f$  will **break**, and any egg dropped **at or below** floor  $f$  will **not break**.

Each move, you may take an unbroken egg and drop it from any floor  $x$  (where  $1 \leq x \leq n$ ). If the egg breaks, you can no longer use it. However, if the egg does not break, you may **reuse** it in future moves.

Return *the **minimum number of moves** that you need to determine **with certainty** what the value of  $f$  is.*

#### Example 1:

**Input:**  $k = 1, n = 2$

**Output:** 2

**Explanation:**

Drop the egg from floor 1. If it breaks, we know that  $f = 0$ .

Otherwise, drop the egg from floor 2. If it breaks, we know that  $f = 1$ .

If it does not break, then we know  $f = 2$ .

Hence, we need at minimum 2 moves to determine with certainty what the value of  $f$  is.

#### Example 2:

**Input:**  $k = 2, n = 6$

**Output:** 3

#### Example 3:

**Input:**  $k = 3, n = 14$

**Output:** 4

#### Constraints:

- $1 \leq k \leq 100$
- $1 \leq n \leq 10^4$

## Previous Solution

```
class Solution {
    public int superEggDrop(int k, int n) {
        // Note the most difficult f value to determine.
        // 1 2 => 1-2 (f=2)
        // 2 6 => 3-4-5-6 (f=6), 3-5-6 (f=6),
        // 3 14 => 8-9-10-11-12-13-14, 8-11-13-14 (f=14),
        // 4 16 => 9-12-13-16

        //A.
        // Floor x - dp(k, x)
        // not broken => dp(k,n-x)
        // broken      => dp(k-1,x-1)
        if(k>=n){
            return n;
        } else if(n%2==1)
            return n/k+k%2;
        else{
            return n/k+k%2;
        }
    }
}
```

## Standard Solution (DFS)

Reference:

<https://www.geeksforgeeks.org/egg-dropping-puzzle-dp-11/>

```
class Solution {

    public int eggDrop(int E, int F) {
        //A. limiting case.
        // 999, 1 => 1
        // 999, 0 => 0
        // 1, 999 => 999
        // If there are no floors, then no trials needed. OR if there is one floor, one trial needed.
        if (F == 1 || F == 0) return F;

        // We need F trials for one egg and F floors
        if (E == 1) return F;

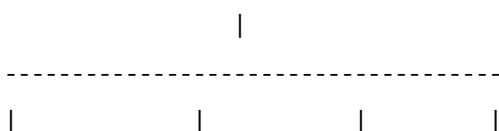
        //A. start dropping eggs.
        int min = Integer.MAX_VALUE;
        int x, res;

        // Consider all droppings from 1st floor to kth floor and return the minimum of these values plus 1.
        for (x = 1; x <= F; x++) {
            res = Math.max(eggDrop(E - 1, x - 1), eggDrop(E, F - x)); // if the egg is broken, go down,
otherwise, go up.
            if (res < min) min = res;
        }
        return min + 1;
    }
}
```

Note: The above function computes the same subproblems again and again. See the following partial recursion tree,  $E(2, 2)$  is being evaluated twice.

There will be many repeated subproblems when you draw the complete recursion tree even for small values of  $N$  and  $K$ .

$E(2, 4)$



x=1/		x=2/		x=3/		x=4/	
/		/		....		....	
/		/					
E(1, 0)	E(2, 3)	E(1, 1)	E(2, 2)				
/	/...	/					
x=1/		.....					
/							
E(1, 0)	E(2, 2)						
/							
	.....						

Partial recursion tree for 2 eggs and 4 floors.

## Standard Solution (DP)

```
class Solution {

    // A utility function to get maximum of two integers
    static int max(int a, int b) {
        return (a > b) ? a : b;
    }

    /* Function to get minimum number of trials needed in worst case with E eggs and F floors */
    static int eggDrop(int E, int F) {
        /* A 2D table where entry eggFloor[i][j] will represent minimum number of trials needed for i eggs
        and j floors. */
        int eggFloor[][] = new int[E + 1][F + 1];
        int res;
        int i, j, x;

        //A. limiting case.
        // 999, 1 => 1
        // 999, 0 => 0
        // 1, 999 => 999

        // 0 1 2 3 4 E
        // 0 0 0 0 0 0
        // 1 0 1 1 1 1
        // 2 0 2 x x x
        // 3 0 3 x x x
        // 4 0 4 x x x
        // F ... ?
        // To calculate the minimum number of trials, you need to drop the egg from each previous floor.
        // We need one trial for one floor and 0 trials for 0 floors
        for (i = 1; i <= E; i++) {
            eggFloor[i][1] = 1;
            eggFloor[i][0] = 0;
        }

        // We always need j trials for one egg and j floors.
        for (j = 1; j <= F; j++) eggFloor[1][j] = j;

        //A. start dropping eggs.
        // Fill rest of the entries in table using optimal substructure property
        for (i = 2; i <= E; i++) {
            for (j = 2; j <= F; j++) {
```

```

        eggFloor[i][j] = Integer.MAX_VALUE;
        for (x = 1; x <= j; x++) {
            res = 1 + max(eggFloor[i - 1][x - 1], eggFloor[i][j - x]);
            if (res < eggFloor[i][j]) eggFloor[i][j] = res;
        }
    }
    // eggFloor[E][F] holds the result
    return eggFloor[E][F];
}
}

```

## Standard Solution (Memoization)

```

class Solution {
    static final int MAX = 1000;

    static int[][] memo = new int[MAX][MAX];

    static int eggDrop(int E, int F) {

        if (memo[E][F] != -1) {
            return memo[E][F];
        }

        //A. limiting case.
        // 999, 1 => 1
        // 999, 0 => 0
        // 1, 999 => 999

        //   0 1 2 3 4 E
        // 0 0 0 0 0 0
        // 1 0 1 1 1 1
        // 2 0 2 x x x
        // 3 0 3 x x x
        // 4 0 4 x x x
        // F ... ?
        // To calculate the minimum number of trials, you need to drop the egg from each previous floor.
        if (F == 1 || F == 0) return F;
        if (E == 1) return F;

        //A. start dropping eggs.
        int min = Integer.MAX_VALUE, x, res;
        for (x = 1; x <= F; x++) {
            res = Math.max(eggDrop(E - 1, x - 1), eggDrop(E, F - x));
            if (res < min) min = res;
        }
        memo[E][F] = min + 1;
        return min + 1;
    }
}

```

## Count Palindromic Subsequences

Given a string of digits  $s$ , return *the number of palindromic subsequences of  $s$  having length 5*. Since the answer may be very large, return it **modulo**  $10^9 + 7$ .

### Note:

- A string is **palindromic** if it reads the same forward and backward.
- A **subsequence** is a string that can be derived from another string by deleting some or no characters without

changing the order of the remaining characters.

#### Example 1:

**Input:** s = "103301"

**Output:** 2

**Explanation:**

There are 6 possible subsequences of length 5: "10330", "10331", "10301", "10301", "13301", "03301".

Two of them (both equal to "10301") are palindromic.

#### Example 2:

**Input:** s = "0000000"

**Output:** 21

**Explanation:** All 21 subsequences are "00000", which is palindromic.

#### Example 3:

**Input:** s = "9999900000"

**Output:** 2

**Explanation:** The only two palindromic subsequences are "99999" and "00000".

#### Constraints:

- $1 \leq s.length \leq 10^4$
- s consists of digits.

## Standard Solution

```
class Solution {
    private static final long MOD = (long) 1e9 + 7;

    public int countPalindromes(String S) {
        char[] chars = S.toCharArray();
        int[] pre = new int[10], suf = new int[10];
        int[][] pre2 = new int[10][10], suf2 = new int[10][10];
        // suf [ num - quantity ]
        // suf2 [ num - previous num - previous quantity ]
        // 103301
        // 1 2 0 2 0 0 0 0 0 0
        // 1 2 0 2 0 0 0 0 0 0
        // 0 0 0 0 0 0 0 0 0 0
        // 2 2 0 1 0 0 0 0 0 0
        // ...
        //A. traverse string s from the end.
        for (int i = chars.length - 1; i >= 0; --i) {
            //B. get the current number at index i.
            int num = chars[i] - '0';
            //B. add the number of digits that appear earlier
            for (int j = 0; j < 10; ++j)
                suf2[num][j] += suf[j];
            //B. add quantity
            ++suf[num];
        }
        long ans = 0L;
        //A. traverse string s from the start.
        for (char val : chars) {
            val -= '0';
            //B. subtract quantity
            --suf[val];
            //B. subtract the number that appears earlier
            for (int j = 0; j < 10; ++j)
                suf2[val][j] -= suf[j];
            //B. subtract the number that appears earlier
```

```

        for (int j = 0; j < 10; ++j)
            for (int k = 0; k < 10; ++k)
                ans += (long) pre2[j][k] * suf2[j][k]; // 枚举所有字符组合
        for (int j = 0; j < 10; ++j)
            pre2[val][j] += pre[j];
        ++pre[val];
    }
    return (int) (ans % MOD);
}
}
}

```

### Greedy

#### Destroying Asteroids

You are given an integer mass, which represents the original mass of a planet.

You are further given an integer array asteroids, where asteroids[i] is the mass of the  $i^{\text{th}}$  asteroid.

You can arrange for the planet to collide with the asteroids in **any arbitrary order**.

If the mass of the planet is **greater than or equal to** the mass of the asteroid, the asteroid is **destroyed** and the planet **gains** the mass of the asteroid. Otherwise, the planet is destroyed.



Return true *if all asteroids can be destroyed. Otherwise, return false.*

### Example 1:

**Input:** mass = 10, asteroids = [3,9,19,5,21]

**Output:** true

**Explanation:** One way to order the asteroids is [9,19,5,3,21]:

- The planet collides with the asteroid with a mass of 9. New planet mass:  $10 + 9 = 19$
  - The planet collides with the asteroid with a mass of 19. New planet mass:  $19 + 19 = 38$
  - The planet collides with the asteroid with a mass of 5. New planet mass:  $38 + 5 = 43$
  - The planet collides with the asteroid with a mass of 3. New planet mass:  $43 + 3 = 46$
  - The planet collides with the asteroid with a mass of 21. New planet mass:  $46 + 21 = 67$
- All asteroids are destroyed.

### Example 2:

**Input:** mass = 5, asteroids = [4,9,23,4]

**Output:** false

**Explanation:**

The planet cannot ever gain enough mass to destroy the asteroid with a mass of 23.

After the planet destroys the other asteroids, it will have a mass of  $5 + 4 + 9 + 4 = 22$ .

This is less than 23, so a collision would not destroy the last asteroid.

### Constraints:

- $1 \leq \text{mass} \leq 10^5$
- $1 \leq \text{asteroids.length} \leq 10^5$
- $1 \leq \text{asteroids}[i] \leq 10^5$

## Previous Solution

```
class Solution {
    public boolean asteroidsDestroyed(int mass, int[] asteroids) {
        boolean result=false;
        boolean checked=false;
        for(int i=0; i<asteroids.length; i++){
            //A. check whether the asteroid has been checked.
            if(asteroids[i]==-1)continue;
            else checked=true;
            int astMass=asteroids[i];
            if(astMass>mass) continue;
            asteroids[i]=-1;
            //A. return result according the previous result.
            if(asteroidsDestroyed(mass+astMass, asteroids)) result = true;
            asteroids[i]=astMass;
        }
        return result || !checked;
    }
}
```

## Standard Solution

```
class Solution {
    public boolean asteroidsDestroyed(int mass, int[] asteroids) {
        long tmp=mass;
        Arrays.sort(asteroids);
        for (int i = 0; i < asteroids.length; i++) {
            //A. compare from the smallest one.
            if(tmp>= asteroids[i]) {
                tmp+=asteroids[i];
            }else {
                return false;
            }
        }
        return true;
    }
}
```

```

        return false;
    }
}
return true;
}
}

```

## HashTable

Value

The **index** is more suitable as a count information rather than the number of numbers.

## Max Chunks To Make Sorted II

You are given an integer array `arr`.

We split `arr` into some number of **chunks** (i.e., partitions), and individually sort each chunk. After concatenating them, the result should equal the sorted array.

Return *the largest number of chunks we can make to sort the array*.

### Example 1:

Input: `arr = [5,4,3,2,1]`

Output: 1

Explanation:

Splitting into two or more chunks will not return the required result.

For example, splitting into `[5, 4], [3, 2, 1]` will result in `[4, 5, 1, 2, 3]`, which isn't sorted.

### Example 2:

Input: `arr = [2,1,3,4,4]`

Output: 4

Explanation:

We can split into two chunks, such as `[2, 1], [3, 4, 4]`.

However, splitting into `[2, 1], [3], [4], [4]` is the highest number of chunks possible.

### Constraints:

- $1 \leq \text{arr.length} \leq 2000$
- $0 \leq \text{arr}[i] \leq 10^8$

## Previous Solution

```

class Solution {
    private Map<Integer, Integer> indMap=new HashMap<>(); // ind - val

    public int maxChunksToSorted(int[] arr) {
        //A. create a new array by sorting the arr.
        int[] reversedArr=Arrays.copyOf(arr,arr.length);
        Arrays.sort(reversedArr);
        //A. public data.
        int sum=0;
        int beginInd=-1;
        int endInd=-1;
        int indRange=-1;
        //A. traverse arr to populate indMap.
        for(int i=0; i<arr.length; i++){
            indMap.add(arr[i],i);
        }
        //A. traverse reverseArr.
        for(int i=0; i<reverseArr.length; i++){

```

```

        int currentVal=reverseArr[i];
        //B. arr[i] equals reverseArr[i].
        if(currentVal==arr[i]){
            sum++;
        }
        //B. currentVal[i] is lesser than arr[i].
        // reverseArr [1,2,3,4,4]
        // arr [2,3,1,4,4]
        } else{
            //C. check for the presence of indRange.
            if(indRange!=-1)
                //C. find the value index and update the indRange.
                beginInd=i;
            endInd=indMap.get(currentVal);
            indRange=endInd-beginInd-1;
        }
    }
}

```

## Standard Solution

```

class Solution {
    public int maxChunksToSorted(int[] arr) {
        //A. public data
        Map<Integer, Integer> cnt = new HashMap<Integer, Integer>(); // value - times
        int res = 0;
        //A. create a new array by sorting the arr.
        int[] sortedArr = new int[arr.length];
        System.arraycopy(arr, 0, sortedArr, 0, arr.length);
        Arrays.sort(sortedArr);
        //A. traverse the sortedArr.
        for (int i = 0; i < sortedArr.length; i++) {
            int x = arr[i], y = sortedArr[i];
            //B. put the value of arr into cnt.
            cnt.put(x, cnt.getOrDefault(x, 0) + 1);
            if (cnt.get(x) == 0) {
                cnt.remove(x);
            }
            //B. put the value of sortedArr into cnt.
            cnt.put(y, cnt.getOrDefault(y, 0) - 1);
            if (cnt.get(y) == 0) {
                cnt.remove(y);
            }
            //B. Make sure all previous data is already present in the sorted array.
            if (cnt.isEmpty()) {
                res++;
            }
        }
        return res;
    }
}

```

## LFU Cache

Design and implement a data structure for a **Least Frequently Used (LFU)** cache.

Implement the **LFUCache** class:

- **LFUCache(int capacity)** Initializes the object with the **capacity** of the data structure.
- **int get(int key)** Gets the value of the **key** if the key exists in the cache. Otherwise, returns -1.
- **void put(int key, int value)** Update the value of the key if present, or inserts the key if not already present. When the cache reaches its **capacity**, it should invalidate and remove the **least frequently used** key before inserting a new item. For this problem,

when there is a **tie** (i.e., two or more keys with the same frequency), the **least recently used key** would be invalidated.

To determine the least frequently used key, a **use counter** is maintained for each key in the cache. The key with the smallest **use counter** is the least frequently used key.

When a key is first inserted into the cache, its **use counter** is set to 1 (due to the put operation). The **use counter** for a key in the cache is incremented when either a get or put operation is called on it.

The functions **get** and **put** must each run in  $O(1)$  average time complexity.

#### Example 1:

##### Input

```
["LFUCache", "put", "put", "get", "put", "get", "get", "put", "get", "get", "get"]
[[2], [1, 1], [2, 2], [1], [3, 3], [2], [3], [4, 4], [1], [3], [4]]
```

##### Output

```
[null, null, null, 1, null, -1, 3, null, -1, 3, 4]
```

##### Explanation

```
// cnt(x) = the use counter for key x
// cache=[] will show the last used order for tiebreakers (leftmost element is most recent)
LFUCache lfu = new LFUCache(2);
lfu.put(1, 1); // cache=[1,_], cnt(1)=1
lfu.put(2, 2); // cache=[2,1], cnt(2)=1, cnt(1)=1
lfu.get(1);    // return 1
               // cache=[1,2], cnt(2)=1, cnt(1)=2
lfu.put(3, 3); // 2 is the LFU key because cnt(2)=1 is the smallest, invalidate 2.
               // cache=[3,1], cnt(3)=1, cnt(1)=2
lfu.get(2);    // return -1 (not found)
lfu.get(3);    // return 3
               // cache=[3,1], cnt(3)=2, cnt(1)=2
lfu.put(4, 4); // Both 1 and 3 have the same cnt, but 1 is LRU, invalidate 1.
               // cache=[4,3], cnt(4)=1, cnt(3)=2
lfu.get(1);    // return -1 (not found)
lfu.get(3);    // return 3
               // cache=[3,4], cnt(4)=1, cnt(3)=3
lfu.get(4);    // return 4
               // cache=[4,3], cnt(4)=2, cnt(3)=3
```

#### Constraints:

- $1 \leq \text{capacity} \leq 10^4$
- $0 \leq \text{key} \leq 10^5$
- $0 \leq \text{value} \leq 10^9$
- At most  $2 * 10^5$  calls will be made to get and put.

## Previous Solution

```
class LFUCache {
    //A. public data that stores usage counts, key, value.
    private Map<Integer, Integer> data=new HashMap();
    private Map<Integer, Integer> counts=new HashMap();

    public LFUCache(int capacity) {

    }

    public void put(int key, int value) {
        this.data.put(key,value);
        this.counts.compute(key,(key,val)->val==null?1:++val);
    }

    public int get(int key) {

    }

}

/**
```

```

* Your LFUCache object will be instantiated and called as such:
* LFUCache obj = new LFUCache(capacity);
* int param_1 = obj.get(key);
* obj.put(key,value);
*/

```

## Standard Solution

```

class Node implements Comparable<Node> {
    int cnt, time, key, value;

    Node(int cnt, int time, int key, int value) {
        this.cnt = cnt;
        this.time = time;
        this.key = key;
        this.value = value;
    }

    public boolean equals(Object anObject) {
        if (this == anObject) {
            return true;
        }
        if (anObject instanceof Node) {
            Node rhs = (Node) anObject;
            return this.cnt == rhs.cnt && this.time == rhs.time;
        }
        return false;
    }

    public int compareTo(Node rhs) {
        return cnt == rhs.cnt ? time - rhs.time : cnt - rhs.cnt;
    }

    public int hashCode() {
        return cnt * 100000007 + time;
    }
}

class LFUCache {
    // cache capacity and timestamp
    int capacity, time;
    Map<Integer, Node> key_table;
    TreeSet<Node> S;

    public LFUCache(int capacity) {
        this.capacity = capacity;
        this.time = 0;
        key_table = new HashMap<Integer, Node>();
        S = new TreeSet<Node>();
    }

    public void put(int key, int value) {
        if (capacity == 0) {
            return;
        }
        if (!key_table.containsKey(key)) {
            //A. If the cache capacity limit is reached
            if (key_table.size() == capacity) {
                //B. Delete least recently used cache from the key_table and S set.
                key_table.remove(S.first().key);
                S.remove(S.first());
            }
            //A. Create a new cache.
            Node cache = new Node(1, ++time, key, value);
            //A. Put the new cache into the key_table and S set.
            key_table.put(key, cache);
            S.add(cache);
        } else {
            //A. Here is similar to the get() method

```

```

        Node cache = key_table.get(key);
        S.remove(cache);
        cache.cnt += 1;
        cache.time = ++time;
        cache.value = value;
        S.add(cache);
        key_table.put(key, cache);
    }
}
public int get(int key) {
    if (capacity == 0) {
        return -1;
    }
    //A. Return -1 if there is no key in the key_table.
    if (!key_table.containsKey(key)) {
        return -1;
    }
    //A. Return old cache from the key_table.
    Node cache = key_table.get(key);
    //A. delete old cache from S set.
    S.remove(cache);
    //A. update old cache.
    cache.cnt += 1;
    cache.time = ++time;
    //A. put new cache back into the key_table and S set.
    S.add(cache);
    key_table.put(key, cache);
    return cache.value;
}
}

```

### Sort queries by query frequency

There are 10 files, each of which is 1 GB in size.

Each line of each file stores a user's query, and the queries in each file may be repeated.

Please sort by query frequency.

## Standard Solution

```

import java.io.*;
import java.util.*;
import java.util.Map.Entry;

public class QueryFrequencySorter {

    public static void main(String[] args) {
        String[] inputFiles = {"file1.txt", "file2.txt", "file3.txt", "file4.txt", "file5.txt",
                               "file6.txt", "file7.txt", "file8.txt", "file9.txt", "file10.txt"};
        String outputFile = "sorted_queries.txt";

        try {
            // Step 1: Count frequencies
            Map<String, Integer> frequencyMap = countFrequencies(inputFiles);

            // Step 2: Sort queries by frequency
            List<Map.Entry<String, Integer>> sortedEntries = sortFrequencies(frequencyMap);

            // Step 3: Write sorted queries to output file
            writeSortedQueriesToFile(sortedEntries, outputFile);

            System.out.println("Sorted queries written to " + outputFile);
        } catch (IOException e) {
            e.printStackTrace();
        }
    }
}

```

```

    }

    private static Map<String, Integer> countFrequencies(String[] inputFiles) throws IOException {
        Map<String, Integer> frequencyMap = new HashMap<>();

        for (String fileName : inputFiles) {
            BufferedReader reader = new BufferedReader(new FileReader(fileName));
            String query;
            while ((query = reader.readLine()) != null) {
                frequencyMap.put(query, frequencyMap.getOrDefault(query, 0) + 1);
            }
            reader.close();
        }

        return frequencyMap;
    }

    private static List<Map.Entry<String, Integer>> sortFrequencies(Map<String, Integer> frequencyMap) {
        List<Map.Entry<String, Integer>> entryList = new ArrayList<>(frequencyMap.entrySet());
        entryList.sort((entry1, entry2) -> entry2.getValue().compareTo(entry1.getValue()));
        return entryList;
    }

    private static void writeSortedQueriesToFile(List<Map.Entry<String, Integer>> sortedEntries, String
outputFile) throws IOException {
        BufferedWriter writer = new BufferedWriter(new FileWriter(outputFile));
        for (Map.Entry<String, Integer> entry : sortedEntries) {
            writer.write(entry.getKey() + ": " + entry.getValue());
            writer.newLine();
        }
        writer.close();
    }
}

```

## Heap

### The 100 most frequent words

Given a file of size 1 gigabyte, **each line** in the file is **a word**, and each word **is limited to 16 bytes**.

Return **the 100 most frequent words**, with a memory **limit of 10 megabytes**.

#### Read the File in Chunks

Given the memory limitation, you **can't load the entire file into memory at once**. You'll read the file in manageable chunks.

#### Use a Hash Map with Count-Min Sketch

Use a hash map combined **with a count-min sketch** to approximate the frequency of each word. This helps manage the large size of the dataset while keeping memory usage within limits.

#### Maintain a Min-Heap

Maintain a min-heap **to keep track of the top 100 most frequent words**. The heap will help efficiently track the highest frequencies.

## Standard Solution

#### Hash Map for Counting:

A hash map (wordCountMap) stores the frequency of each word.

#### Heap Management:

A min-heap is used to maintain **the top 100 most frequent words**.

Whenever the hash map exceeds a certain size (to avoid memory overflow), the current word counts are used to update the heap.

#### Updating the Heap:

The updateHeap method ensures the heap contains the top 100 words by frequency.

If a word's frequency in the current chunk is higher than **the minimum in the heap**, it replaces the minimum.

```
import java.io.*;
import java.util.*;

public class TopFrequentWords {
    private static final int MAX_WORD_LENGTH = 16;
    private static final int CHUNK_SIZE = 1024 * 1024; // 1MB
    private static final int HEAP_SIZE = 100;

    public static void main(String[] args) throws IOException {
        String filePath = "path/to/your/file.txt";
        findTopKFrequentWords(filePath);
    }

    public static void findTopKFrequentWords(String filePath) throws IOException {
        Map<String, Integer> wordCountMap = new HashMap<>();
        PriorityQueue<Map.Entry<String, Integer>> minHeap = new PriorityQueue<>(HEAP_SIZE,
        Map.Entry.comparingByValue());

        try (BufferedReader br = new BufferedReader(new FileReader(filePath))) {
            char[] buffer = new char[CHUNK_SIZE];
            int bytesRead;

            while ((bytesRead = br.read(buffer)) != -1) {
                String[] words = new String(buffer, 0, bytesRead).split("\\s+");

                for (String word : words) {
                    if (word.length() <= MAX_WORD_LENGTH) {
                        wordCountMap.put(word, wordCountMap.getOrDefault(word, 0) + 1);
                    }
                }

                if (wordCountMap.size() > 100000) {
                    updateHeap(minHeap, wordCountMap);
                    wordCountMap.clear();
                }
            }

            updateHeap(minHeap, wordCountMap);
            printTopKWords(minHeap);
        }

        private static void updateHeap(PriorityQueue<Map.Entry<String, Integer>> minHeap, Map<String, Integer>
        wordCountMap) {
            for (Map.Entry<String, Integer> entry : wordCountMap.entrySet()) {
                if (minHeap.size() < HEAP_SIZE) {
                    minHeap.offer(entry);
                } else if (entry.getValue() > Objects.requireNonNull(minHeap.peek()).getValue()) {
                    minHeap.poll();
                    minHeap.offer(entry);
                }
            }
        }

        private static void printTopKWords(PriorityQueue<Map.Entry<String, Integer>> minHeap) {
            List<Map.Entry<String, Integer>> result = new ArrayList<>(minHeap);
            result.sort((a, b) -> b.getValue() - a.getValue());

            for (Map.Entry<String, Integer> entry : result) {
                System.out.println(entry.getKey() + ": " + entry.getValue());
            }
        }
    }
}
```



Given a sequence of **10 billion unsigned integers**, how can I compute the median of these 10 billion numbers, with a memory limit of 512 megabytes.

## Standard Solution

```
import java.io.*;
import java.nio.file.*;
import java.util.*;

public class MedianFinder {
    private static final long TOTAL_NUMBERS = 10_000_000_000L;
    private static final int CHUNK_SIZE = 128_000_000; // 128 million integers per chunk(512/4 = 128
megabytes => 134_217_728 integers)
    private static final int MEMORY_LIMIT = 512 * 1024 * 1024; // 512 MB

    public static void main(String[] args) throws IOException {
        String inputFile = "input.dat"; // Path to the input file containing the integers
        String tempDir = "tempChunks"; // Directory to store the sorted chunks

        // Step 1: Chunk the data and sort each chunk
        List<String> chunkFiles = sortChunks(inputFile, tempDir);

        // Step 2: Merge sorted chunks and find the median
        double median = findMedian(chunkFiles);
        System.out.println("The median is: " + median);
    }

    private static List<String> sortChunks(String inputFile, String tempDir) throws IOException {
        List<String> chunkFiles = new ArrayList<>();
        try (BufferedInputStream bis = new BufferedInputStream(new FileInputStream(inputFile))) {
            byte[] buffer = new byte[CHUNK_SIZE * 4];
            int bytesRead;
            int chunkIndex = 0;

            while ((bytesRead = bis.read(buffer)) != -1) {
                int[] numbers = new int[bytesRead / 4];
                for (int i = 0; i < numbers.length; i++) {
                    numbers[i] = (
                        (buffer[i * 4] & 0xFF) << 24) |
                        ((buffer[i * 4 + 1] & 0xFF) << 16) | ((buffer[i * 4 + 2] & 0xFF) << 8) | (buffer[i *
4 + 3] & 0xFF);
                }
                // The byte code in the provided logic represents integers using the two's complement representation.
                // << 24: This shifts the extracted byte 24 bits to the left, placing it in the highest byte position of the
integer.

                // buffer[i * 4 + 1] & 0xFF: This extracts the second byte of the integer.
                // << 16: This shifts the second byte 16 bits to the left, placing it in the second highest byte position.
                // buffer[i * 4 + 2] & 0xFF: This extracts the third byte of the integer.
                // << 8: This shifts the third byte 8 bits to the left, placing it in the third highest byte position.
                // buffer[i * 4 + 3] & 0xFF: This extracts the fourth byte of the integer and places it in the
lowest byte position.

                Arrays.sort(numbers);
                String chunkFile = tempDir + "/chunk" + chunkIndex + ".dat";
                writeChunk(numbers, chunkFile);
                chunkFiles.add(chunkFile);
                chunkIndex++;
            }
        }
        return chunkFiles;
    }

    private static void writeChunk(int[] numbers, String chunkFile) throws IOException {
        try (DataOutputStream dos = new DataOutputStream(new BufferedOutputStream(new
```

```

FileOutputStream(chunkFile)))) {
    for (int number : numbers) {
        dos.writeInt(number);
    }
}

private static double findMedian(List<String> chunkFiles) throws IOException {
    PriorityQueue<ChunkReader> minHeap = new PriorityQueue<>(Comparator.comparingInt(ChunkReader::peek));
    for (String chunkFile : chunkFiles) {
        ChunkReader reader = new ChunkReader(chunkFile);
        if (reader.hasNext()) {
            minHeap.add(reader);
        }
    }

    long median1Position = TOTAL_NUMBERS / 2;
    long median2Position = median1Position + 1;

    int currentPosition = 0;
    int median1 = 0, median2 = 0;

    while (!minHeap.isEmpty()) {
        ChunkReader reader = minHeap.poll();
        int number = reader.next();
        currentPosition++;

        if (currentPosition == median1Position) {
            median1 = number;
        }
        if (currentPosition == median2Position) {
            median2 = number;
            break;
        }

        if (reader.hasNext()) {
            minHeap.add(reader);
        }
    }

    return (median1 + median2) / 2.0;
}

class ChunkReader {
    private DataInputStream dis;
    private int nextNumber;

    public ChunkReader(String chunkFile) throws IOException {
        dis = new DataInputStream(new BufferedInputStream(new FileInputStream(chunkFile)));
        if (dis.available() > 0) {
            nextNumber = dis.readInt();
        }
    }

    public boolean hasNext() throws IOException {
        return dis.available() > 0;
    }

    public int next() throws IOException {
        int result = nextNumber;
        if (dis.available() > 0) {
            nextNumber = dis.readInt();
        }
        return result;
    }

    public int peek() {

```

```

        return nextNumber;
    }
}

```

### Find the first 500 numbers out of 5 million numbers

Given 1000 arrays, each containing 500 elements and arranged in order, how to find the first 500 numbers out of these 5 million numbers?

## Standard Solution

```

import java.util.PriorityQueue;
import java.util.Comparator;

class Element {
    int value;
    int arrayIndex;
    int elementIndex;

    Element(int value, int arrayIndex, int elementIndex) {
        this.value = value;
        this.arrayIndex = arrayIndex;
        this.elementIndex = elementIndex;
    }
}

public class FindFirst500Numbers {

    public static int[] findFirst500Numbers(int[][] arrays) {
        PriorityQueue<Element> minHeap = new PriorityQueue<>(Comparator.comparingInt(e -> e.value));
        int[] result = new int[500];
        int resultIndex = 0;

        // Initialize the heap with the first element of each array
        for (int i = 0; i < arrays.length; i++) {
            if (arrays[i].length > 0) {
                // There must be at least one element that is on the smaller side, because the number of
                // elements reaches 1000, which is half the size of the array.
                minHeap.offer(new Element(arrays[i][0], i, 0));
            }
        }

        // Extract the minimum element from the heap and push the next element from the same array
        while (resultIndex < 500 && !minHeap.isEmpty()) {
            Element minElement = minHeap.poll();
            result[resultIndex++] = minElement.value;

            if (minElement.elementIndex + 1 < arrays[minElement.arrayIndex].length) {
                int nextValue = arrays[minElement.arrayIndex][minElement.elementIndex + 1];
                minHeap.offer(new Element(nextValue, minElement.arrayIndex, minElement.elementIndex + 1));
            }
        }

        return result;
    }

    public static void main(String[] args) {
        // Example usage
        int[][] arrays = new int[1000][500];
        // Fill the arrays with sorted numbers for testing
        for (int i = 0; i < 1000; i++) {
            for (int j = 0; j < 500; j++) {
                arrays[i][j] = i * 500 + j;
            }
        }

        int[] result = findFirst500Numbers(arrays);
    }
}

```

```

    for (int num : result) {
        System.out.print(num + " ");
    }
}

```

## Linked List

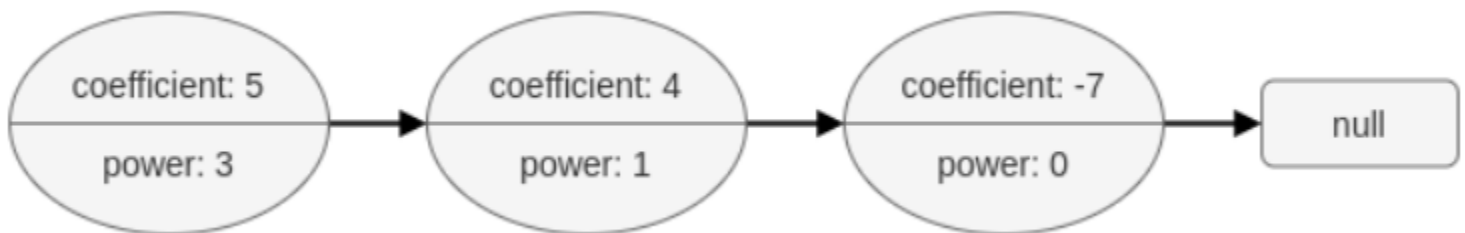
### Add Two Polynomials Represented as Linked Lists

A polynomial linked list is a special type of linked list where every node represents a term in a polynomial expression.

Each node has three attributes:

- coefficient: an integer representing the number multiplier of the term. The coefficient of the term  $9x^4$  is 9.
- power: an integer representing the exponent. The power of the term  $9x^4$  is 4.
- next: a pointer to the next node in the list, or null if it is the last node of the list.

For example, the polynomial  $5x^3 + 4x - 7$  is represented by the polynomial linked list illustrated below:



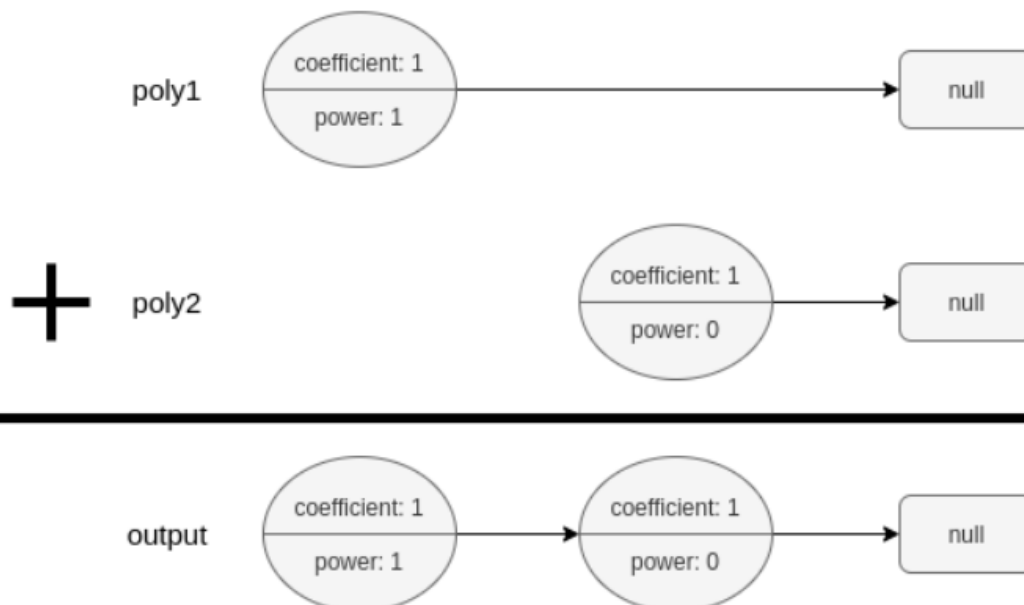
The polynomial linked list must be in its standard form: the polynomial must be in strictly descending order by its power value. Also, terms with a coefficient of 0 are omitted.

Given two polynomial linked list heads, poly1 and poly2, add the polynomials together and return the head of the sum of the polynomials.

PolyNode format:

The input/output format is as a list of n nodes, where each node is represented as its [coefficient, power]. For example, the polynomial  $5x^3 + 4x - 7$  would be represented as:  $[[5,3],[4,1],[-7,0]]$ .

#### Example 1:



**Input:** poly1 = [[1,1]], poly2 = [[1,0]]

**Output:** [[1,1],[1,0]]

**Explanation:** poly1 = x. poly2 = 1. The sum is x + 1.

**Example 2:**

**Input:** poly1 = [[2,2],[4,1],[3,0]], poly2 = [[3,2],[-4,1],[-1,0]]

**Output:** [[5,2],[2,0]]

**Explanation:** poly1 =  $2x^2 + 4x + 3$ . poly2 =  $3x^2 - 4x - 1$ . The sum is  $5x^2 + 2$ . Notice that we omit the "0x" term.

**Example 3:**

**Input:** poly1 = [[1,2]], poly2 = [[-1,2]]

**Output:** []

**Explanation:** The sum is 0. We return an empty list.

**Constraints:**

- $0 \leq n \leq 10^4$
- $-10^9 \leq \text{PolyNode.coefficient} \leq 10^9$
- $\text{PolyNode.coefficient} \neq 0$
- $0 \leq \text{PolyNode.power} \leq 10^9$
- $\text{PolyNode.power} > \text{PolyNode.next.power}$

## Standard Solution1

```
class Solution {
    public PolyNode addPoly(PolyNode l, PolyNode r) {
        if (l == null) return r;
        if (r == null) return l;
        if (l.power == r.power) {
            l.coefficient += r.coefficient;
            if (l.coefficient == 0) return addPoly(l.next, r.next);
            l.next = addPoly(l.next, r.next);
            return l;
        } else if (l.power > r.power) {
            l.next = addPoly(l.next, r);
            return l;
        } else {
            r.next = addPoly(l, r.next);
            return r;
        }
    }
}
```

## Standard Solution2

```
class Solution {
    public PolyNode addPoly(PolyNode poly1, PolyNode poly2) {
        PolyNode dummyHead = new PolyNode();
        PolyNode temp = dummyHead;
        PolyNode node1 = poly1, node2 = poly2;
        while (node1 != null || node2 != null) {
            int power1 = node1 != null ? node1.power : -1;
            int power2 = node2 != null ? node2.power : -1;
            PolyNode curr;
            if (power1 > power2) {
                curr = new PolyNode(node1.coefficient, power1);
                node1 = node1.next;
            } else if (power1 < power2) {
                curr = new PolyNode(node2.coefficient, power2);
                node2 = node2.next;
            } else {
                curr = new PolyNode(node1.coefficient + node2.coefficient, power1);
                node1 = node1.next;
                node2 = node2.next;
            }
            temp.next = curr;
            temp = temp.next;
        }
        return dummyHead.next;
    }
}
```

```

        if (curr.coefficient != 0) {
            temp.next = curr;
            temp = temp.next;
        }
    }
    return dummyHead.next;
}
}

```

## Math

### Euclidean algorithm

```

public class CommonDivisors {
    // Function to compute GCD using the Euclidean algorithm
    public static int gcd(int a, int b) {
        while (b != 0) {
            int temp = b;
            b = a % b;    // b = remainder
            a = temp;     // a=b
        }
        return a;
    }
}

```

The GCD always exists unless both numbers are zero.

### Token Bucket Algorithm

The token bucket algorithm **fills the bucket at a certain rate**, allowing requests **to consume tokens**. Once the bucket is empty, **the request is denied**.

Bucket:

Contains tokens, replenished **at a fixed rate**.

Request:

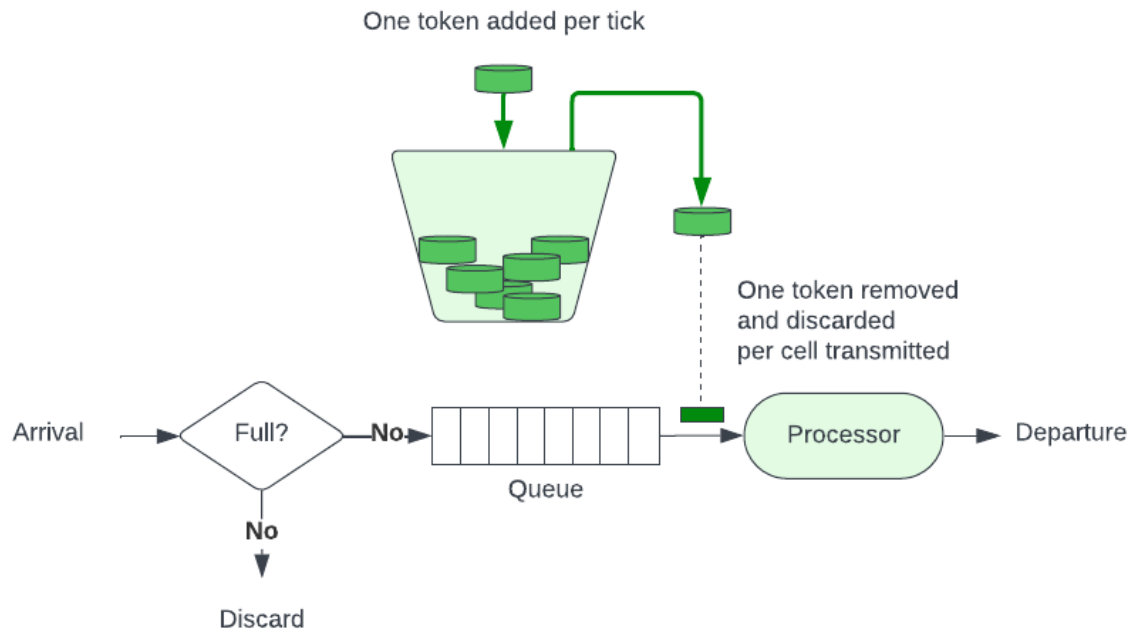
Consumes a token. **If the bucket is empty**, the request is denied.

When the token bucket is full and new tokens arrive, these new tokens **are typically discarded**.

This means that once the bucket reaches its maximum capacity, no more tokens can be added until some are consumed by incoming requests.

Burst Capability:

Allows for sudden bursts in traffic.



## Standard Solution

```

import java.util.concurrent.Executors;
import java.util.concurrent.ScheduledExecutorService;
import java.util.concurrent.TimeUnit;

public class TokenBucket {
    private final int capacity;
    private int tokens;
    private final int refillRate;
    private final ScheduledExecutorService scheduler;

    public TokenBucket(int capacity, int refillRate) {
        this.capacity = capacity;
        this.tokens = capacity; // bucket size
        this.refillRate = refillRate;
        this.scheduler = Executors.newScheduledThreadPool(1);
        startRefilling();
    }

    private void startRefilling() {
        scheduler.scheduleAtFixedRate(() -> {
            synchronized (TokenBucket.this) {
                if (tokens < capacity) {
                    tokens++;
                    System.out.println("Token added. Current tokens: " + tokens);
                } else {
                    System.out.println("Bucket is full. Token discarded.");
                }
            }
        }, 0, 1000 / refillRate, TimeUnit.MILLISECONDS);
    }

    public synchronized boolean allowRequest() {
        if (tokens > 0) {
            tokens--;
            System.out.println("Request allowed. Current tokens: " + tokens);
            return true;
        } else {
            System.out.println("Request denied. No tokens available.");
        }
    }
}

```

```

        return false;
    }
}

public static void main(String[] args) throws InterruptedException {
    TokenBucket tokenBucket = new TokenBucket(10, 2); // Capacity 10, Refill rate 2 tokens/sec

    for (int i = 0; i < 15; i++) {
        Thread.sleep(1000); // 1 request per second
        boolean allowed = tokenBucket.allowRequest();
        System.out.println("Request " + (i + 1) + ": " + (allowed ? "Allowed" : "Denied"));
    }

    tokenBucket.scheduler.shutdown();
}
}

```

### Fixed Window algorithm

The Fixed Window algorithm counts requests in fixed intervals and limits the number of requests per interval. Once the timed interval is reached, the counter is reset to zero.

Window Size:

Fixed duration (e.g., 1 minute).

Request Count:

Resets at the end of each window.

Problem

Unable to control sudden surge in requests.

## Standard Solution

```

import java.util.concurrent.atomic.AtomicInteger;
import java.util.concurrent.Executors;
import java.util.concurrent.ScheduledExecutorService;
import java.util.concurrent.TimeUnit;

public class FixedWindowRateLimiter {
    private final int limit;
    private final AtomicInteger currentCount;
    private final ScheduledExecutorService scheduler;

    public FixedWindowRateLimiter(int limit, int windowSizeInSeconds) {
        this.limit = limit; // window size
        this.currentCount = new AtomicInteger(0);
        this.scheduler = Executors.newScheduledThreadPool(1);
        startResetTask(windowSizeInSeconds);
    }

    private void startResetTask(int windowSizeInSeconds) {
        scheduler.scheduleAtFixedRate(() -> {
            currentCount.set(0);
            System.out.println("Window reset. Count set to 0.");
        }, 0, windowSizeInSeconds, TimeUnit.SECONDS);
    }

    public boolean allowRequest() {
        if (currentCount.incrementAndGet() <= limit) {
            System.out.println("Request allowed. Current count: " + currentCount.get());
            return true;
        } else {
            System.out.println("Request denied. Limit exceeded.");
            return false;
        }
    }

    public static void main(String[] args) throws InterruptedException {

```



```

        FixedWindowRateLimiter rateLimiter = new FixedWindowRateLimiter(10, 10); // 10 requests per 10
seconds

        for (int i = 0; i < 15; i++) {
            Thread.sleep(1000); // 1 request per second
            boolean allowed = rateLimiter.allowRequest();
            System.out.println("Request " + (i + 1) + ": " + (allowed ? "Allowed" : "Denied"));
        }

        rateLimiter.scheduler.shutdown();
    }
}

```

### Sliding Window Algorithm

The Sliding Window algorithm is a more accurate version of the Fixed Window, using overlapping windows to smooth out traffic.

The sliding window **can move forward over time** and **count requests during this time**.

Sliding Window:

**Partially overlaps** with the previous window.

Request Count:

More accurate, prevents bursts **around window boundaries**.

### Standard Solution

```

import java.util.concurrent.atomic.AtomicInteger;
import java.util.concurrent.locks.ReentrantLock;

public class SlidingWindowRateLimiter {
    private final int limit;
    private final long windowSizeInMillis;
    private final AtomicInteger currentCount;
    private final ReentrantLock lock;

    private long windowStart;

    public SlidingWindowRateLimiter(int limit, int windowSizeInSeconds) {
        this.limit = limit;
        this.windowSizeInMillis = windowSizeInSeconds * 1000L; // window size
        this.currentCount = new AtomicInteger(0);
        this.lock = new ReentrantLock();
        this.windowStart = System.currentTimeMillis();
    }

    public boolean allowRequest() {
        long now = System.currentTimeMillis();
        lock.lock();
        try {
            if (now - windowStart >= windowSizeInMillis) {
                // Move the window forward
                windowStart = now;
                currentCount.set(0);
            }
            if (currentCount.incrementAndGet() <= limit) {
                System.out.println("Request allowed. Current count: " + currentCount.get());
                return true;
            } else {
                System.out.println("Request denied. Limit exceeded.");
                return false;
            }
        } finally {
            lock.unlock();
        }
    }

    public static void main(String[] args) throws InterruptedException {

```

```

        SlidingWindowRateLimiter rateLimiter = new SlidingWindowRateLimiter(10, 10); // 10 requests per 10
seconds

        for (int i = 0; i < 15; i++) {
            Thread.sleep(1000); // 1 request per second
            boolean allowed = rateLimiter.allowRequest();
            System.out.println("Request " + (i + 1) + ": " + (allowed ? "Allowed" : "Denied"));
        }
    }
}

```

### Leaky Bucket algorithm

The Leaky Bucket algorithm ensures **a constant outflow of requests**, smoothing out bursts in traffic.

Requests within the bucket **leak out at a constant rate**, and **if the bucket is full, incoming requests are dropped**.

Bucket:

Holds incoming requests.

Rate:

Requests **leak out at a constant rate**.

Overflow:

If the bucket is full, incoming requests **are discarded**.

### Standard Solution

```

import java.util.concurrent.LinkedBlockingQueue;
import java.util.concurrent.ScheduledExecutorService;
import java.util.concurrent.Executors;
import java.util.concurrent.TimeUnit;

public class LeakyBucket {
    private final LinkedBlockingQueue<Integer> queue;
    private final int capacity;
    private final int leakRate;
    private final ScheduledExecutorService scheduler;

    public LeakyBucket(int capacity, int leakRate) {
        this.capacity = capacity; // bucket size
        this.leakRate = leakRate;
        this.queue = new LinkedBlockingQueue<>(capacity);
        this.scheduler = Executors.newScheduledThreadPool(1);
        startLeaking();
    }

    private void startLeaking() {
        scheduler.scheduleAtFixedRate(() -> {
            if (!queue.isEmpty()) {
                queue.poll();
                System.out.println("Request processed. Queue size: " + queue.size());
            }
        }, 0, 1000 / leakRate, TimeUnit.MILLISECONDS);
    }

    public synchronized boolean allowRequest() {
        if (queue.size() < capacity) {
            queue.offer(1);
            System.out.println("Request allowed. Queue size: " + queue.size());
            return true;
        } else {
            System.out.println("Request denied. Queue is full.");
            return false;
        }
    }

    public static void main(String[] args) throws InterruptedException {
        LeakyBucket leakyBucket = new LeakyBucket(10, 2); // Capacity 10, Leak rate 2 requests/sec

        for (int i = 0; i < 15; i++) {

```

```

        Thread.sleep(500); // 2 requests per second
        boolean allowed = leakyBucket.allowRequest();
        System.out.println("Request " + (i + 1) + ": " + (allowed ? "Allowed" : "Denied"));
    }

    leakyBucket.scheduler.shutdown();
}
}

```

## Wu-Manber Algorithm

The WM (Wu-Manber) algorithm is an efficient multi-pattern string matching algorithm designed to handle large sets of patterns.

It was developed by Sun Wu and Udi Manber and is particularly known for its high performance in applications where multiple patterns need to be matched simultaneously, such as intrusion detection systems, text search engines, and bioinformatics.

## Key Concepts

Hashing:

The algorithm **uses hashing** to preprocess the patterns and create a hash table for quick lookups.

Shift Table:

A shift table is used to skip unnecessary comparisons, similar to the Boyer-Moore algorithm.

Prefix and Suffix Matching:

The algorithm matches patterns by comparing prefixes and suffixes to quickly identify potential matches.

BC	ar	ch	ea	ha	he	rc	se	others
shift	0	0	1	1	2	1	2	3

WM Shift table.

a	r	O	s	e	a	r	c	h
			h	e	a	r		
			c	h	a	r	t	

c	h	O	a	r	c	h
---	---	---	---	---	---	---

## Standard Solution

Define the WM Algorithm Class

```

import java.util.HashMap;
import java.util.Map;

public class WuManber {
    private final int B = 2; // Block size
    private final int minPatternLength;
    private final Map<String, Integer> shiftTable;
    private final Map<String, String[]> hashTable;

    public WuManber(String[] patterns) {
        this.minPatternLength = patterns[0].length();
        this.shiftTable = new HashMap<>();
        this.hashTable = new HashMap<>();
        preprocess(patterns);
    }

    private void preprocess(String[] patterns) {
        for (String pattern : patterns) {
            int m = pattern.length();
            for (int i = 0; i <= m - B; i++) {
                String block = pattern.substring(i, i + B);
                shiftTable.put(block, Math.min(shiftTable.getOrDefault(block, m - B + 1), m - B - i));
                hashTable.computeIfAbsent(block, k -> new String[0]);
                String[] existing = hashTable.get(block);
            }
        }
    }
}

```

```

        String[] newArr = new String[existing.length + 1];
        System.arraycopy(existing, 0, newArr, 0, existing.length);
        newArr[existing.length] = pattern;
        hashTable.put(block, newArr);
    }
}

public void search(String text) {
    int n = text.length();
    int i = minPatternLength - B;

    while (i < n) {
        String block = text.substring(i, i + B);
        if (shiftTable.containsKey(block)) {
            int shift = shiftTable.get(block);
            if (shift == 0) {
                // Potential match found, verify it
                verifyMatch(text, i);
            }
            i += shift;
        } else {
            i += minPatternLength - B + 1;
        }
    }
}

private void verifyMatch(String text, int position) {
    String block = text.substring(position, position + B);
    if (hashTable.containsKey(block)) {
        for (String pattern : hashTable.get(block)) {
            if (text.startsWith(pattern, position - (pattern.length() - B))) {
                System.out.println("Pattern found at index " + (position - (pattern.length() - B)));
            }
        }
    }
}
}
}

Use the WM Algorithm
public class Main {
    public static void main(String[] args) {
        String[] patterns = {"he", "she", "his", "hers"};
        WuManber wm = new WuManber(patterns);

        String text = "ushers";
        wm.search(text);
    }
}

```

### Aho-Corasick algorithm

The Aho-Corasick algorithm is a powerful and efficient **multi-pattern string matching algorithm**, designed to locate multiple patterns within a text simultaneously.

It constructs a finite state machine that resembles a digital trie of the keywords, augmented with **additional links** to allow for efficient failure transitions.

### Key Concepts:

Trie Construction:

The algorithm first constructs a trie from the given set of keywords.

Failure Links:

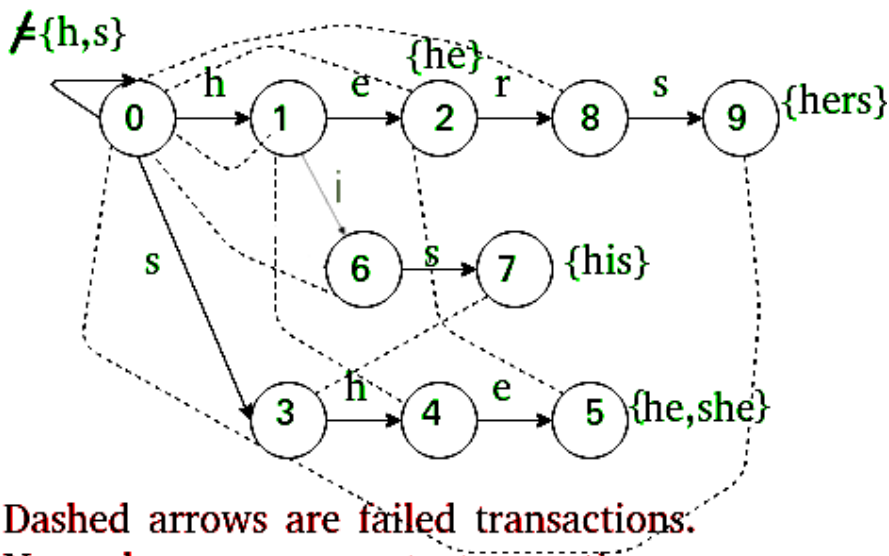
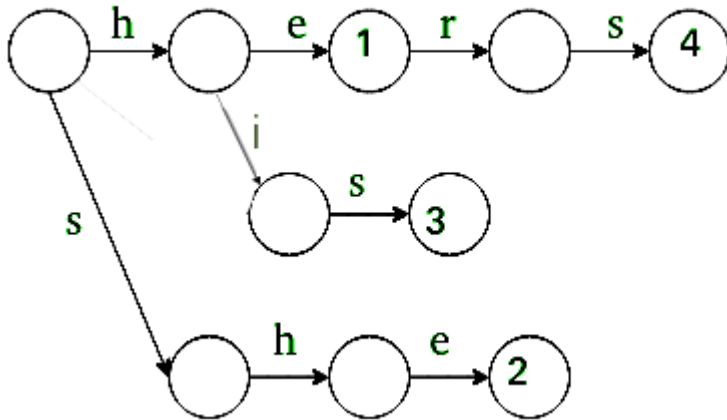
It then adds failure links to the trie. These links are used **to transition to the longest possible suffix** of the current state when a mismatch occurs.

Matching:

The text is processed in a single pass, and the state machine navigates through the trie to find all occurrences of the patterns.

## Standard Solution

Trie for Arr[] = { he , she, his , hers }



**Dashed arrows are failed transactions.**  
**Normal arrows are goto transactions.**

### Define the Trie Node

```
import java.util.HashMap;
import java.util.Map;

class TrieNode {
    Map<Character, TrieNode> children = new HashMap<>();
    TrieNode failureLink = null;
    boolean isEndOfWord = false;
}
```

### Construct the Trie

```
import java.util.ArrayList;
import java.util.LinkedList;
import java.util.List;
import java.util.Queue;

class AhoCorasick {
    private final TrieNode root;

    public AhoCorasick() {
        root = new TrieNode();
    }

    public void addKeyword(String keyword) {
```

```

TrieNode currentNode = root;
for (char ch : keyword.toCharArray()) {
    currentNode = currentNode.children.computeIfAbsent(ch, k -> new TrieNode());
}
currentNode.isEndOfWord = true;
}

// Constructs failure links to enable efficient mismatch handling.
public void buildFailureLinks() {
    Queue<TrieNode> queue = new LinkedList<>();
    for (TrieNode child : root.children.values()) {
        child.failureLink = root;
        queue.add(child);
    }

    while (!queue.isEmpty()) {
        TrieNode currentNode = queue.poll();

        for (Map.Entry<Character, TrieNode> entry : currentNode.children.entrySet()) {
            char ch = entry.getKey();
            TrieNode childNode = entry.getValue();
            queue.add(childNode);

            TrieNode failureLink = currentNode.failureLink;
            while (failureLink != null && !failureLink.children.containsKey(ch)) {
                failureLink = failureLink.failureLink;
            }

            if (failureLink == null) {
                childNode.failureLink = root;
            } else {
                childNode.failureLink = failureLink.children.get(ch);
            }
        }
    }
}

// Searches for keywords in the given text and returns the end positions of the matches.
public List<Integer> search(String text) {
    List<Integer> result = new ArrayList<>();
    TrieNode currentNode = root;

    for (int i = 0; i < text.length(); i++) {
        char ch = text.charAt(i);
        while (currentNode != null && !currentNode.children.containsKey(ch)) {
            currentNode = currentNode.failureLink;
        }

        if (currentNode == null) {
            currentNode = root;
            continue;
        }

        currentNode = currentNode.children.get(ch);
        TrieNode tempNode = currentNode;

        while (tempNode != null) {
            if (tempNode.isEndOfWord) {
                result.add(i);
            }
            tempNode = tempNode.failureLink;
        }
    }

    return result;
}
}

```

## Use the Aho-Corasick Algorithm

```
import java.util.List;

public class Main {
    public static void main(String[] args) {
        AhoCorasick ahoCorasick = new AhoCorasick();
        ahoCorasick.addKeyword("he");
        ahoCorasick.addKeyword("she");
        ahoCorasick.addKeyword("his");
        ahoCorasick.addKeyword("hers");

        ahoCorasick.buildFailureLinks();

        String text = "ushers";
        List<Integer> matches = ahoCorasick.search(text);

        for (Integer match : matches) {
            System.out.println("Pattern found at index " + (match + 1 - "she".length()));
        }
    }
}
```

## Snowflake Algorithm

### Key Features of Snowflake Algorithm

Uniqueness:

Each generated ID is unique across the system.

Sort Order:

IDs are **roughly sortable by time**, which helps in ordering records.

High Throughput:

The algorithm can generate IDs **at a very high rate**.

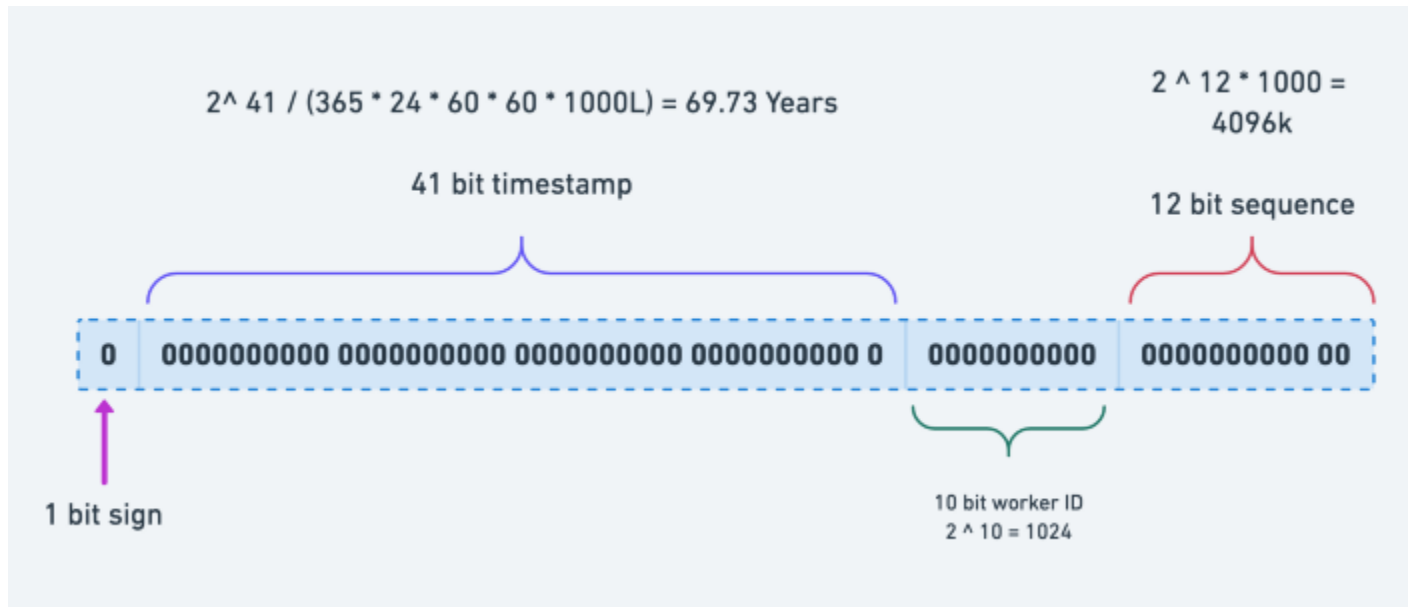
Distributed:

IDs can be generated independently on multiple nodes.

### Structure of a Snowflake ID

A typical Snowflake ID is a 64-bit integer composed of several parts:

The structure of a 64-bit Snowflake ID can be visualized as follows:



Timestamp (41 bits):

This part of the ID represents the timestamp in milliseconds since a custom epoch. It can hold a value for approximately 69 years.

Data Center ID (5 bits):

This part identifies the data center where the ID was generated. It supports up to 32 different data centers.

Machine ID (5 bits):

This part identifies the machine or worker within the data center. It supports up to 32 different machines per data center.

Sequence Number (12 bits):

This is a counter that is incremented for IDs generated within the same millisecond. It allows for 4096 unique IDs per millisecond per machine.

## Standard Solution

```
public class SnowflakeIdGenerator {
    private final long epoch = 1288834974657L;
    private final long dataCenterIdBits = 5L;
    private final long workerIdBits = 5L;
    private final long maxDataCenterId = -1L ^ (-1L << dataCenterIdBits);
    private final long maxWorkerId = -1L ^ (-1L << workerIdBits);
    private final long sequenceBits = 12L;
    private final long workerIdShift = sequenceBits;
    private final long dataCenterIdShift = sequenceBits + workerIdBits;
    private final long timestampLeftShift = sequenceBits + workerIdBits + dataCenterIdBits;
    private final long sequenceMask = -1L ^ (-1L << sequenceBits);

    private long workerId;
    private long dataCenterId;
    private long sequence = 0L;
    private long lastTimestamp = -1L;

    public SnowflakeIdGenerator(long workerId, long dataCenterId) {
        if (workerId > maxWorkerId || workerId < 0) {
            throw new IllegalArgumentException(String.format("Worker ID can't be greater than %d or less than 0", maxWorkerId));
        }
        if (dataCenterId > maxDataCenterId || dataCenterId < 0) {
            throw new IllegalArgumentException(String.format("Data Center ID can't be greater than %d or less than 0", maxDataCenterId));
        }
        this.workerId = workerId;
        this.dataCenterId = dataCenterId;
    }

    public synchronized long nextId() {
        long timestamp = timeGen();

        if (timestamp < lastTimestamp) {
            throw new RuntimeException("Clock moved backwards. Refusing to generate id for " + (lastTimestamp - timestamp) + " milliseconds");
        }

        if (lastTimestamp == timestamp) {
            sequence = (sequence + 1) & sequenceMask;
            if (sequence == 0) {
                timestamp = tilNextMillis(lastTimestamp);
            }
        } else {
            sequence = 0L;
        }

        lastTimestamp = timestamp;

        return ((timestamp - epoch) << timestampLeftShift)
            | (dataCenterId << dataCenterIdShift)
            | (workerId << workerIdShift)
            | sequence;
    }
}
```



```

protected long tilNextMillis(long lastTimestamp) {
    long timestamp = timeGen();
    while (timestamp <= lastTimestamp) {
        timestamp = timeGen();
    }
    return timestamp;
}

protected long timeGen() {
    return System.currentTimeMillis();
}
}

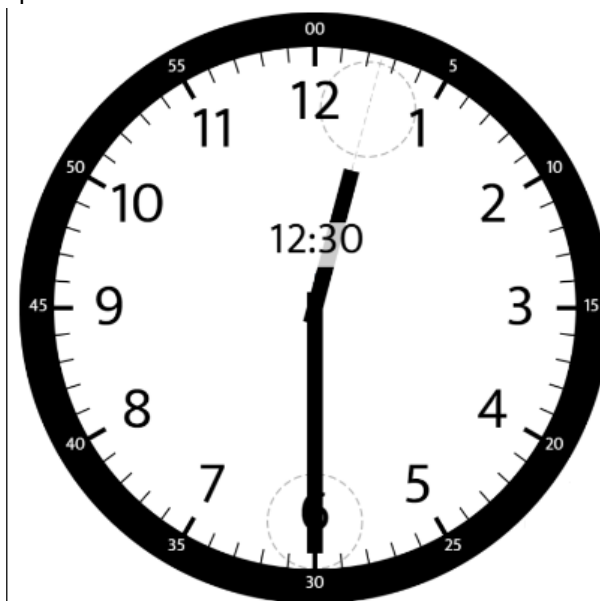
```

### Angle Between Hands of a Clock

Given two numbers, **hour** and **minutes**, return the smaller angle (in degrees) formed between the **hour** and the **minute** hand.

Answers within  $10^5$  of the actual value will be accepted as correct.

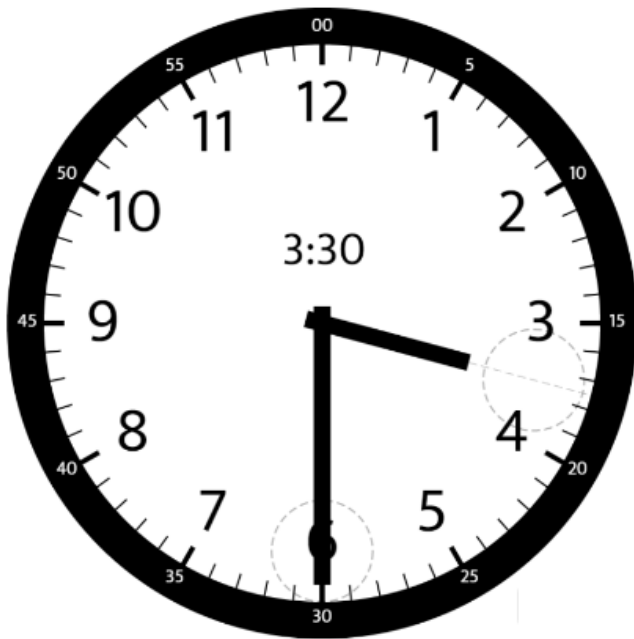
Example 1:



Input: hour = 12, minutes = 30

Output: 165

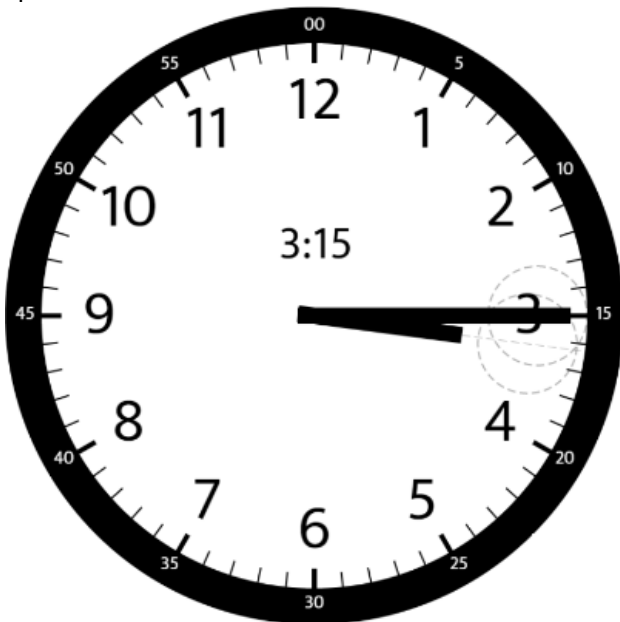
Example 2:



Input: hour = 3, minutes = 30

Output: 75

Example 3:



Input: hour = 3, minutes = 15

Output: 7.5

#### Constraints:

- $1 \leq \text{hour} \leq 12$
- $0 \leq \text{minutes} \leq 59$

#### Previous Solution

```
class Solution {
    public double angleClock(int hour, int minutes) {
        //A. public data.
        int hourToMin=hour==12?0:hour*5; // [0], 5, 10
        double additionalHourToMin=5*minutes/60.0; // 2.5, 5
        double distance=Math.abs((hourToMin+additionalHourToMin)-minutes);
```

```

        double result=distance*360/60;
        return result>180?360-result:result;
    }
}

```

## Standard Solution

```

class Solution {
    public double angleClock(int hour, int minutes) {
        int oneMinAngle = 6;
        int oneHourAngle = 30;

        double minutesAngle = oneMinAngle * minutes;
        double hourAngle = (hour % 12 + minutes / 60.0) * oneHourAngle;

        double diff = Math.abs(hourAngle - minutesAngle);
        return Math.min(diff, 360 - diff);
    }
}

```

## Binary Search

Given an array of integers `nums` which is sorted in ascending order, and an integer `target`, write a function to search `target` in `nums`. If `target` exists, then return its index. Otherwise, return `-1`.

You must write an algorithm with  $O(\log n)$  runtime complexity.

### Example 1:

**Input:** `nums = [-1,0,3,5,9,12]`, `target = 9`

**Output:** 4

**Explanation:** 9 exists in `nums` and its index is 4

### Example 2:

**Input:** `nums = [-1,0,3,5,9,12]`, `target = 2`

**Output:** -1

**Explanation:** 2 does not exist in `nums` so return -1

### Constraints:

- $1 \leq \text{nums.length} \leq 10^4$
- $-10^4 < \text{nums}[i]$ ,  $\text{target} < 10^4$
- All the integers in `nums` are **unique**.
- `nums` is sorted in ascending order.

## Standard Solution

```

class Solution {
    public int search(int[] nums, int target) {
        int left = 0, right = nums.length - 1;
        while (left <= right) {
            int mid = (right - left) / 2 + left;
            int num = nums[mid];
            if (num == target) {
                return mid;
            } else if (num > target) {
                right = mid - 1;
            } else {
                left = mid + 1;
            }
        }
        return -1;
    }
}

```

Given an unsorted integer array **nums**. Return the *smallest positive integer* that is *not present* in **nums**. You must implement an algorithm that runs in  $O(n)$  time and uses  $O(1)$  auxiliary space.

**Example 1:**

**Input:** nums = [1,2,0]

**Output:** 3

**Explanation:** The numbers in the range [1,2] are all in the array.

**Example 2:**

**Input:** nums = [3,4,-1,1]

**Output:** 2

**Explanation:** 1 is in the array but 2 is missing.

**Example 3:**

**Input:** nums = [7,8,9,11,12]

**Output:** 1

**Explanation:** The smallest positive integer 1 is missing.

**Constraints:**

- $1 \leq \text{nums.length} \leq 10^5$
- $-2^{31} \leq \text{nums}[i] \leq 2^{31} - 1$

## Previous Solution

```
class Solution {
    public int firstMissingPositive(int[] nums) {
        //A. end conditions.
        if(nums.length==1&&nums[0]<=0){
            return 1;
        }
        if(nums.length==1&&nums[0]>1){
            return 1;
        }
        if(nums.length==1&&nums[0]==1){
            return 2;
        }
        //A. sort nums
        for (int i = 0; i < nums.length; i++) {
            for (int j = i+1; j < nums.length; j++) {
                if(nums[i]>nums[j]){
                    int temp=nums[i];
                    nums[i]=nums[j];
                    nums[j]=temp;
                }
            }
        }
        int res=-1;
        //3(1) 5(r) 9 8 => 4
        //-1(1) 1(r) 9 8 => 8
        for (int left=0,right=1; right < nums.length; right++,left++) {
            if(left==0&&nums[left]>1)return 1;
            if(nums[right]<=1)continue;
            if(nums[right]!=nums[left]+1&&nums[right]!=nums[left]){
                if(nums[left]>=0){
                    return nums[left]+1;
                }else{
                    return 1;
                }
            }
        }
        if(res!=-1)return res;
        // -3 -1 1
        // 1 2 3 4 5 6 7
    }
}
```

```

        else if(nums[nums.length-1]>=1) return nums[nums.length-1]+1;
        // -9 -8 -7 -6
        else return 1;
    }
}

```

## Reverse Linked List

Given the head of a singly linked list, reverse the list, and return the reversed list.

### Constraints:

- The number of nodes in the list is the range [0, 5000].
- $-5000 \leq \text{Node.val} \leq 5000$

## Previous Solution

```

class Solution {
    public ListNode reverseList(ListNode head) {
        // 1 -> 2 -> 3 -> 4
        // 1 <- 2 <- 3 <- 4
        // prev ~ next
        //A. Focus on intermediate repetitive operations and then complete special cases.
        ListNode first=null;
        ListNode prev=head;
        if(head==null) return head;
        if(head.next==null) return head;
        ListNode next=head.next;
        while(next!=null){
            //B. switch values.
            ListNode temp=next.next;
            next.next=prev;
            prev.next=first;
            //B. move pointers.
            first=prev;
            prev=next;
            if(temp!=null)next=temp;
            else break;
        }
        return next;
    }
}

```

## Standard Solution

```

class Solution {
    public ListNode reverseList(ListNode head) {
        ListNode prev = null;
        ListNode curr = head;
        while (curr != null) {
            ListNode next = curr.next;
            curr.next = prev;
            prev = curr;
            curr = next;
        }
        return prev;
    }
}

```

## Maximal Rectangle

Given a **rows x cols** binary **matrix** filled with 0's and 1's, find the largest rectangle containing only 1's and return *its area*.

**Example 1:**

1	0	1	0	0
1	0	1	1	1
1	1	1	1	1
1	0	0	1	0

**Input:** matrix = `[["1","0","1","0","0"],["1","0","1","1","1"],["1","1","1","1","1"],["1","0","0","1","0"]]`

**Output:** 6

**Explanation:** The maximal rectangle is shown in the above picture.

**Example 2:**

**Input:** matrix = `[["0"]]`

**Output:** 0

**Example 3:**

**Input:** matrix = `[["1"]]`

**Output:** 1

**Constraints:**

- rows == matrix.length
- cols == matrix[i].length
- 1 <= row, cols <= 200
- matrix[i][j] is '0' or '1'.

### Shortest Palindrome

You are given a string *s*. You can convert *s* to a **palindrome** by adding characters in front of it.

Return *the shortest palindrome you can find by performing this transformation*.

**Example 1:**

**Input:** *s* = "aacecaaa"

**Output:** "aaacecaaa"

**Example 2:**

**Input:** *s* = "abcd"

**Output:** "dcbabcd"

### The Skyline Problem

A city's **skyline** is the outer contour of the silhouette formed by all the buildings in that city when viewed from a distance.

Given the locations and heights of all the buildings, return *the skyline formed by these buildings collectively*.

The geometric information of each building is given in the array **buildings** where **buildings[i] = [left<sub>i</sub>, right<sub>i</sub>, height<sub>i</sub>]**:

- left<sub>i</sub> is the x coordinate of the left edge of the i<sup>th</sup> building.
- right<sub>i</sub> is the x coordinate of the right edge of the i<sup>th</sup> building.

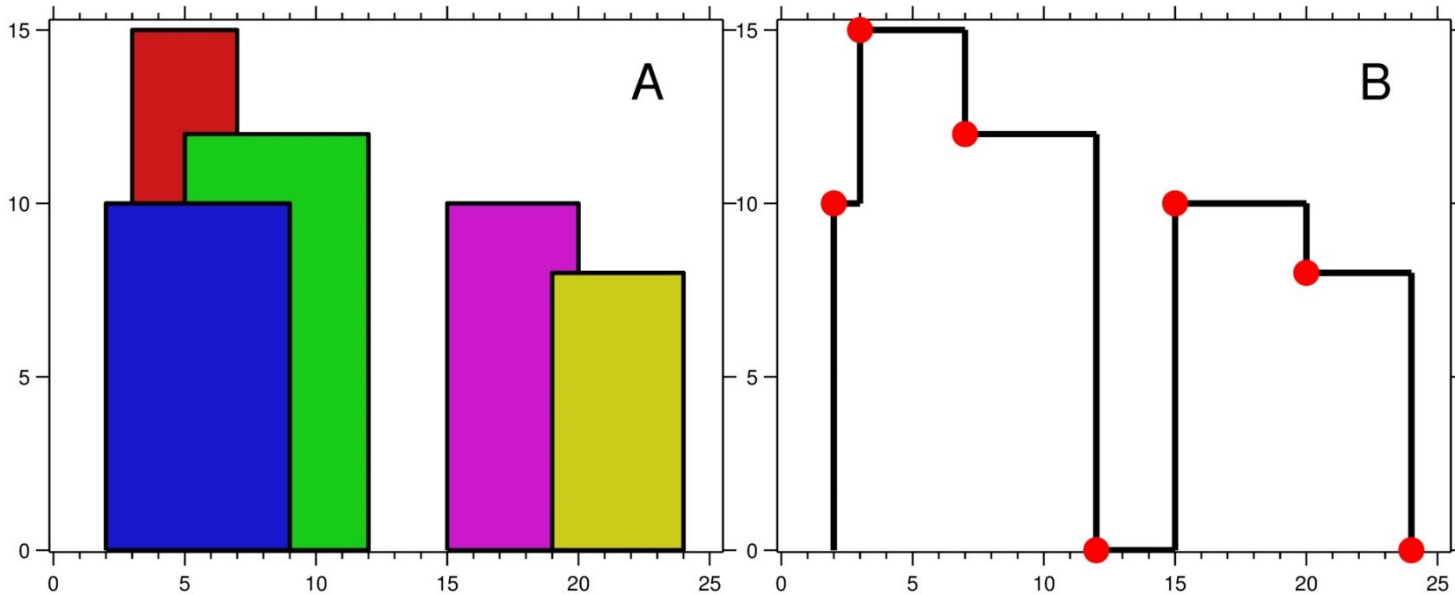
- $height_i$  is the height of the  $i^{th}$  building.

You may assume all buildings are perfect rectangles grounded on an absolutely flat surface at height 0.

The **skyline** should be represented as a list of "key points" **sorted by their x-coordinate** in the form  $[[x_1, y_1], [x_2, y_2], \dots]$ . Each key point is the left endpoint of some horizontal segment in the skyline except the last point in the list, which always has a y-coordinate 0 and is used to mark the skyline's termination where the rightmost building ends. Any ground between the leftmost and rightmost buildings should be part of the skyline's contour.

**Note:** There must be no consecutive horizontal lines of equal height in the output skyline. For instance,  $[\dots, [2, 3], [4, 5], [7, 5], [11, 5], [12, 7], \dots]$  is not acceptable; the three lines of height 5 should be merged into one in the final output as such:  $[\dots, [2, 3], [4, 5], [12, 7], \dots]$

Example 1:



**Input:** buildings =  $[[2, 9, 10], [3, 7, 15], [5, 12, 12], [15, 20, 10], [19, 24, 8]]$

**Output:**  $[[2, 10], [3, 15], [7, 12], [12, 0], [15, 10], [20, 8], [24, 0]]$

**Explanation:**

Figure A shows the buildings of the input.

Figure B shows the skyline formed by those buildings. The red points in figure B represent the key points in the output list.

Example 2:

**Input:** buildings =  $[[0, 2, 3], [2, 5, 3]]$

**Output:**  $[[0, 3], [5, 0]]$

**Constraints:**

- $1 \leq \text{buildings.length} \leq 10^4$
- $0 \leq \text{left}_i < \text{right}_i \leq 2^{31} - 1$
- $1 \leq \text{height}_i \leq 2^{31} - 1$
- buildings is sorted by  $\text{left}_i$  in non-decreasing order.

### Basic Calculator

Given a string **s** representing a valid expression, implement a basic calculator to evaluate it, and return *the result of the evaluation*.

**Note:** You are **not** allowed to use any built-in function which evaluates strings as mathematical expressions, such as `eval()`.

Example 1:

**Input:** s = "1 + 1"

**Output:** 2

**Example 2:**

**Input:** s = "2-1 + 2"

**Output:** 3

**Example 3:**

**Input:** s = "(1+(4+5+2)-3)+(6+8)"

**Output:** 23

**Constraints:**

- $1 \leq s.length \leq 3 \times 10^5$
- s consists of digits, '+', '-', '(', ')', and ' '.
- s represents a valid expression.
- '+' is **not** used as a unary operation (i.e., "+1" and "+(2 + 3)" is invalid).
- '-' could be used as a unary operation (i.e., "-1" and "-(2 + 3)" is valid).
- There will be no two consecutive operators in the input.
- Every number and running calculation will fit in a signed 32-bit integer.

### Sliding Window Maximum

You are given an array of integers **nums**, there is a sliding window of size **k** which is moving from the very left of the array to the very right. You can only see the **k** numbers in the window.

Each time the sliding window moves right by one position.

Return *the max sliding window*.

**Example 1:**

**Input:** nums = [1,3,-1,-3,5,3,6,7], k = 3

**Output:** [3,3,5,5,6,7]

**Explanation:**

Window position	Max
-----	-----
[1 3 -1] -3 5 3 6 7	<b>3</b>
1 [3 -1 -3] 5 3 6 7	<b>3</b>
1 3 [-1 -3 5] 3 6 7	<b>5</b>
1 3 -1 [-3 5 3] 6 7	<b>5</b>
1 3 -1 -3 [5 3 6] 7	<b>6</b>
1 3 -1 -3 5 [3 6 7]	<b>7</b>

**Example 2:**

**Input:** nums = [1], k = 1

**Output:** [1]

**Constraints:**

- $1 \leq \text{nums.length} \leq 10^5$
- $-10^4 \leq \text{nums}[i] \leq 10^4$
- $1 \leq k \leq \text{nums.length}$

### Integer to English Words

Convert a non-negative integer **num** to its English words representation.



**Example 1:**

**Input:** num = 123

**Output:** "One Hundred Twenty Three"

**Example 2:**

**Input:** num = 12345

**Output:** "Twelve Thousand Three Hundred Forty Five"

**Example 3:**

**Input:** num = 1234567

**Output:** "One Million Two Hundred Thirty Four Thousand Five Hundred Sixty Seven"

**Constraints:**

- $0 \leq \text{num} \leq 2^{31} - 1$

### Find Median from Data Stream

The **median** is the middle value in an ordered integer list. If the size of the list is even, there is no middle value, and the median is the mean of the two middle values.

- For example, for `arr = [2,3,4]`, the median is 3.
- For example, for `arr = [2,3]`, the median is  $(2 + 3) / 2 = 2.5$ .

Implement the MedianFinder class:

- `MedianFinder()` initializes the `MedianFinder` object.
- `void addNum(int num)` adds the integer num from the data stream to the data structure.
- `double findMedian()` returns the median of all elements so far. Answers within  $10^{-5}$  of the actual answer will be accepted.

**Example 1:****Input**

["MedianFinder", "addNum", "addNum", "findMedian", "addNum", "findMedian"]

[[], [1], [2], [], [3], []]

**Output**

[null, null, null, 1.5, null, 2.0]

**Explanation**

```
MedianFinder medianFinder = new MedianFinder();
medianFinder.addNum(1); // arr = [1]
medianFinder.addNum(2); // arr = [1, 2]
medianFinder.findMedian(); // return 1.5 (i.e., (1 + 2) / 2)
medianFinder.addNum(3); // arr[1, 2, 3]
medianFinder.findMedian(); // return 2.0
```

**Constraints:**

- $-10^5 \leq \text{num} \leq 10^5$
- There will be at least one element in the data structure before calling `findMedian`.
- At most  $5 * 10^4$  calls will be made to `addNum` and `findMedian`.

**Follow up:**

- If all integer numbers from the stream are in the range `[0, 100]`, how would you optimize your solution?
- If 99% of all integer numbers from the stream are in the range `[0, 100]`, how would you optimize your solution?

## Previous Solution

```

class MedianFinder {
    public MedianFinder() {
    }

    public void addNum(int num) {
    }

    public double findMedian() {
    }
}

/**
 * Your MedianFinder object will be instantiated and called as such:
 * MedianFinder obj = new MedianFinder();
 * obj.addNum(num);
 * double param_2 = obj.findMedian();
 */

```

### Serialize and Deserialize Binary Tree

Serialization is the process of converting a data structure or object into a sequence of bits so that it can be stored in a file or memory buffer, or transmitted across a network connection link to be reconstructed later in the same or another computer environment.

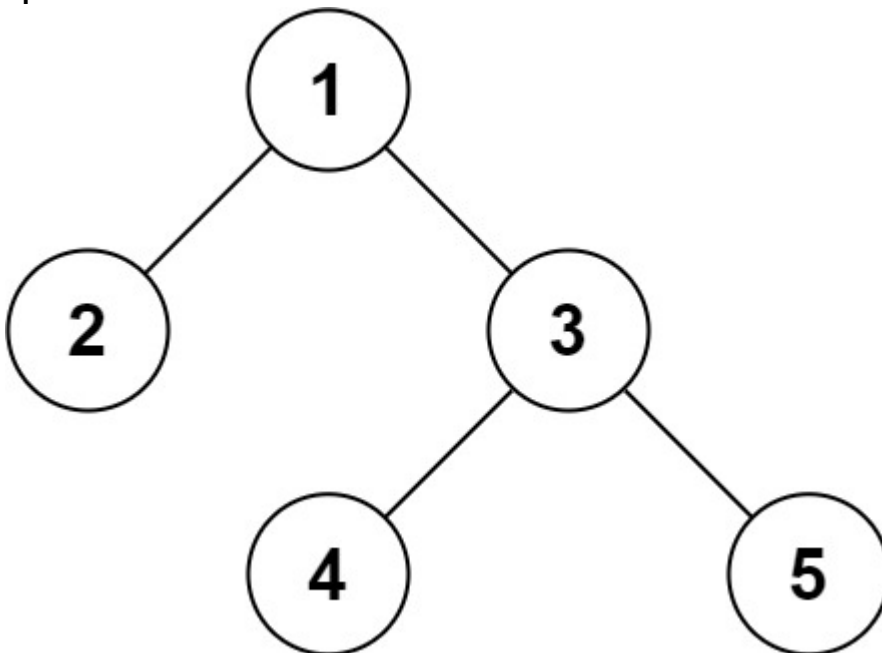
Design an algorithm to serialize and deserialize a binary tree. There is no restriction on how your serialization/deserialization algorithm should work.

You just need to ensure that a binary tree can be serialized to a string and this string can be deserialized to the original tree structure.

**Clarification:** The input/output format is the same as [how LeetCode serializes a binary tree](#).

You do not necessarily need to follow this format, so please be creative and come up with different approaches yourself.

**Example 1:**



**Input:** root = [1,2,3,null,null,4,5]

**Output:** [1,2,3,null,null,4,5]

**Example 2:**

**Input:** root = []

**Output:** []

**Constraints:**

- The number of nodes in the tree is in the range [0, 10<sup>4</sup>].
- -1000 <= Node.val <= 1000

## Previous Solution

```
/**
 * Definition for a binary tree node.
 * public class TreeNode {
 *     int val;
 *     TreeNode left;
 *     TreeNode right;
 *     TreeNode(int x) { val = x; }
 * }
 */
public class Codec {

    // Encodes a tree to a single string.
    public String serialize(TreeNode root) {

    }

    // Decodes your encoded data to tree.
    public TreeNode deserialize(String data) {

    }

}

// Your Codec object will be instantiated and called as such:
// Codec ser = new Codec();
// Codec deser = new Codec();
// TreeNode ans = deser.deserialize(ser.serialize(root));
```

## Reconstruct Itinerary

You are given a list of airline **tickets** where **tickets[i] = [from<sub>i</sub>, to<sub>i</sub>]** represent the departure and the arrival airports of one flight. Reconstruct the itinerary in order and return it.

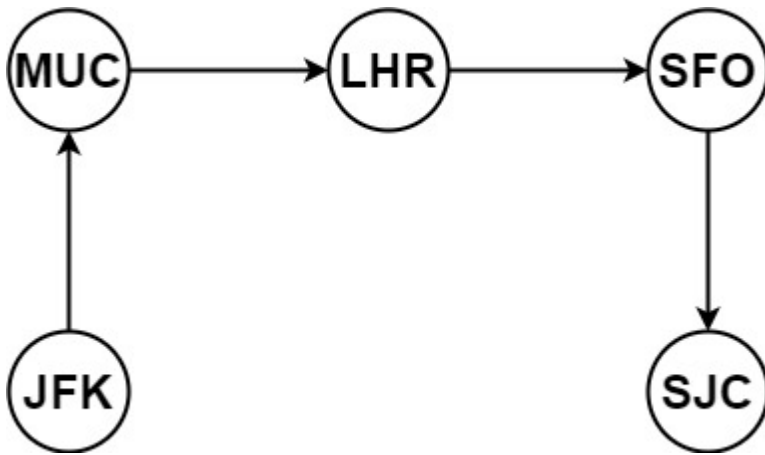
All of the tickets belong to a man who departs from **"JFK"**, thus, the itinerary must begin with **"JFK"**.

If there are multiple valid itineraries, you should return the itinerary that has the smallest lexical order when read as a single string.

- For example, the itinerary **["JFK", "LGA"]** has a smaller lexical order than **["JFK", "LGB"]**.

You may assume all tickets form at least one valid itinerary. You must use all the tickets once and only once.

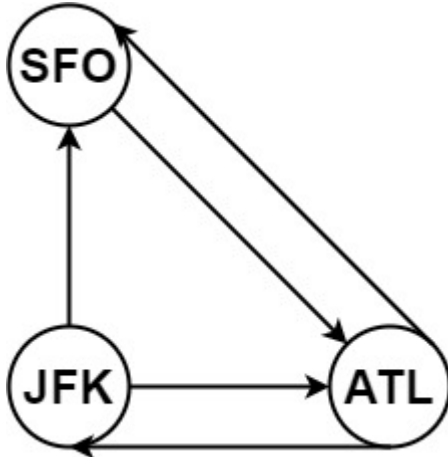
### Example 1:



**Input:** tickets = [["MUC","LHR"],["JFK","MUC"],["SFO","SJC"],["LHR","SFO"]]

**Output:** ["JFK","MUC","LHR","SFO","SJC"]

**Example 2:**



**Input:** tickets = [["JFK","SFO"],["JFK","ATL"],["SFO","ATL"],["ATL","JFK"],["ATL","SFO"]]

**Output:** ["JFK","ATL","JFK","SFO","ATL","SFO"]

**Explanation:** Another possible reconstruction is ["JFK","SFO","ATL","JFK","ATL","SFO"] but it is larger in lexical order.

**Constraints:**

- $1 \leq \text{tickets.length} \leq 300$
- $\text{tickets}[i].\text{length} == 2$
- $\text{from}_i.\text{length} == 3$
- $\text{to}_i.\text{length} == 3$
- $\text{from}_i$  and  $\text{to}_i$  consist of uppercase English letters.
- $\text{from}_i \neq \text{to}_i$

### Palindrome Pairs

You are given a **0-indexed** array of **unique** strings **words**.

A **palindrome pair** is a pair of integers  $(i, j)$  such that:

- $0 \leq i, j < \text{words.length}$ ,
- $i \neq j$ , and
- $\text{words}[i] + \text{words}[j]$  (the concatenation of the two strings) is a palindrome.

Return an array of all the **palindrome pairs** of **words**.

You must write an algorithm with  $O(\sum \text{of words}[i].\text{length})$  runtime complexity.

**Example 1:**

**Input:** words = ["abcd","dcba","lls","s","sssll"]

**Output:** [[0,1],[1,0],[3,2],[2,4]]

**Explanation:** The palindromes are ["abccddcba","dcbaabcd","slls","llssssll"]

**Example 2:**

**Input:** words = ["bat","tab","cat"]

**Output:** [[0,1],[1,0]]

**Explanation:** The palindromes are ["battab","tabbat"]

**Example 3:**

**Input:** words = ["a",""]

**Output:** [[0,1],[1,0]]

**Explanation:** The palindromes are ["a","a"]

**Constraints:**

- 1 <= words.length <= 5000
- 0 <= words[i].length <= 300
- words[i] consists of lowercase English letters.

**Insert Delete GetRandom O(1) - Duplicates allowed**

**RandomizedCollection** is a data structure that contains a collection of numbers, possibly duplicates (i.e., a multiset). It should support inserting and removing specific elements and also reporting a random element.

Implement the **RandomizedCollection** class:

- **RandomizedCollection()** Initializes the empty **RandomizedCollection** object.
- **bool insert(int val)** Inserts an item **val** into the multiset, even if the item is already present. Returns **true** if the item is not present, **false** otherwise.
- **bool remove(int val)** Removes an item **val** from the multiset if present. Returns **true** if the item is present, **false** otherwise.  
Note that if **val** has multiple occurrences in the multiset, we only remove one of them.
- **int getRandom()** Returns a random element from the current multiset of elements.  
The probability of each element being returned is **linearly related** to the number of the same values the multiset contains.

You must implement the functions of the class such that each function works on **average O(1)** time complexity.

**Note:** The test cases are generated such that **getRandom** will only be called if there is **at least one** item in the **RandomizedCollection**.

**Example 1:**

**Input**

["RandomizedCollection", "insert", "insert", "insert", "getRandom", "remove", "getRandom"]  
[[], [1], [1], [2], [], [1], []]

**Output**

[null, true, false, true, 2, true, 1]

**Explanation**

```
RandomizedCollection randomizedCollection = new RandomizedCollection();
randomizedCollection.insert(1); // return true since the collection does not contain 1.
// Inserts 1 into the collection.
randomizedCollection.insert(1); // return false since the collection contains 1.
// Inserts another 1 into the collection. Collection now contains [1,1].
randomizedCollection.insert(2); // return true since the collection does not contain 2.
```

```

// Inserts 2 into the collection. Collection now contains [1,1,2].
randomizedCollection.getRandom(); // getRandom should:
// - return 1 with probability 2/3, or
// - return 2 with probability 1/3.
randomizedCollection.remove(1); // return true since the collection contains 1.
// Removes 1 from the collection. Collection now contains [1,2].
randomizedCollection.getRandom(); // getRandom should return 1 or 2, both equally likely.

```

#### Constraints:

- $-2^{31} \leq \text{val} \leq 2^{31} - 1$
- At most  $2 * 10^5$  calls **in total** will be made to insert, remove, and getRandom.
- There will be **at least one** element in the data structure when getRandom is called.

#### Previous Solution

```

class RandomizedCollection {
    public RandomizedCollection() {
    }
    public boolean insert(int val) {
    }
    public boolean remove(int val) {
    }
    public int getRandom() {
    }
}

/**
 * Your RandomizedCollection object will be instantiated and called as such:
 * RandomizedCollection obj = new RandomizedCollection();
 * boolean param_1 = obj.insert(val);
 * boolean param_2 = obj.remove(val);
 * int param_3 = obj.getRandom();
 */

```

#### Delete Node in a Linked List

There is a singly-linked list **head** and we want to delete a node **node** in it.

You are given the node to be deleted **node**. You will **not be given access** to the first node of **head**.

All the values of the linked list are **unique**, and it is guaranteed that the given node **node** is not the last node in the linked list.

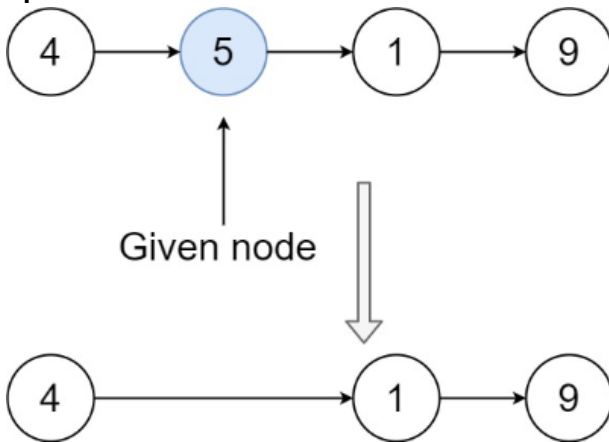
Delete the given node. Note that by deleting the node, we do not mean removing it from memory. We mean:

- The value of the given node should not exist in the linked list.
- The number of nodes in the linked list should decrease by one.
- All the values before **node** should be in the same order.
- All the values after **node** should be in the same order.

#### Custom testing:

- For the input, you should provide the entire linked list **head** and the node to be given **node**. **node** should not be the last node of the list and should be an actual node in the list.
- We will build the linked list and pass the node to your function.
- The output will be the entire list after calling your function.

### Example 1:

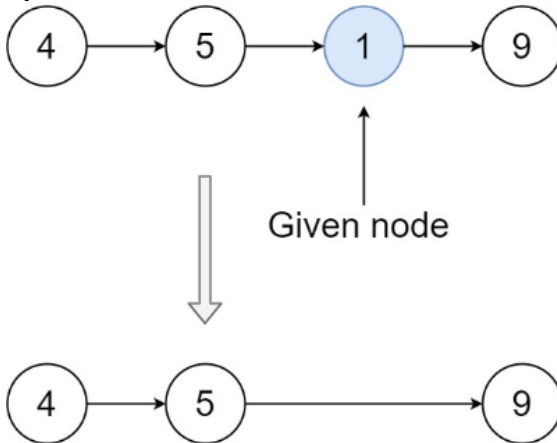


**Input:** head = [4,5,1,9], node = 5

**Output:** [4,1,9]

**Explanation:** You are given the second node with value 5, the linked list should become 4 -> 1 -> 9 after calling your function.

### Example 2:



**Input:** head = [4,5,1,9], node = 1

**Output:** [4,5,9]

**Explanation:** You are given the third node with value 1, the linked list should become 4 -> 5 -> 9 after calling your function.

### Constraints:

- The number of the nodes in the given list is in the range [2, 1000].
- $-1000 \leq \text{Node.val} \leq 1000$
- The value of each node in the list is **unique**.
- The node to be deleted is **in the list** and is **not a tail** node.

## Standard Solution

```
class Solution {  
    public void deleteNode(ListNode node) {  
        //A. transform the next node to the current node.  
        node.val=node.next.val;  
        node.next=node.next.next;  
    }  
}
```

## Queue

### Rearrange String k Distance Apart

Given a string `s` and an integer `k`, rearrange `s` such that the same characters are at least distance `k` from each other. If it is not possible to rearrange the string, return an empty string `""`.

Example 1:

Input: `s = "aabbcc"`, `k = 3`

Output: `"abcabc"`

Explanation: The same letters are at least a distance of 3 from each other.

Example 2:

Input: `s = "aaabc"`, `k = 3`

Output: `""`

Explanation: It is not possible to rearrange the string.

Example 3:

Input: `s = "aaadbcc"`, `k = 2`

Output: `"abacabcd"`

Explanation: The same letters are at least a distance of 2 from each other.

Constraints:

$1 \leq s.length \leq 3 * 10^5$

`s` consists of only lowercase English letters.

$0 \leq k \leq s.length$

## Previous Solution

```
class Solution {
    public String rearrangeString(String s, int k) {
        char[] charList=s.toCharArray();
        Deque<Integer>
availableIndList=IntStream.range(0,s.length).boxed().collect(Collectors.toCollection(LinkedList::new));
        Queue<Integer> currentIndList=new LinkedList();
        //A. breadth-first search

    }

    private void findRoute(char[] charList, Deque<Integer> availableIndList,
        Queue<Integer> currentIndList, int distance ){

        //A. check if current character is available.
        Integer availableInd = availableIndList.pollFirst();
        char originalChar = charList[availableInd];
        boolean isMatching=true;
        for(int i = availableInd; i>=0&& i>=availableInd-distance; i--){
            char compareChar=charList[i];
            if(originalChar==compareChar)isMatching=false;
        }
        if(isMatching)currentIndList.offer(availableInd);

    }

}
```

## Standard Solution



```

class Solution {
    public String rearrangeString(String s, int k) {
        //A. create a map[ character - quantity ]
        int[] map = new int[26];
        for(char c : s.toCharArray()){
            map[c - 'a']++;
        }
        //A. public data
        PriorityQueue<Integer> heap = new PriorityQueue<>((o1, o2) -> map[o2] - map[o1]); // [0,2,5...25]
        StringBuilder ans = new StringBuilder(); // "acf"
        Queue<Integer> temp = new LinkedList<>(); // [0,2,5]
        //A. add existed characters to heap
        for(int i = 0; i < map.length; i++){
            if(map[i] > 0) heap.add(i);
        }
        while(!heap.isEmpty()){
            //B. poll current character
            int curr = heap.poll();
            temp.add(curr);
            map[curr]--;
            ans.append((char)('a' + curr));
            if(temp.size() >= k){
                int mem = temp.poll();
                if(map[mem] > 0) heap.offer(mem);
            }
        }

        return ans.length() == s.length() ? ans.toString() : "";
    }
}

```

## Recursion

### Reverse Nodes in k-Group

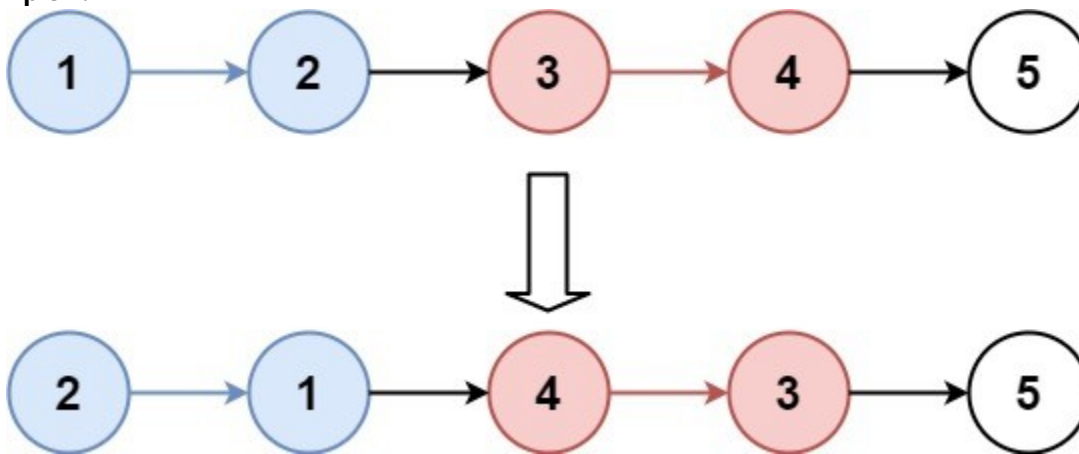
Given the **head** of a linked list, reverse the nodes of the list **k** at a time, and return *the modified list*.

**k** is a positive integer and is less than or equal to the length of the linked list.

If the number of nodes is not a multiple of **k** then left-out nodes, in the end, should remain as it is.

You may not alter the values in the list's nodes, only nodes themselves may be changed.

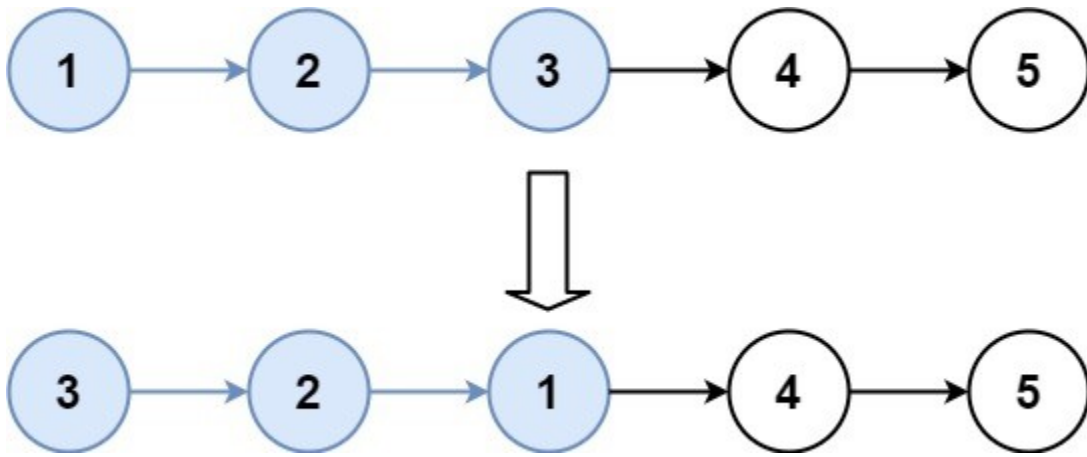
**Example 1:**



**Input:** head = [1,2,3,4,5], k = 2

**Output:** [2,1,4,3,5]

**Example 2:**



**Input:** head = [1,2,3,4,5], k = 3

**Output:** [3,2,1,4,5]

#### Constraints:

- The number of nodes in the list is n.
- $1 \leq k \leq n \leq 5000$
- $0 \leq \text{Node.val} \leq 1000$

#### Previous Solution

```
/**
 * Definition for singly-linked list.
 * public class ListNode {
 *     int val;
 *     ListNode next;
 *     ListNode() {}
 *     ListNode(int val) { this.val = val; }
 *     ListNode(int val, ListNode next) { this.val = val; this.next = next; }
 * }
 *
 * Input: head = [1,2,3,4,5], k = 3
 * Output: [3,2,1,4,5]
 */
```

```
class Solution {
    public ListNode reverseKGroup(ListNode head, int k) {
        //A. traverse the linked list.
        ListNode preLastNode=null;
        ListNode curLastNode=null;
        ListNode result=null;
        while(head!=null){
            //B. use a deque to store the k elements.
            //NOTE: hold the current element instead of creating a new deque.
            Deque<ListNode> lifo=new LinkedList<>();
            int i=0;
            for(; i<k&&head!=null; i++){
                lifo.offerLast(head);
                head=head.next;
            }
            //B. If we have a full group of k nodes, reverse them.
            if(i==k){
                //C. reverse the first sequence.
                if(preLastNode==null){
                    preLastNode=lifo.pollLast();
                    if(result==null)result=preLastNode;
                }
                //C. middle sequences.
                while(!lifo.isEmpty()){
                    preLastNode.next=lifo.pollLast();
                }
            }
        }
    }
}
```

```

        preLastNode=preLastNode.next;
    }
    //C. set the next field of the last node to null.
    curLastNode=preLastNode;
}else{
    //C. preserve the order of remaining items for the first sequence.
    if(preLastNode==null){
        preLastNode=lifo.pollFirst();
        if(result==null)result=preLastNode;
    }
    //C. middle sequences.
    while(!lifo.isEmpty()){
        preLastNode.next=lifo.pollFirst();
        preLastNode=preLastNode.next;
    }
    //C. set the next field of the last node to null.
    curLastNode=preLastNode;
}
}
curLastNode.next=null;
return result;
}
public class ListNode {
    int val;
    ListNode next;
    ListNode() {}
    ListNode(int val) { this.val = val; }
    ListNode(int val, ListNode next) { this.val = val; this.next = next; }
}

```

## Standard Solution

```

class Solution {
    public ListNode reverseKGroup(ListNode head, int k) {
        if (head == null) return head;
        ListNode p = head;
        int i = 1;
        while (p != null && p.next != null && i < k) {
            p = p.next;
            i++;
        }
        if (i < k) return head;
        ListNode h = head;
        ListNode pre = null;
        ListNode next = p.next;
        // A      B      C
        // A.next=pre  B.next=pre      Use variable pre to hold the previous node.
        // pre=A      pre = B
        // A=B      B=C
        while (h != next) {
            ListNode t = h.next;
            h.next = pre;
            pre = h;
            h = t;
        }
        head.next = reverseKGroup(next, k);
        return p;
    }
}

```

## Sudoku Solver

Write a program to solve a Sudoku puzzle by filling the empty cells.

A sudoku solution must satisfy **all of the following rules**:

1. Each of the digits **1-9** must occur exactly once in each row.
2. Each of the digits **1-9** must occur exactly once in each column.
3. Each of the digits **1-9** must occur exactly once in each of the 9 **3x3** sub-boxes of the grid.

The '.' character indicates empty cells.

**Example 1:**

5	3			7				
6			1	9	5			
	9	8					6	
8				6				3
4			8		3			1
7				2				6
	6					2	8	
			4	1	9			5
				8			7	9

**Input:** board =

```
[["5","3",".", ".", "7",".", ".", ".", "."],["6",".", ".", "1","9","5",".", ".", "."],[".", "9","8",".", ".", ".", "6","."],["8",".", ".", "6",".", ".", "3"],["4",
".", ".", "8",".", "3",".", ".", "1"],
["7",".", ".", "2",".", ".", "6"],[".", "6",".", ".", "2","8","."],[".", ".", "4","1","9",".", "5"],[".", ".", "8",".", "7","9"]]
```

**Output:**

```
[["5","3","4","6","7","8","9","1","2"],["6","7","2","1","9","5","3","4","8"],["1","9","8","3","4","2","5","6","7"],["8","5","9","7","6","
1","4","2","3"],["4","2","6","8","5","3","7","9","1"],
["7","1","3","9","2","4","8","5","6"],["9","6","1","5","3","7","2","8","4"],["2","8","7","4","1","9","6","3","5"],["3","4","5","2","8","6
","1","7","9"]]
```

**Explanation:** The input board is shown above and the only valid solution is shown below:

5	3	4	6	7	8	9	1	2
6	7	2	1	9	5	3	4	8
1	9	8	3	4	2	5	6	7
8	5	9	7	6	1	4	2	3
4	2	6	8	5	3	7	9	1
7	1	3	9	2	4	8	5	6
9	6	1	5	3	7	2	8	4
2	8	7	4	1	9	6	3	5
3	4	5	2	8	6	1	7	9

**Constraints:**

- board.length == 9
- board[i].length == 9
- board[i][j] is a digit or '.'.
- It is **guaranteed** that the input board has only one solution.

## Previous Solution

```
public class Solution3 {

    private Map<Integer, Set<Integer>> gridMap=new HashMap<>();
    private Map<Integer, Set<Integer>> rowMap=new HashMap<>();
    private Map<Integer, Set<Integer>> colMap =new HashMap<>();
```

```

public static void main(String[] args) {
    char[][] board = new char[][]{
        {'5', '3', '.', '.', '7', '.', '.', '.', '.'},
        {'6', '.', '.', '1', '9', '5', '.', '.', '.'},
        {'.', '9', '8', '.', '.', '.', '6', '.', '.'},
        {'8', '.', '.', '6', '.', '.', '.', '3', '.'},
        {'4', '.', '.', '8', '.', '3', '.', '.', '1', '.'},
        {'7', '.', '.', '2', '.', '.', '.', '6', '.'},
        {'.', '6', '.', '.', '2', '8', '.', '.', '.'},
        {'.', '.', '4', '1', '9', '.', '.', '5', '.'},
        {'.', '.', '8', '.', '7', '9', '.', '.'}};
    Solution3 solution3 = new Solution3();
    solution3.solveSudoku(board);
}

public void solveSudoku(char[][] board) {
    //A. traverse the entire board and collect all constraints.
    for (int i = 0; i < 9; i++) {
        for (int j = 0; j < 9; j++) {
            final char curChar=board[i][j];
            if(board[i][j]!='.'){
                collectGridConstraints(board, i, j);
            }
        }
    }
    //A. depth first search for the sudoku board.
    dfs(board, 0, 0, 0, new int[board.length][board[0].length]);
}

private void collectGridConstraints(char[][] board, int i, int j) {
    //B. collect grid constraints.
    int gridInd = getGridIndex(i, j);
    int gridVal=Character.getNumericValue(board[i][j]);
    gridMap.computeIfPresent(gridInd,(key,val)->{
        val.add(gridVal);
        return val;
    });
    gridMap.putIfAbsent(getGridIndex(i, j), new HashSet<>(){
        add(gridVal);
    });
    //B. collect row constraints.
    rowMap.computeIfPresent(i,(key, val)->{
        val.add(gridVal);
        return val;
    });
    rowMap.putIfAbsent(i,new HashSet<>(){
        add(gridVal);
    });
    colMap.computeIfPresent(j,(key, val)->{
        val.add(gridVal);
        return val;
    });
    colMap.putIfAbsent(j,new HashSet<>(){
        add(gridVal);
    });
}

private boolean dfs(char[][] board, int row, int col, int sum, int[][] path){
    //A. end conditions.
    if(invalidGrid(row, col))return false;
    if(path[row][col]==1)return false;
    // skip already checked grids.
    //if(board[row][col]=='0')return false;
    if(sum>=75){
        return true;
    }
    // R R 1 x x x x x (0,0) (0,3) (0,6) column/3
    // . R . x x x x x (1,0) (1,3) (1,6)

```

```

// 6 4 5 x x x x x
// x x x x x x x x (3,0) (3,3) (3,6)
// x x x x x x x x
// x x x x x x x x
// R - recursion parameter coordinates

//A. if the current grid already has a value, do nothing but increase the sum by one.
if(board[row][col]!='.'){
    path[row][col]=1;
    boolean res= dfs(board, row+1, col, sum+1, path)
    || dfs(board, row-1, col, sum+1, path)
    || dfs(board, row, col+1, sum+1, path)
    || dfs(board, row, col-1, sum+1, path);
    path[row][col]=0;
    return res;
}
//A. set a valid value for the current grid.
int gridIndex = getGridIndex(row, col);
for(int i=1;i<=9;i++){
    if(rowMap.get(row).contains(i))continue;
    if(colMap.get(col).contains(i))continue;
    if(gridMap.get(gridIndex).contains(i))continue;
    board[row][col]=(char)(i+'0');
    collectGridConstraints(board, row, col);
    path[row][col]=1;
    boolean res= dfs(board, row+1, col, sum+1, path)
    || dfs(board, row-1, col, sum+1, path)
    || dfs(board, row, col+1, sum+1, path)
    || dfs(board, row, col-1, sum+1, path);
    path[row][col]=0;
    clearGridConstraints(board, row, col);
    return res;
}
return false;
}

private void clearGridConstraints(char[][] board, int i, int j) {
    //B. collect grid constraints.
    int gridInd = getGridIndex(i, j);
    int gridVal=Character.getNumericValue(board[i][j]);
    gridMap.computeIfPresent(gridInd,(key,val)->{
        val.remove(gridVal);
        return val;
    });

    //B. collect row constraints.
    rowMap.computeIfPresent(i,(key, val)->{
        val.remove(gridVal);
        return val;
    });

    colMap.computeIfPresent(j,(key, val)->{
        val.remove(gridVal);
        return val;
    });

    board[i][j]='.';
}

private boolean invalidGrid(int row, int col){
    return row<0 || col <0 || row>=9 || col>=9;
}

private int getGridIndex(int row, int col){

```

```

//A. don't perform validity checks.
//A. row<3
if(row<3 && col<3){
    return 1;
}else if(row<3 && col>=3 && col<6){
    return 2;
}else if(row<3 && col>=6 && col<9){
    return 3;
//A. row>=3 && row<6
}else if(row>=3 && row<6 && col<3){
    return 4;
}else if(row>=3 && row<6 && col>=3 && col<6){
    return 5;
}else if(row>=3 && row<6 && col>=6 && col<9){
    return 6;
//A. row>=6 && row<9
}else if(row>=6 && row<9 && col<3){
    return 7;
}else if(row>=6 && row<9 && col>=3 && col<6){
    return 8;
}else if(row>=6 && row<9 && col>=6 && col<9){
    return 9;
}
return -1;
}
}

```

## Standard Solution

```

package com.citi.ccb.cashmgmt;

class Solution4 {
    public void solveSudoku(char[][] board) {
        solve(board);
    }

    public boolean solve (char[][] board){
        for(int i=0;i<9;i++){
            for(int j=0;j<9;j++){
                // N 2 1 x x x x x x (0,0) (0,3) (0,6) column/3
                // . 3 . x x x x x x (1,0) (1,3) (1,6)
                // 6 4 5 x x x x x x
                // x x x x x x x x x (3,0) (3,3) (3,6)
                // x x x x x x x x x
                // x x x x x x x x x
                // R - recursion parameter coordinates
                // N - 9 traversals

                //A. skip grids with a numeric value.
                if(board[i][j]!='.'){
                    for(char digit='1';digit<='9';digit++){
                        //A. Actually, A lot of recursion is skipped because the logic below already sets a
                        value for the grid.
                        if(isValid(board,i,j,digit)){
                            board[i][j]=digit;
                            if(solve(board)==true){
                                return true;
                            }
                        }
                        else{
                            board[i][j]='.';
                        }
                    }
                }
                //B. if there are no valid digits, stop recursion.
                return false;
            }
        }
    }
}
return true;

```

```

    }

    public boolean isValid(char[][] board,int row,int col,char digit){
        for(int i=0;i<9;i++){
            if(board[i][col]==digit){
                return false;
            }
            if(board[row][i]==digit){
                return false;
            }
            if(board[3*(row/3)+i/3][3*(col/3)+i%3]==digit){
                return false;
            }
        }
        return true;
    }
}

```

### Set

#### The common URLs between files a and b

Given two files a and b, each file contains **5 billion URLs**, each URL is **64 bytes**, find the common URLs between files a and b. The memory limit is **4 GB**.

External Sorting or Hash Partitioning:

Given the large size of the data, you'll need to break down the problem into **smaller, manageable chunks**.

One approach is to use external sorting or hash partitioning to split the data into smaller chunks that can fit into memory.

Two-Pass Algorithm:

First Pass: Partition **both files into smaller chunks** using hash functions.

Second Pass: Process **these chunks** to find the common URLs.

Memory Constraints:

Each URL is 64 bytes.

With 5 billion URLs in each file, each file is 320 GB (5 billion \* 64 bytes).

Processing these files directly would require substantial memory, which exceeds the 4 GB limit.

Memory Overhead:

Java's runtime environment (JVM) itself consumes memory.

Data structures such as **hash sets** also add overhead.

It's prudent to leave some buffer **to ensure smooth operation** and **avoid out-of-memory errors**.

## Standard Solution

Partitioning the Files:

The partitionFile method reads the original file and writes each URL to one of the smaller partition files based on a hash of the URL.

This ensures that URLs that could be common are in the same partition.

Finding Common URLs:

The findCommonURLs method reads corresponding partition files from both sets, loads one partition into a hash set, and then checks each URL in the other partition against this set to find common URLs.

```
import java.io.*;
```



```

import java.util.*;

public class CommonURLs {
    private static final int URL_SIZE = 64;
    private static final int PARTITION_COUNT = 1000; // Adjust based on memory limits

    public static void main(String[] args) throws IOException {
        String fileA = "path/to/fileA";
        String fileB = "path/to/fileB";
        String partitionDirA = "path/to/partitionDirA";
        String partitionDirB = "path/to/partitionDirB";

        // Step 1: Partition the files
        partitionFile(fileA, partitionDirA);
        partitionFile(fileB, partitionDirB);

        // Step 2: Find common URLs in partitions
        findCommonURLs(partitionDirA, partitionDirB);
    }

    private static void partitionFile(String inputFile, String outputDir) throws IOException {
        BufferedReader reader = new BufferedReader(new FileReader(inputFile));
        List<BufferedWriter> writers = new ArrayList<>();
        for (int i = 0; i < PARTITION_COUNT; i++) {
            writers.add(new BufferedWriter(new FileWriter(outputDir + "/part" + i + ".txt")));
        }

        String url;
        while ((url = reader.readLine()) != null) {
            int partition = url.hashCode() % PARTITION_COUNT;
            if (partition < 0) partition += PARTITION_COUNT;
            writers.get(partition).write(url);
            writers.get(partition).newLine();
        }

        reader.close();
        for (BufferedWriter writer : writers) {
            writer.close();
        }
    }

    private static void findCommonURLs(String partitionDirA, String partitionDirB) throws IOException {
        for (int i = 0; i < PARTITION_COUNT; i++) {
            Set<String> setA = new HashSet<>();
            BufferedReader readerA = new BufferedReader(new FileReader(partitionDirA + "/part" + i + ".txt"));
            String url;
            while ((url = readerA.readLine()) != null) {
                setA.add(url);
            }
            readerA.close();

            BufferedReader readerB = new BufferedReader(new FileReader(partitionDirB + "/part" + i + ".txt"));
            while ((url = readerB.readLine()) != null) {
                if (setA.contains(url)) {
                    System.out.println(url);
                }
            }
            readerB.close();
        }
    }
}

```

## Sorting

### 插入排序

## Bubble Sort

Time Complexity:  $O(n^2)$

Space Complexity:  $O(1)$

### Standard Solution

```
public class BubbleSort {
    public static void bubbleSort(int[] arr) {
        int len = arr.length;
        for (int i = 0; i < len; i++) {
            for (int j = i; j < len; j++) {
                if (arr[i] > arr[j]) {
                    int temp = arr[i];
                    arr[i] = arr[j];
                    arr[j] = temp;
                }
            }
        }
    }

    public static void main(String[] args) {
        int[] arr = {64, 34, 25, 12, 22, 11, 90};
        bubbleSort(arr);
        System.out.print("Sorted array: ");
        for (int i : arr) {
            System.out.print(i + " ");
        }
    }
}
```

## Merge Sort

6 5 3 1 8 7 2 4

Time Complexity:  $O(n \log n)$

Space Complexity:  $O(n)$

### Standard Solution

```
public class MergeSort {
    public static void mergeSort(int[] arr, int left, int right) {
        //A. Check whether the range is valid (Initial range is [0, arr.length - 1]).
        if (left < right) {
            //A. Calculate the middle index.
            // 0 1 2 3 4 5
            // 2 3 4          left 2  right 4  middle = 3
            // 2 3 4 5        left 2  right 5  middle = 3
            int middle = (left + right) / 2;
            //A. partition the array.
```

```

        mergeSort(arr, left, middle);
        mergeSort(arr, middle + 1, right);
        //A. sort the partitions.
        merge(arr, left, middle, right);
    }
}

public static void merge(int[] arr, int left, int middle, int right) {
    //A. Create two arrays for both left and right partitions and store elements in them.
    int lLen = middle - left + 1;
    int rLen = right - middle;
    int[] lArr = new int[lLen];
    int[] rArr = new int[rLen];

    for (int i = 0; i < lLen; ++i)
        lArr[i] = arr[left + i];
    for (int j = 0; j < rLen; ++j)
        rArr[j] = arr[middle + 1 + j];

    int i = 0, j = 0;
    int k = left;
    // A1. Compare elements from the left and right subarrays.
    // A2. Place elements with smaller values on the left side of the main array.
    while (i < lLen && j < rLen) {
        if (lArr[i] <= rArr[j]) {
            arr[k] = lArr[i];
            i++;
        } else {
            arr[k] = rArr[j];
            j++;
        }
        k++;
    }
    //A. append the remaining items to the tail.
    while (i < lLen) {
        arr[k] = lArr[i];
        i++;
        k++;
    }

    while (j < rLen) {
        arr[k] = rArr[j];
        j++;
        k++;
    }
}

public static void main(String[] args) {
    int[] arr = {38, 27, 43, 3, 9, 82, 10};
    mergeSort(arr, 0, arr.length - 1);
    for (int num : arr) {
        System.out.print(num + " ");
    }
}
}

```

## Quick Sort

6 5 3 1 8 7 2 4

Time Complexity:

Best Case  $O(n \log n)$

Average Case:  $O(n \log n)$

Worst Case  $O(n^2)$

Space Complexity:

Best/Average Case  $O(\log n)$  (in-place)

Worst Case  $O(n)$  (due to recursion stack in the worst case scenario)

## Standard Solution

```
public class QuickSort {
    public static void quickSort(int[] arr, int low, int high) {
        if (low < high) {
            int pi = partition(arr, low, high);
            quickSort(arr, low, pi - 1);
            quickSort(arr, pi + 1, high);
        }
    }

    public static int partition(int[] arr, int low, int high) {
        int pivot = arr[high];
        int i = (low - 1);
        for (int j = low; j < high; j++) {
            if (arr[j] < pivot) {
                i++;
                int temp = arr[i];
                arr[i] = arr[j];
                arr[j] = temp;
            }
        }
        int temp = arr[i + 1];
        arr[i + 1] = arr[high];
        arr[high] = temp;
        return i + 1;
    }

    public static void main(String[] args) {
        int[] arr = {10, 7, 8, 9, 1, 5};
        int n = arr.length;
        quickSort(arr, 0, n - 1);
        for (int num : arr) {
            System.out.print(num + " ");
        }
    }
}
```

## Merge k Sorted Lists

You are given an array of **k** linked-lists **lists**, each linked-list is sorted in ascending order. Merge all the linked-lists into one sorted linked-list and return it.

Example 1:

Input: lists = [[1,4,5],[1,3,4],[2,6]]

Output: [1,1,2,3,4,4,5,6]

Explanation: The linked-lists are:

```
[
  1->4->5,
  1->3->4,
  2->6
]
```

merging them into one sorted list:

1->1->2->3->4->4->5->6

Example 2:

Input: lists = []

Output: []

Example 3:

Input: lists = [[]]

Output: []

Constraints:

- $k == \text{lists.length}$
- $0 \leq k \leq 104$
- $0 \leq \text{lists}[i].\text{length} \leq 500$
- $-104 \leq \text{lists}[i][j] \leq 104$
- $\text{lists}[i]$  is sorted in ascending order.
- The sum of  $\text{lists}[i].\text{length}$  will not exceed 104.

## Previous Solution

```
class Solution {
    public ListNode mergeKLists(ListNode[] lists) {
        //A. check lists
        if(lists.length==0)return new ListNode();
        if(lists.length==1)return lists[0];
        //A. public data
        ListNode firstMergeListNode=lists[0];
        ListNode mergeListNode=lists[0];

        //A. traverse lists(level 1)
        for(int i=1; i<lists.length; i++){
            ListNode currentListNode=lists[i];
            //B. traverse linked-list(level 2)
            while(currentListNode!=null){
                //C. public data
                ListNode nextMergeListNode=mergeListNode.next; //nullable
                ListNode nextCurrentListNode=currentListNode.next; //nullable
                //C. merge currentListNode into mergeListNode
                if(
                    mergeListNode.next!=null
                    &&currentListNode.val>=mergeListNode.val
                    &&currentListNode.val<nextMergeListNode.val
                    ||mergeListNode.next==null
                    &&currentListNode.val>=mergeListNode.val){
                    //D. merge node
                    mergeListNode.next=currentListNode;
                    currentListNode.next=nextMergeListNode;
                }
            }
        }
    }
}
```

```

        currentListNode=nextCurrentListNode;
    }
}
return mergeListNode;
}
}

```

## Standard Solution

```

public ListNode mergeTwoLists(ListNode a, ListNode b) {
    //A. check lists
    if (a == null || b == null) {
        return a != null ? a : b;
    }
    //A. public data
    ListNode head = new ListNode(0); // create a new linked list
    ListNode tail = head, aPtr = a, bPtr = b;
    //A. traverse linked List a and b
    while (aPtr != null && bPtr != null) {
        //B. append aPtr with the small value to the tail end
        if (aPtr.val < bPtr.val) {
            tail.next = aPtr;
            aPtr = aPtr.next;
        }
        //B. append bPtr with the small value to the tail end
        else {
            tail.next = bPtr;
            bPtr = bPtr.next;
        }
        tail = tail.next;
    }
    tail.next = (aPtr != null ? aPtr : bPtr);
    return head.next;
}

```

### Skip List

#### Design Skiplist

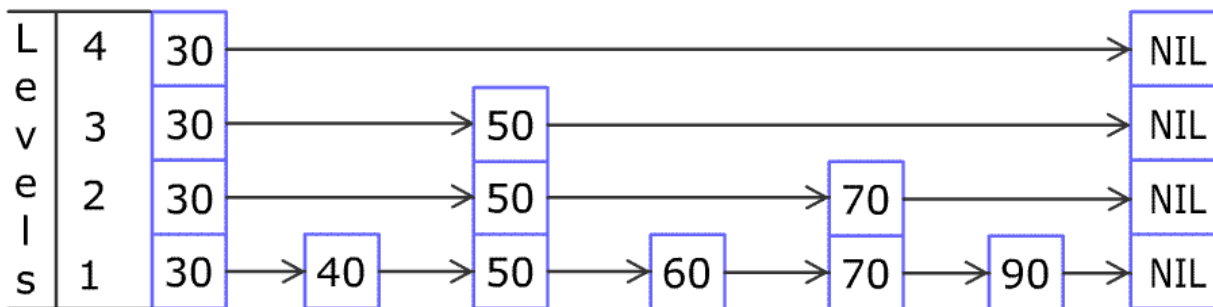
Design a Skiplist without using any built-in libraries.

A skiplist is a data structure that takes  $O(\log(n))$  time to add, erase and search.

Comparing with treap and red-black tree which has the same function and performance, the code length of Skiplist can be comparatively short and the idea behind Skiplists is just simple linked lists.

For example, we have a Skiplist containing [30,40,50,60,70,90] and we want to add 80 and 45 into it.

The Skiplist works this way:



Artyom Kalinin [CC BY-SA 3.0], via [Wikimedia Commons](#)

You can see there are many layers in the Skiplist. Each layer is a sorted linked list.

With the help of the top layers, add, erase and search can be faster than  $O(n)$ .

It can be proven that the average time complexity for each operation is  $O(\log(n))$  and space complexity is  $O(n)$ .

See more about Skiplist: [https://en.wikipedia.org/wiki/Skip\\_list](https://en.wikipedia.org/wiki/Skip_list)

Implement the Skiplist class:

- **Skiplist()** Initializes the object of the skiplist.
- **bool search(int target)** Returns **true** if the integer **target** exists in the Skiplist or **false** otherwise.
- **void add(int num)** Inserts the value **num** into the SkipList.
- **bool erase(int num)** Removes the value **num** from the Skiplist and returns **true**.

If **num** does not exist in the Skiplist, do nothing and return **false**.

If there exist multiple **num** values, removing any one of them is fine.

Note that duplicates may exist in the Skiplist, your code needs to handle this situation.

#### Example 1:

##### Input

```
["Skiplist", "add", "add", "add", "search", "add", "search", "erase", "erase", "search"]  
[[], [1], [2], [3], [0], [4], [1], [0], [1], [1]]
```

##### Output

```
[null, null, null, null, false, null, true, false, true, false]
```

##### Explanation

```
Skiplist skiplist = new Skiplist();  
skiplist.add(1);  
skiplist.add(2);  
skiplist.add(3);  
skiplist.search(0); // return False  
skiplist.add(4);  
skiplist.search(1); // return True  
skiplist.erase(0); // return False, 0 is not in skiplist.  
skiplist.erase(1); // return True  
skiplist.search(1); // return False, 1 has already been erased.
```

#### Constraints:

- $0 \leq \text{num}, \text{target} \leq 2 * 10^4$
- At most  $5 * 10^4$  calls will be made to search, add, and erase.

## Previous Solution

```
class Skiplist {  
  
    private class ListNode {  
        private int value;  
        private ListNode left;  
        private ListNode right;  
  
        public ListNode(int value){  
            this.value=value;  
        }  
    }  
    private ListNode root;  
  
    public Skiplist() {  
  
    }  
  
    public boolean search(int target) {  
        ListNode curNode=root;  
        while(curNode!=null){  
            if(target<curNode.value){  
                curNode=curNode.left;  
            }  
        }  
        return curNode!=null && curNode.value==target;  
    }  
}
```

```

        }else if(target>curNode.value){
            curNode=curNode.right;
        }else{
            return true;
        }
    }
    return false;
}

public void add(int num) {
    if(root==null){
        root=new ListNode(num);
        return;
    }
    ListNode curNode=root;
    while(curNode!=null){
        if(num<curNode.value){
            if(curNode.left==null){
                curNode.left=new ListNode(num);
                break;
            }
            curNode=curNode.left;
        }else{
            if(curNode.right==null){
                curNode.right=new ListNode(num);
                break;
            }
            curNode=curNode.right;
        }
    }
}

}

public boolean erase(int num) {
    ListNode curNode=root;
    ListNode preNode=null;
    boolean left=false;
    while(curNode!=null){
        if(num<curNode.value){
            preNode=curNode;
            curNode=curNode.left;
            left=true;
        }else if(num>curNode.value){
            preNode=curNode;
            curNode=curNode.right;
            left=false;
        }else{
            if(preNode!=null) {
                if(left){
                    ListNode leftBranch=curNode.left;
                    preNode.left=curNode.right;
                    while(curNode!=null){
                        if(curNode.left==null){
                            curNode.left=leftBranch;
                        }
                        curNode=curNode.left;
                    }
                }
                else {
                    ListNode rightBranch=curNode.right;
                    preNode.left=curNode.right;
                    while(curNode!=null){
                        if(curNode.right==null){
                            curNode.right=rightBranch;
                        }
                        curNode=curNode.right;
                    }
                }
            }
        }
    }
}

```



```

        }
    }else{
        return false;
    }
}
}
return false;
}
}

/**
 * Your Skiplist object will be instantiated and called as such:
 * Skiplist obj = new Skiplist();
 * boolean param_1 = obj.search(target);
 * obj.add(num);
 * boolean param_3 = obj.erase(num);
 */

```

## Standard Solution

```

class SkiplistNode {
    int val;
    SkiplistNode[] forward;

    public SkiplistNode(int val, int maxLevel) {
        this.val = val;
        this.forward = new SkiplistNode[maxLevel];
    }
}

class Skiplist {
    static final int MAX_LEVEL = 32;
    static final double P_FACTOR = 0.25;
    private SkiplistNode head;
    private int level;
    private Random random;

    public Skiplist() {
        this.head = new SkiplistNode(-1, MAX_LEVEL);
        this.level = 0;
        this.random = new Random();
    }

    public boolean search(int target) {
        SkiplistNode curr = this.head;
        //A. Traverse the curr.forward list.
        for (int i = level - 1; i >= 0; i--) {
            //B. Find the element at level i that is smaller than and closest to target.
            while (curr.forward[i] != null && curr.forward[i].val < target) {
                curr = curr.forward[i];
            }
        }
        curr = curr.forward[0];
        //A. Check whether the value of the current element is equal to target.
        if (curr != null && curr.val == target) {
            return true;
        }
        return false;
    }

    public void add(int num) {
        SkiplistNode[] update = new SkiplistNode[MAX_LEVEL]; // a list of nodes with a maximum level.
        Arrays.fill(update, head);
        SkiplistNode listHead = this.head;
        //A[IMP]. step 1(do nothing).
        // update:
        //   H           H           H           H           update
    }
}

```

```

// x x x x   x x x x   x x x x   x x x x   lists with the maximum level.
for (int i = level - 1; i >= 0; i--) { // the previous level or 0
    //A[IMP]. step 2.1 ("update" list) (the value is greater than num).
    //   H       H       H       H
    // N N N x   N N N x   N N N x   N N N x

    //           sep 2.2 ("update" list, head) (the value is less than num).
    //   N       N       N       N
    // x x x x   x x x x   x x x x   x x x x
    // head = N
    while (listHead.forward[i] != null && listHead.forward[i].val < num) {
        listHead = listHead.forward[i];
    }
    update[i] = listHead;
}
int lv = randomLevel();
level = Math.max(level, lv);
//A. update level.
SkiplistNode newNode = new SkiplistNode(num, lv); //The current node with a random maximum level.
for (int i = 0; i < lv; i++) {
    //B[IMP]. step 1 ("update" list, new node) (level is a maximum random Level).
    // new Node:
    //   N
    // x x x

    // update:
    //   H       H       H       H
    // N N N x   N N N x   N N N x   N N N x

    //B[IMP]. step 2.1 ("update" list, new node) (the value is greater than num)
    // new Node:
    //   0
    // N N N

    //   H       H       H       H
    // 0 0 0 x   0 0 0 x   0 0 0 x   0 0 0 x

    //           sep 2.2 ("update" list, new node) (the value is less than num)
    // new Node:
    //   0
    // x x x

    //   N       N       N       N
    // 0 0 0 x   0 0 0 x   0 0 0 x   0 0 0 x
    // head = N
    newNode.forward[i] = update[i].forward[i];
    update[i].forward[i] = newNode;
}
}

public boolean erase(int num) {
    SkiplistNode[] update = new SkiplistNode[MAX_LEVEL];
    SkiplistNode curr = this.head;
    for (int i = level - 1; i >= 0; i--) {
        /* 找到第 i 层小于且最接近 num 的元素*/
        while (curr.forward[i] != null && curr.forward[i].val < num) {
            curr = curr.forward[i];
        }
        update[i] = curr;
    }
    curr = curr.forward[0];
    /* 如果值不存在则返回 false */
    if (curr == null || curr.val != num) {
        return false;
    }
    for (int i = 0; i < level; i++) {
        if (update[i].forward[i] != curr) {

```

```

        break;
    }
    /* 对第 i 层的状态进行更新, 将 forward 指向被删除节点的下一跳 */
    update[i].forward[i] = curr.forward[i];
}
/* 更新当前的 level */
while (level > 1 && head.forward[level - 1] == null) {
    level--;
}
return true;
}

private int randomLevel() {
    int lv = 1;
    /* 随机生成 lv */
    while (random.nextDouble() < P_FACTOR && lv < MAX_LEVEL) {
        lv++;
    }
    return lv;
}
}

```

### Best Meeting Point

Given an  $m \times n$  binary grid `grid` where each 1 marks the home of one friend, return *the minimal total travel distance*.

The **total travel distance** is the sum of the distances between the houses of the friends and the meeting point.

The distance is calculated using **Manhattan Distance**, where  $\text{distance}(p1, p2) = |p2.x - p1.x| + |p2.y - p1.y|$ .

#### Example 1:

1	0	0	0	1
0	0	0	0	0
0	0	1	0	0

**Input:** `grid = [[1,0,0,0,1],[0,0,0,0,0],[0,0,1,0,0]]`

**Output:** 6

**Explanation:** Given three friends living at (0,0), (0,4), and (2,2).

The point (0,2) is an ideal meeting point, as the total travel distance of  $2 + 2 + 2 = 6$  is minimal.

So return 6.

#### Example 2:

**Input:** `grid = [[1,1]]`

**Output:** 1

#### Constraints:

- $m == \text{grid.length}$
- $n == \text{grid}[i].\text{length}$
- $1 \leq m, n \leq 200$

- `grid[i][j]` is either 0 or 1.
- There will be **at least two** friends in the grid.

## Previous Solution

### Largest Values From Labels

You are given  $n$  item's value and label as two integer arrays `values` and `labels`. You are also given two integers `numWanted` and `useLimit`.

Your task is to find a subset of items with the **maximum sum** of their values such that:

- The number of items is **at most** `numWanted`.
- The number of items with the same label is **at most** `useLimit`.

Return the maximum sum.

#### Example 1:

**Input:** `values = [5,4,3,2,1]`, `labels = [1,1,2,2,3]`, `numWanted = 3`, `useLimit = 1`

Output: 9

Explanation:

The subset chosen is the first, third, and fifth items with the sum of values  $5 + 3 + 1$ .

#### Example 2:

**Input:** `values = [5,4,3,2,1]`, `labels = [1,3,3,3,2]`, `numWanted = 3`, `useLimit = 2`

Output: 12

Explanation:

The subset chosen is the first, second, and third items with the sum of values  $5 + 4 + 3$ .

#### Example 3:

**Input:** `values = [9,8,8,7,6]`, `labels = [0,0,0,1,1]`, `numWanted = 3`, `useLimit = 1`

Output: 16

Explanation:

The subset chosen is the first and fourth items with the sum of values  $9 + 7$ .

#### Constraints:

- $n == \text{values.length} == \text{labels.length}$
- $1 \leq n \leq 2 \cdot 10^4$
- $0 \leq \text{values}[i], \text{labels}[i] \leq 2 \cdot 10^4$
- $1 \leq \text{numWanted}, \text{useLimit} \leq n$

## Previous Solution

```
class Solution {
    public int largestValsFromLabels(int[] values, int[] labels, int numWanted, int useLimit) {
        //A. sort values.
        for(int i=0; i<values.length; i++){
            for(int j=i+1; j<values.length; j++){
                if(values[j]<values[i]){
                    int temp1=values[i];
                    values[i]=values[j];
                    values[j]=temp1;
                    int temp2=labels[i];
                    labels[i]=labels[j];
                    labels[j]=temp2;
                }
            }
        }
        //A. save the number of labels.
        Map<Integer, Integer> labelCountMap=new HashMap();
```

```

int sum=0;
for(int i=values.length-1; i>=0 && numWanted>0; i--){
    int curLabel=labels[i];
    labelCountMap.compute(curLabel, (key, val)->val!=null?val+1: 1 );
    if(labelCountMap.get(curLabel)>useLimit)continue;
    sum+=values[i];
    numWanted--;
}
return sum;
}
}

```

## Standard Solution

```

class Solution {
    public int largestValsFromLabels(int[] values, int[] labels, int numWanted, int useLimit) {
        int n = values.length;
        Integer[] ids = new Integer[n];
        //A. initialize ids.
        for (int i = 0; i < n; i++) {
            ids[i] = i;
        }
        //A. sort ids (Keep the order of the value array unchanged and save the order with the ids array).
        Arrays.sort(ids, (a, b) -> values[b] - values[a]);
        int ans = 0, choose = 0;
        Map<Integer, Integer> cnt = new HashMap<Integer, Integer>();
        for (int i = 0; i < n && choose < numWanted; ++i) {
            int label = labels[ids[i]];
            if (cnt.getOrDefault(label, 0) == useLimit) {
                continue;
            }
            ++choose;
            ans += values[ids[i]];
            cnt.put(label, cnt.getOrDefault(label, 0) + 1);
        }
        return ans;
    }
}

```

TEMP