

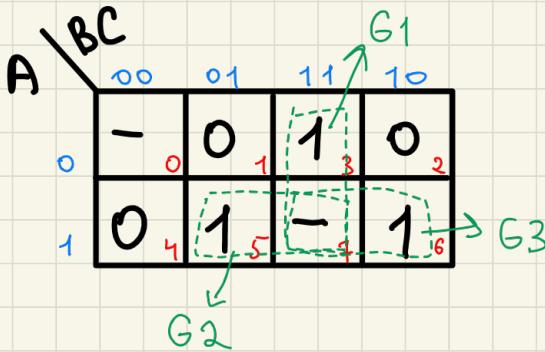
# LAB 4

Question 1.

a)

$$F(A, B, C) = \sum m (3, 5, 6)$$

$$d(A, B, C) = \sum m (0, 7)$$



$$G_1 = BC$$

$$G_2 = AC$$

$$G_3 = AB$$

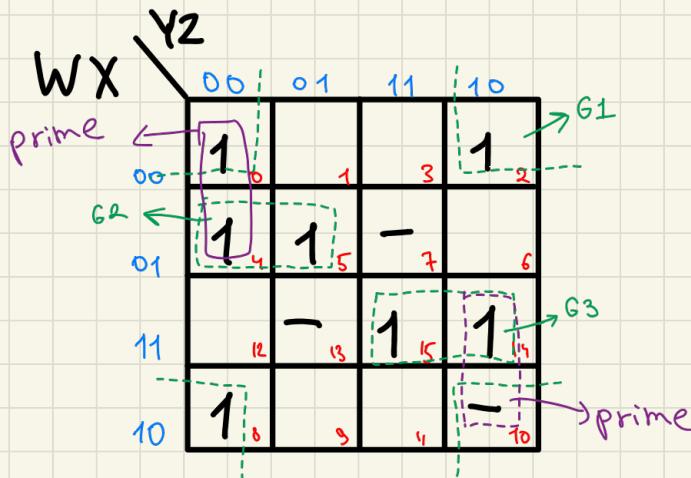
Prime implicants: BC, AC, AB

Essential prime implicants: BC, AC, AB

$$F = BC + AC + AB$$

b)  $F(W, X, Y, Z) = \sum m(0, 2, 4, 5, 8, 14, 15)$

$d(W, X, Y, Z) = \sum m(7, 10, 13)$



$$G_1 = X'Z' \quad G_2 = W'X'Y' \quad G_3 = WXY$$

Prime Implicants:  $X'Z'$ ,  $W'X'Y'$ ,  $WXY$ ,  $W'Y'Z'$ ,  $WYZ'$

Essential prime imp:  $X'Z'$ ,  $W'X'Y'$ ,  $WXY$

$$\underline{F = X'Z' + W'X'Y' + WXY}$$

Question 2.

a)  $F(W, X, Y, Z) = \sum m(5, 6, 11, 12)$

$$d(W, X, Y, Z) = \sum m(0, 1, 2, 9, 10, 14, 15)$$

W X Y Z

	00	01	11	10
00	-	-	0	-
01	0	1	0	1
11	1	0	-	-
10	0	-	1	-

G4 → 00, 01, 11  
G2 → 10  
G3 → 01, 11  
G1 → 10

$$G_1 = WY \quad G_2 = YZ' \quad G_3 = WXZ' \quad G_4 = W'Y'Z$$

$$F = WY + YZ' + WXZ' + W'Y'Z$$


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b)

W X Y Z

	00	01	11	10
00	-	-	0	-
01	0	1	0	1
11	1	0	-	-
10	0	-	1	-

G3 → 00, 01, 11  
G1 → 10  
G2 ← 00  
G4 → 10

$$G_1 = X + Z \quad G_2 = W + Y + Z$$

$$G_3 = W + Y' + Z' \quad G_4 = W' + X' + Z'$$

$$F = (X+Z)(W+Y+Z)(W+Y'+Z')(W'+X'+Z')$$

### Question 3

$$T_1 = B'C$$

$$T_2 = A'B$$

$$T_3 = A + T_1$$

$$T_4 = D \oplus T_2'$$

$$F = T_3 + T_4$$

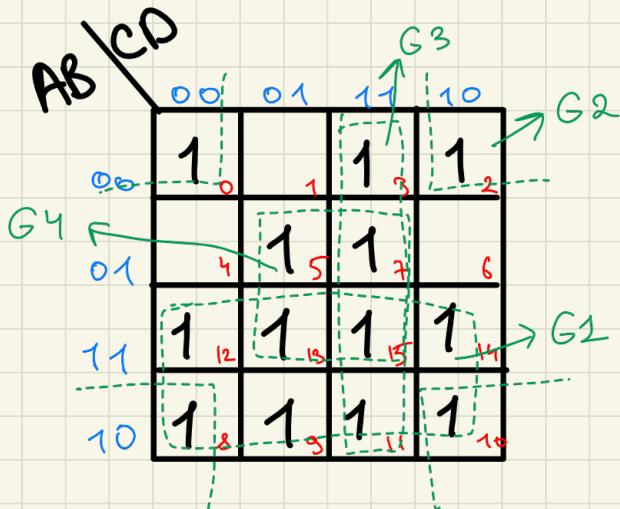
$$G = D' + T_2$$

A	B	C	D	T1	T2	T3	T4	F	G
0	0	0	0	0	0	0	1	1	1
0	0	0	1	0	0	0	0	0	0
0	0	1	0	1	0	1	1	1	1
0	0	1	1	1	0	1	0	1	0
0	1	0	0	0	1	0	0	0	1
0	1	0	1	0	1	0	1	1	1
0	1	1	0	0	1	0	0	0	1
0	1	1	1	0	1	0	1	1	1
1	0	0	0	0	0	1	1	1	1
1	0	0	1	0	0	1	0	1	0
1	0	1	0	1	0	1	1	1	1
1	0	1	1	1	0	1	0	1	0
1	1	0	0	0	0	1	1	1	1
1	1	0	1	0	0	1	0	1	0
1	1	1	0	0	0	1	1	1	1
1	1	1	1	0	0	1	0	1	0

# Question 4

K-map for F

$$F = \sum m(0, 2, 3, 5, 7, 8, 9, 10, 11, 12, 13, 14, 15)$$



$$G_1 = A \quad G_2 = B'D' \quad G_3 = CD \quad G_4 = BD$$

$$\underline{F = A + B'D' + CD + BD}$$

K-map for G

$$G = \sum m(0, 2, 4, 5, 6, 7, 8, 10, 12, 14)$$

AB'CD

	00	01	11	10
00	1 0	1	3	1 2
01	1 4	1 5	1 7	1 8
11	1 6		15	1 14
10	1 9	3	11	1 16

G1 → 1  
G2 → 1

$$G_1 = D'$$

$$G_2 = A'B$$

$$\underline{G = D' + A'B}$$

Question 5

$$F = T3 + T4$$

$\underbrace{4+4+1}_{9 \text{ literals}}$

$$A + B'D' + CD + BD$$

$\underbrace{\quad\quad\quad}_{8 \text{ literals}}$

$$G = D' + T2$$

$\underbrace{1+2+1}_{4 \text{ literals}}$

$$D' + A'B$$

$\underbrace{\quad\quad\quad}_{4 \text{ literals}}$

for G

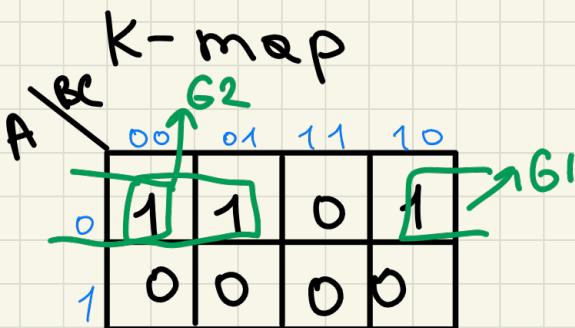
Ans: for F it is simpler, it is same

# Question 6

a)

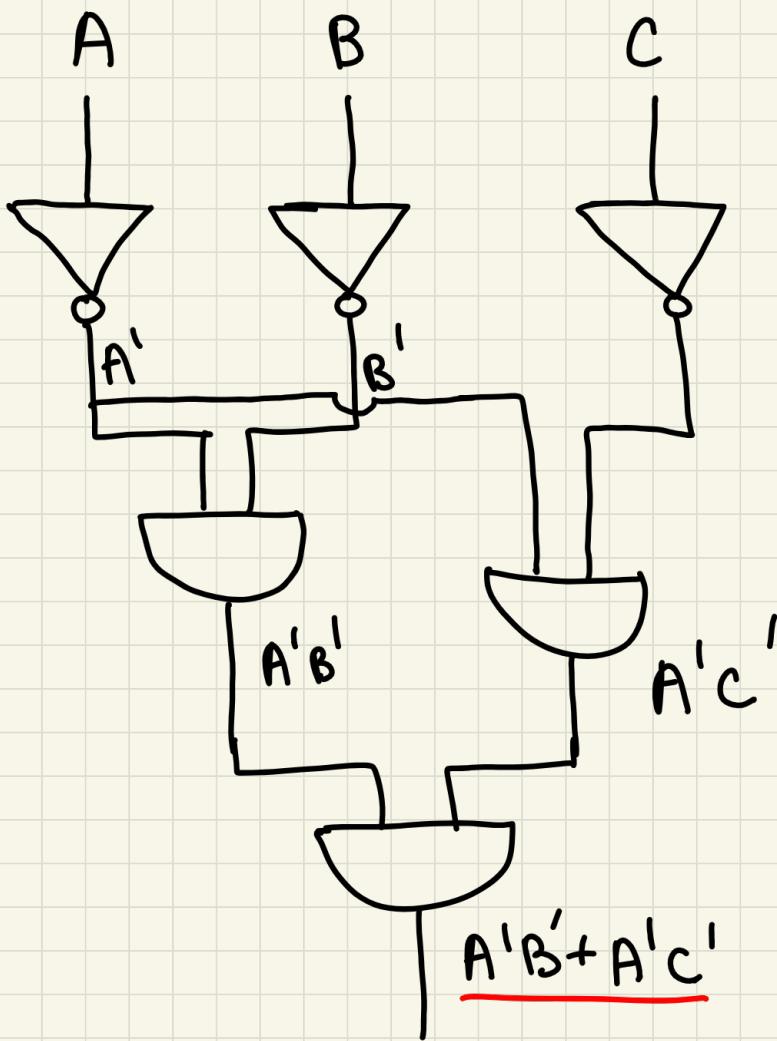
A	B	C	D	F
0	0	0	0	1
0	0	0	1	1
0	1	0	2	1
1	1	1	3	0
1	0	0	4	0
1	1	1	5	0
1	1	0	6	0
1	1	1	7	0

$$F = \sum m(0, 1, 2)$$



$$G1 = A' C' \quad G2 = A' B'$$

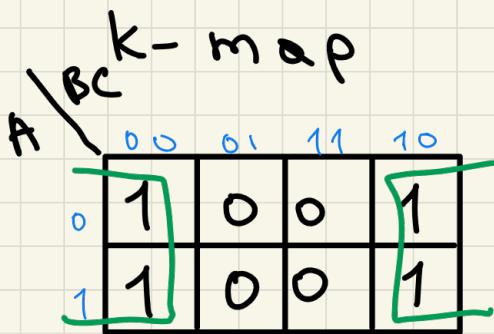
$$F = A' C' + A' B'$$



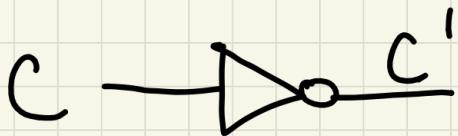
b)

A	B	C	D	F
0	0	0	0	1
0	0	1	1	0
0	1	0	2	1
1	1	1	3	0
1	0	0	4	1
1	0	1	5	0
1	1	0	6	1
1	1	1	7	0

$$F = \sum m(0, 2, 4, 6)$$

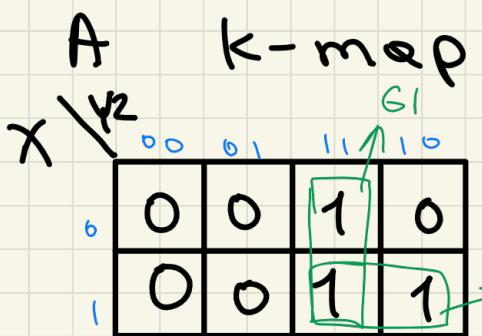


$$\text{Group} = C'$$



Question 7

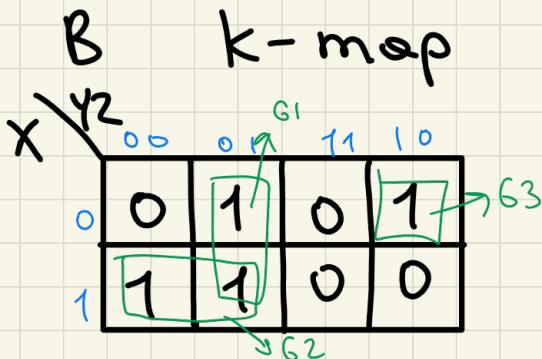
X	Y	Z	D <sub>in</sub>	D <sub>out</sub>	A	B	C
0	0	0	0	1	0	0	1
0	0	1	1	2	0	1	0
0	1	0	2	3	0	1	1
1	1	1	3	4	1	0	0
1	0	1	4	5	0	1	1
1	1	0	5	6	1	0	0
1	1	1	6	7	1	1	0



$$G1 = YZ$$

$$G2 = XY$$

$$A = YZ + XY$$

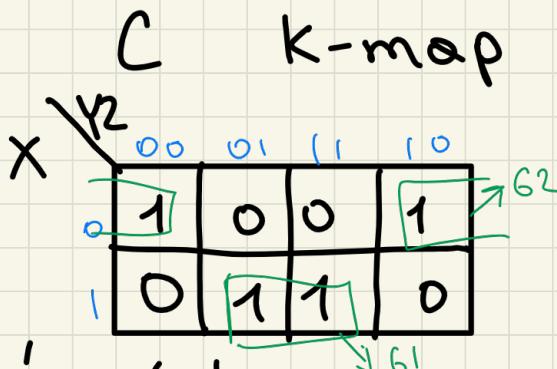


$$G1 = Y'Z$$

$$G2 = XY'$$

$$G3 = X'Y2'$$

$$B = Y'Z + XY' + X'Y2'$$

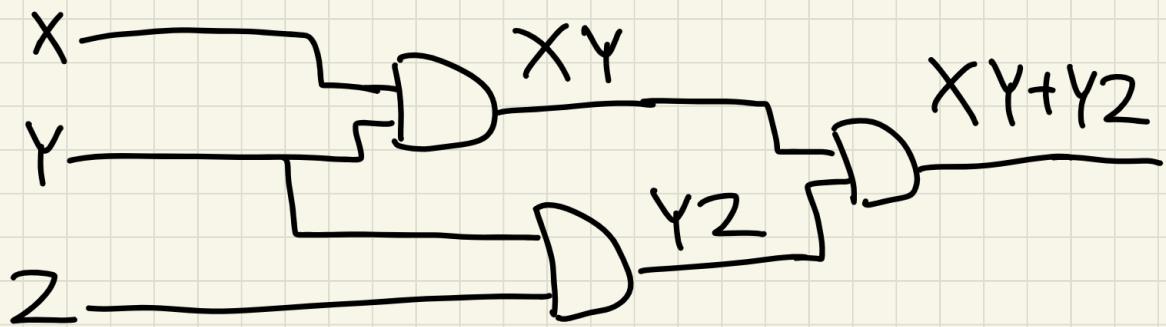


$$G1 = XZ$$

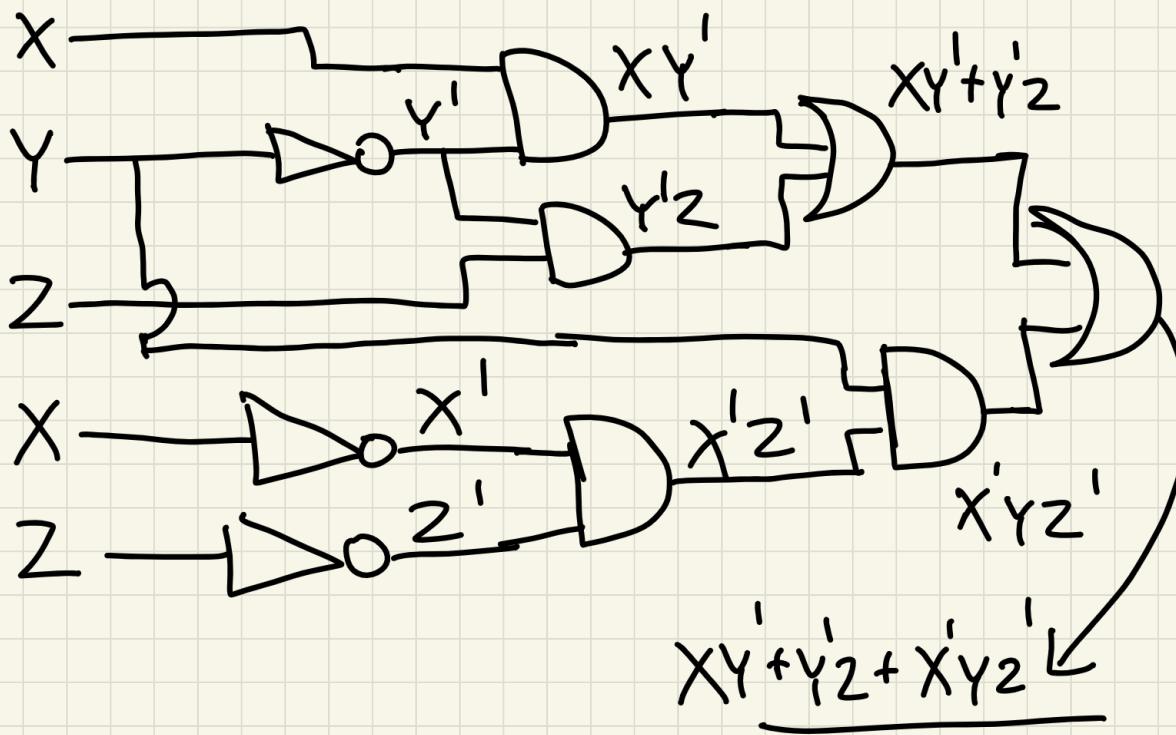
$$G2 = X'Z'$$

$$C = XZ' + X'Z'$$

$$A = XY + YZ$$



$$B = XY' + Y'Z + X'YZ'$$



$$C = XZ + X'Z'$$

