

January 8, 2026

Base 2, 8, 16

$$\begin{array}{cccccccccccc} & 7 & 6 & 5 & 4 & 3 & 2 & 1 & 0 & & & & & \\ \text{Binary } (11111111) & \rightarrow & (& & & & & &) & & & & & \\ & & & & & & & & & & & & & \end{array}$$
$$1 \cdot 2^7 + 1 \cdot 2^6 + 1 \cdot 2^5 + 1 \cdot 2^4 + 1 \cdot 2^3 + 1 \cdot 2^2 + 1 \cdot 2^1 + 1 \cdot 2^0$$
$$= 128 + 64 + 32 + 16 + 8 + 4 + 2 + 1 =$$
$$= 255_{10}$$

$$\begin{array}{ccccccc} & 2 & 1 & 0 & & & \\ (377)_8 & = & 3 \cdot 8^2 & + & 7 \cdot 8^1 & + & 7 \cdot 8^0 & = & 255_{10} \end{array}$$

$$\begin{array}{ccccccc} & 1 & 0 & & & & \\ (FF)_{16} & \rightarrow & (& & & &)_{10} \end{array}$$

base 16:

$$16^{\overset{1}{F}} + 16^{\circ F} = 16 \cdot 15 + 15 = 255_{10}$$

Decimal $()_{10}$ \rightarrow $()_2$
 $()_{10} \rightarrow ()_8$
 $()_{10} \rightarrow ()_{16}$

10
11
12
13
14
15
A
B
C
D
E
F

HEX

$$\begin{array}{r}
 255 \mid 2 \\
 \hline
 254 \mid 127 \mid 2 \\
 \hline
 126 \mid 63 \mid 2 \\
 \hline
 62 \mid 31 \mid 2 \\
 \hline
 30 \mid 15 \mid 2 \\
 \hline
 14 \mid 7 \mid 2 \\
 \hline
 6 \mid 3 \mid 2 \\
 \hline
 2 \mid 1 \\
 \hline
 \end{array}$$

$255_{10} = 1111111_2$
 (A blue arrow points from the bottom of the binary representation to the first remainder '1' in the division process.)

114₁₀

$$\begin{array}{r|l} 114 & 2 \\ \hline 114 & 57 \\ \hline 0 & 56 \\ & 28 \\ & 14 \\ & 7 \\ & 3 \\ & 1 \end{array}$$

1110010₂

$$(0.12)_{10} \rightarrow ()_2 = (.000111)_2$$

$0.12 \times 2 = 0.24$	0	just fraction ↓
$0.24 \times 2 = 0.48$	0	
$0.48 \times 2 = 0.96$	0	
$0.96 \times 2 = 1.92$	1	
$0.92 \times 2 = 1.84$	1	
$0.84 \times 2 = 1.68$	1	

Dec.	Binary	Dec.	Binary
1	0001	9	1001
2	0010	10	1010
3	0011	11	1011
4	0100	12	1100
5	0101	13	1101
6	0110	14	1110
7	0111	15	1111
8	1000		

A B C D E F
Hex.

Binary addition

$$\begin{array}{r}
 \times \quad 01100 \\
 \quad 10001 \\
 \hline
 \quad 11101
 \end{array}$$

$$\begin{array}{r}
 \overset{1}{+} \overset{1}{1} \overset{1}{0} \overset{1}{1} 1 0 \\
 1 0 1 1 1 \\
 \hline
 \underline{1} [0 1 1 0 1]
 \end{array}$$

$$(1)_2 + (1)_2 = (10)_2$$

$$(\overset{1}{1}0)_2 + (1)_2 = (11)_2$$

It is overflow, machine should know that it is overflow

Binary subtraction

$$\begin{array}{r}
 \overset{0}{-} \overset{0}{0} \\
 \hline
 0
 \end{array}
 \quad
 \begin{array}{r}
 \overset{1}{-} \overset{1}{1} \\
 \hline
 0
 \end{array}
 \quad
 \begin{array}{r}
 \overset{1}{-} \overset{0}{0} \\
 \hline
 1
 \end{array}
 \quad
 \begin{array}{r}
 \overset{0}{-} \overset{1}{1} \\
 \hline
 1
 \end{array}$$

$$\begin{array}{r}
 - 10110 \\
 10010 \\
 \hline
 00100
 \end{array}$$

$$\begin{array}{r}
 - 10110 \\
 10011 \\
 \hline
 00011
 \end{array}$$

1's complement

logic operation

$$(10101111)_2$$

1's complement is inverse of digits

$$(01010000)_2 \text{ 1's comp.}$$

$$(01010001)_2 \text{ 2's complement}$$

$$(0101)_2 = (5)_{10}$$

January 13, 2026

$(r-1)$'s r 's complements

radix = base

$$r=10 \quad L=4 \quad N=2468 \quad r^4=10000$$

$$r^4 - 1 = 9999$$

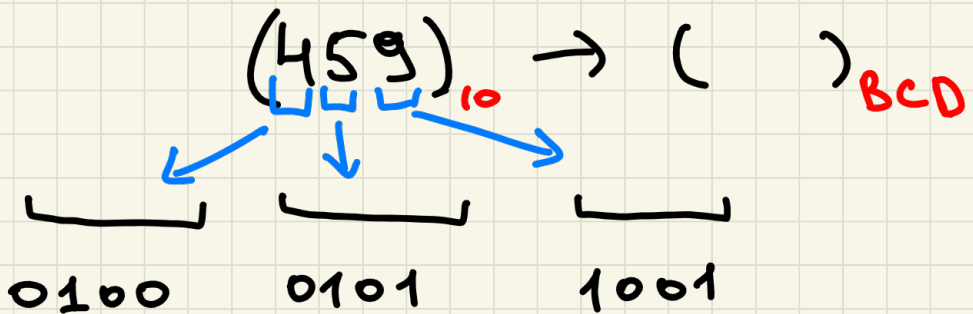
Therefore

$$\begin{array}{r} 9999 \\ - 2468 \\ \hline \underline{7531} \end{array}$$

Decimal $(185)_{10}$

Binary $(10111001)_2$

Binary Coded Decimal BCD



$$4_{10} + 8_{10} = 12_{10}$$

BCD range
(0-9)

$$0100_2 + 1000_2 = 1100_2 \rightarrow 12_{10}$$

$$0110_2 \rightarrow 6_{10}$$

$(\underline{0001} \underline{0010})_{BCD}$

$$\begin{array}{r}
 + 162 \\
 769 \\
 \hline
 931
 \end{array}$$

Binary Coded Decimal

$$\begin{array}{r}
 0001 \quad 0110 \quad 0010 \\
 0111 \quad 0110 \quad 1001 \\
 \hline
 \end{array}$$

$$\begin{array}{r}
 1000 \quad \underline{1100} \quad \underline{1011} \\
 \text{doesn't exist in BCD} \quad \text{more than 9} \\
 \text{to solve add } 6_{10}
 \end{array}$$

$$\begin{array}{r}
 0110 \quad 0110 \\
 \hline
 \underline{1001} \quad \underline{0011} \quad \underline{0001} \\
 9 \quad 3 \quad 1
 \end{array}$$

encoding \rightarrow public UTF-8
 encryption \rightarrow special key

BOOLEAN LOGIC

$$A+B \rightarrow A \text{ or } B$$

$$A.B \rightarrow A \text{ and } B$$

$$A', \bar{A} \rightarrow \text{NOT } A$$

inputs

A	B	$A \cdot B$	$A + B$	A'	B'
0	0	0	0	1	1
0	1	0	1	1	0
1	0	0	1	0	1
1	1	1	1	0	0