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TCSS381: Computer Security

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## Lab 2: RSA Public-Key Encryption and Signature Lab

### Task 1. Deriving the Private Key

Given code solves the first task of this lab:

```
#include <stdio.h>
#include <openssl/bn.h>
#define NBITS 128
/* printBN is a helper function: receives a char and two BIGNUMs.
   It converts the BIGNUMs to hex and prints their values after the msg.
*/
void printBN(char *msg, BIGNUM *a, BIGNUM *b) {
    char *st1 = BN_bn2hex(a);
    char *st2 = BN_bn2hex(b);
    printf("%s (%s,%s)\n", msg, st1, st2);
    OPENSSL_free(st1);
    OPENSSL_free(st2);
}
int main() {
    BN_CTX *ctx = BN_CTX_new();
    BIGNUM *p = BN_new();
    BIGNUM *q = BN_new();
    BIGNUM *e = BN_new();
    BIGNUM *n = BN_new();
    BIGNUM *phi = BN_new();
    BIGNUM *d = BN_new();
    BIGNUM *res = BN_new();
    BIGNUM *pMinusOne = BN_new();
    BIGNUM *qMinusOne = BN_new();
    /* p, q, e - arbitrary prime numbers.
       Note they are only 128 bits for simplicity - usually 512 bits
    */
    BN_hex2bn(&p, "F7E75FDC469067FFDC4E847C51F452DF");
    BN_hex2bn(&q, "E85CED54AF57E53E092113E62F436F4F");
    BN_hex2bn(&e, "0D88C3");
    // Define n as p*q
    BN_mul(n, p, q, ctx);
    // Print public key
    printBN("Public key: ", e, n);
    // Define pMinusOne as (p-1)
    BN_sub(pMinusOne, p, BN_value_one());
    // Define qMinusOne as (q-1)
    BN_sub(qMinusOne, q, BN_value_one());
    // Define phi(n) as (p-1)*(q-1)
    BN_mul(phi, pMinusOne, qMinusOne, ctx);
    // Output error and exit program if e and phi aren't relatively prime.
```

```

    BN_gcd(res, phi, e, ctx);
    if (!BN_is_one(res)) {
        printf("Improper input. e and/or phi are not relatively prime.
Exiting program.\n");
        exit(0);
    }
    /* Derive the private key given the values of e and phi.
    Store the result in d
    */
    BN_mod_inverse(d, e, phi, ctx);
    // Print the private key
    printBN("Private key", d, n);
    // Free the BIGNUM's
    BN_clear_free(p);
    BN_clear_free(q);
    BN_clear_free(e);
    BN_clear_free(n);
    BN_clear_free(res);
    BN_clear_free(phi);
    BN_clear_free(d);
    BN_clear_free(pMinusOne);
    BN_clear_free(qMinusOne);
    return 0;
}

```

[11/03/22] seed@VM:/mnt\$ gcc -o RSA\_Task1 RSA\_Task1.c -lcrypto

[11/03/22] seed@VM:/mnt\$ ./RSA\_Task1

Public keys:

(0D88C3,  
E103ABD94892E3E74AFD724BF28E78366D9676BCCC70118BD0AA1968DBB143D1)

Private keys:

(3587A24598E5F2A21DB007D89D18CC50ABA5075BA19A33890FE7C28A9B496AEB,  
E103ABD94892E3E74AFD724BF28E78366D9676BCCC70118BD0AA1968DBB143D1)

## Task 2. Encrypting a Message

Given code solves the second task of this lab:

```

#include <stdio.h>
#include <openssl/bn.h>
/* printBN is a helper function: receives a char and a BIGNUM.
    It prints the hex of the BIGNUM after the msg.
    */
void printBN(char *msg, BIGNUM *a) {
    char *st = BN_bn2hex(a);
    printf("%s %s\n", msg, st);
    OPENSSL_free(st);
}
int main() {
    BN_CTX *ctx = BN_CTX_new();
    BIGNUM *e = BN_new();
    BIGNUM *C = BN_new();
    BIGNUM *M = BN_new();

```

```

    BIGNUM *n = BN_new();
    //Same hex value of 010001 - part of the public key.
    BN_dec2bn(&e, "65537");
    // Part of the public key.
    BN_hex2bn(&n,
"DCBFFE3E51F62E09CE7032E2677A78946A849DC4CDDE3A4D0CB81629242FB1A5");
    // "A top secret!" in hex.
    BN_hex2bn(&M, "4120746f702073656372657421");

    // Store the result of the encrypted message given values e, n, and M.
    BN_mod_exp(C, M, e, n, ctx);
    // Output the encrypted message.
    printBN("Encryption result:", C);
    // Free the BIGNUM's.
    BN_clear_free(n);
    BN_clear_free(e);
    BN_clear_free(M);
    BN_clear_free(C);
    return 0;
}
[11/03/22]seed@VM:/mnt$ gcc -o RSA_Task2 RSA_Task2.c -lcrypto
[11/03/22]seed@VM:/mnt$ ./RSA_Task2
Encrypted Message:
6FB078DA550B2650832661E14F4F8D2CFAEF475A0DF3A75CACDC5DE5CFC5FADC

```

### Task 3. Decrypting a Message

Given code solves the third task of this lab:

```

#include <stdio.h>
#include <string.h>
#include <openssl/bn.h>
// hex_to_int receives a char, in hex, and returns the int value
int hex_to_int(char c) {
    int first = c / 16 - 3;
    int second = c % 16;
    int result = first*10 + second;
    if(result > 9) result--;
    return result;
}
/* hex_to_ascii is a helper function for PrintBNHex2ASCII - receives chars.
   It assumes input to be hex and returns their ASCII value as an int.
*/
int hex_to_ascii(char c, char d) {
    int high = hex_to_int(c) * 16;
    int low = hex_to_int(d);
    return high+low;
}
/* printBN is a helper function - receives a char and a BIGNUM.
   It converts the BIGNUM to hex and prints its value after the msg.
*/
void printBN(char *msg, BIGNUM *a) {

```

```

    char *st = BN_bn2hex(a);
    printf("%s %s\n", msg, st);
    OPENSSL_free(st);
}
/* printBNHex2ASCII is a helper function - receives a char and BIGNUM.
   It assumes the BIGNUM is ASCII text in hex form.
   It converts the BIGNUM to hex and then converts the result to ASCII.
   It prints the msg received followed by the ASCII value of the BIGNUM.
*/
void printBNHex2ASCII(char *msg, BIGNUM *a) {
    char *st = BN_bn2hex(a);
    printf("%s", msg);
    int length = strlen(st);
    int i;
    char buf = 0;
    for (i = 0; i < length; i++) {
        if (i % 2 != 0) {
            printf("%c", hex_to_ascii(buf, st[i]));
        } else {
            buf = st[i];
        }
    }
    printf("\n");
    OPENSSL_free(st);
}

int main() {
    BN_CTX *ctx = BN_CTX_new();
    BIGNUM *C = BN_new();
    BIGNUM *M = BN_new();
    BIGNUM *n = BN_new();
    BIGNUM *d = BN_new();
    // The public key.
    BN_hex2bn(&n,
"DCBFFE3E51F62E09CE7032E2677A78946A849DC4CDDE3A4D0CB81629242FB1A5");
    // The private key.
    BN_hex2bn(&d,
"74D806F9F3A62BAE331FFE3F0A68AFE35B3D2E4794148AACBC26AA381CD7D30D");
    // Cipher Text.
    BN_hex2bn(&C,
"8C0F971DF2F3672B28811407E2DABBE1DA0FEBBBD7C7DCB67396567EA1E2493F");
    // Decrypt the cipher text (C) given n and d, and store the result in M.
    BN_mod_exp(M, C, d, n, ctx);
    // Print the decrypted text as is.
    printBN("Decryption result (in hex):", M);
    // Print the decrypted text after a conversion to ASCII.
    printBNHex2ASCII("Decryption result (in ASCII):", M);
    // Free the BIGNUMs.
    BN_clear_free(n);
    BN_clear_free(d);
    BN_clear_free(M);
}

```

```

    BN_clear_free(C);
    return 0;
}
[11/03/22]seed@VM:/mnt$ gcc -o RSA_Task3 RSA_Task3.c -lcrypto
[11/03/22]seed@VM:/mnt$ ./RSA_Task3
Decryption result (in hex): 50617373776F72642069732064656573
Decryption result (in ASCII):Password is dees

```

#### Task 4. Signing a Message

We used the RSA encryption for signature to first get the hexadecimal representations of the two strings:

```

python -c 'print("I owe you $2000".encode("hex"))'
49206f77652079f75202432303030
python -c 'print("I owe you $3000".encode("hex"))'
49206f77652079f64520243303030

```

After running a file with following encryption code, we got the signatures of the two messages (screenshot is below the code):

```

BIGNUM* encrypt(BIGNUM* message, BIGNUM* mod, BIGNUM* pub_key) {
    BN_CTX *ctx = BN_CTX_new();
    BIGNUM* enc = BN_new();
    BN_mod_exp(enc, message, mod, pub_key, ctx);
    BN_CTX_free(ctx);
    return enc;
}

```

Signature of M1: 80A55421D72345AC199836F60D51DC9594E2BDB4  
AE20C804823FB71660DE7B82

Signature of M2: 04FC9C53ED7BBE4ED4BE2C24B0BDF7184B96290  
B4ED4E3959F58E94B1ECEA2EB

#### Task 5. Verifying a Signature

We got the hex string from the message M, which we then compiled and ran using code provided below to verify Alice's signature, which ended up being valid.

```

int verify() {
    // initialize
    BN_CTX *ctx = BN_CTX_new();
    BIGNUM *n = BN_new();
    BIGNUM *e = BN_new();
    BIGNUM *M = BN_new();
    BIGNUM *C = BN_new();
    BIGNUM *S = BN_new();
    // assign values
    BN_hex2bn(&n, "AE1CD4DC432798D933779FBD46C6E1247F0CF1233595113AA51B450F18116115");
    BN_dec2bn(&e, "65537");
    //hex encode for "Launch a missile."
    BN_hex2bn(&M, "4c61756e63682061206d697373696c652e");
}

```

```

BN_hex2bn(&S,
"643D6F34902D9C7EC90CB0B2BCA36C47FA37165C0005CAB026C0542CBDB6802F");
BN_mod_exp(C, S, e, n, ctx);
// validate the signature
if (BN_cmp(C, M) == 0) {
printf("Signature is valid!\n");
} else {
printf("Signature is invalid!\n");
}

//clear data
BN_clear_free(n);
BN_clear_free(e);
BN_clear_free(M);
BN_clear_free(C);
BN_clear_free(S);
return 0;
}

```

### Task 6. Manually Verifying an X.509 Certificate

```

#include <stdio.h>
#include <openssl/bn.h>
void printBN(char *msg, BIGNUM *a) {
    char *st = BN_bn2hex(a);
    printf("%s %s\n", msg, st);
    OPENSSL_free(st);
}

int main() {
    BN_CTX *ctx = BN_CTX_new();
    BIGNUM *n = BN_new();
    BIGNUM *e = BN_new();
    BIGNUM *S = BN_new();
    BIGNUM *M = BN_new();
    BIGNUM *C = BN_new();
    /* Values gathered from seedsecuritylabs.org via terminal and extracted
       from c1.pem using "openssl x509 -in c1.pem -noout -modulus"
    */
    BN_hex2bn(&n,
"B6E02FC22406C86D045FD7EF0A6406B27D22266516AE42409BCEDC9F9F76073EC330558719B9
4F940E5A941F5556B4C2022AAFD098EE0B40D7C4D03B72C8149EEF90B111A9AED2C8B8433AD90
B0BD5D595F540AFC81DED4D9C5F57B786506899F58ADAD2C7051FA897C9DCA4B182842DC6ADA5
9CC71982A6850F5E44582A378FFD35F10B0827325AF5BB8B9EA4BD51D027E2DD3B4233A30528C
4BB28CC9AAC2B230D78C67BE65E71B74A3E08FB81B71616A19D23124DE5D79208AC75A49CBACD
17B21E4435657F532539D11C0A9A631B199274680A37C2C25248CB395AA2B6E15DC1DDA020B82
1A293266F144A2141C7ED6D9BF2482FF303F5A26892532F5EE3");
    /* Input extracted from c1.pem using "openssl x509 -in c1.pem -text
       noout | grep Exponent"
    */
    BN_dec2bn(&e, "65537");
    /* Input extracted from c0.pem using "openssl x509 -in c0.pem -text -
       noout"
    */
}

```





[illegible]

```
[11/03/22]seed@VM:/mnt$ openssl x509 -in cl.pem -noout -modulus
Modulus=B6E02FC22406C86D045FD7EFA0A4606B27D2266516AE42409BCEDC9F9F76073EC330558719B94F940E5A941F5556B4C
222AAAF0D98EEB0407C4D03B7C78149EEF90B111A9AED2C8B843AD90B0805D595F5404FC810ED4D9CF5F7B786506899F58ADA
D2C7051FA897C9DC4A8182842D6C6ADA59CC71982A6850F5E44582A378FFD3F510B0827325AF5BB889EA4BD51D027E2D03B4233A
3052844BB28C9AAC2B230D78C678E65E71B74A3E08FB81B71616A19D23124DE5079208AC75A49CBACD17B21E4435657F53239
1D1C0A9A631B199274680A37C2D5248CB39A58E615DC1DDA020B821A293266F14A42141C7ED069BF2482F3F562892532
F5EE3
[11/03/22]seed@VM:/mnt$ openssl x509 -in cl.pem -text -noout | grep Exponent
Exponent: 65537 (0x10001)
```

```

11/03/22]seed@VM:/mnt/openssl x509 -in c1.pem -text -noout
Certificate:
    Data:
        Version: 3 (0x2)
        Serial Number:
            04:e1:e7:a4:dc:5c:f2:f3:6d:c0:2b:42:b8:5d:15:9f
        Signature Algorithm: sha256WithRSASign
        Issuer: C = US, O = DigiCert Inc, OU = www.digicert.com, CN = DigiCert High Assurance EV Root CA
        Validity
            Not Before: Oct 22 12:00:00 2013 GMT
            Not After : Oct 22 12:00:00 2028 GMT
        Subject: C = US, O = DigiCert Inc, OU = www.digicert.com, CN = DigiCert SHA2 High Assurance Server CA
        Subject Public Key Info:
            Public Key Algorithm: rsaEncryption
            RSA Public-Key: (2048 bit)
            Modulus:
                00:b6:e0:2f:c2:24:06:c8:6d:04:5f:d7:ef:0a:64:
                06:b2:7d:22:26:65:16:ae:42:40:9b:ce:dc:9f:9f:
                76:07:3e:c3:30:55:87:19:b9:4f:94:0e:5a:94:1f:
                55:56:b4:c2:02:2a:af:d0:98:ee:0b:40:d7:c4:d0:
                3b:72:c8:14:9e:ef:90:b1:11:a9:ae:d2:c8:b8:43:
                3a:d9:0b:0b:d5:d5:95:f5:40:af:c8:1d:ed:4d:9c:
                5f:57:b7:86:50:68:99:f5:8a:da:d2:c7:05:1f:a8:
                97:c9:dc:a4:b1:82:84:2d:c6:ad:a5:9c:c7:19:82:
                a6:85:0f:5e:44:58:2a:37:8f:fd:35:1f:0b:08:27:
                32:5a:f5:bb:8b:9e:a4:bd:51:0d:27:e2:dd:3b:42:
                33:a3:05:28:c4:bb:28:cc:9a:ac:2b:23:0d:78:c6:
                7b:6e:5e:71:b7:4a:3e:08:fb:61:b7:16:16:a1:8d:
                23:12:4d:e5:d7:92:08:ac:75:a4:9c:ba:cd:17:b2:
                1e:44:35:65:7f:53:25:39:d1:lc:0a:9a:63:1b:19:
                92:74:68:0a:37:c2:c2:52:48:cb:39:5a:a2:b6:e1:
                5d:cl:dd:a0:20:b8:21:a2:93:26:6f:14:4a:21:41:
                c7:ed:6d:9b:f2:48:2f:f3:03:f5:a2:68:92:53:2f:
                5e:e3
            Exponent: 65537 (0x10001)
    X509v3 extensions:
        X509v3 Basic Constraints: critical
            CA:TRUE, pathlen:0
        X509v3 Key Usage: critical
            Digital Signature, Certificate Sign, CRL Sign
        X509v3 Extended Key Usage:
            TLS Web Server Authentication, TLS Web Client Authentication
        Authority Information Access:

```



To extract the body of the server's certificate, we parsed the server's certificate:

```
[11/03/22]seed@VM:/mnt$ openssl asn1parse -i -in c0.pem
 0:d=0  hl=4  l=1840 cons: SEQUENCE
 4:d=1  hl=4  l=1560 cons: SEQUENCE
 8:d=2  hl=2  l=  3 cons: cont [ 0 ]
10:d=3  hl=2  l=  1 prim: INTEGER           :02
13:d=2  hl=2  l= 16 prim: INTEGER           :02493E07FA9E375A2DBBC61D94430FCF
31:d=2  hl=2  l= 13 cons: SEQUENCE
33:d=3  hl=2  l=  9 prim: OBJECT            :sha256WithRSAEncryption
44:d=3  hl=2  l=  0 prim: NULL
46:d=2  hl=2  l= 112 cons: SEQUENCE
48:d=3  hl=2  l= 11 cons: SET
50:d=4  hl=2  l=  9 cons: SEQUENCE
52:d=5  hl=2  l=  3 prim: OBJECT            :countryName
57:d=5  hl=2  l=  2 prim: PRINTABLESTRING :US
61:d=3  hl=2  l= 21 cons: SET
63:d=4  hl=2  l= 19 cons: SEQUENCE
65:d=5  hl=2  l=  3 prim: OBJECT            :organizationName
70:d=5  hl=2  l= 12 prim: PRINTABLESTRING :DigiCert Inc
84:d=3  hl=2  l= 25 cons: SET
86:d=4  hl=2  l= 23 cons: SEQUENCE
88:d=5  hl=2  l=  3 prim: OBJECT            :organizationalUnitName
93:d=5  hl=2  l= 16 prim: PRINTABLESTRING :www.digicert.com
111:d=3  hl=2  l= 47 cons: SET
113:d=4  hl=2  l= 45 cons: SEQUENCE
115:d=5  hl=2  l=  3 prim: OBJECT            :commonName
120:d=5  hl=2  l= 38 prim: PRINTABLESTRING :DigiCert SHA2 High Assurance Server CA
160:d=2  hl=2  l= 30 cons: SEQUENCE
162:d=3  hl=2  l= 13 prim: UTCTIME           :200506000000Z
177:d=3  hl=2  l= 13 prim: UTCTIME           :220414120000Z
192:d=2  hl=2  l= 106 cons: SEQUENCE
194:d=3  hl=2  l= 11 cons: SET
196:d=4  hl=2  l=  9 cons: SEQUENCE
198:d=5  hl=2  l=  3 prim: OBJECT            :countryName
203:d=5  hl=2  l=  2 prim: PRINTABLESTRING :US
207:d=3  hl=2  l= 19 cons: SET
209:d=4  hl=2  l= 17 cons: SEQUENCE
211:d=5  hl=2  l=  3 prim: OBJECT            :stateOrProvinceName
216:d=5  hl=2  l= 10 prim: PRINTABLESTRING :California
228:d=3  hl=2  l= 22 cons: SET
230:d=4  hl=2  l= 20 cons: SEQUENCE
232:d=5  hl=2  l=  3 prim: OBJECT            :localityName
237:d=5  hl=2  l= 13 prim: PRINTABLESTRING :San Francisco
```

```
[11/03/22]seed@VM:/mnt$ openssl asn1parse -i -in c0.pem -strparse 4 -out c0_body.bin -noout
[11/03/22]seed@VM:/mnt$ sha256sum c0_body.bin
0640f8d13c0789ff0ed5437cf4bc9f2827d52146dddf38aefc2c17747d45f28  c0_body.bin
```

Using the values obtained earlier, we ran the updated program, validating the signature:

```
[11/03/22]seed@VM:/mnt$ gcc -o RSA_Task6 RSA_Task6.c -lcrypto
[11/03/22]seed@VM:/mnt$ ./RSA_Task6
Signature is has been proven valid
```