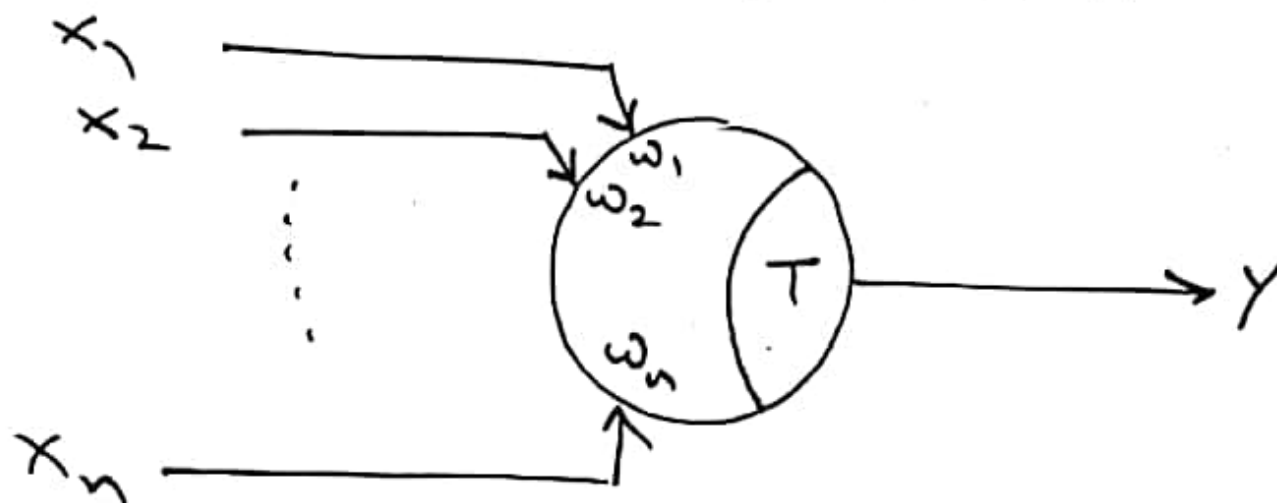


"Soft Computing"

①

* Threshold logic model



input

weight Threshold

output

$$x_1 w_1 + x_2 w_2 + \dots + x_n w_n = \sum_{i=1}^n w_i x_i$$

$$\text{if } \sum_{i=1}^n w_i x_i \geq T \quad \therefore Y=1$$

$$\text{if } \sum_{i=1}^n w_i x_i < T \quad \therefore Y=0$$



Ex = find expression for output Y for the following circuit



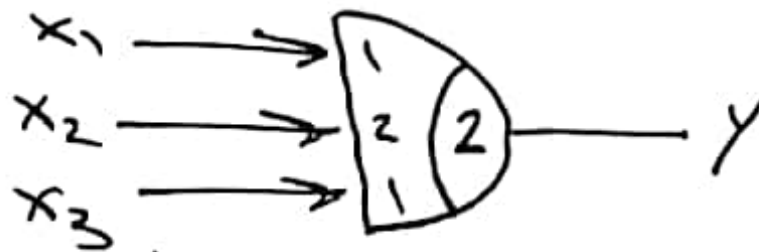
$$\text{ans } T=2 \quad \sum_{i=1}^3 w_i x_i = x_1 + 2x_2 + x_3$$

$$Y = f(x_1, x_2, x_3)$$

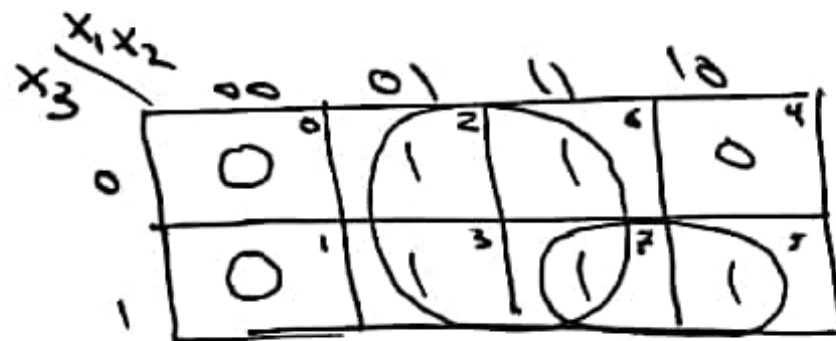
$$Y=1 \quad \text{for} \quad \sum_{i=1}^3 w_i x_i \geq 2$$

$$Y=0 \quad \text{for} \quad \sum_{i=1}^3 w_i x_i < 2$$

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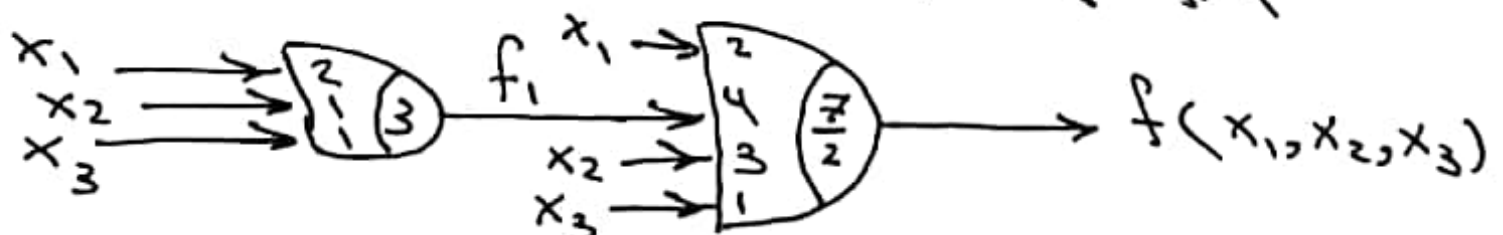
	x_1	x_2	x_3	$\sum w_i x_i$	Y
0	0	0	0	0	0
1	0	0	1	1	0
2	0	1	0	2	1
3	0	1	1	3	1
4	1	0	0	1	0
5	1	0	1	2	1
6	1	1	0	3	1
7	1	1	1	4	1



$$Y = f(x_1, x_2, x_3) = x_2 + x_1 x_3$$

$$Y = f(x_1, x_2, x_3) = \sum m(2, 3, 5, 6, 7)$$

Ex For the switching function $f(x_1, x_2, x_3)$ realize by the two level threshold gate of fig



for $f_1(x_1, x_2, x_3)$ $T=3$

$$\sum_{i=1}^3 w_i x_i = 2x_1 + x_2 + x_3 \geq 3 \quad f_1 = 1$$

$$< 3 \quad f_1 = 0$$

for $f(x_1, x_2, x_3)$ $T=3.5$

$$\sum_{i=1}^3 w_i x_i = 2x_1 + 4f_1 + 3x_2 + x_3 \geq 3.5 \quad f = 1$$

$$< 3.5 \quad f = 0$$

x_1	x_2	x_3	$2x_1 + x_2 + x_3$	$T=3$ f_1	$2x_1 + 4f_1 + 3x_2 + x_3$	$T=3.5$ f
0	0	0	0	0	0	0
0	0	1	1	0	1	0
0	1	0	1	0	3	0
0	1	1	2	0	4	1
1	0	0	2	0	2	0
1	0	1	3	1	7	1
1	1	0	3	1	9	1
1	1	1	4	1	10	1

$x_1 x_2$	00	01	11	10
x_3				
0	0 ⁰	0 ²	1 ⁴	0 ⁶
1	0 ¹	1 ³	1 ⁷	1 ⁵

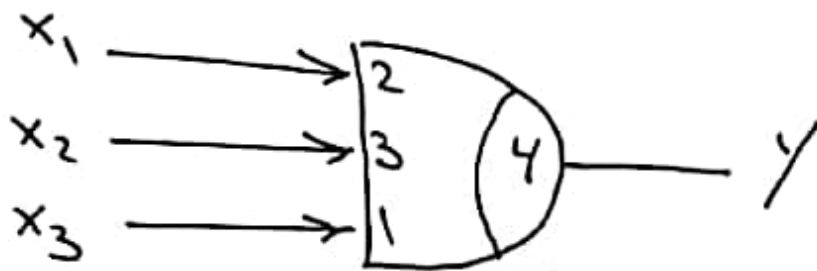
$$f(x_1, x_2, x_3) = x_1 x_2 + x_2 x_3 + x_1 x_3$$

$$f(x_1, x_2, x_3) : \sum m(3, 5, 6, 7)$$

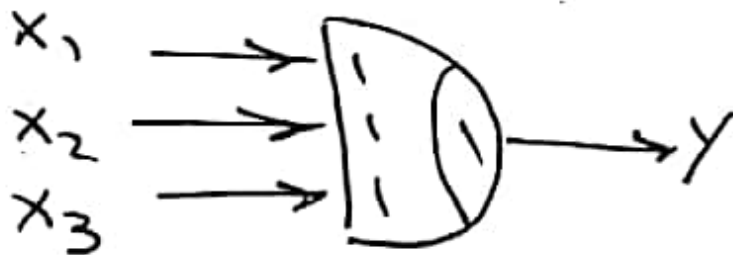
note

$$y = \begin{cases} 2x_1 + 3x_2 + x_3 > 4 \end{cases}$$

or

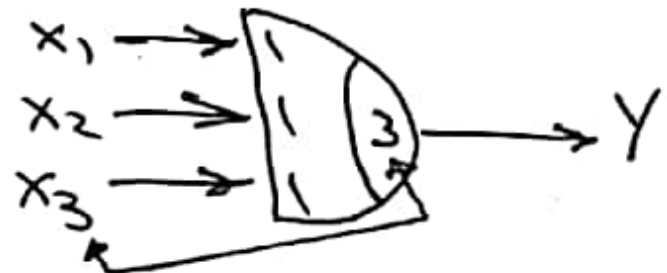


note



OR gate

x_1	x_2	x_3	Σ	Y
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	2	1
1	0	0	1	1
1	0	1	2	1
1	1	0	2	1
1	1	1	3	1



AND gate

x_1	x_2	x_3	Σ	Y
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	2	0
1	0	0	1	0
1	0	1	2	0
1	1	0	2	0
1	1	1	3	1

* function can be linear separable or not

$x_1, x_2 \rightarrow 2 \text{ dimension}$

(x_2, x_1)

$(1\ 0)$

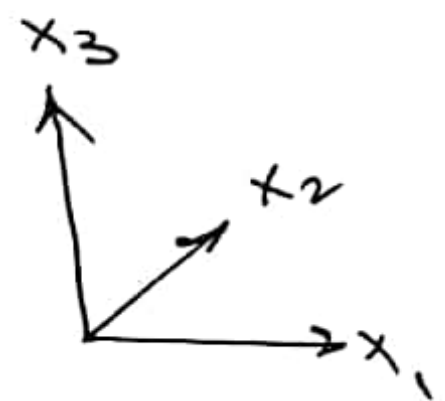
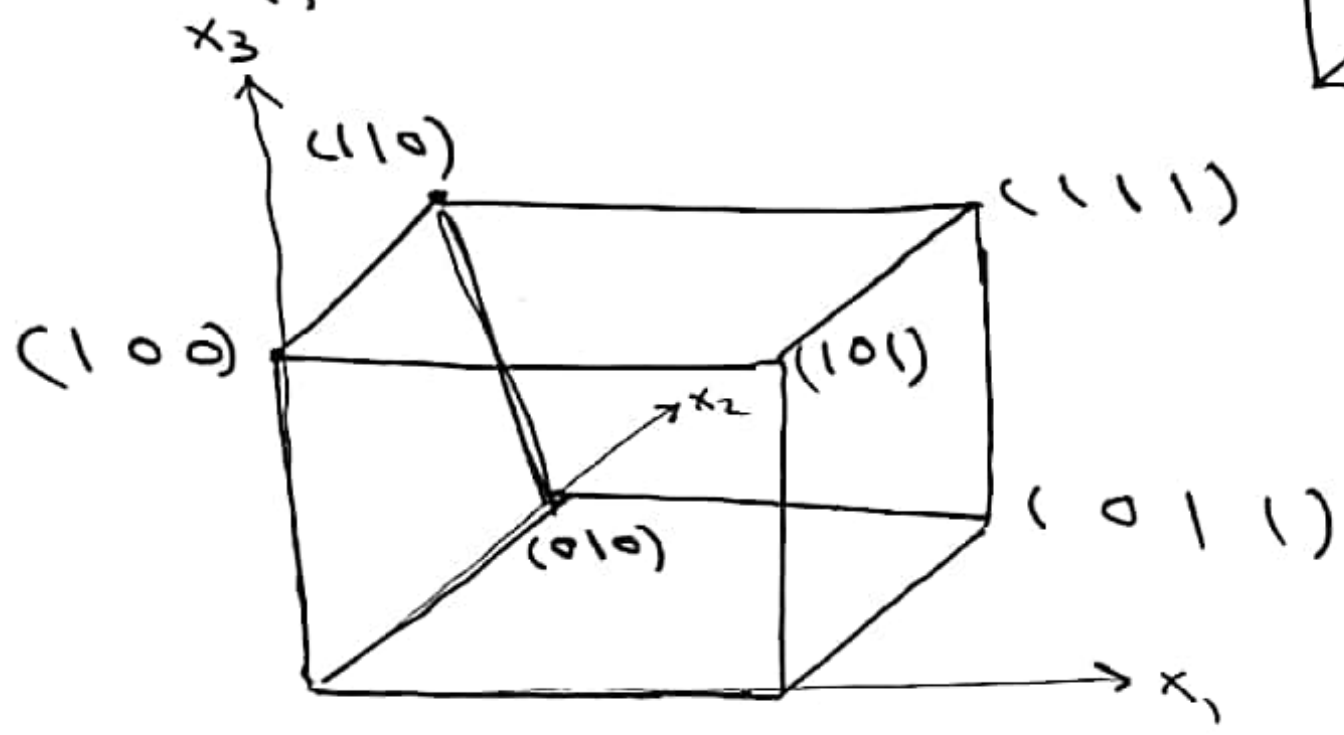
$(1\ 1)$

$(0\ 0)$

$(0\ 1)$



$x_1, x_2, x_3 \rightarrow \text{Three dimension}$
 (x_3, x_2, x_1)

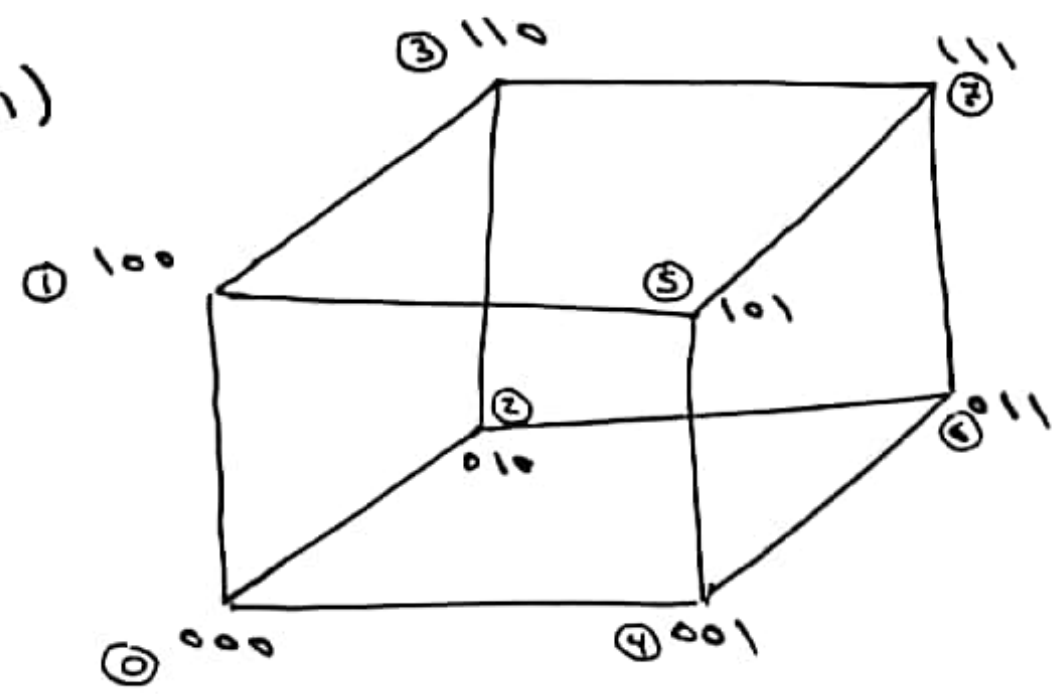


$(0\ 0\ 0)$
 $x_3\ x_2\ x_1$

$(0\ 0\ 1)$

in general

(x_3, x_2, x_1)

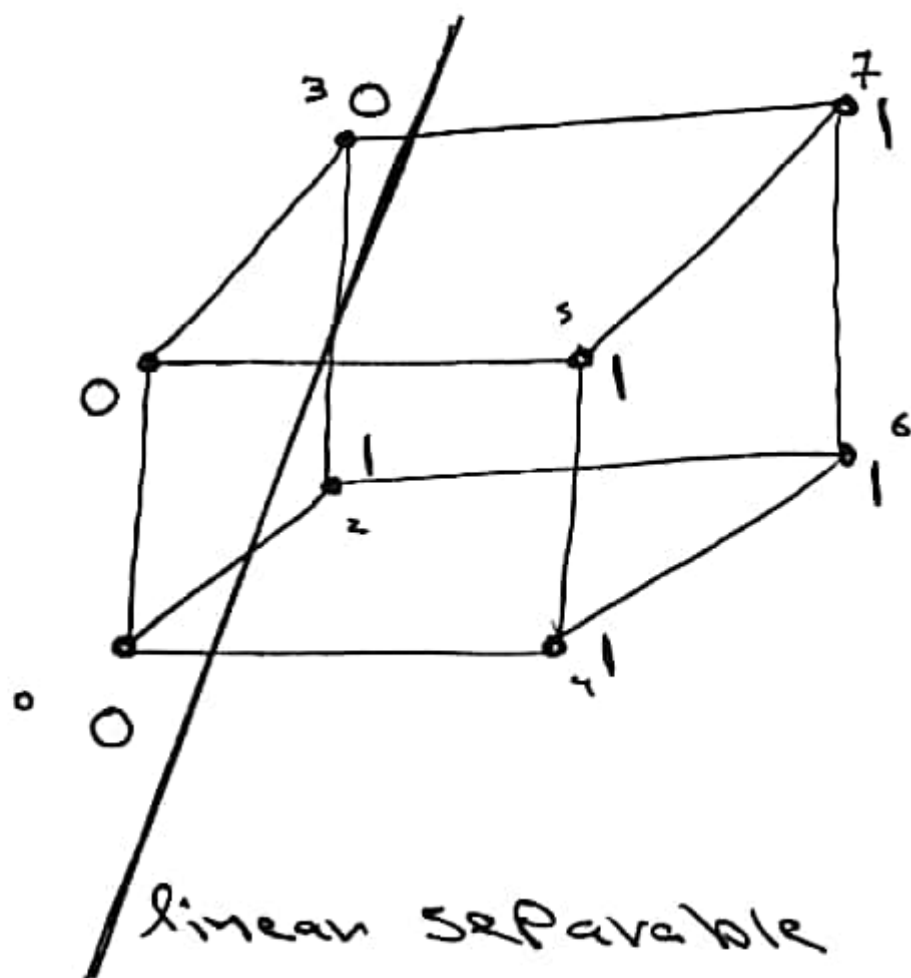


Ex for the function $f(x) = x_1 + x_2 \bar{x}_3$

can be represented by 3-dimensions or not with linear separable

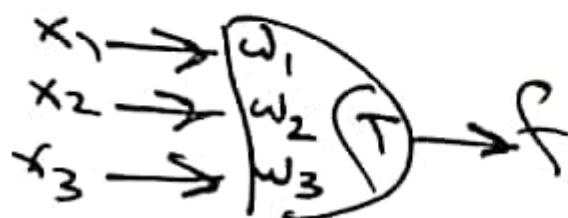
ans

	x_1	x_2	x_3	f
0	0	0	0	0
1	0	0	1	0
2	0	1	0	1
3	0	1	1	0
4	1	0	0	1
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1



can be represented with Threshold
one stage

$$\sum = w_1 x_1 + w_2 x_2 + w_3 x_3$$

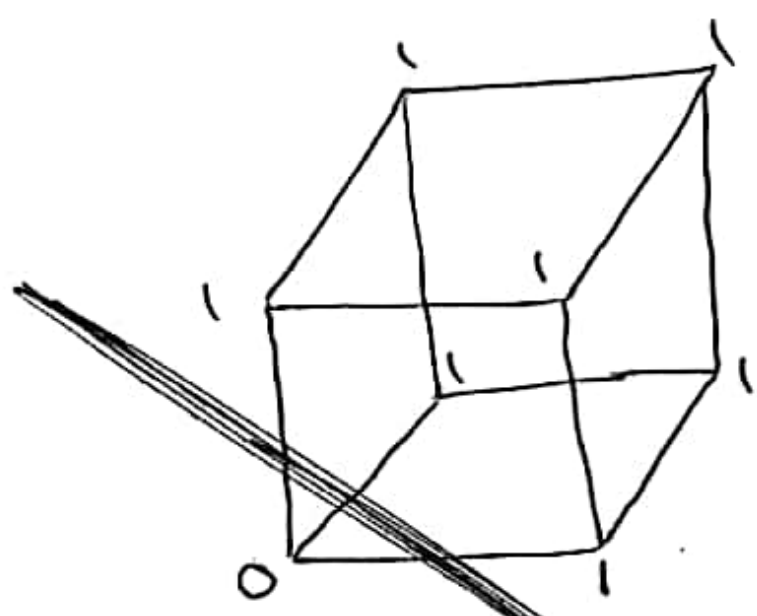


Q. Show if function are linearly separable or not

$$f_5 = x_1 + \bar{x}_1 x_2 + x_3$$

ans

	x_1	x_2	x_3	f_5
0	0	0	0	0
1	0	0	1	1
2	0	1	0	1
3	0	1	1	1
4	1	0	0	1
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1



yes can be linear separable

∴
* linear separable mean can be realize by using single threshold gate.

Synthesis of threshold network
Coho parameter (b_i)



to find coho parameter

$$\begin{aligned} 0 &\rightarrow -1 \\ 1 &\rightarrow +1 \end{aligned}$$

$$b_i = \sum_{p=1}^{2^n-1} f(x) x_i$$

1. \bar{x} \bar{y}
domain $(-1, 1)$

use $x_0 = +1$ for all min term

طريقة 2 domain $(0, 1)$

$$b_0 = (\text{no. of } f(x)=1) - (\text{no. of } f(x)=0)$$

b_i = agreements - Disagreement

to find Threshold

$$T = \frac{1}{2} \left[\left(\sum_{i=1}^n a_i \right) - (a_0) + 1 \right]$$

where a_i is weighted according to value of b_i

Ex for $f(x) = \bar{x}_1 x_2 + x_3$ find Chow Parameter
ans

x_0	x_1	x_2	x_3	$f(x)$	$f(x)x_0$	$f(x)x_1$	$f(x)x_2$	$f(x)x_3$
+1	-1	-1	-1	-1	-1	+1	+1	+1
+1	-1	-1	+1	+1	+1	-1	-1	+1
+1	-1	+1	-1	+1	+1	-1	+1	-1
+1	-1	+1	+1	+1	+1	-1	+1	+1
+1	+1	-1	-1	-1	-1	-1	+1	+1
+1	+1	-1	+1	+1	+1	+1	-1	+1
+1	+1	+1	-1	-1	-1	-1	-1	+1
+1	+1	+1	+1	+1	+1	+1	+1	+1
chow parameter					+2	-2	+2	+6

$b_0 \quad b_1 \quad b_2 \quad b_3$

$$b_0 = +2 \quad b_1 = -2 \quad b_2 = +2 \quad b_3 = +6$$

Ex ② For function $f(x) = \bar{x}_1 x_2 + x_3$
 find Chow parameters using (0,1)

ans domain
 ① realize

x_0	x_1	x_2	x_3	$f(x)$	with x_0	with x_1	with x_2	with x_3
1	0	0	0	0	a	a	a	a
1	0	0	1	1	a	a	a	a
1	0	1	0	1	a	a	a	a
1	0	1	1	1	a	a	a	a
1	1	0	0	0	a	a	a	a
1	1	0	1	1	a	a	a	a
1	1	1	0	0	a	a	a	a
1	1	1	1	1	a	a	a	a
					+2	-2	+2	+6

$$b_0 = 5 - 3 = 2$$

$$b_1 = 3 - 5 = -2$$

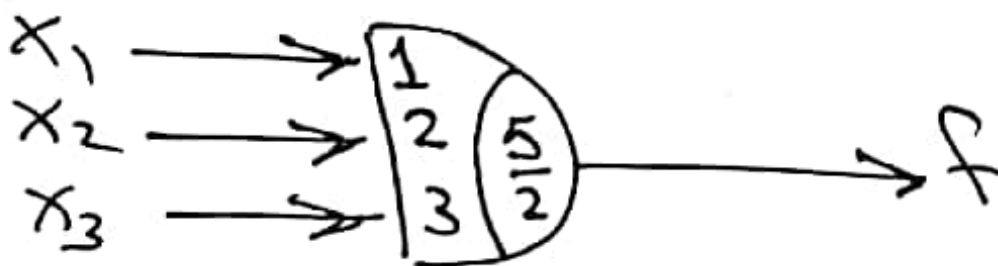
$$b_2 = 5 - 3 = +2$$

$$b_3 = 7 - 1 = +6$$

b_0	b_1	b_2	b_3
+2	-2	+2	+6
↓	↓	↓	↓
2	1	2	3
a_0	a_1	a_2	a_3

$$T = \frac{1}{2} [a_1 + a_2 + a_3 - a_0 + 1]$$

$$= \frac{1}{2} [1 + 2 + 3 - 2 + 1] = \frac{5}{2}$$



realize the Boolean function $f(x)$ with single threshold gate

x_1	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1
x_2	0	0	0	0	1	1	1	1	0	0	0	0	1	1	1	1	1
x_3	0	0	1	1	0	0	1	1	0	0	1	1	0	1	1	1	1
x_4	0	1	0	1	0	1	0	1	0	1	0	1	0	0	1	1	1
$f(x)$	0	0	0	0	1	1	1	1	0	1	1	1	1	1	1	1	1

ans

$$b_0 = 11 - 5 = 6$$

$$b_1 = 11 - 5 = 6$$

$$b_2 = 13 - 3 = 10$$

$$b_3 = 9 - 7 = 2$$

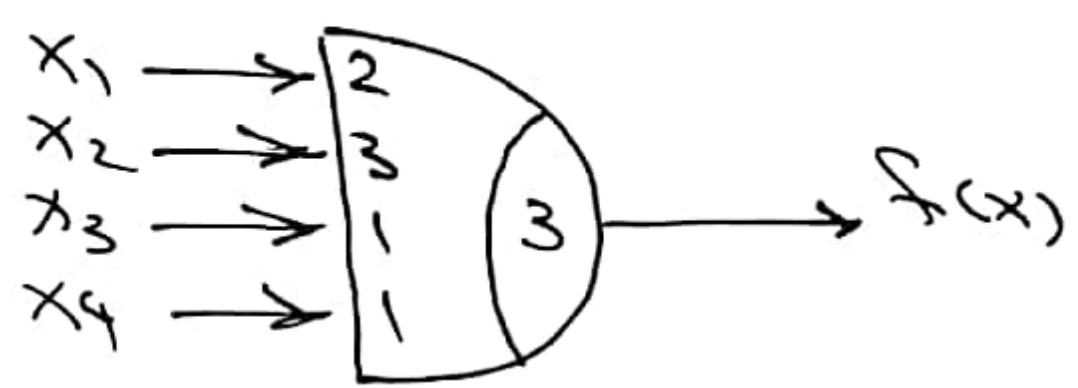
$$b_4 = 9 - 7 = 2$$

b_0	b_1	b_2	b_3	b_4
6	6	10	2	2
↓	↓	↓	↓	↓
2	2	3	1	1
a_0	a_1	a_2	a_3	a_4

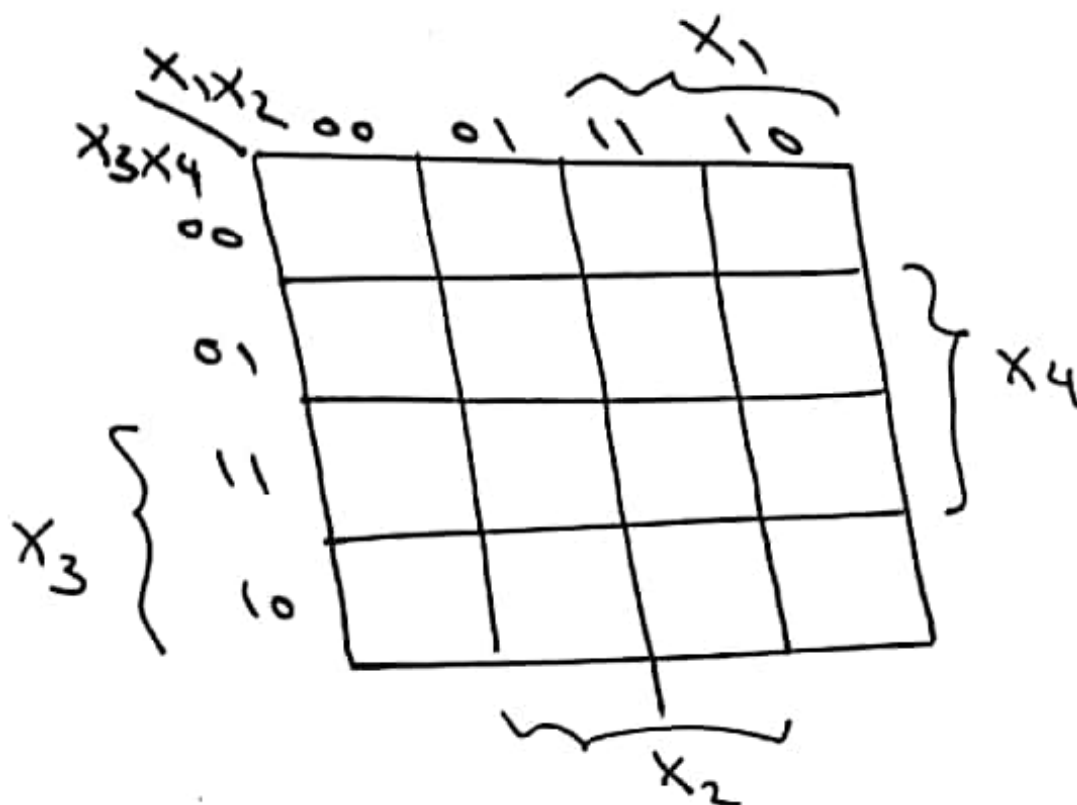
$$T = \frac{1}{2} [a_1 + a_2 + a_3 + a_4 - a_0 + 1]$$

$$= \frac{1}{2} [2 + 3 + 1 + 1 - 2 + 1]$$

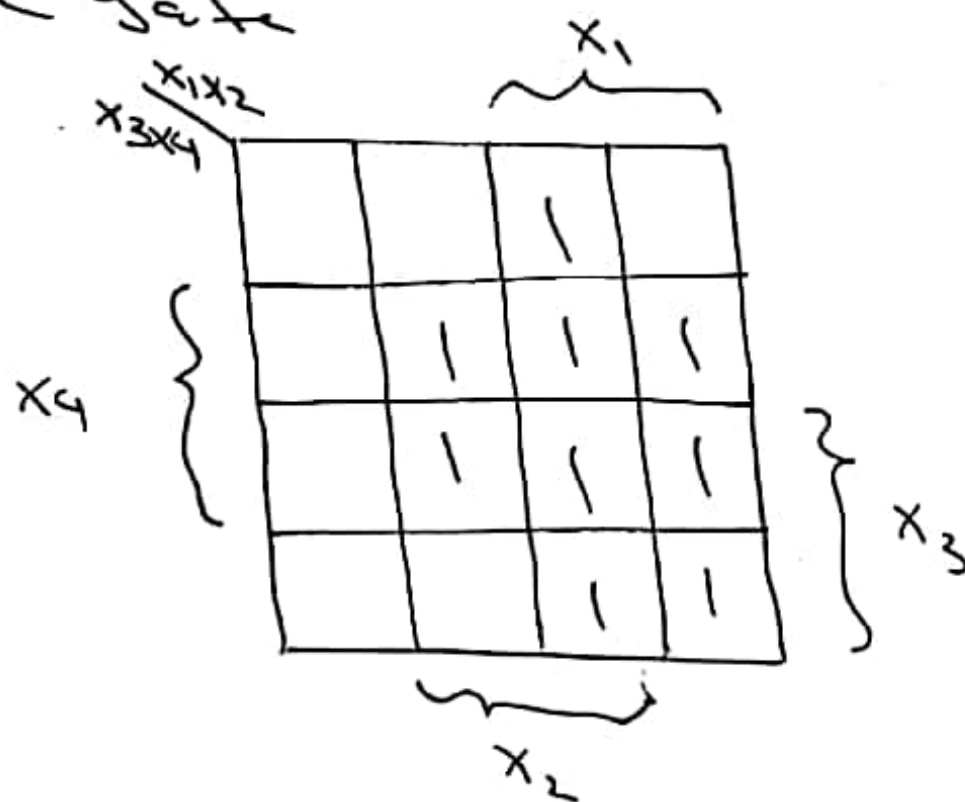
$$T = 3$$



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Ex realize the following switching function with single threshold logic gate



ans

$$b_0 = 9 - 7 = 2$$

$$b_1 = 2(7 - 2) = 10$$

$$b_2 = 2(6 - 3) = 6$$

$$b_3 = 2(5 - 4) = 2$$

$$b_4 = 2(6 - 3) = 6$$

b_0	b_1	b_2	b_3	b_4
2	10	6	2	6
↓	↓	↓	↓	↓
1	3	2	1	2
a_0	a_1	a_2	a_3	a_4

$$\begin{aligned}
 T &= \frac{1}{2} [a_1 + a_2 + a_3 + a_4 - a_0 + 1] \\
 &= \frac{1}{2} [3 + 2 + 1 + 2 - 1 + 1] \\
 &= 4
 \end{aligned}$$

