

# UNIT 2

## Lecture 23

### Tuple Relational Calculus

# Relational Languages

- Relational Algebra
  - It is an procedural language.
- Relational Calculus
  - It is an non procedural language (or Declarative Language)

# Relational Calculus

## 1. Tuple Relational Calculus (TRC)

- In this query language we work on tuple variable which ranges over relations.

## 2. Domain Relational Calculus (DRC)

- In this query language we work on domain variables which ranges over relations.

# Tuple Relational Calculus

- When we write a relational-algebra expression, we provide a sequence of procedures that generates the answer to our query.
- The tuple relational calculus, by contrast, is a **nonprocedural** query language. It describes the desired information without giving a specific procedure for obtaining that information.
- A query in the tuple relational calculus is expressed as

$$\{t \mid P(t)\}$$

that is, it is the set of all tuples  $t$  such that predicate  $P$  is true for  $t$ .

- we use  $t[A]$  to denote the value of tuple  $t$  on attribute  $A$ , and
- we use  $t \in r$  to denote that tuple  $t$  is in relation  $r$ .

# TRC Example : 1

Display all the information of students whose branch is CSE.

**RA :  $\sigma_{\text{branch} = \text{"CSE"}}(\text{STUDENT})$**

**SQL > select \* from student where br = 'CSE';**

**TRC :  $\{ t \mid t \in \text{STUDENT} \wedge t[\text{branch}] = \text{"CSE"} \}$**

## STUDENT

Rollno	Sname	Sem	Branch	Marks	Pno
1	RAM	3	CSE	40	121
2	SHYAM	5	CSE	50	122
3	MOHAN	7	CSE	55	123
4	GOPAL	5	IT	65	121
5	RINKI	3	MECH	40	122
6	PINKI	3	ETC	90	123

## OUTPUT

Rollno	Sname	Sem	Branch	Marks	Pno
1	RAM	3	CSE	40	121
2	SHYAM	5	CSE	50	122
3	MOHAN	7	CSE	55	123

# TRC Example : 2

Display all the information of students whose sem is 3.

RA :  $\sigma_{sem=3}(STUDENT)$

SQL > select \* from student where sem = 3;

TRC :  $\{t \mid t \in STUDENT \wedge t[sem] = 3\}$

**STUDENT**

Rollno	Sname	Sem	Branch	Marks	Pno
1	RAM	3	CSE	40	121
2	SHYAM	5	CSE	50	122
3	MOHAN	7	CSE	55	123
4	GOPAL	5	IT	65	121
5	RINKI	3	MECH	40	122
6	PINKI	3	ETC	90	123

**OUTPUT**

Rollno	Sname	Sem	Branch	Marks	Pno
1	RAM	3	CSE	40	121
5	RINKI	3	MECH	40	122
6	PINKI	3	ETC	90	123

# TRC Example : 3

Display all the information of students whose marks is greater than 50.

RA :  $\sigma_{\text{marks} > 50}(\text{STUDENT})$

SQL > select \* from student where marks > 50;

TRC :  $\{ t \mid t \in \text{STUDENT} \wedge t[\text{marks}] > 50 \}$

## STUDENT

Rollno	Sname	Sem	Branch	Marks	Pno
1	RAM	3	CSE	40	121
2	SHYAM	5	CSE	50	122
3	MOHAN	7	CSE	55	123
4	GOPAL	5	IT	65	121
5	RINKI	3	MECH	40	122
6	PINKI	3	ETC	90	123

## OUTPUT

Rollno	Sname	Sem	Branch	Marks	Pno
3	MOHAN	7	CSE	55	123
4	GOPAL	5	IT	65	121
6	PINKI	3	ETC	90	123

# TRC Example : 4

Display all the information of students whose branch is CSE or sem is 3.

RA :  $\sigma_{\text{branch} = \text{"CSE"} \vee \text{sem} = 3}(\text{STUDENT})$

SQL > select \* from student where branch = 'CSE' or sem = 3;

TRC :  $\{ t \mid t \in \text{STUDENT} \wedge t[\text{branch}] = \text{"CSE"} \vee t[\text{sem}] = 3 \}$

## STUDENT

Rollno	Sname	Sem	Branch	Marks	Pno
1	RAM	3	CSE	40	121
2	SHYAM	5	CSE	50	122
3	MOHAN	7	CSE	55	123
4	GOPAL	5	IT	65	121
5	RINKI	3	MECH	40	122
6	PINKI	3	ETC	90	123

## OUTPUT

Rollno	Sname	Sem	Branch	Marks	Pno
1	RAM	3	CSE	40	121
2	SHYAM	5	CSE	50	122
3	MOHAN	7	CSE	55	123
5	RINKI	3	MECH	40	122
6	PINKI	3	ETC	90	123



# TRC Example : 5

Display all the information of students whose branch is CSE and sem is 3.

**RA :**  $\sigma_{\text{branch} = \text{"CSE"} \wedge \text{sem} = 3}(\text{STUDENT})$

**SQL > select \* from student where branch = 'CSE' and sem = 3;**

**TRC :**  $\{ t \mid t \in \text{STUDENT} \wedge t[\text{branch}] = \text{"CSE"} \wedge t[\text{sem}] = 3 \}$

**STUDENT**

Rollno	Sname	Sem	Branch	Marks	Pno
1	RAM	3	CSE	40	121
2	SHYAM	5	CSE	50	122
3	MOHAN	7	CSE	55	123
4	GOPAL	5	IT	65	121
5	RINKI	3	MECH	40	122
6	PINKI	3	ETC	90	123

**OUTPUT**

Rollno	Sname	Sem	Branch	Marks	Pno
1	RAM	3	CSE	40	121

# TRC Example : 6

Display the names of all the students.

**RA :  $\Pi_{sname} (STUDENT)$**

**SQL > select distinct sname from student;**

**TRC :  $\{ t \mid \exists s \in STUDENT (t[sname] = s[sname]) \}$**

## STUDENT

Rollno	Sname	Sem	Branch	Marks	Pno
1	RAM	3	CSE	40	121
2	SHYAM	5	CSE	50	122
3	MOHAN	7	CSE	55	123
4	GOPAL	5	IT	65	121
5	RINKI	3	MECH	40	122
6	PINKI	3	ETC	90	123

## OUTPUT

Sname
RAM
SHYAM
MOHAN
GOPAL
RINKI
PINKI

# TRC Example : 7

Display the name and semester value of all the students.

RA :  $\Pi_{sname, sem} (STUDENT)$

SQL > select distinct sname, sem from student;

TRC :  $\{ t \mid \exists s \in STUDENT (t[sname] = s[sname] \wedge t[sem] = s[sem]) \}$

## STUDENT

Rollno	Sname	Sem	Branch	Marks	Pno
1	RAM	3	CSE	40	121
2	SHYAM	5	CSE	50	122
3	MOHAN	7	CSE	55	123
4	GOPAL	5	IT	65	121
5	RINKI	3	MECH	40	122
6	PINKI	3	ETC	90	123

## OUTPUT

Sname	Sem
RAM	3
SHYAM	5
MOHAN	7
GOPAL	5
RINKI	3
PINKI	3

# TRC Example : 8

Display the name of all the students of CSE branch.

**RA :  $\Pi_{\text{sname}}(\sigma_{\text{branch} = \text{"CSE"}}(\text{STUDENT}))$**

**SQL > select distinct sname from (select \* from student where branch = 'CSE');**

**TRC : TRC : { t |  $\exists s \in \text{STUDENT} (t[\text{sname}] = s[\text{sname}] \wedge s[\text{branch}] = \text{"CSE"})$  }**

## STUDENT

Rollno	Sname	Sem	Branch	Marks	Pno
1	RAM	3	CSE	40	121
2	SHYAM	5	CSE	50	122
3	MOHAN	7	CSE	55	123
4	GOPAL	5	IT	65	121
5	RINKI	3	MECH	40	122
6	PINKI	3	ETC	90	123

## OUTPUT

Sname
RAM
SHYAM
MOHAN

# TRC Example : 9

Display the name of branches in which project 121 or 122 or both are running.

**RA :**  $\Pi_{\text{branch}}(\sigma_{\text{pno} = 121}(\text{STUDENT})) \cup \Pi_{\text{branch}}(\sigma_{\text{pno} = 122}(\text{STUDENT}))$

**SQL > select distinct branch from student where pno = 121 Union select distinct branch from student where pno = 122;**

**TRC :**  $\{ t \mid \exists s \in \text{STUDENT} (t[\text{branch}] = s[\text{branch}] \wedge s[\text{pno}] = 121) \vee \exists u \in \text{STUDENT} (t[\text{branch}] = u[\text{branch}] \wedge u[\text{pno}] = 122) \}$

## STUDENT

Rollno	Sname	Sem	Branch	Marks	Pno
1	RAM	3	CSE	40	121
2	SHYAM	5	CSE	50	122
3	MOHAN	7	CSE	55	123
4	GOPAL	5	IT	65	121
5	RINKI	3	MECH	40	122
6	PINKI	3	ETC	90	123

## OUTPUT

Branch	Branch	Branch
CSE	CSE	CSE
IT	MECH	IT
		MECH

# TRC Example : 10

Display the name of branches in which project 121 and 122 are running.

**RA :**  $\Pi_{\text{branch}}(\sigma_{\text{pno} = 121}(\text{STUDENT})) \cap \Pi_{\text{branch}}(\sigma_{\text{pno} = 122}(\text{STUDENT}))$

**SQL > select distinct branch from student where pno = 121 intersect select distinct branch from student where pno = 122;**

**TRC :**  $\{ t \mid \exists s \in \text{STUDENT} (t[\text{branch}] = s[\text{branch}] \wedge s[\text{pno}] = 121) \wedge \exists u \in \text{STUDENT} (t[\text{branch}] = u[\text{branch}] \wedge u[\text{pno}] = 122) \}$

## STUDENT

Rollno	Sname	Sem	Branch	Marks	Pno
1	RAM	3	CSE	40	121
2	SHYAM	5	CSE	50	122
3	MOHAN	7	CSE	55	123
4	GOPAL	5	IT	65	121
5	RINKI	3	MECH	40	122
6	PINKI	3	ETC	90	123

## OUTPUT

Branch	Branch	Branch
CSE	CSE	CSE
IT	MECH	

# TRC Example : 11

Display the name of branches in which project 121 is running but 122 is not.

**RA :**  $\Pi_{\text{branch}}(\sigma_{\text{pno} = 121}(\text{STUDENT})) - \Pi_{\text{branch}}(\sigma_{\text{pno} = 122}(\text{STUDENT}))$

**SQL > select distinct branch from student where pno = 121 minus / except select distinct branch from student where pno = 122;**

**TRC :**  $\{t \mid \exists s \in \text{STUDENT} (t[\text{branch}] = s[\text{branch}] \wedge s[\text{pno}] = 121) \\ \wedge \neg \exists u \in \text{STUDENT} (t[\text{branch}] = u[\text{branch}] \wedge u[\text{pno}] = 122)\}$

## STUDENT

Rollno	Sname	Sem	Branch	Marks	Pno
1	RAM	3	CSE	40	121
2	SHYAM	5	CSE	50	122
3	MOHAN	7	CSE	55	123
4	GOPAL	5	IT	65	121
5	RINKI	3	MECH	40	122
6	PINKI	3	ETC	90	123

## OUTPUT

Branch	Branch	Branch
CSE	CSE	IT
IT	MECH	

# TRC Example : 12

## STUDENT

Rollno	Sname	Sem	Branch	Marks	Pno
1	RAM	3	CSE	40	121
2	SHYAM	5	CSE	50	122
3	MOHAN	7	CSE	55	123
4	GOPAL	5	IT	65	121
5	RINKI	3	MECH	40	122
6	PINKI	3	ETC	90	123

## PROJECT

$\sqcap_{sname, pname} (STUDENT \bowtie_{student.pno = project.pno} PROJECT)$

Pno	Pname	Duration
121	P1	10
122	P2	20
123	P3	30

Sname	Pname
RAM	P1
GOPAL	P1
SHYAM	P2
RINKI	P2
MOHAN	P3
PINKI	P3

SQL > select distinct sname, pname from student inner join project on  
student.pno = project.pno; [SQL 99 syntax]

SQL > select distinct sname, pname from student, project where student.pno  
= project.pno;

TRC :  $\{ t \mid \exists s \in STUDENT (t[sname] = s[sname])$   
 $\wedge \exists p \in PROJECT (t[pname] = p[pname] \wedge s[pno] = p[pno])) \}$



# TRC Example : 13

## STUDENT

Rollno	Sname	Sem	Branch	Marks	Pno
1	RAM	3	CSE	40	121
2	SHYAM	5	CSE	50	122
3	MOHAN	7	CSE	55	123
4	GOPAL	5	IT	65	121
5	RINKI	3	MECH	40	122
6	PINKI	3	ETC	90	123

## PROJECT

Pno	Pname	Duration
121	P1	10
122	P2	20
123	P3	30

$\Pi_{\text{branch, pno}}(\text{STUDENT}) \div \Pi_{\text{pno}}(\text{PROJECT})$

## OUTPUT

Branch
CSE

## Equivalent SQL Query

SQL > select distinct branch from student s1  
where not exists (select pno from project p  
where not exists (select branch from student s2  
where s1.branch = s2.branch and p.pno = s2.pno));

TRC :  $\{ t \mid \exists s \in \text{STUDENT} (t[\text{branch}] = s[\text{branch}]$   
 $\wedge \forall p \in \text{PROJECT} \rightarrow (s[\text{pno}] = p[\text{pno}])) \}$

# Formal Definition of Tuple Relational Calculus

- A tuple-relational-calculus expression is of the form

$$\{t \mid P(t)\}$$

where  $P$  is a *formula*.

- Several tuple variables may appear in a formula.
- A tuple variable is said to be a *free variable* unless it is quantified by a  $\exists$  or  $\forall$ .
- Thus, in

$$\text{TRC} : \{t \in \text{STUDENT} \wedge \exists p \in \text{PROJECT} (t[pno] = p[pname])\}$$

$t$  is a free variable. Tuple variable  $p$  is said to be a *bound* variable.

# Formal Definition of Tuple Relational Calculus

- A tuple-relational-calculus formula is built up out of *atoms*.
- An atom has one of the following forms:
  - $s \in r$ , where  $s$  is a tuple variable and  $r$  is a relation (we do not allow use of the  $\in$  operator)
  - $s[x] \Theta u[y]$ , where  $s$  and  $u$  are tuple variables,  $x$  is an attribute on which  $s$  is defined,  $y$  is an attribute on which  $u$  is defined, and  $\Theta$  is a comparison operator ( $<, \leq, =, =, >, \geq$ ); we require that attributes  $x$  and  $y$  have domains whose members can be compared by  $\Theta$
  - $s[x] \Theta c$ , where  $s$  is a tuple variable,  $x$  is an attribute on which  $s$  is defined,  $\Theta$  is a comparison operator, and  $c$  is a constant in the domain of attribute  $x$

# Formal Definition of Tuple Relational Calculus

- We build up formulae from atoms by using the following rules:
  - An atom is a formula.
  - If  $P1$  is a formula, then so are  $\neg P1$  and  $(P1)$ .
  - If  $P1$  and  $P2$  are formulae, then so are  $P1 \vee P2$ ,  $P1 \wedge P2$ , and  $P1 \Rightarrow P2$ .
  - If  $P1(s)$  is a formula containing a free tuple variable  $s$ , and  $r$  is a relation, then  $\exists s \in r (P1(s))$  and  $\forall s \in r (P1(s))$  are also formulae.

# Formal Definition of Tuple Relational Calculus

- As we could for the relational algebra, we can write equivalent expressions that are not identical in appearance.
- In the tuple relational calculus, these equivalences include the following three rules:
  1.  $P1 \wedge P2$  is equivalent to  $\neg(\neg(P1) \vee \neg(P2))$ .
  2.  $\forall t \in r (P1(t))$  is equivalent to  $\neg \exists t \in r (\neg P1(t))$ .
  3.  $P1 \Rightarrow P2$  is equivalent to  $\neg(P1) \vee P2$ .

# Safety of Expressions

- There is one final issue to be addressed. A tuple-relational-calculus expression may generate an infinite relation.
- Suppose that we write the expression

$$\{t \mid \neg (t \in STUDENT)\}$$

- There are infinitely many tuples that are not in STUDENT.
- Most of these tuples contain values that do not even appear in the database! Clearly, we do not wish to allow such expressions.
- This query is known as unsafe query in tuple relational calculus.

For Video lecture on this topic please subscribe to my youtube channel.

The link for my youtube channel is

[https://www.youtube.com/channel/UCRWGtE76JITp1iim6aOTRuW?sub\\_confirmation=1](https://www.youtube.com/channel/UCRWGtE76JITp1iim6aOTRuW?sub_confirmation=1)