Regression- kNN, Linear, Decision tree

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https://www.kaggle.com/datasets/budincsevity/szeged-weather

in linear regression the target variable y is quantitative and x is the predictor which can be quantitative or qualitative. It displays the relationship between x and y. Strengths are, it works well when there is a linear pattern in the data, it has low variance, and is a pretty simple algorithm. Weaknesses are, it has high bias because its looking for a linear relation in the data, so it doesn't perform well when there are non-linear relationships.

#read in the data set

```
#options(stringsAsFactors = FALSE)
df <- read.csv("weatherHistory-2.csv", header=TRUE)
whist <- df[,c(4,5,6,7,8,9,11)]
attach(whist)
str(whist)</pre>
```

```
'data.frame':
                   96453 obs. of 7 variables:
##
   $ Temperature..C.
                             : num 9.47 9.36 9.38 8.29 8.76 ...
##
   $ Apparent.Temperature..C.: num 7.39 7.23 9.38 5.94 6.98 ...
                             : num 0.89 0.86 0.89 0.83 0.83 0.85 0.95 0.89 0.82 0.7
##
  $ Humidity
##
   $ Wind.Speed..km.h.
                             : num 14.12 14.26 3.93 14.1 11.04 ...
   $ Wind.Bearing..degrees. : num
                                    251 259 204 269 259 258 259 260 259 279 ...
##
   $ Visibility..km.
                              : num 15.8 15.8 15 15.8 15.8 ...
##
   $ Pressure..millibars.
                              : num 1015 1016 1016 1016 1017 ...
```

a. Divide into train and test

```
set.seed(1234)
i <- sample(1:nrow(df), 0.80*nrow(df), replace=FALSE)
train <- whist[i,]
test <- whist[-i,]</pre>
```

b. 5 R functions for data exploration using the training data.

tail(train, n=2)

	TemperatureC. <dbl></dbl>	Apparent.TemperatureC. <dbl></dbl>	Humidity <dbl></dbl>	Wind.Speedkm.h. <dbl></dbl>	Wir		
57481	13.894444	13.894444	0.69	3.1234			
31612	1.111111	-2.272222	0.85	11.2700			
2 rows 1-6 of 8 columns							

```
dim(train)
```

```
## [1] 77162 7
```

```
str(train)
```

```
'data.frame':
                    77162 obs. of 7 variables:
##
##
   $ Temperature..C.
                              : num 8 13.4 8.89 17.83 1.31 ...
##
   $ Apparent.Temperature..C.: num 6.76 13.4 7.71 17.83 1.31 ...
                              : num 0.99 0.83 0.93 0.96 1 0.73 0.93 0.62 0.76 0.93 .
##
   $ Humidity
##
   $ Wind.Speed..km.h.
                              : num 7.63 17.11 8.05 12.41 3.53 ...
   $ Wind.Bearing..degrees. : num 121 138 130 220 247 179 271 341 138 41 ...
##
   $ Visibility..km.
##
                              : num 0.612 15.875 3.059 8.372 0.37 ...
   $ Pressure..millibars.
                              : num 1021 1009 1009 1012 1032 ...
```

```
summary(train)
```

```
##
    Temperature..C.
                       Apparent.Temperature..C.
                                                     Humidity
                                                                    Wind.Speed..km.h.
##
    Min.
            :-21.822
                       Min.
                               :-27.717
                                                  Min.
                                                          :0.0000
                                                                    Min.
                                                                            : 0.000
                                                  1st Ou.:0.6000
##
    1st Qu.:
              4.614
                       1st Qu.: 2.283
                                                                     1st Qu.: 5.796
    Median : 11.978
                       Median : 11.978
                                                  Median :0.7800
                                                                    Median : 9.918
##
##
    Mean
            : 11.933
                       Mean
                               : 10.855
                                                  Mean
                                                          :0.7348
                                                                    Mean
                                                                            :10.799
##
    3rd Qu.: 18.839
                       3rd Qu.: 18.839
                                                  3rd Qu.: 0.8900
                                                                     3rd Qu.:14.120
           : 39.589
##
                               : 38.661
                                                          :1.0000
                                                                            :63.853
##
    Wind.Bearing..degrees. Visibility..km. Pressure..millibars.
    Min.
                                    : 0.00
##
               0.0
                             Min.
                                              Min.
                                                          0
##
    1st Ou.:116.0
                             1st Ou.: 8.34
                                              1st Ou.:1012
    Median :180.0
                             Median :10.05
                                              Median:1016
##
##
    Mean
            :187.6
                             Mean
                                    :10.34
                                              Mean
                                                      :1003
##
    3rd Qu.:290.0
                             3rd Qu.:14.81
                                              3rd Qu.:1021
##
    Max.
           :359.0
                             Max.
                                    :16.10
                                              Max.
                                                      :1046
```

head(train, n=5)

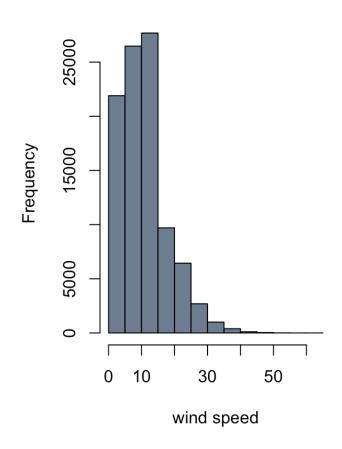
	TemperatureC. <dbl></dbl>	Apparent.TemperatureC. <dbl></dbl>	Humidity <dbl></dbl>	Wind.Speedkm.h. <dbl></dbl>	Wir			
41964	8.000000	6.761111	0.99	7.6314				
15241	13.400000	13.400000	0.83	17.1143				
33702	8.888889	7.705556	0.93	8.0500				
83023	17.827778	17.827778	0.96	12.4131				
80756	1.311111	1.311111	1.00	3.5259				
5 rows 1-6 of 8 columns								

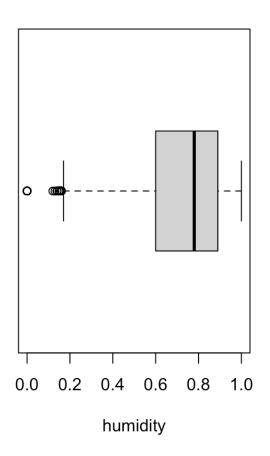
c. 2 informative graphs, using the training data.

Displays a histogram that shows windspeed frequency and a box plot which displays the humidity.

```
par(mfrow=c(1,2))
hist(Wind.Speed..km.h., col="slategray", main="wind speed frequency",xlab="wind speed
")
boxplot(Humidity,horizontal=TRUE, xlab="humidity")
```

wind speed frequency





Build a linear regression with all predictors except columns 1,2,3,10 and 12

lm1 <- lm(Apparent.Temperature..C.~., data=train)
summary(lm1)</pre>

```
##
## Call:
## lm(formula = Apparent.Temperature..C. ~ ., data = train)
##
## Residuals:
##
      Min
               10 Median
                               3Q
                                      Max
## -4.3617 -0.7152 -0.1068 0.6824
##
## Coefficients:
##
                           Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         -2.605e+00 4.439e-02 -58.684 < 2e-16 ***
## Temperature..C.
                         1.125e+00 5.472e-04 2056.862 < 2e-16 ***
                          1.052e+00 2.702e-02 38.955 < 2e-16 ***
## Humidity
                         -9.569e-02 5.910e-04 -161.925 < 2e-16 ***
## Wind.Speed..km.h.
## Wind.Bearing..degrees. 5.372e-04 3.642e-05 14.750 < 2e-16 ***
## Visibility..km.
                         1.105e-04 1.026e-03
                                                 0.108
                                                          0.914
## Pressure..millibars. 1.868e-04 3.317e-05 5.630 1.81e-08 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.078 on 77155 degrees of freedom
## Multiple R-squared: 0.9899, Adjusted R-squared: 0.9899
## F-statistic: 1.255e+06 on 6 and 77155 DF, p-value: < 2.2e-16
```

Evaluate

```
pred1 <- predict(lm1, newdata=test)
cor1 <- cor(pred1, test$Apparent.Temperature..C.)
mse1 <- mean((pred1-test$Apparent.Temperature..C.)^2)
print(paste('correlation:', cor1))</pre>
```

```
## [1] "correlation: 0.994878444357297"
```

```
print(paste('mse:', mse1))
```

```
## [1] "mse: 1.15909871906881"
```

kNN for regression

cor is 0.9907, mse is 4.638

```
library(caret)
```

```
## Loading required package: ggplot2
```

```
## Loading required package: lattice
```

```
# fit the model
fit <- knnreg(train[,1:7],train[,1],k=3)

# Evaluate
pred2 <- predict(fit, test[,1:7])
cor_knn1 <- cor(pred2, test$Apparent.Temperature..C.)
mse_knn1 <- mean((pred2- test$Apparent.Temperature..C.)^2)
rmse_knn1 <- (sqrt(mse_knn1))

print(paste('correlation:', cor_knn1))</pre>
```

```
## [1] "correlation: 0.990757671363682"
```

```
print(paste('mse:', mse_knn1))
```

```
## [1] "mse: 4.63857430739458"
```

Scale the data

```
train_scaled <- train[,1:7]
means <- sapply(train_scaled,mean)
stdvs <- sapply(train_scaled,sd)
train_scaled <- scale(train_scaled, center=means, scale=stdvs)
test_scaled <- scale(test[,1:7], center=means, scale=stdvs)</pre>
```

kNN on scaled data

scaling the data performed better. cor before was 0.9908 and after is 0.9986. mse before was 4.6386, and now is 0.3296

```
fit <- knnreg(train_scaled, train$Apparent.Temperature..C., k=3)
pred3 <- predict(fit, test_scaled)
cor_knn2 <- cor(pred3, test$Apparent.Temperature..C.)
mse_knn2 <- mean((pred3 - test$Apparent.Temperature..C.)^2)
print(paste('correlation:', cor_knn2))</pre>
```

```
## [1] "correlation: 0.998561485590879"

print(paste('mse:', mse_knn2))
```

```
## [1] "mse: 0.329554309396625"
```

Find the best k

Try various values of k. K=9 gves the best values

```
cor_k <- rep(0,20)
mse_k <- rep(0,20)

i <- 1
for (k in seq(1, 10, 2)){
   fit_k <- knnreg(train_scaled,train$Apparent.Temperature..C., k=k)
   pred_k <-predict(fit_k, test_scaled)
   cor_k[i] <- cor(pred_k, test$Apparent.Temperature..C.)
   mse_k[i] <- mean((pred_k - test$Apparent.Temperature..C.)^2)
   print(paste("k=", k, cor_k[i], mse_k[i]))
   i <- i + i
}</pre>
```

```
## [1] "k= 1 0.997540182758721 0.557735966877665"

## [1] "k= 3 0.998561485590879 0.329554309396625"

## [1] "k= 5 0.998750024604675 0.290759920432771"

## [1] "k= 7 0.998800549217474 0.283070876112961"

## [1] "k= 9 0.998837244464568 0.278818882197203"
```

```
which.min(mse_k)
```

```
## [1] 3
```

```
which.max(cor_k)
```

```
## [1] 16
```

scaled knn regression

cor is 0.9988 and mse is 0.2788 which is better than on the scaled data using k=3

```
fit <- knnreg(train_scaled, train$Apparent.Temperature..C., k=9)
pred4 <- predict(fit, test_scaled)
cor_knn3 <- cor(pred4, test$Apparent.Temperature..C.)
mse_knn3 <- mean((pred4 - test$Apparent.Temperature..C.)^2)
print(paste("cor=", cor_knn3))</pre>
```

```
## [1] "cor= 0.998837244464568"
```

```
print(paste("mse=", mse_knn3))
```

```
## [1] "mse= 0.278818882197203"
```

Using tree

Correlation was 0.9786 and rmse was 2.19

```
#install.packages("tree")
library(tree)

tree1 <- tree(Apparent.Temperature..C.~., data=train)
summary(tree1)</pre>
```

```
##
## Regression tree:
## tree(formula = Apparent.Temperature..C. ~ ., data = train)
## Variables actually used in tree construction:
## [1] "Temperature..C."
## Number of terminal nodes:
## Residual mean deviance: 4.931 = 380400 / 77160
## Distribution of residuals:
##
        Min.
              1st Ou.
                          Median
                                             3rd Qu.
                                      Mean
                                                          Max.
## -19.62000 -1.58500 -0.04461
                                   0.00000
                                                       8.96800
                                             1.53800
```

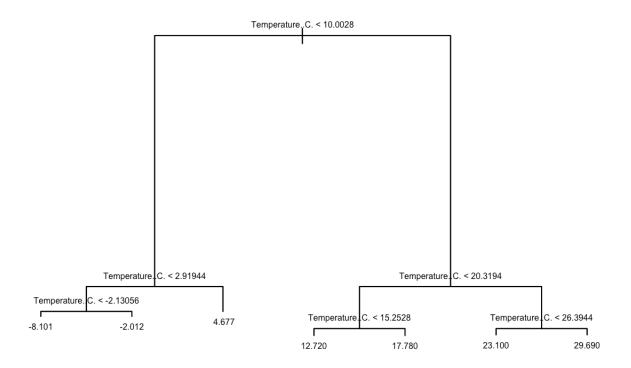
```
pred5 <- predict(tree1, newdata=test)
print(paste('correlation:', cor(pred5, test$Apparent.Temperature..C.)))</pre>
```

```
## [1] "correlation: 0.978610523738168"
```

```
rmse_tree <- sqrt(mean((pred5-test$Apparent.Temperature..C.)^2))
print(paste('rmse:', rmse_tree))</pre>
```

```
## [1] "rmse: 2.19112277024394"
```

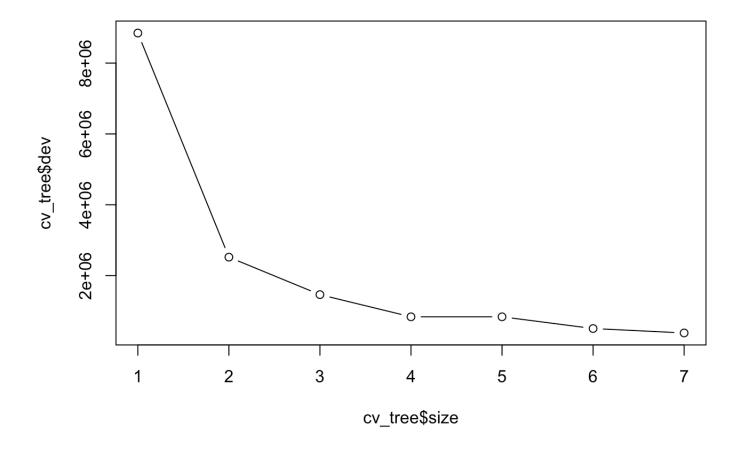
```
plot(tree1)
text(tree1, cex=0.5, pretty=0)
```



Cross validation

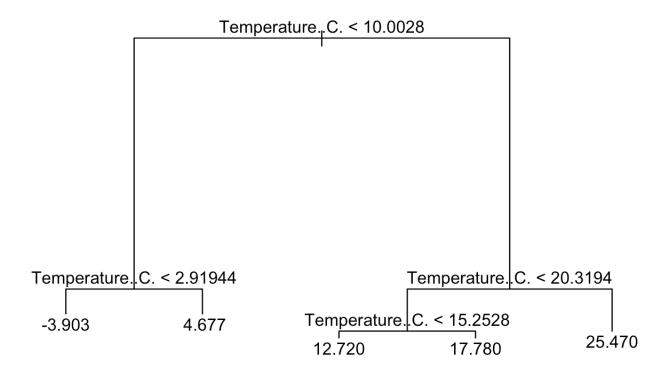
to try to get better results

```
cv_tree <- cv.tree(tree1)
plot(cv_tree$size, cv_tree$dev, type='b')</pre>
```



prune the tree

```
tree_pruned <- prune.tree(tree1, best=5)
plot(tree_pruned)
text(tree_pruned, pretty=0)</pre>
```



test on pruned tree

For the unpruned tree, correlation was 0.9786 and rmse was 2.19. The cor for the pruned tree is 0.9625 which is slightly lower than the correlation for the unpruned tree, and the rmse is 2.8898 which is higher. So pruning didn't improve the result. Although decision tree didn't perform the best, random forest produced very good results with a correlation of 0.9996 and rmse of 0.3133. Bagging also performed really well with the correlation of 0.9999 and rmse of 0.1607. For linear regression the correlation was 0.9949 and mse was 1.1591 so it performed better than using decision trees. Knn regression had a cor of 0.9908 and mse of 4.6386 and after scaling using k=9 we got a cor of 0.9988 and mse of 0.2788 which is much better. So overall not taking random forest and bagging into account, knn performed the best, then linear regression, followed by decision tree regression.

```
pred_pruned <- predict(tree_pruned, newdata = test)
cor_pruned <- cor(pred_pruned, test$Apparent.Temperature..C.)
rmse_pruned <- rmse_pruned <- sqrt(mean((pred_pruned-test$Apparent.Temperature..C.)^2
))
print(paste('cor:', cor_pruned))</pre>
```

```
## [1] "cor: 0.962487132707812"

print(paste('rmse:', rmse_pruned))

## [1] "rmse: 2.88983347843392"
```

Random Forest

Will outperform the decision tree but will lose interpretability.

```
#install.packages("randomForest")
library(randomForest)

## randomForest 4.7-1.1

## Type rfNews() to see new features/changes/bug fixes.
```

```
##
## Attaching package: 'randomForest'
```

```
## The following object is masked from 'package:ggplot2':
##
## margin
```

```
set.seed(1234)
rf <- randomForest(Apparent.Temperature..C.~., data=train, importance=TRUE)
rf</pre>
```

predict on the random forest

Correlation is slightly higher and rmse is much lower than what we got for linear regression.

```
pred_rf <- predict(rf, newdata = test)
cor_rf <- cor(pred_rf, test$Apparent.Temperature..C.)
print(paste('cor:', cor_rf))</pre>
```

```
## [1] "cor: 0.999605069000984"
```

```
rmse_rf <- sqrt(mean((pred_rf-test$Apparent.Temperature..C.)^2))
print(paste('rmse:',rmse_rf))</pre>
```

```
## [1] "rmse: 0.313284504282562"
```

bagging

```
bag <- randomForest(Apparent.Temperature..C.~., data=train, mtry = 6)
bag</pre>
```

predict on bagging

bagging also produced good results with a high correlation of 0.9999 and rmse of 0.1607. It also did best out of all the algorithms.

```
pred_bag <- predict(bag, newdata = test)
cor_bag <- cor(pred_bag, test$Apparent.Temperature..C.)
print(paste('cor:', cor_bag))</pre>
```

```
## [1] "cor: 0.999887006056601"
```

```
rmse_bag <- sqrt(mean((pred_bag-test$Apparent.Temperature..C.)^2))
print(paste('rmse:',rmse_bag))</pre>
```

```
## [1] "rmse: 0.16072651526701"
```

Linear regression outperformed decision tree regression likely due to the fact that linear regression usually does better than decision trees when the underlying function is linear. In the dataset used there is a strong linear relation hence the result. Decision trees suffers from high variance so it didn't do that well. However, random forest produced very good results because it counteracts the high variance. knn regression after scaling performed the best out of all algorithms overall likely because knn works well on low dimensions and there were only 6 features.