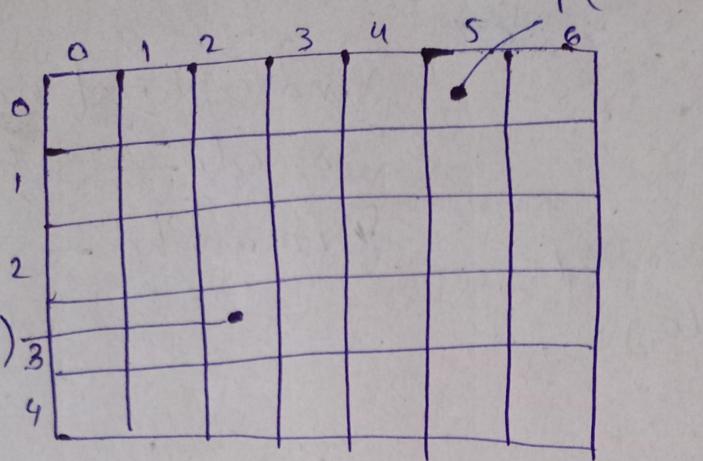


15/1/2025



$$D_e(P, Q) = \sqrt{(x-s)^2 + (y-t)^2}$$

$$= \sqrt{(0-3)^2 + (5-2)^2}$$

$$= \sqrt{9+9} = \sqrt{18} = 3\sqrt{2} \text{ unit (Ans)}$$

This is Eucleidian distance.

|| D_4 distance

$$D_4(P, Q) = |x-s| + |y-t|$$

$$= |0-3| + |5-2|$$

$$= 3+3 = 6 \text{ unit (Ans)}$$

|| Chessboard distance

$$D_B(P, Q) = \max(|x-s|, |y-t|)$$

$$= \max(3, 3) = 3 \text{ unit (Ans)}$$

Histogram Specification / or Histogram mapping

10 marks

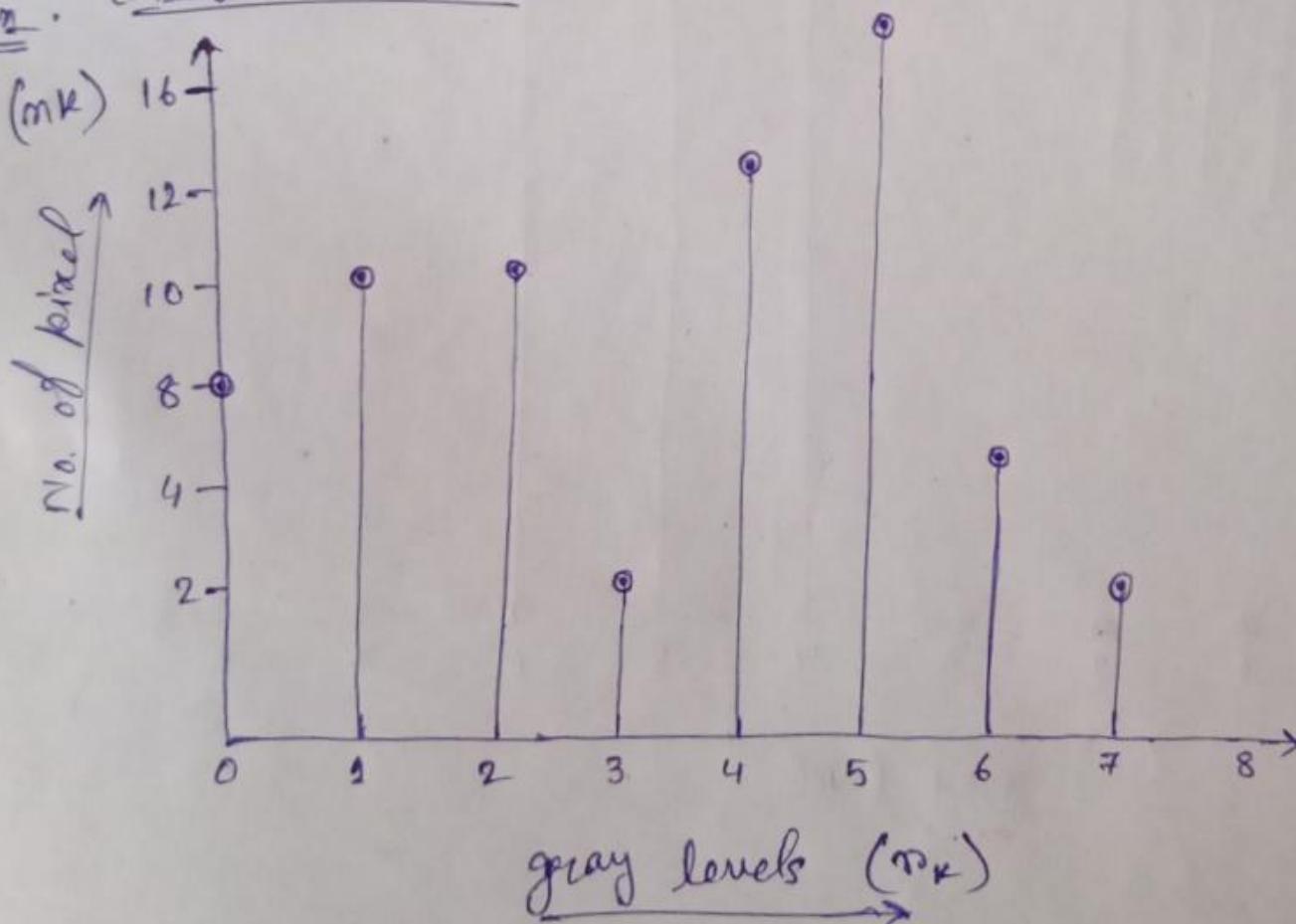
Original Image

gray level	0	1	2	3	4	5	6	7
No of pixel	8	10	10	2	12	16	4	2

Desired Image / Target Image

gray level	0	1	2	3	4	5	6	7
No of pixel	0	0	0	0	20	20	16	8

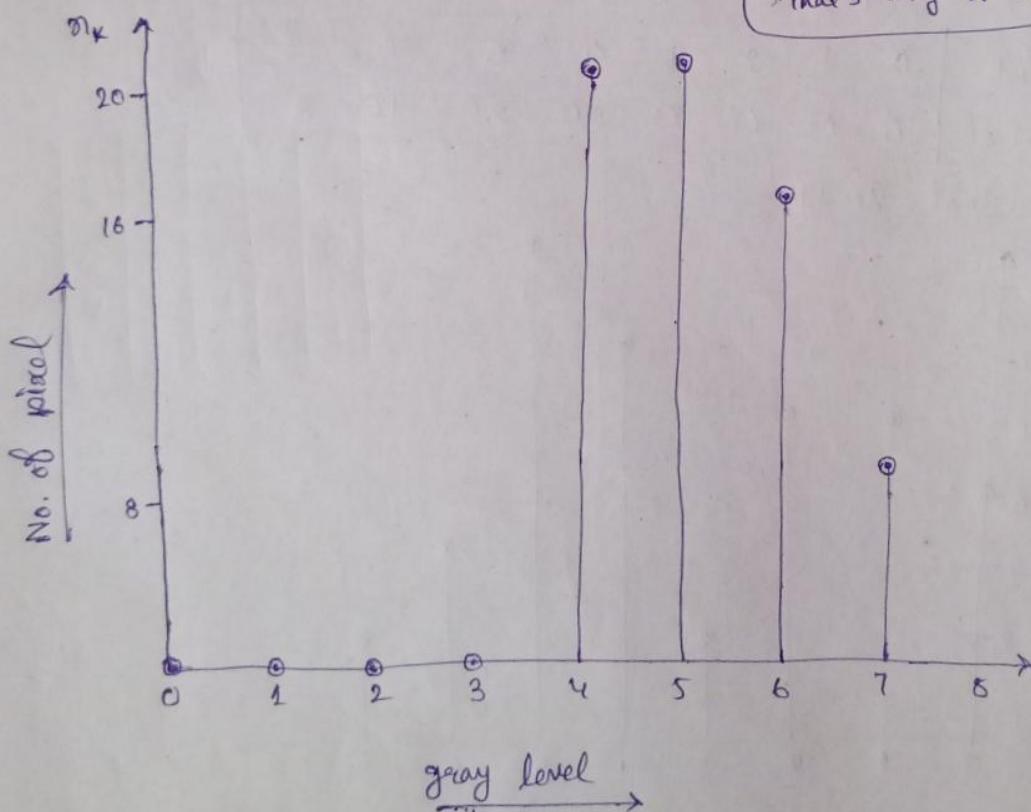
Soln: Original Image:



Histogram of original image

Gray levels γ_k	No. of pixels n_k	$P(\gamma_k) = n_k/n$ (PDF)	S_k CDF	$S_k \times 7$	Histogram equilized level
0	8	0.125	0.125	0.875	1
1	10	0.156 0.156	0.281	1.967	2
2	10	0.156 0.156	0.437	3.059	3
3	2	0.031 0.031	0.468	3.276	3
4	12	0.188 0.188	0.656	4.592	5
5	16	0.25 0.25	0.906	6.342	6
6	4	0.063 0.063	0.969	6.783	7
7	2	0.031	1	7	7
$n=64$					

Desired Image



Why $S_k \times 7$? → Here we are assuming 8 bits (0-7)
7 is 3 bits digits. $7 \rightarrow 111$. So,
 $2^3 = 8$. Let, $8 = L$. But in
formula we have to use $L-1$.
That's why it is $S_k \times (L-1)$

Histogram of desired image —

gray levels n_k	No. of pixels n_k	$P(n_k) = n_k/n$ (PDF)	S _k CDF	S _k × 7	Histogram equilized level
0	0	0	0	0	0
1	0	0	0	0	0
2	0	0	0	0	0
3	0	0	0	0	0
4	20	0.313	0.313	2.191	2
5	20	0.313	0.626	4.403	4
6	16	0.25	0.876	6.132	6
7	8	0.125	1.001	7.007	7
$\sum n_k = 64$					

Mapping

Gray level	$H(0)$	$H(D)$	Mapping
0	1	0	4 ✓
1	2	0	4 ✓
2	3	0	5 ✓
3	3	0	5 ✓
4	5	2	6 ✓
5	6	4	6 ✓
6	7	6	7 ✓
7	7	7	7 ✓

Modified Image :

Gray level	0	1	2	3	4	5	6	7
No. of pixels	0	0	0	0	18	12	28	6

gray level slicing

① With Background

$$a \leq v \leq b$$

where $a=3$, $b=6$ (given)

Ex. 1
pixel

	0	1	2	3	4
0	0
1	.	.	.	253	.
2	.	.	250	253	.
3	.	2	.	.	.
4	0				

Ex. 2 $3 \leq v \leq 6 = 7$
otherwise 0

1	4	2	7	5
3	2	4	5	2
2	6	5	7	0
4	6	6	5	1
0	2	3	2	1

Ans

1	7	2	7	7
7	2	7	7	2
2	7	7	7	0
7	7	7	7	1
0	2	7	2	1

② Without Background
 $3 \leq v \leq 6 = 7$
 otherwise 0

1	4	2	7	5
3	2	4	5	2
2	6	5	7	0
4	6	6	5	1
0	2	3	2	1

↓

0	7	0	7	7
7	0	7	7	0
0	7	7	7	0
7	7	7	7	0
0	0	7	0	0

Bit plane Slicing:

167	133	111
144	140	135
169	159	148

Step 1: Binary format for above image is

10100111	10000101	01101111
10010000	10001100	10000111
10011111	10011010	10010100

for 1st digit: Binary format of 167

1	0	1	0	0	1	1	1
MSB	7 th bit	6 th bit	5 th bit	4 th bit	3 rd bit	2 nd bit	LSB

Step 2: Bit plane slicing of above example.

1	1	0
1	1	1
1	1	1

8 bit
(MSB bit)
Plane

0	0	1
0	0	0
0	0	0

7 bit

1	0	1
0	0	0
0	0	0

6 bit

1	0	1
0	0	1
1	1	0

2 bit

0	0	0
1	0	0
1	1	1

5 bit

0	0	1
0	1	0
1	1	0

4 bit

1	1	1
0	1	1
1	0	1

3 bit

1	1	1
0	0	1
1	0	0

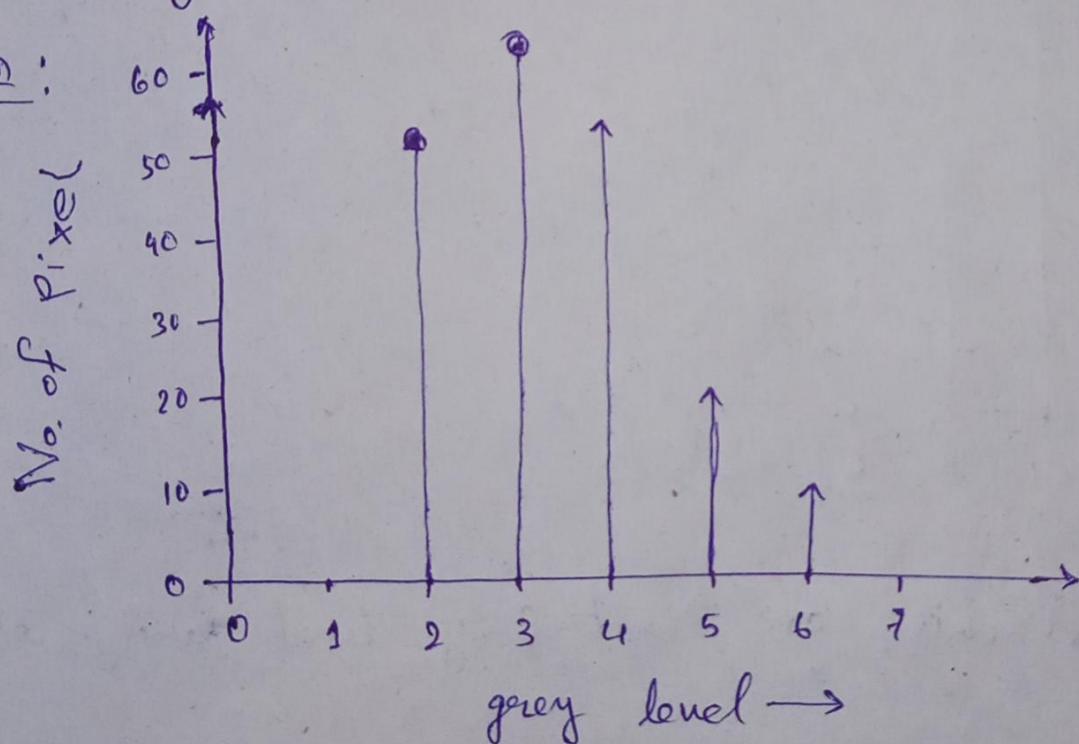
2 bit

LSB plane

DIPHistogram stretching / Contrast stretching

grey level	0	1	2	3	4	5	6	7
No. of pixels	0	0	50	60	50	20	10	0

Perform histogram stretching such that the new image has dynamic range $[0 \rightarrow 7]$.

Sol:

$$s_{\min} = 0$$

$$s_{\max} = 7$$

$$r_{\min} = 2$$

$$r_{\max} = 6$$

$$\text{Slope, } S = \left(\frac{S_{\max} - S_{\min}}{r_{\max} - r_{\min}} \right) \times (r - r_{\min}) + S_{\min}$$

when, $r = 2$

$$S_2 = \left(\frac{7-0}{6-2} \right) \times (2-2) + 0 = \frac{7}{4} \times 0 + 0 = 0$$

when, $r = 3$

$$S_3 = \left(\frac{7-0}{6-2} \right) \times (3-2) + 0 = \frac{7}{4} \times 1 + 0 = 1.75 \approx 2$$

when, $r = 4$

$$S_4 = \left(\frac{7-0}{6-2} \right) \times (4-2) + 0 = \frac{7}{4} \times 2 + 0 = 3.5 \approx 4$$

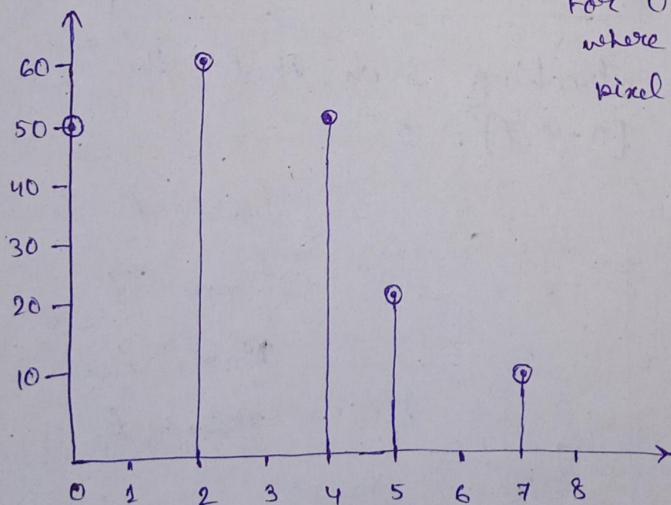
when, $r = 5$

$$S_5 = \left(\frac{7-0}{6-2} \right) \times (5-2) + 0 = \frac{7}{4} \times 3 = 5.25 \approx 5$$

when, $r = 6$

$$S_6 = \left(\frac{7-0}{6-2} \right) \times (6-2) + 0 = \frac{7}{4} \times 4 + 0 = 7$$

For 0, $r = 2$ and in graph where grey level = 2 there no. of pixel = 50.



Qn: Apply contrast stretching on 3-bit grey level image of size 4×4 .

Solu:

$f(x, y)$

2	1	2	1
4	5	5	6
3	2	1	4
6	2	1	6

DIP

$$f(x,y) =$$

6	7	7	7	3
5	1	1	2	2
5	0	5	0	3
0	0	3	3	3
5	1	1	4	4

- 1) Apply grey scale slicing for the image where $3 \leq r \leq 5$
- 2) Construct Image Histogram Equilization
- 3) Find Image Negative
- 4) Distance from P to Q (CITY Block)

3) Apply Grey Scale Slicing

with Background $a \leq r \leq b$ where, $a=3$
 $b=5$

6	7	7	7	3
5	1	1	2	2
5	0	5	0	3
0	0	3	3	3
5	1	1	4	4

$$3 \leq r \leq 5 = 7$$

otherwise r as it is

6	7	7	7	7
7	1	1	2	2
7	0	7	0	7
0	0	7	7	7
7	1	1	7	7

without
Background

0	0	0	0	7
7	0	0	0	0
7	0	7	0	7
0	0	7	7	7
7	0	0	7	7

Range
 $3 \leq r \leq 5 = 7$
without 0

3) Image Negative

Max Value = 7 ~ $(111)_2$

$$\begin{aligned} \text{Formula} \quad S &= (L-1) \cdot r^m \\ &= (8-1) \cdot 7^0 \\ &= 7 - 7^0 \end{aligned}$$

No. of bit
 $L = 3$
Formula - I
 $L = 2^m$
 $2^3 = 8$

Negative

1	0	0	0	4
2	6	6	5	5
2	7	2	7	4
7	7	4	4	4
2	6	6	3	3

④ *

Distance = $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

 $f(x,y) = \begin{matrix} 0 & 1 & 2 & 3 & 4 \\ 6 & 7 & 7 & 7 & 3 \\ 1 & 5 & 1 & 1 & 2 \\ 2 & 5 & 0 & 5 & 0 \\ 3 & 0 & 0 & 3 & 3 \\ 4 & 5 & 1 & 1 & 4 \end{matrix}$

$P(x_1, y_1)$
 $(1, 3)$

$Q(x_2, y_2)$

$P(x_1, y_1)$
 $(1, 3)$

$$\begin{aligned} d(P, Q) &= |x_1 - x_2| + |y_1 - y_2| \\ &\text{let } P(1, 3), Q(3, 1) \\ d(P, Q) &= |1 - 3| + |3 - 1| \\ &= 2 + 2 = 4 \end{aligned}$$

2)

Grey Level	0	1	2	3	4	5	6	7
No. of Pixel	4	4	2	5	2	4	1	3

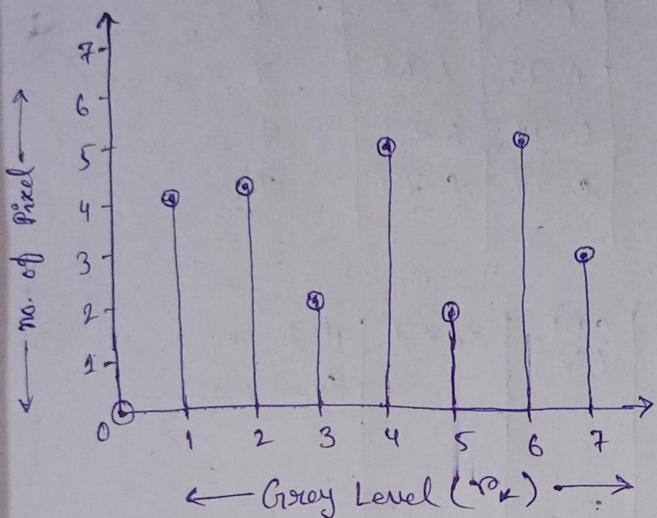
$n = 25$

Grey Level (r_K)	No. of Pixel (n_K)	$P(r_K) = \frac{n_K}{n}$ (PDF)	S_K (CDP)	$S_K \times 7$	Histogram Equalized
0	4	0.16	0.16	1.12	1
1	4	0.16	0.32	2.24	2
2	2	0.08	0.4	2.8	3
3	5	0.2	0.6	4.2	4
4	2	0.08	0.68	4.76	5
5	4	0.16	0.84	5.88	6
6	1	0.04	0.88	6.16	6
7	3	0.12	1	7	7
				$\overline{n = 25}$	

• New Image

6	7	7	7	4
6	2	2	3	3
6	1	6	1	4
1	1	4	4	4
6	2	2	5	5

Grey Level	0	1	2	3	4	5	6	7
No. of Pixel	0	4	4	2	5	2	5	3



Input Image :-

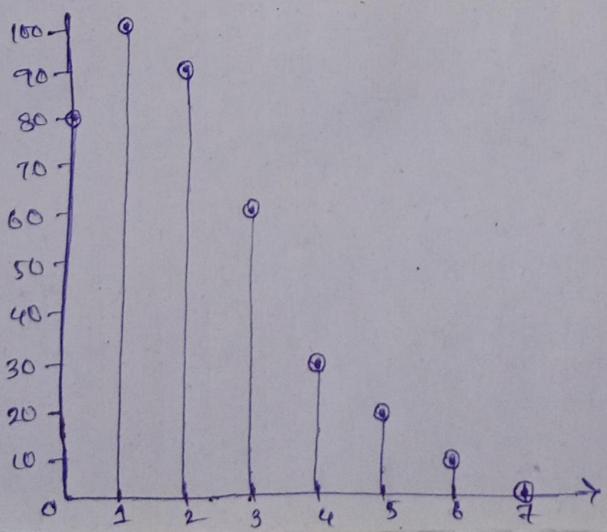
On

Grey level	0	1	2	3	4	5	6	7
No. of pixel	80	100	90	60	30	20	10	0

Target / Desired Image :-

Grey level	0	1	2	3	4	5	6	7
No. of Pixel	0	0	0	60	80	100	80	70

Aus.



Grey level (r_k)	No. of Pixel (n_k)	PDF $P(r_k) = \frac{n_k}{n}$	CDF (S_k)	$S_k \times 7$	Histogram Equilized
0	80	0.20	0.20	1.4	1
1	100	0.25	0.45	3.15	3
2	90	0.23	0.68	4.76	5
3	60	0.15	0.83	5.81	6
4	30	0.07	0.9	6.3	6
5	20	0.05	0.95	6.65	7
6	10	0.02	0.97	6.79	7
7	0	0	0.97	6.79	7
$\sum n_k = 390$					

Grey level (r_k)	No. of Pixel (n_k)	PDF $P(r_k) = \frac{n_k}{n}$	CDF (S_k)	$S_k \times 7$	Histogram Equilized
0	0	0			
1	0	0			
2	0	0			
3	60	0.15			
4	80	0.20			
5	100	0.25			
6	80				
7	70				
$\sum n_k = 390$					

Logical Operation

① AND operation:

A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

		f(x,y)		
		1	1	1
0		1	0	0
0	1	0	0	0
1	0	0	1	0
1	1	1	0	1

		f ₁ (x,y)		
		1	1	1
0		0	0	1
0	1	0	0	0
1	0	0	0	1
1	1	0	1	1

		g(x,y)		
		1	1	1
0		0	0	0
0	1	0	0	0
1	0	0	0	0
1	1	0	0	0

② OR operation:

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1

		g(x,y)		
		1	1	1
0		0	1	1
0	1	1	1	1
1	0	1	1	1
1	1	1	1	1

③ NOT operation:

Y	Y
0	1
1	0

$$\Theta(x,y) \rightarrow \text{of}[f(x,y)]$$

0	0	0
1	0	1
1	0	1
1	0	1

Logical Image Arithmetic:

- ① Detect Differences: Image subtraction can be used to find difference between of the objects.
- ② De-noise: Adding successive image of the same scene can reduce random noise.
- ③ Collection of Illumination: Dividing two images can correct shadow and non-homogenous illumination.
- ④ Adjust Brightness: Multiplying pixel values by number > 1 , while dividing the factor > 1 can darken the image.
- ⑤ Blend Images: Varying the value ~~of~~ between 0 & 1. Then it make transition images.

MSE = Mean Square Error

SNR = Signal to Noise Ratio

PSNR = Peak Signal to Noise Ratio

These are used to measure the quality of images and sequence.

Qn What is MSE?

Ans) MSE is a error measurement of original image and distorted image.

• PSNR → Ratio of the max. possible signal power to the power of the noise that effects the signal.

Unit is DB [Decibal]

• Measure a quantity of contrast or reconstructed image. It indicates that higher PSR value indicates better quality.

- SNR → Measure quality of any signal.
- MSE → Avg. of the sequence errors between the original and distorted image. It compares the original image with distorted image. The lower noise MSE value indicates lesser.

Problems:

$$\textcircled{1} \quad f(x,y) = \begin{bmatrix} 3 & 2 & 1 \\ 1 & 2 & 1 \\ 3 & 2 & 2 \end{bmatrix}, \quad \hat{f}(x,y) = \begin{bmatrix} 3 & 2 & 2 \\ 1 & 1 & 2 \\ 1 & 1 & 1 \end{bmatrix}$$

MSE Formula:

$$\text{MSE} = \frac{1}{MN} \sum_{i=0}^{M-1} \sum_{j=0}^{N-1} [f(x,y) - \hat{f}(x,y)]^2$$

Sol:

$$\text{MSE} = \frac{1}{9} [(3-3)^2 + (2-2)^2 + (1-2)^2 + (1-1)^2 + (2-1)^2 + (1-2)^2 + (3-1)^2 + (2-1)^2 + (2-1)^2]$$

$$= \frac{1}{9} \times 9 = 1$$

Problem \textcircled{2}:

$$f(x,y) = \begin{bmatrix} 3 & 2 & 1 \\ 1 & 2 & 1 \\ 3 & 2 & 2 \end{bmatrix}, \quad \hat{f}(x,y) = \begin{bmatrix} 3 & 2 & 2 \\ 1 & 1 & 2 \\ 1 & 1 & 1 \end{bmatrix}$$

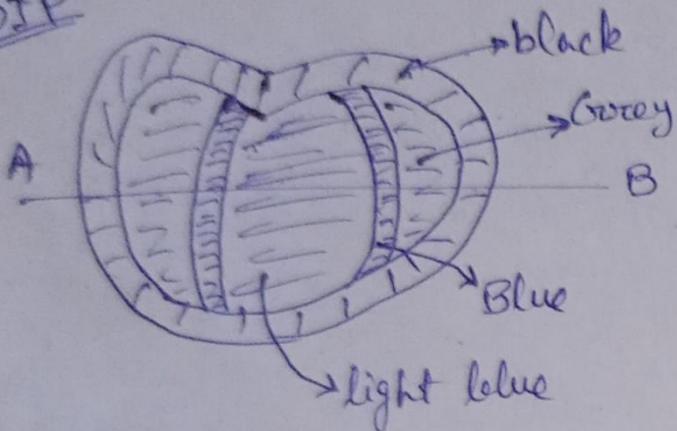
SNR Formula:

$$\text{SNR} = 20 \log_{10} \frac{\sum_{i=0}^{M-1} \sum_{j=0}^{N-1} [f(x,y)]^2}{\sum_{i=0}^{M-1} \sum_{j=0}^{N-1} [f(x,y) - \hat{f}(x,y)]^2}$$

Sol:

$$\text{SNR} = 20 \log_{10} \frac{[9+4+1+1+4+1+9+4+4]}{9}$$

$$= 20 \log_{10} \frac{37}{9} = \underline{12.27}$$



darker $\rightarrow 0$

0 - black = low intensity

grey - slightly higher

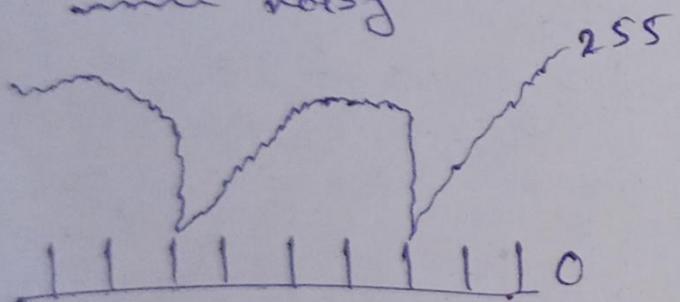
blue - Medium Intensity

light blue - High Intensity

white - very high intensity

Sampling & Quantization:

— clear
~~~~ noisy



## Image Negative & Thresholding:

### ① Image Negative:

|    |    |    |    |
|----|----|----|----|
| 12 | 68 | 64 | 32 |
| 8  | 12 | 15 | 32 |
| 8  | 10 | 16 | 28 |
| 36 | 40 | 52 | 65 |

Original

How much is  $L = ?$

$$65 = 1000100$$

$$L = 2^n = 2^7 = 128$$

$$S = (L-1) - R = 127 - 80$$

|     |     |     |    |
|-----|-----|-----|----|
| 115 | 59  | 63  | 95 |
| 119 | 115 | 112 | 95 |
| 119 | 117 | 111 | 99 |
| 91  | 87  | 75  | 62 |

Negative Image

Problem ① :

Thresholding with  $T = 4$ .

|   |   |   |   |
|---|---|---|---|
| 4 | 3 | 5 | 2 |
| 3 | 6 | 4 | 6 |
| 2 | 2 | 6 | 5 |
| 7 | 6 | 4 | 1 |

$$\text{If } R = 0, 1, 2, 3 \Rightarrow S = 0 \\ R = 4, 5, 6, 7 \Rightarrow S = 7$$

$$S = \begin{cases} L-1 = 7; & R \geq 4 \\ 0; & R < 4. \end{cases}$$

$$L = ?$$

7 is max. number

$$14 \rightarrow 3 \text{ bit}$$

$$2^3 = 8 \therefore L = 8, L-1 = 7$$

$$S = (L-1) - R$$

Ans:

|                   |                   |                   |   |
|-------------------|-------------------|-------------------|---|
| $\frac{7-4}{2^3}$ | 0                 | $\frac{7-5}{2^2}$ | 0 |
| 0                 | $\frac{7-6}{2^1}$ | $\frac{7-4}{2^3}$ |   |
| 0                 | 0                 |                   |   |
| $\frac{7-7}{2^0}$ | $\frac{7-6}{2^1}$ | $\frac{7-4}{2^3}$ | 0 |
| = 0               | 21                | = 3               | 0 |

Zooming:  $\xleftarrow{\text{Zoom in}} \xrightarrow{\text{(Doubling Row & Column)}}$

|   |   |
|---|---|
| 4 | 3 |
| 3 | 6 |

$2 \times 2$

|   |   |   |   |
|---|---|---|---|
| 4 | 4 | 3 | 3 |
| 4 | 4 | 3 | 3 |
| 3 | 3 | 6 | 6 |
| 3 | 3 | 6 | 6 |

point operation.

Shrinking:

## Sampling & Quantization :-

D - 31/11/25

These are the processes used to convert analog signal into digital signal.

1) What is sampling?

→ The process of collecting data from an analog source at regular intervals.

→ It determines the special resolution of an image.

→ Digitizing the coordinate value is called sampling.

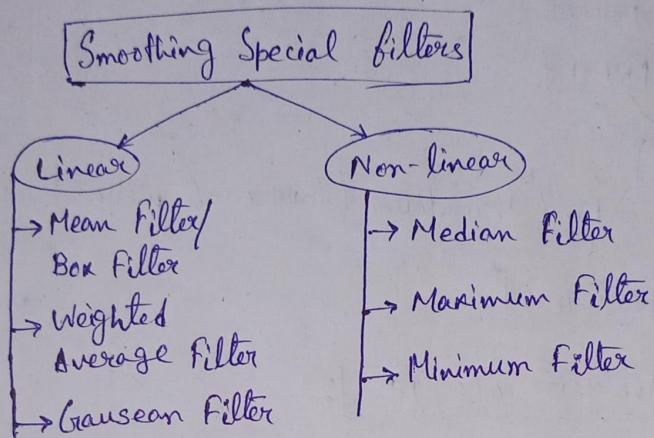
2) What is quantization?

→ The process of converting a continuous set of values into a discrete set of values.

→ Also digitizing the amplitude value is called quantization.

Smoothing Special filters are used for blurring and noise reduction.

- Bluring is used in Pre-processing task such as removal of small details from an image prior to (large) object extraction.
- Noise Reduction can be accomplished by blurring with a linear as well as non-linear filter.



Smoothing Linear Filters:- They are known as averaging or low-pass-filters as they are simply average of the pixels content in neighbourhood of the pixel.

The process in a result in an image with reduced sharp transition in intensity which ultimately leads to noise reduction.

(A) Mean Filter/Box Filter:- (B) Weighted Average Filter

$$\frac{1}{9} \alpha \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} \quad \left. \right\} \text{Mask}$$

- Gives more (less) weight to pixel near (away from) the output location.

(iii) Gaussian Filter:- Weights are samples of 2D gaussian filter.

$$g_{rs}(x, y) = \frac{1}{2\pi\sigma^2} e^{-\frac{(x^2+y^2)}{2\sigma^2}}$$

Blur Edge Reduce contrast

It is used to Blur image & reduce its contrast.

- Non Linear Filter / Order Statistical Filter :-

These response is based on ordering (ranking). The pixels containing image area encompassed by the filter and then replacing value of the pixel by the value determined the ranking result

Median Filter : - Median of the pixel values

Maximum Filter : - To find the maximum of all pixel values

Minimum Filter : - To find the minimum of all pixel values

- Median of the Pixel Values:-

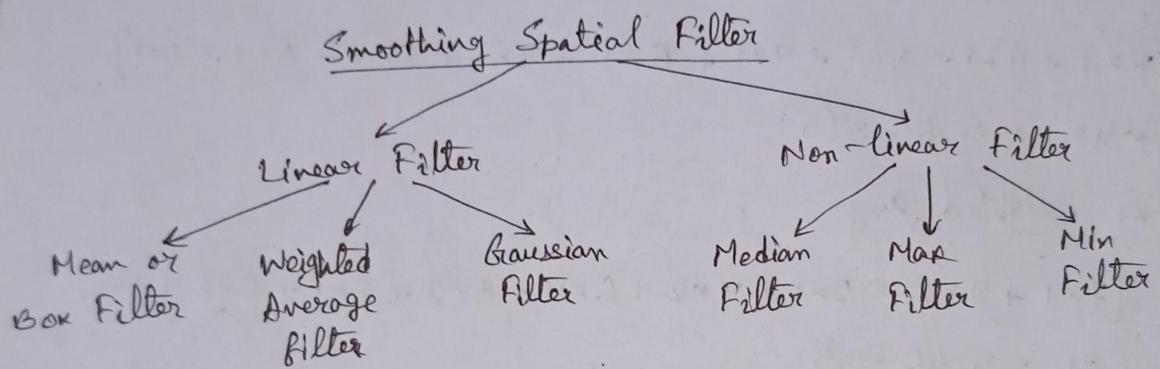
|   |   |   |
|---|---|---|
| 3 | 1 | 0 |
| 5 | 4 | 6 |
| 2 | 3 | 2 |

8, 7, 2, 1, ③, 8, 4, 5, 6  
↓  
Median

## Smoothing Spatial Filter:

Smoothing Spatial Filters are used for blurring and noise reduction.

- Blurring: Blurring is used in preprocessing task. Such as removal of small details from an image prior to object extraction.
- Noise reduction: It can be done by blurring with both linear and non-linear filters.



## Mask:

### ① Mean / Box filter

$$\frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} \quad 3 \times 3$$

### ② Weighted Avg. filter

$$\frac{1}{16} \begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix}$$

### ③ Gaussian Filter

$$G_G(x, y) = \frac{1}{2\pi\sigma^2} e^{-(x^2+y^2)/2\sigma^2}$$

For 2D,

$$\frac{1}{16} \begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix}$$

Qn: Consider the image and calculate the output of the pixel (2,2). If ~~the~~ smoothing is done using (3×3) neighbourhood. Mean Filters have it is used.

|           |   |   |     |     |   |   |   |
|-----------|---|---|-----|-----|---|---|---|
| $f(x, y)$ | 0 | 0 | 0   | 0   | 0 | 0 | 0 |
|           | 0 | 1 | 8   | 8   | 0 | 7 | 0 |
|           | 0 | 4 | (7) | 9   | 5 | 7 | 0 |
|           | 0 | 5 | 4   | (6) | 8 | 6 | 0 |
|           | 0 | 4 | 2   | 0   | 1 | 5 | 0 |
|           | 0 | 0 | 1   | 0   | 2 | 0 | 0 |
|           | 0 | 0 | 0   | 0   | 0 | 0 | 0 |
|           |   |   |     |     |   |   |   |

$$\frac{1}{9} [8 \times 1 + 9 \times 1 + 5 \times 1 + 4 \times 1 + 6 \times 1 + 8 \times 1 + 2 \times 1 + 0 \times 1 + 1 \times 1] \\ = \frac{1}{9} \times 42 = 4.66 \approx 5$$

⑧ For weighted Avg.

$$= \frac{1}{16} [7 \times 1 + 9 \times 2 + 5 \times 1 + 4 \times 2 + 6 \times 4 + 8 \times 2 + 2 \times 1 + 0 \times 2 + 1 \times 1] \\ = \frac{1}{16} \times 81 = 5.06 \approx ⑤$$

## Non-Linear Filter

i) Median Filter, [Mask is empty]. | let,  
 $\text{pos}(u_{i,j})$

if n is odd  
mid val  
else  
mid 2 avg

Let  $\text{pos} = (2, 2)$

Ans = 5

Max replace with max value

Min replace with min value

題 O padding :

|             |   |   |   |   |   |
|-------------|---|---|---|---|---|
| <u>ext:</u> | 0 | 0 | 0 | 0 | 0 |
|             | 0 | 2 | 2 | 2 | 0 |
|             | 0 | 1 | 0 | 1 | 0 |
|             | 0 | 8 | 0 | 5 | 0 |
|             | 0 | 0 | 0 | 0 | 0 |

(i) 0 padding

DIP

(ii) Pixel Examine

(iii) Convolution and Correlation

$$I = \{0\ 0\ 1\ 0\ 0\} \quad \text{mask} K = \{3\ 2\ 8\}$$

$$0\ 0\ 0\ 0\ 1\ 0\ 0\ 0\ 0$$

Step 1: Rotate the mask by 180  $\rightarrow$ i) ~~convolution~~

(ii)

$$0\ 0\ 0\ 0\ 1\ 0\ 0\ 0\ 0 \\ * (0\ 0\ 3\ 2\ 8\ 0\ 0)$$

$$8 \times 0 + 2 \times 0 + 3 \times 0$$

Qn) Let  $I = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$  be an image and  $K = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$  be the kernel/mask.

$$\begin{bmatrix} 3 & 4 \\ 1 & 2 \end{bmatrix} \rightarrow \begin{bmatrix} 4 & 3 \\ 2 & 1 \end{bmatrix}$$

$$\begin{array}{c|cc|c} & O_1 & O_2 & O_3 \\ \hline O_1 & 0 & 0 & 0 \\ O_2 & 0 & 3 & 3 \\ O_3 & 0 & 0 & 0 \end{array} \quad \begin{array}{c} 0 \\ 0 \\ 0 \end{array} \quad \Rightarrow \quad \begin{array}{ccc} 3 & 9 & 6 \\ 12 & 30 & 18 \\ 9 & 21 & 12 \end{array}$$

(i) 0 padding —

$$\begin{array}{c|cc|cc|c} & O_1 & O_2 & O_3 & O_4 & O_5 \\ \hline O_1 & 0 & 0 & 0 & 0 & 0 \\ O_2 & 0 & 3 & 2 & 1 & 0 \\ O_3 & 0 & 6 & 4 & 2 & 0 \\ O_4 & 0 & 3 & 1 & 5 & 0 \\ O_5 & 0 & 0 & 0 & 0 & 0 \end{array}$$

$$\rightarrow \quad \begin{array}{ccc} 0 & 2 & 0 \\ 2 & 3 & 1 \\ 0 & 2 & 0 \end{array}$$

(ii) Pixel Examine —

$$\begin{array}{c|cc|cc|c} & O_1 & O_2 & O_3 & O_4 & O_5 \\ \hline O_1 & 3 & 3 & 2 & 1 & 1 \\ O_2 & 3 & 3 & 2 & 1 & 1 \\ O_3 & 6 & 6 & 4 & 2 & 2 \\ O_4 & 3 & 3 & 1 & 5 & 5 \\ O_5 & 3 & 3 & 1 & 5 & 5 \end{array}$$

$$\rightarrow$$

$$\begin{array}{ccc} 3 & 2 & 2 \\ 3 & 3 & 2 \\ 3 & 3 & 4 \end{array}$$

1) Show the convolution & correlation for the image.

$$\text{Img. } I = \begin{bmatrix} 6 & 4 & 5 \\ 3 & 3 & 2 \\ 1 & 5 & 4 \end{bmatrix} \text{ where Kernel } K = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 3 & 2 \\ 2 & 4 & 5 \end{bmatrix}$$

Ans: Convolution:

Step 1: (Rotate K  $180^\circ$  clockwise):

$$K = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 3 & 2 \\ 2 & 4 & 5 \end{bmatrix} \rightarrow \begin{bmatrix} 2 & 4 & 1 \\ 4 & 3 & 2 \\ 5 & 2 & 3 \end{bmatrix} \rightarrow \begin{bmatrix} 5 & 4 & 2 \\ 2 & 3 & 4 \\ 3 & 2 & 1 \end{bmatrix} = \underline{\text{mask}}$$

Step 2:

padding to Img

Step 3:

Mask possible position and calculate to mask final image.

|   |   |   |   |   |
|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 |
| 0 | 6 | 4 | 5 | 0 |
| 0 | 3 | 3 | 2 | 0 |
| 0 | 1 | 5 | 4 | 0 |

$$(x) \text{Mask} = (6 \times 2) + (4 \times 3) + (5 \times 4) + (3 \times 3) + (2 \times 1)$$

$$= 12 + 12 + 20 + 9 + 6 + 2 = 61$$

$$(x) \text{Mask} = (4 \times 2) + (5 \times 3) + (3 \times 3) + (2 \times 2)$$

$$= 8 + 15 + 9 + 4$$

$$= 36$$

$$(x) \text{Mask} = (6 \times 3) + (4 \times 4) + (3 \times 2) + (3 \times 1)$$

$$= 18 + 16 + 6 + 3$$

$$= 43$$

$$\textcircled{1} (6 \times 4) + (4 \times 2) + (3 \times 3) + (3 \times 4) + (1 \times 2) + (5 \times 1)$$

$$= 24 + 8 + 9 + 12 + 2 + 5 = \textcircled{60}$$

$$\textcircled{2} (6 \times 5) + (4 \times 4) + (5 \times 2) + (3 \times 2) + (3 \times 3) + (2 \times 4) + (1 \times 3) + (5 \times 2) + (4 \times 1)$$

$$= 30 + 16 + 10 + 6 + 9 + 8 + 3 + 10 + 4 = \textcircled{96}$$

$$\textcircled{3} (4 \times 5) + (5 \times 4) + (3 \times 2) + (2 \times 3) + (5 \times 3) + (4 \times 2)$$

$$= 20 + 20 + 6 + 6 + 15 + 8 = \textcircled{75}$$

$$\textcircled{4} (3 \times 4) + (3 \times 2) + (1 \times 3) + (5 \times 4)$$

$$= 12 + 6 + 3 + 20 = \textcircled{41}$$

$$\textcircled{5} (3 \times 5) + (3 \times 4) + (2 \times 2) + (1 \times 2) + (5 \times 3) + (4 \times 4)$$

$$= 15 + 12 + 4 + 2 + 15 + 16 = \textcircled{64}$$

$$\textcircled{6} (3 \times 5) + (2 \times 4) + (5 \times 2) + (4 \times 3)$$

$$= 15 + 8 + 10 + 12 = \textcircled{45}$$

|    |    |    |
|----|----|----|
| 43 | 61 | 36 |
| 60 | 96 | 75 |
| 41 | 64 | 45 |

### Correlation:

Same as previous but without changing K. K is used as mask as it is.

|            |
|------------|
| Friday     |
| 5:10 pm    |
| Class Test |
| (DIP)      |
| Mark : 15  |

## Sharpening Special Filter

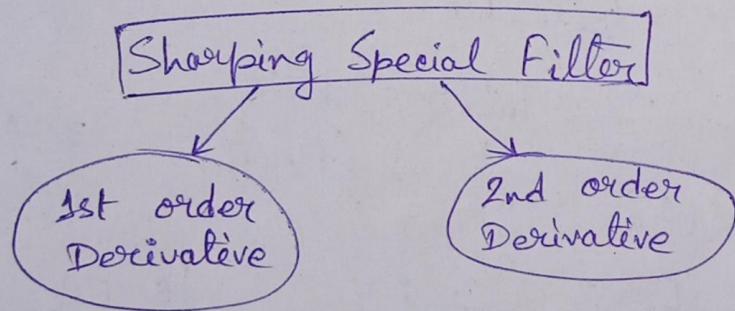
The principle objective is to highlight transition in intensity. Application include electronic printing medical imaging, industrial inspection.

- Blurring is pixel Averaging.
- Sharpening is special differentiation.

By sharpening  
we find  
boundary

Strength of the response of derivative operator is proportional to the degree of intensity discontinuity at the point of each operator apply.

Therefore image differentiation enhance edges and other discontinuity (such as Noise) and deemphathizes areas which have slowly varies.



- ⇒ It highlights grey level discontinuity in an image.
- ⇒ It ~~deemphasizes~~ deemphathizes is an image that slowly varies the image.

Wrap Around

# Sharpening Special Filter

(\*)

$$\text{I/P Image} = \begin{bmatrix} 8 & 5 & 4 \\ 0 & 6 & 2 \\ 1 & 3 & 7 \end{bmatrix}, \text{ Mask} = \begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

mask

|   |   |   |   |   |
|---|---|---|---|---|
| 7 | 1 | 3 | 7 | 1 |
| 4 | 8 | 5 | 4 | 8 |
| 2 | 0 | 6 | 2 | 0 |
| 7 | 1 | 3 | 7 | 1 |
| 4 | 8 | 5 | 4 | 8 |

WRAP AROUND

Step - 1

$$(7 \times 0 + 1 \times 1 + 3 \times 0 + 4 \times 1 + 8 \times (-4) + 5 \times 1 + 2 \times 0 + 0 \times 1 + 6 \times 0) \\ = (0 + 1 + 0 + 4 - 32 + 5 + 0 + 0) \\ = -22.$$

Step - 2

$$(1 \times 0 + 3 \times 1 + 7 \times 0 + 8 \times 1 + 5 \times (-4) + 4 \times 1 + 0 \times 0 + 6 \times 1 + 2 \times 0) \\ = (0 + 3 + 0 + 8 - 20 + 4 + 0 + 6 + 0) \\ = (11 - 20 + 10) = 1$$

Step - 3

$$(3 \times 0 + 7 \times 1 + 1 \times 0 + 5 \times 1 + 4 \times (-4) + 8 \times 1 + 6 \times 0 + 2 \times 1 + 0 \times 0) \\ = (0 + 7 + 0 + 5 - 16 + 8 + 0 + 2 + 0) \\ = 22 - 16 = 6$$

Step - 4

$$(4 \times 0 + 8 \times 1 + 5 \times 0 + 2 \times 1 + 0 \times -4 + 6 \times 1 + 7 \times 0 + 1 \times 1 + 3 \times 0) \\ = (0 + 8 + 0 + 2 - 0 + 6 + 0 + 1 + 0) \\ = 17$$

Step - 5

$$(8 \times 0 + 5 \times 1 + 4 \times 0 + 0 \times 1 + 6 \times (-4) + 2 \times 1 + 1 \times 0 + 3 \times 1 + 7 \times 0) \\ = (0 + 5 + 0 + 0 - 24 + 2 + 0 + 3 + 0) \\ = (-24 + 10) = -14$$

Step - 6

$$(5 \times 0 + 4 \times 1 + 8 \times 0 + 6 \times 1 + 2 \times -4 + 0 \times 1 + 3 \times 0 + 7 \times 1 + 1 \times 0) \\ = (0 + 4 + 0 + 6 - 8 + 0 + 0 + 7 + 0) = 17 - 8 = 9$$

### Step - 7

$$\begin{aligned}
 & (2 \times 0 + 0 \times 1 + 6 \times 0 + 7 \times 1 + 1 \times -4 + 3 \times 1 + 4 \times 0 + 8 \times 1 + 5 \times 0) \\
 & = (0 + 0 + 0 + 7 - 4 + 3 + 0 + 8 + 0) \\
 & = 18 - 4 = 14
 \end{aligned}$$

### Step - 8

$$\begin{aligned}
 & (0 \times 0 + 6 \times 1 + 2 \times 0 + 1 \times 1 + 3 \times -4 + 7 \times 1 + 8 \times 0 + 5 \times 1 + 4 \times 0) \\
 & = (0 + 6 + 0 + 1 - 12 + 7 + 0 + 5 + 0) \\
 & = 19 - 12 = 7
 \end{aligned}$$

### Step - 9

$$\begin{aligned}
 & (6 \times 0 + 2 \times 1 + 0 \times 0 + 3 \times 1 + 7 \times -4 + 1 \times 1 + 5 \times 0 + 4 \times 1 + 8 \times 0) \\
 & = (0 + 2 + 0 + 3 - 28 + 1 + 0 + 4 + 0) \\
 & = 10 - 28 = -18
 \end{aligned}$$

$$\begin{bmatrix} -22 & 1 & 6 \\ 17 & -14 & 9 \\ 14 & 7 & -18 \end{bmatrix}$$

Output Image

$$\begin{bmatrix} 0 & 1 & 6 \\ 17 & 0 & 9 \\ 14 & 7 & 0 \end{bmatrix}$$

Final Image

(Qn. 2)

$$\begin{bmatrix} 8 & 5 & 4 \\ 0 & 6 & 2 \\ 1 & 3 & 7 \end{bmatrix}$$

I/P Image

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & -8 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

Mask

(Here, Step - 1: Pixel Replication

Step - 2: Find the value in their position

Ans 2 -

Pixel Replication

$$\begin{array}{ccccc}
 8 & 8 & 5 & 4 & 4 \\
 8 & \boxed{8} & \boxed{5} & \boxed{4} & \boxed{4} \\
 0 & 0 & 6 & 2 & 2 \\
 1 & 1 & 3 & 7 & 7
 \end{array}$$

Mask

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & -8 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

$$\bullet (8 \times 1 + 5 \times 1 + 4 \times 1 + 0 \times 1 + 6 \times (-8) + 2 \times 1 + 1 \times 1 + 3 \times 1 + 7 \times 1)$$

$$= (8 + 5 + 4 + 0 - 48 + 2 + 1 + 3 + 7)$$

$$= 30 - 48 = \cancel{-18} = -18 \rightarrow 0$$

$$\bullet (5 \times 1 + 4 \times 1 + 4 \times 1 + 6 \times 1 + 2 \times (-8) + 2 \times 1 + 3 \times 1 + 7 \times 1 + 7 \times 1)$$

$$= (5 + 4 + 4 + 6 - 16 + 2 + 3 + 7 + 7)$$

$$= 38 - 16 = 22$$

Qn)

$$\begin{bmatrix} 1 & 2 & 3 & 2 \\ 4 & 2 & 5 & 1 \\ 1 & 2 & 6 & 3 \\ 2 & 6 & 4 & 7 \end{bmatrix}$$

Median Filter by Pixel  
Replication.

→ Apply pixel Replication

|   |   |   |   |   |   |
|---|---|---|---|---|---|
| 1 | 1 | 2 | 3 | 2 | 2 |
| 1 | 1 | 2 | 3 | 2 | 2 |
| 4 | 4 | 2 | 5 | 1 | 1 |
| 1 | 1 | 2 | 6 | 3 | 3 |
| 2 | 2 | 6 | 4 | 7 | 7 |
| 2 | 2 | 6 | 4 | 7 | 7 |

Step-1

For Pixel-1: 8 ✗ ✗ ✗ ✗ ② ✗ ✗ ✗ ✗

[2]

← increasing order

For Pixel-2: ✗ ✗ ✗ ✗ ② ✗ ✗ ✗ ✗

[2]

For Pixel -3:  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  ②  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$

$\boxed{2}$

For Pixel -4:  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  ②  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$

$\boxed{2}$

Step-2

For P-1  $\rightarrow$   $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  ②  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  K = 2

For P-2  $\rightarrow$   $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  ②  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  K = 2

For P-3  $\rightarrow$   $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  ②  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  K = 2

For P-4  $\rightarrow$   $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  ③  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  K = 3

Step-3

P-1:  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  ②  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  K = 2

P-2:  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  ④  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  K = 4

P-3:  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  ④  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  K = 4

P-4:  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  ④  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  K = 4

Step-4

P-1:  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  ②  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  K = 2

P-2:  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  ④  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  K = 4

P-3:  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  ⑥  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  K = 6

P-4:  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  ⑥  $\begin{matrix} \times & \times & \times & \times & \end{matrix}$  K = 6

Output Image:-

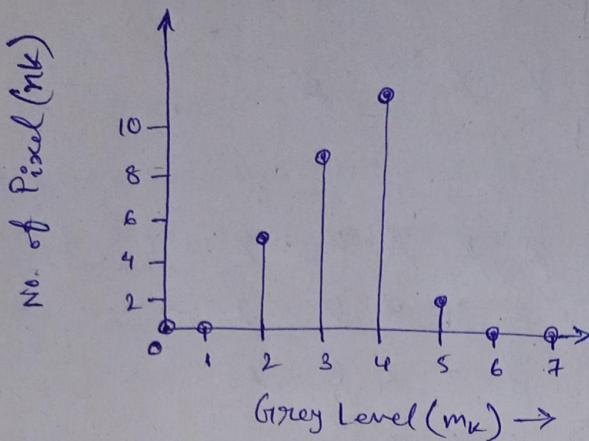
$$\begin{bmatrix} 2 & 2 & 2 & 2 \\ 2 & 2 & 2 & 3 \\ 2 & 4 & 4 & 4 \\ 2 & 4 & 6 & 6 \end{bmatrix}$$

Contrast Stretching

Bn. 2)

| Grey Level   | 0 | 1 | 2 | 3 | 4  | 5 | 6 | 7 |
|--------------|---|---|---|---|----|---|---|---|
| No. of Pixel | 0 | 0 | 5 | 8 | 10 | 2 | 0 | 0 |

Histogram of that given Image :-



$s = \text{gray level}$

$$\text{slope } (s) = \left( \frac{S_{\max} - S_{\min}}{r^o_{\max} - r^o_{\min}} \right) * (r^o - r^o_{\min}) + S_{\min}$$

$$S_{\max} = 7, S_{\min} = 0, r^o_{\max} = 5, r^o_{\min} = 2$$

when  $r^o = 2$ ,

$$s = \left( \frac{7-0}{5-2} \right) * (2-2) + 0 = \frac{7}{3} * 0 + 0 = 0$$

when  $r^o = 3$ ,

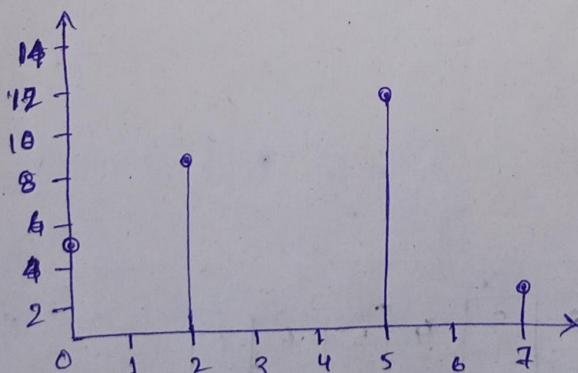
$$s = \left( \frac{7-0}{5-2} \right) * (3-2) + 0 = \frac{7}{3} * 1 + 0 = \frac{7}{3} = 2.3 \approx 2$$

when  $r^o = 4$

$$s = \left( \frac{7-0}{5-2} \right) * (4-2) + 0 = \frac{7}{3} * 2 = \frac{14}{3} \approx 5$$

when  $r^o = 5$

$$s = \left( \frac{7-0}{5-2} \right) * (5-2) + 0 = \frac{7}{3} * 3 = 7$$



Segmentation is the process to partition of image to multiple part of the image

in multiple criteria, like -

- pixel characteristics
- boundary of image
- color

Example :

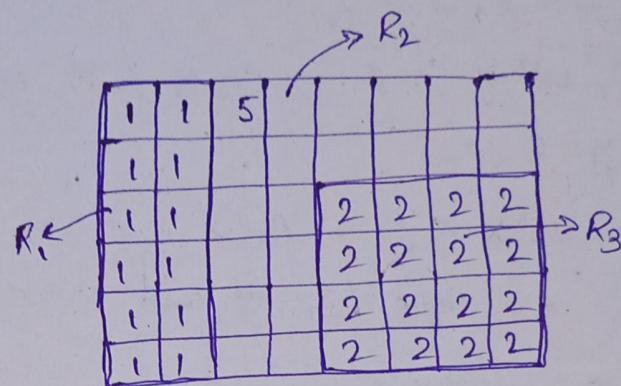
$$\text{Total pixel} = 8 \times 6 = 48$$

intensity

$$\rightarrow 1 = 12 \xrightarrow{\text{frequency}}$$

$$2 = 12$$

$$5 = 24$$



Purpose : To reduce noise, Iris detection  
To detect object,

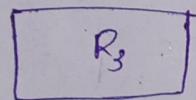
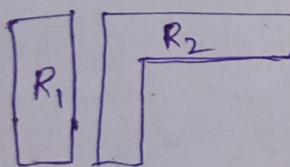
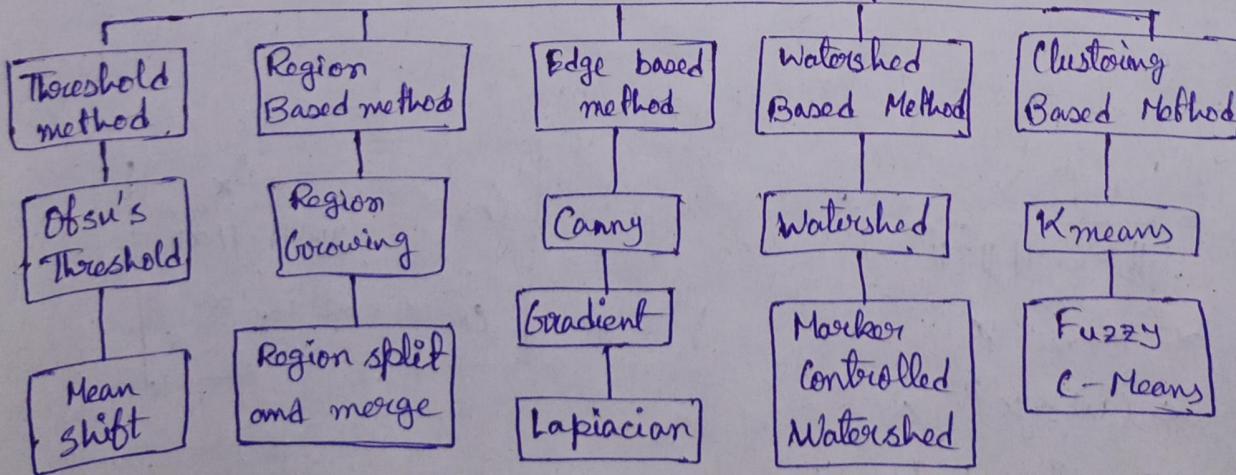


Image Segmentation

- Types



Thresholding

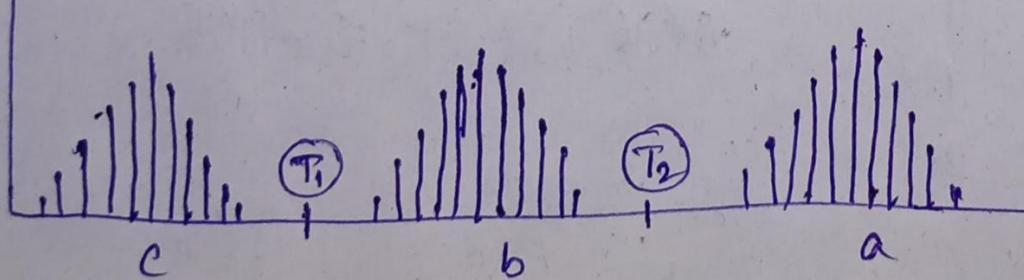
It is carried out with the assumption that the range of intensity levels being carried out by object of interest is different from background.

Steps:

- A Threshold  $T$  is selected
- Any point  $(x, y)$  in the image at which  $f(x, y) > T$  is called an object point.
- The segmented image denoted by  $g(x, y)$  given by

$$g(x, y) = \begin{cases} 1 & \text{if } f(x, y) > T \\ 0 & \text{if } f(x, y) \leq T \end{cases}$$

$$g(x, y) = \begin{cases} a & \text{if } f(x, y) > T_2 \\ b & \text{if } T_1 < f(x, y) \leq T_2 \\ c & \text{if } f(x, y) \leq T_1 \end{cases}$$



## Example

$$\text{let } T = \frac{5+3+9+2+1+7+8+4+2}{9}$$

$$\begin{bmatrix} 5 & 3 & 9 \\ 2 & 1 & 7 \\ 8 & 4 & 2 \end{bmatrix}$$

$$= \frac{41}{9} = 4.55 \approx 5$$

$$\textcircled{\$} \quad C_{T_1} = \{7, 8, 9\}$$

$$C_{T_2} = \{1, 2, 2, 3, 4, 5\}$$

$$M_1 = \frac{7+8+9}{3}$$

$$= \frac{24}{3} = \textcircled{8}$$

$$M_2 = \frac{1+2+2+3+4+5}{6}$$

$$= \frac{17}{6} = 2.83 = \textcircled{3}$$

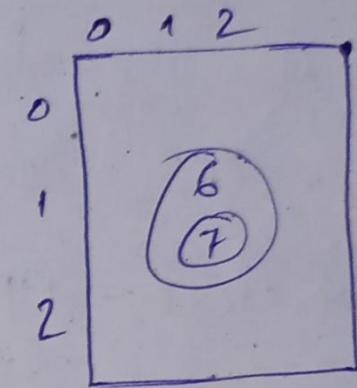
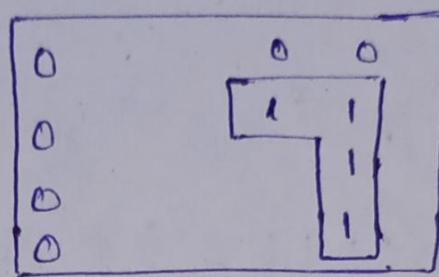
$$T = \frac{1}{2}(8+3)$$

$$= \frac{11}{2} = 5.5 = \underline{\underline{5}} \text{ Ans}$$

Region Growing :

Apply region growing on the following image with the initial point at (2,2) and threshold value as 2 by applying 4 connectivity. (By default 8 connection)

⇒ Absolute Difference = 2



$$7-6=1 \leq 2$$

Qn: Apply region growing on the image with seed point at 6 and threshold value is 3.

Sol:

Take any 6.

By default 8 connectivity,

Now, threshold = 3

∴ Absolute Difference = 3

Let the initial position for 6 is (0,1)

|                |   |                |   |   |   |   |
|----------------|---|----------------|---|---|---|---|
| 5 <sup>a</sup> | 6 | 6 <sup>a</sup> | 7 | 6 | 7 | 6 |
| 6 <sup>a</sup> | 7 | 6 <sup>a</sup> | 7 | 5 | 5 | 4 |
| 6 <sup>a</sup> | 6 | 4              | 4 | 3 | 2 | 5 |
| 5              | 4 | 5              | 4 | 2 | 3 | 4 |
| 0              | 3 | 2              | 3 | 3 | 2 | 4 |
| 0              | 0 | 0              | 0 | 2 | 2 | 5 |
| 1              | 1 | 0              | 1 | 0 | 3 | 4 |
| 1              | 0 | 1              | 0 | 2 | 3 | 5 |

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | 1 |
| 1 | 1 | 1 | 1 | 0 | 0 | 0 | 1 | 1 |
| 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |   |
| 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |   |
| 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |   |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

Consider the  
connectivity  
of 6 only.