1 Let G be a group of orders pq, where P and q are distinct primers. Prove that G is abelian.

Answers: False

Reason: Counter example 59, |59/26=2.3 but 53 is non-abelian.

2 Prove that if G is a group of order p2, where p is prime, then G is abelian if and only if it has P+1 subgroups of order P.

Answers: False

Reason: Every group of orders p2 is abelian. There are exactly two types: Cp2 and Cpxcp. The connect equivalence is:

"G= $Cp\times Cp\Leftrightarrow G$  has P+1 subgroups of orders P". Both groups are abelian.

13 Let G be the a finite group and H be a proper subgroup of G. Prove that the union of all conjugates on H cannot be equal to G.

Answers: False

Reason: For finite G the union of conjugates of a proper subgroup connot covers G. A finite group cannot be a union of finitely many proper subgroups.



6 Prove that in any group Gr, the set of clements of finite order forms a subgroup of Gr. a tall som

Answers: False

reliar

Reason: In abelian group yes; but not always. Example: Infinite dihedral group two reflections (orders 2) multiply to a notation of infinite order. I robro to egso, closière fails. Li plus bro di noisolo ei il

Answerd; False

6 Let G be a finite group and p be the smallest proine dividing 101. Prove that any subgroup of index pin G is types: cps and epxep. The connect equilamonis:

Boo of Answers: Travers did 149 and 200 pox 90 = 10

Reason: Action on casets gives homomorphism into sp; using smallest-prime property the image must force the subgroup to be nonmak. Don't ed is to !

1 Let G be a finite group and p be a prime number. If G has exactly one subgroup of order pk for each kin, where pri divides (Gil, prove that G hap a normal sylow most cover co. A finite group quong dust A . & aros tomos

Books that the union of all conjugates on H cannot be equal to

Answers: Trave Travel property property plans

Reason: Unique subgroup of orders pris the unique sylow p-subgroup and uniqueness implies noromality.