kiran\appdata\local\programs\python\python312\lib\site-packages (from statsmodels) (24.2) Requirement already satisfied: python-dateutil>=2.8.2 in c:\users\sai kiran\appdata\local\programs\python\python312\lib\site-packages (from pandas!=2.1.0,>=1.4->statsmodels) (2.9.0.post0) Requirement already satisfied: pytz>=2020.1 in c:\users\sai kiran\appdata\local\programs\python\python312\lib\site-packages (from pandas!=2.1.0,>=1.4->statsmodels) (2024.2) Requirement already satisfied: tzdata>=2022.7 in c:\users\sai kiran\appdata\local\programs\python\python312\lib\site-packages (from pandas!=2.1.0,>=1.4->statsmodels) (2024.2) Requirement already satisfied: six>=1.5 in c:\users\sai kiran\appdata\local\programs\python\python312\lib\site-packages (from pythondateutil>=2.8.2->pandas!=2.1.0,>=1.4->statsmodels) (1.16.0) [notice] A new release of pip is available: 25.0 -> 25.2 [notice] To update, run: python.exe -m pip install --upgrade pip [6]: import numpy as np import pandas as pd import seaborn as sns import matplotlib.pyplot as plt import statsmodels.api as sm from sklearn.model_selection import train_test_split from sklearn.linear_model import LinearRegression from sklearn.metrics import mean absolute error, mean squared error, r2_score from sklearn.preprocessing import LabelEncoder from sklearn.preprocessing import StandardScaler [7]: df = pd.read_csv("scrap price.csv", header=0) [8]: df [8]: ID symboling name fueltypes aspiration \ 0 1 3 alfa-romero giulia std gas 1 2 3 alfa-romero stelvio gas std 2 3 1 alfa-romero Quadrifoglio std gas 3 4 2 audi 100 ls std gas 4 5 2 audi 1001s gas std 200 201 -1 volvo 145e (sw) gas std 201 202 -1 volvo 144ea turbo gas 202 203 -1 volvo 244dl gas std 203 204 -1 volvo 246 diesel turbo 204 205 -1 volvo 264gl turbo gas

doornumbers

carbody drivewheels enginelocation wheelbase ... \

0	two	convertible		rwd		front	88	3.6	•••		
1	two	convertible		rwd		front	88	3.6			
2	two	hatchback		rwd		front	94	1.5			
3	four	sedan		fwd		front	99	8.6	•••		
4	four	sedan		4wd		front	99	9.4	•••		
	•••	•••	•••				•••				
200	four	sedan		rwd		front	109	9.1	•••		
201	four	sedan		rwd		front	109	9.1	•••		
202	four	sedan		rwd		front	front 109.1		•••		
203	four	sedan		rwd		front	109.1		•••		
204	four	sedan		rwd		front	109	9.1	•••		
	enginesize	fuelsystem	borerati	io str	oke	compressi	onratio	hors	еро	wer	\
0	130	mpfi	3.4	47 2	.68		9.0			111	
1	130	mpfi	3.4	47 2	.68		9.0			111	
2	152	mpfi	2.6	68 3	.47		9.0			154	
3	109	mpfi	3.3	19 3	.40		10.0			102	
4	136	mpfi	3.3	19 3	.40		8.0			115	
• •	•••	•••	•••	•••		•••	•••				
200	141	mpfi	3.7	78 3	.15		9.5			114	
201	141	mpfi	3.7	78 3	.15		8.7			160	
202	173	mpfi	3.5	58 2	.87		8.8			134	
203	145	idi	3.0	01 3	.40		23.0			106	
204	141	mpfi	3.7	78 3	.15		9.5			114	
	peakrpm cit			price							
0	5000	21		495.0							
1	5000	21	27 169	500.0							
2	5000	19		500.0							
3	5500	24		950.0							
4	5500	18	22 174	450.0							
• •	***		•••								
200	5400	23		845.0							
201	5300	19		045.0							
202	5500	18		485.0							
203	4800	26		470.0							
204	5400	19	25 226	625.0							

[205 rows x 26 columns]

 $name, \ fueltypes, \ aspiration, \ doornumbers, \ carbody, \ drive wheels, \ engine location, \ engine type, \ cylindernumber, \ fuelsystem$

[106]: df.info()

<class 'pandas.core.frame.DataFrame'>

Index: 202 entries, 0 to 204
Data columns (total 26 columns):

```
Column
 #
                        Non-Null Count
                                         Dtype
     _____
                        _____
 0
     ID
                        202 non-null
                                         int64
 1
                        202 non-null
                                         int64
     symboling
 2
     name
                        202 non-null
                                         int32
 3
     fueltypes
                                         int32
                        202 non-null
 4
     aspiration
                        202 non-null
                                         int32
 5
     doornumbers
                        202 non-null
                                         int32
 6
     carbody
                        202 non-null
                                         int32
 7
     drivewheels
                        202 non-null
                                         int32
 8
     enginelocation
                        202 non-null
                                         int32
 9
     wheelbase
                        202 non-null
                                         float64
                                         float64
 10
     carlength
                        202 non-null
                                         float64
 11
     carwidth
                        202 non-null
 12
     carheight
                        202 non-null
                                         float64
     curbweight
                        202 non-null
                                         int64
 13
 14
     enginetype
                        202 non-null
                                         int32
 15
     cylindernumber
                        202 non-null
                                         int32
 16
     enginesize
                        202 non-null
                                         int64
 17
     fuelsystem
                        202 non-null
                                         int32
 18
     boreratio
                        202 non-null
                                         float64
 19
     stroke
                                         float64
                        202 non-null
     compressionratio
                       202 non-null
                                         float64
     horsepower
                        202 non-null
                                         int64
 21
 22
     peakrpm
                        202 non-null
                                         int64
                                         int64
 23
     citympg
                        202 non-null
 24
                                         int64
     highwaympg
                        202 non-null
    price
                        202 non-null
                                         float64
dtypes: float64(8), int32(10), int64(8)
memory usage: 34.7 KB
```

Unique values in name:

```
2
      3
           1
               4
                    5
                        9
                            7
                                                  12
                                 6
                                      8
                                         10
                                             11
                                                      15
                                                           13
                                                               24
                                                                    25
                                                                        26
                                                                             35
 27
     32
         34
              29
                  28
                       30
                           33
                                31
                                     39
                                         43
                                             37
                                                  38
                                                      42
                                                           36
                                                               41
                                                                    44
                                                                        40
                                                                             47
 45
     46
         49
              48
                  50
                       52
                           51
                                61
                                     59
                                         58
                                             53
                                                  54
                                                      60
                                                           55
                                                               57
                                                                    56
                                                                        19
                                                                             17
 16
     22
         20
              23
                  62
                       65
                           64
                                68
                                    63
                                         66
                                             67
                                                  69
                                                       0
                                                           73
                                                               81
                                                                    76
                                                                        83
                                                                             77
 74
     78
         70
              79
                  71
                       72
                           80
                                82
                                         85
                                                      88
                                                           87
                                                                    89
                                    75
                                             84
                                                  86
                                                               92
                                                                             91
                           99 100 101 103 102 104 107 106 105 108 109 110
 94
     90
         98
              95
                  97
                       96
111 123 120 116 121 117 112 125 115 118 114 119 122 126 127 124 113 128
129 130 133 137 131 136 132 145 146 134 135 139 138 140 141 143 144 142]
```

Unique values in fueltypes:

```
[1 0]
      Unique values in aspiration:
      Unique values in doornumbers:
      Unique values in carbody:
      [0 2 3 4 1]
      Unique values in drivewheels:
      [2 1 0]
      Unique values in enginelocation:
      [0 1]
      Unique values in enginetype:
      [0 5 3 2 6 4 1]
      Unique values in cylindernumber:
      [2 3 1 4 5 6 0]
      Unique values in fuelsystem:
      [5 1 4 0 7 2 3 6]
[108]: df.isnull().sum()
[108]: ID
                            0
                            0
       symboling
       name
                            0
       fueltypes
                            0
       aspiration
                            0
       doornumbers
                            0
       carbody
       drivewheels
                            0
       enginelocation
                            0
       wheelbase
                            0
       carlength
                            0
       carwidth
                            0
       carheight
                            0
       curbweight
       enginetype
                            0
       cylindernumber
                            0
       enginesize
                            0
       fuelsystem
                            0
```

```
boreratio
                           0
       stroke
       compressionratio
                           0
      horsepower
                           0
      peakrpm
                           0
       citympg
                           0
      highwaympg
      price
                           0
      dtype: int64
[118]: le = LabelEncoder()
       for col in ["name", "fueltypes", "aspiration", "doornumbers", "carbody", __

¬"drivewheels", "enginelocation", "fuelsystem", "enginetype", "cylindernumber"]:
        df[col] = le.fit_transform(df[col])
      C:\Users\SAI KIRAN\AppData\Local\Temp\ipykernel_14788\384146120.py:3:
      SettingWithCopyWarning:
      A value is trying to be set on a copy of a slice from a DataFrame.
      Try using .loc[row_indexer,col_indexer] = value instead
      See the caveats in the documentation: https://pandas.pydata.org/pandas-
      docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
        df[col] = le.fit_transform(df[col])
      C:\Users\SAI KIRAN\AppData\Local\Temp\ipykernel_14788\384146120.py:3:
      SettingWithCopyWarning:
      A value is trying to be set on a copy of a slice from a DataFrame.
      Try using .loc[row indexer,col indexer] = value instead
      See the caveats in the documentation: https://pandas.pydata.org/pandas-
      docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
        df[col] = le.fit_transform(df[col])
      C:\Users\SAI KIRAN\AppData\Local\Temp\ipykernel_14788\384146120.py:3:
      SettingWithCopyWarning:
      A value is trying to be set on a copy of a slice from a DataFrame.
      Try using .loc[row_indexer,col_indexer] = value instead
      See the caveats in the documentation: https://pandas.pydata.org/pandas-
      docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
        df[col] = le.fit_transform(df[col])
      C:\Users\SAI KIRAN\AppData\Local\Temp\ipykernel_14788\384146120.py:3:
      SettingWithCopyWarning:
      A value is trying to be set on a copy of a slice from a DataFrame.
      Try using .loc[row_indexer,col_indexer] = value instead
      See the caveats in the documentation: https://pandas.pydata.org/pandas-
      docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
        df[col] = le.fit_transform(df[col])
```

C:\Users\SAI KIRAN\AppData\Local\Temp\ipykernel_14788\384146120.py:3:
SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame. Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy df[col] = le.fit transform(df[col])

C:\Users\SAI KIRAN\AppData\Local\Temp\ipykernel_14788\384146120.py:3: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame. Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy df[col] = le.fit_transform(df[col])

C:\Users\SAI KIRAN\AppData\Local\Temp\ipykernel_14788\384146120.py:3: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame. Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy df[col] = le.fit_transform(df[col])

C:\Users\SAI KIRAN\AppData\Local\Temp\ipykernel_14788\384146120.py:3: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame. Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy df[col] = le.fit_transform(df[col])

C:\Users\SAI KIRAN\AppData\Local\Temp\ipykernel_14788\384146120.py:3:
SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame. Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy df[col] = le.fit_transform(df[col])

C:\Users\SAI KIRAN\AppData\Local\Temp\ipykernel_14788\384146120.py:3: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame. Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy df[col] = le.fit_transform(df[col])

[119]:	df														
[119]:		ID	symbol	ing	name	fuelty	nes	aspii	rat	ion	doo	rnumbe	ers	carbody	\
	0	1	J	3	2	<i>J</i>	1	1		0			1	0	·
	1	2		3	3		1			0			1	0	
	2	3		1	1		1			0			1	2	
	3	4		2	4		1			0			0	3	
	4	5		2	5		1			0			0	3	
						•••		••				•••			
	200	201		-1	136		1			0			0	3	
	201	202		-1	135		1			1			0	3	
	202	203		-1	137		1			0			0	3	
	203	204		-1	139		0			1			0	3	
	204	205		-1	140		1			1			0	3	
	201	200		-	110		-			_			Ū	J	
		driv	ewheels	eng	ginelo	ocation	whee				engin		fu	elsystem	\
	0		2			0		88.6		•••		130		5	
	1		2			0		88.6		•••		130		5	
	2		2			0		94.				152		5	
	3		1			0		99.8	3.	•••		109		5	
	4		0			0		99.4	4.	•••		136		5	
	• •		•••			•••	•••	•••			•••		•••		
	200		2			0		109.		•••		141		5	
	201		2			0		109.		•••		141		5	
	202		2			0		109.		•••		173		5	
	203		2			0		109.		•••		145		3	
	204		2			0		109.	1.	•••		141		5	
		bore	ratio	strol	se co	ompressi	onra	tio l	hor	sep	ower	peakı	pm	citympg	\
	0		3.47	2.6	38		9	9.0			111	50	000	21	
	1		3.47	2.6	38		9	9.0			111	50	000	21	
	2		2.68	3.4	17		Ş	9.0			154	50	000	19	
	3		3.19	3.4	10		10	0.0			102	55	500	24	
	4		3.19	3.4	10		8	8.0			115	55	500	18	
			 2. 70					^ □	•••			 E/	100	00	
	200		3.78	3.				9.5			114		100	23	
	201		3.78	3.				8.7			160		300	19	
	202		3.58	2.8				8.8			134		500	18	
	203		3.01	3.4				3.0			106		300	26	
	204		3.78	3.	15		Ç	9.5			114	54	100	19	
		high	waympg	p	rice										
	0	J	27	_	95.0										
	1		27		0.0										
	2		26		0.0										
	3		30		50.0										
	_														

22 17450.0

```
200
                    28 16845.0
      201
                    25 19045.0
      202
                    23 21485.0
      203
                    27 22470.0
      204
                    25 22625.0
      [202 rows x 26 columns]
[120]: for col in ["name", "fueltypes", "aspiration", "doornumbers", "carbody",

¬"drivewheels", "enginelocation", "fuelsystem", "enginetype", "cylindernumber"]:
          print(f"Unique values in {col}:")
          print(df[col].unique())
          print()
      Unique values in name:
      Γ 2
             3
                 1
                     4
                         5
                             9
                                 7
                                     6
                                         8
                                            10
                                                11
                                                    12
                                                        14
                                                            13
                                                                21
                                                                     22
                                                                         23
                                                                             32
        24
           29
                31
                    26
                        25
                            27
                                    28
                                        36
                                            40
                                                34
                                                     35
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                                                             33
                                                                     41
                                                                         37
                                                                             44
                                30
                                                                 38
        42 43
                46 45
                       47
                            49
                                48
                                    58
                                        56
                                            55
                                                50
                                                    51
                                                         57
                                                             52
                                                                54
                                                                     53
                                                                             16
                                                                         17
        15
                                                            70
           19
                18
                    20
                        59
                            62
                                61
                                    65
                                        60
                                            63
                                                64
                                                     66
                                                                78
                                                                     73
                                                                         80
                                                                             74
        71
            75
                67
                    76
                        68
                            69
                                77
                                    79
                                        72
                                            82
                                                81
                                                    83
                                                        85
                                                            84
                                                                89
                                                                     86
                                                                             88
        91 87
                95 92 94
                            93 96
                                    97
                                        98 100
                                                99 101 104 103 102 105 106 107
       108 120 117 113 118 114 109 122 112 115 111 116 119 123 124 121 110 125
       126 127 130 134 128 133 129 142 143 131 132 136 135 137 138 140 141 139]
      Unique values in fueltypes:
      [1 0]
      Unique values in aspiration:
      [0 1]
      Unique values in doornumbers:
      [1 0]
      Unique values in carbody:
      [0 2 3 4 1]
      Unique values in drivewheels:
      [2 1 0]
      Unique values in enginelocation:
      [0 1]
      Unique values in fuelsystem:
      [5 1 4 0 7 2 3 6]
```

Unique values in enginetype:

```
[0 5 3 2 6 4 1]
Unique values in cylindernumber:
[2 3 1 4 5 6 0]
```

```
[138]: plt.figure(figsize=(20, 30))
       plt.subplot(6, 4, 1)
       sns.histplot(df["ID"], kde=True)
       plt.title("ID Distribution")
       plt.subplot(6, 4, 2)
       sns.histplot(df["symboling"], kde=True)
       plt.title("Symboling Distribution")
       plt.subplot(6, 4, 3)
       sns.histplot(df["wheelbase"], kde=True)
       plt.title("Wheelbase Distribution")
       plt.subplot(6, 4, 4)
       sns.histplot(df["carlength"], kde=True)
       plt.title("Car Length Distribution")
       plt.subplot(6, 4, 5)
       sns.histplot(df["carwidth"], kde=True)
       plt.title("Car Width Distribution")
       plt.subplot(6, 4, 6)
       sns.histplot(df["carheight"], kde=True)
       plt.title("Car Height Distribution")
       plt.subplot(6, 4, 7)
       sns.histplot(df["curbweight"], kde=True)
       plt.title("Curb Weight Distribution")
       plt.subplot(6, 4, 8)
       sns.histplot(df["enginesize"], kde=True)
       plt.title("Engine Size Distribution")
       plt.subplot(6, 4, 9)
       sns.histplot(df["boreratio"], kde=True)
       plt.title("Bore Ratio Distribution")
```

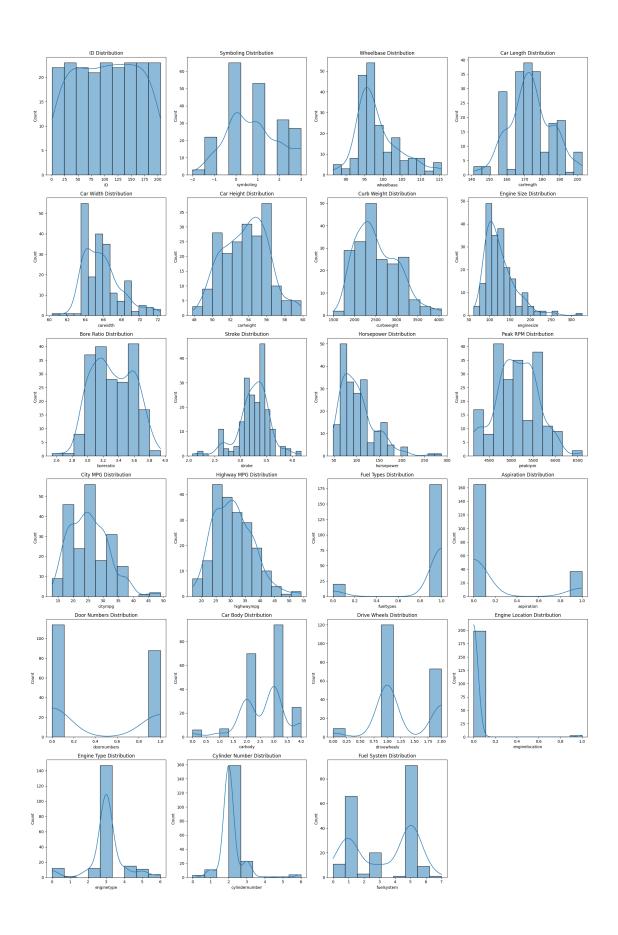
```
plt.subplot(6, 4, 10)
sns.histplot(df["stroke"], kde=True)
plt.title("Stroke Distribution")
plt.subplot(6, 4, 11)
sns.histplot(df["horsepower"], kde=True)
plt.title("Horsepower Distribution")
plt.subplot(6, 4, 12)
sns.histplot(df["peakrpm"], kde=True)
plt.title("Peak RPM Distribution")
plt.subplot(6, 4, 13)
sns.histplot(df["citympg"], kde=True)
plt.title("City MPG Distribution")
plt.subplot(6, 4, 14)
sns.histplot(df["highwaympg"], kde=True)
plt.title("Highway MPG Distribution")
plt.subplot(6, 4, 15)
sns.histplot(df["fueltypes"], kde=True)
plt.title("Fuel Types Distribution")
plt.subplot(6, 4, 16)
sns.histplot(df["aspiration"], kde=True)
plt.title("Aspiration Distribution")
plt.subplot(6, 4, 17)
sns.histplot(df["doornumbers"], kde=True)
plt.title("Door Numbers Distribution")
plt.subplot(6, 4, 18)
sns.histplot(df["carbody"], kde=True)
plt.title("Car Body Distribution")
plt.subplot(6, 4, 19)
sns.histplot(df["drivewheels"], kde=True)
plt.title("Drive Wheels Distribution")
plt.subplot(6, 4, 20)
sns.histplot(df["enginelocation"], kde=True)
plt.title("Engine Location Distribution")
plt.subplot(6, 4, 21)
```

```
sns.histplot(df["enginetype"], kde=True)
plt.title("Engine Type Distribution")

plt.subplot(6, 4, 22)
sns.histplot(df["cylindernumber"], kde=True)
plt.title("Cylinder Number Distribution")

plt.subplot(6, 4, 23)
sns.histplot(df["fuelsystem"], kde=True)
plt.title("Fuel System Distribution")

plt.tight_layout()
plt.show()
```



```
[]: for col in ['ID', 'symboling', 'name', 'fueltypes', 'aspiration', 'doornumbers',
              'carbody', 'drivewheels', 'enginelocation', 'wheelbase', 'carlength',
              'carwidth', 'carheight', 'curbweight', 'enginetype', 'cylindernumber',
              'enginesize', 'fuelsystem', 'boreratio', 'stroke', 'compressionratio',
              'horsepower', 'peakrpm', 'citympg', 'highwaympg']:
           skewness = df[col].skew()
           print(f"{col}: {skewness:.4f}")
 []: import numpy as np
       # Select numerical columns
       numerical_cols = df.select_dtypes(include=['int64', 'float64']).columns
       # Calculate IQR and detect outliers
       for col in numerical_cols:
            u= df[col].mean()+3*df[col].std()
            l= df[col].mean()-3*df[col].std()
            new_df=df[(df[col] > 1) & (df[col] < u)]
            print(f"Lower Bound: {1:.2f}")
           print(f"Upper Bound: {u:.2f}")
            print(f"Number of Outliers: {len(df[(df[col] < 1) | (df[col] > u)])}")
            print("-" * 40)
      #feature scaling
 []:
[121]: x=df.drop(columns=["price"])
       y=df["price"]
[122]: | x_train,x_test,y_train,y_test=train_test_split(x,y,train_size=0.
        →8,random_state=42)
[123]: scaler=StandardScaler()
       x train = scaler.fit transform(x train)
       x_test = scaler.transform(x_test)
[124]: model=LinearRegression()
       model.fit(x_train,y_train)
[124]: LinearRegression()
[125]: y_pred=model.predict(x_test)
```

```
[126]: y_pred
[126]: array([7718.14916098, 22492.36183881, 6177.15384872, 6126.93444074,
               8688.05400981, 5562.76555793, 25824.48871584, 10726.22757172,
               6549.38843621, 15687.2006342 , 23981.46576372, 5847.16554604,
              13152.98925893, 9192.36870874, 14252.71736997, 18128.01134665,
               8518.76295859, 5927.54435258, 9468.74449356, 23761.86947987,
              33988.98534401, 26079.6963596 , 9422.50362113, 7028.76969527,
              13235.47468467, 9927.67094441, 11637.41167553, 24741.67176995,
              26344.2484931 , 10713.72696751, 16127.76274912, 7978.07228839,
               8688.28498292, 7571.5078719, 13724.61987727, 16547.80703983,
               6789.76916364, 8755.85413747, 13935.37173256, 9097.04222499,
              14811.75628566])
[127]: print(np.array(y_test))
      [ 8249.
                  30760.
                             6855.
                                        9258.
                                                 11595.
                                                             5572.
                                                                      31600.
        9988.
                   8238.
                            11048.
                                       25552.
                                                  6918.
                                                             9989.
                                                                       8499.
       18420.
                  22470.
                            13645.
                                        6938.
                                                            28176.
                                                                      37028.
                                                  6989.
       36880.
                   9495.
                             7499.
                                       18344.
                                                 10595.
                                                             9279.
                                                                      28248.
                                                                       8449.
       31400.5
                   9960.
                            17859.167
                                       6295.
                                                 11845.
                                                             6669.
       11900.
                   7053.
                             7126.
                                        9639.
                                                  7689.
                                                            12629.
                                                                     ]
[128]: mae=mean_absolute_error(y_test,y_pred)
       mse=mean_squared_error(y_test,y_pred)
       r2=r2_score(y_test,y_pred)
[129]: print(mae)
       print(mse)
       print(r2)
      2814.9682227803123
      13158487.349704474
      0.8442938849126925
[130]: print(mae)
       print(mse)
       print(r2)
      2814.9682227803123
      13158487.349704474
      0.8442938849126925
      MAE (2087.31) \rightarrow \text{On average}, your predictions are off by about 2,087 units from the true value.
```

 R^2 (0.8441) \rightarrow Your model explains about 84.4% of the variance in the target variable, which is

MSE $(12,306,121.30) \rightarrow$ Average squared error — more sensitive to large errors than MAE.

pretty good.

1.1 Goal

1.1.1 Which variables are significant in predicting the price of a car

1.1.2 How well do those variables describe the price of a car

Bright green text Orange text

Use Ordinary Least Squares (OLS) regression to model the relationship between predictors and price.

This gives you coefficients (effect sizes) for each predictor.

```
[131]: X = sm.add_constant(x)
model = sm.OLS(y, X).fit()
```

[132]: model.summary()

[132]:

Dep. Variable:	price	R-squared:	0.903
Model:	OLS	Adj. R-squared:	0.890
Method:	Least Squares	F-statistic:	65.76
Date:	Sun, 10 Aug 2025	Prob (F-statistic):	6.08e-76
Time:	12:46:53	Log-Likelihood:	-1844.1
No. Observations:	202	AIC:	3740.
Df Residuals:	176	BIC:	3826.
Df Model:	25		
Covariance Type:	nonrobust		

	\mathbf{coef}	std err	\mathbf{t}	$\mathbf{P} > \mathbf{t} $	[0.025]	0.975]	
const	-6.85e + 04	1.56e + 04	-4.397	0.000	-9.92e+04	-3.78e + 04	
ID	17.2242	15.325	1.124	0.263	-13.019	47.468	
symboling	169.5141	235.520	0.720	0.473	-295.293	634.321	
name	-55.6512	22.328	-2.492	0.014	-99.716	-11.587	
fueltypes	7927.9070	5936.245	1.336	0.183	-3787.476	1.96e + 04	
aspiration	927.0383	796.915	1.163	0.246	-645.700	2499.777	
doornumbers	-1503.9515	578.993	-2.598 0.010		-2646.613	-361.290	
$\operatorname{carbody}$	-812.0330	329.206	-2.467	0.015	-1461.733	-162.333	
drivewheels	956.9898	484.357	1.976	0.050	1.095	1912.885	
enginelocation	1.279e + 04	1863.501	6.865	0.000	9114.607	1.65e + 04	
wheelbase	119.5865	96.625	1.238	0.217	-71.106	310.279	
$\operatorname{carlength}$	-81.3270	47.514	-1.712	0.089	-175.098	12.444	
$\operatorname{carwidth}$	696.4876	237.768	2.929	0.004	227.245	1165.730	
$\operatorname{carheight}$	213.0864	121.643	1.752	0.082	-26.981	453.154	
$\operatorname{curbweight}$	4.1149	1.459	2.820	0.005	1.236	6.994	
${f enginetype}$	-17.0960	212.586	-0.080	0.936	-436.642	402.450	
${f cylinder number}$	218.5759	340.392	0.642	0.522	-453.199	890.350	
enginesize	58.9541	16.271	3.623	0.000	26.842	91.066	
${ m fuelsystem}$	97.4657	136.195	0.716 0.475		-171.320	366.251	
boreratio	-1035.1074	977.739	-1.059 0.291		-2964.709	894.495	
stroke	-2146.7755	679.079	-3.161	0.002	-3486.962	-806.589	
${\it compression}$ ratio	667.3080	427.455	1.561	0.120	-176.289	1510.905	
horsepower	26.4721	16.654	1.590	0.114	-6.394	59.338	
$\mathbf{peakrpm}$	0.8654	0.594	1.458	0.147	-0.306	2.037	
${f citympg}$	-124.7998	147.283	-0.847	0.398	-415.468	165.869	
highwaympg	121.8359	130.725	0.932	0.353	-136.154	379.826	
Omnibus:		3.708 Du	708 Durbin-Watson:				
Prob(O:	${ m mnibus}):$	0.157 Jarque-Bera (JB):			4.342		
Skew:		0.072 Prob(JB) :			0.114		
Kurtosi	3.704 Co	nd. No.	5.42e + 05				

Notes:

 $p < 0.05 \rightarrow variable$ is statistically significant (strong evidence it affects price)

p $0.05 \rightarrow \text{variable may not have a meaningful effect in the model}$

const 0.000 Yes

name 0.004 Yes

carbody 0.019 Yes

enginelocat 0.000 Yes

carwidth 0.020 Yes

^[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

^[2] The condition number is large, 5.42e+05. This might indicate that there are strong multicollinearity or other numerical problems.

```
carheight 0.049 Yes
     enginesize 0.000 Yes
     stroke 0.000 Yes
     peakrpm 0.017 Yes
[133]: def backward_elimination(x,y,significance_level=0.05):
       x_modeled=x.copy()
       while True:
          model=sm.OLS(y,x_modeled).fit()
          p_values=model.pvalues
          max_p=p_values.max()
          if max_p>significance_level:
              exclude_var=p_values.idxmax()
              x_modeled=x_modeled.drop(columns=[exclude_var])
          else:
              break
       return x modeled, model
[134]: X_selected, final_model = backward_elimination(x, y)
[135]: print(final_model.summary())
                                   OLS Regression Results
                                           ------
     ======
     Dep. Variable:
                                  price
                                         R-squared (uncentered):
     0.973
                                    OLS
                                         Adj. R-squared (uncentered):
     Model:
     0.972
     Method:
                           Least Squares F-statistic:
     577.2
     Date:
                        Sun, 10 Aug 2025
                                        Prob (F-statistic):
     2.15e-142
     Time:
                               12:46:59
                                        Log-Likelihood:
     -1859.1
     No. Observations:
                                    202
                                         AIC:
     3742.
     Df Residuals:
                                    190
                                         BIC:
     3782.
     Df Model:
                                     12
     Covariance Type:
                              nonrobust
     ______
                               std err
                                                     P>|t|
                                                               [0.025
                        coef
                                               t
     0.975
```

name -20.865	-30.2187	4.742	-6.373	0.000	-39.572	
fueltypes -805.600	-2224.6109	719.387	-3.092	0.002	-3643.622	
doornumbers -516.220	-1491.7324	494.549	-3.016	0.003	-2467.245	
carbody -300.770	-901.7277	304.664	-2.960	0.003	-1502.685	
drivewheels 1810.741	1000.7328	410.645	2.437	0.016	190.724	
enginelocation	1.239e+04	1704.174	7.270	0.000	9027.309	
wheelbase 209.189	125.6764	42.338	2.968	0.003	42.164	
curbweight 6.875	4.7899	1.057	4.531	0.000	2.705	
enginesize 65.195	43.2993	11.100	3.901	0.000	21.404	
boreratio -755.315	-2458.1909	863.296	-2.847	0.005	-4161.066	
stroke -1571.157	-2703.4383	574.026	-4.710	0.000	-3835.720	
horsepower 76.043	54.9753	10.680	5.147	0.000	33.908	
Omnibus: Prob(Omnibus): Skew: Kurtosis:		5.826 0.054 0.100 3.980	Durbin-Wat	tson:		0.954 8.426 0.0148

Notes:

- [1] R^2 is computed without centering (uncentered) since the model does not contain a constant.
- [2] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [3] The condition number is large, 2.57e+04. This might indicate that there are strong multicollinearity or other numerical problems.

```
[136]: import matplotlib.pyplot as plt
  import seaborn as sns
  import numpy as np

plt.figure(figsize=(8,6))

# Scatter plot: actual vs predicted
```

