Question 10.13.2.6 Probability and Random Processes

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Question 10.13.2.6:

A game consists of spinning an arrow which comes to rest pointing at one of the regions (1, 2 or 3) (Fig. 13.1). Are the outcomes 1, 2 and 3 equally likely to occur? Give reasons.

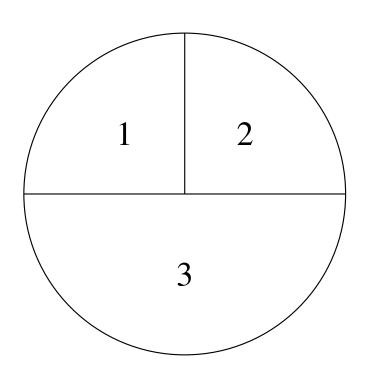


Fig. 0. Fig.13.1

Solution:

Let, the probability mass function

$$p_X(k) = \frac{\text{Angle covered by region k}}{\text{Total angle}}$$
 (1)

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$$\therefore p_X(1) = \frac{90^{\circ}}{360^{\circ}} = \frac{1}{4}$$
 (2)

$$=0.25\tag{3}$$

$$p_X(2) = \frac{90^\circ}{360^\circ} = \frac{1}{4} \tag{4}$$

$$=0.25\tag{5}$$

$$p_X(3) = \frac{180^{\circ}}{360^{\circ}} = \frac{1}{2} \tag{6}$$

$$=0.5\tag{7}$$

$$\therefore p_X(k) = \begin{cases} 0.25 & , k = 1 \\ 0.25 & , k = 2 \\ 0.5 & , k = 3 \end{cases}$$
 (8)

 $p_X(k)$ are not equal for all k. Therefore, the events are not equally likely.