NCERT 11.16.3.33

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Question:11.16.3.33

If A and B are two candidates seeking admission in an engineering College. The probability that A is selected is 0.5 and the probability that both A and B are selected is atmost 0.3. Is it possible that the probability of B getting selected is 0.7?

Solution:

Define a random variables X as:

 $Pr((X = 0) + (X = 1)) \le 1$

Parameter	Value	Description
X	X=0	Probability of A beging selected
	X=1	Probability of B beging selected

TABLE 0: Random Variables

Given that,

$$\Pr((X=0)(X=1)) \le 0.3 \tag{1}$$

$$p_X(0) = 0.5 (2)$$

(3)

We know that.

$$\Pr((X = 0) + (X = 1)) = p_X(0) + p_X(1) - \Pr((X = 0)(X = 1))$$

$$(4)$$

$$\implies \Pr((X = 0)(X = 1)) = p_X(0) + p_X(1) - \Pr((X = 0) + (X = 1))$$

$$(5)$$

$$\implies p_X(0) + p_X(1) - \Pr((X = 0) + (X = 1)) \le 0.3$$

$$\implies p_X(0) + p_X(1) \le 0.3 + \Pr((X = 0) + (X = 1))$$

$$(7)$$

$$\implies p_X(0) + p_X(1) \le 0.3 + 1$$

$$(8)$$

$$\implies p_X(0) + p_X(1) \le 1.3$$

$$(9)$$

$$\implies p_X(1) \le 0.8$$

$$(10)$$

 \therefore It is possible that the probability of B getting selected is 0.7.

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