

12.478

EE25BTECH11049 - Sai Krishna Bakki

Question:

A force $\mathbf{P} = \begin{pmatrix} 2 \\ -5 \\ 6 \end{pmatrix}$ acts on a particle. The particle is moved from point \mathbf{A} to point \mathbf{B} , where the position vectors of \mathbf{A} and \mathbf{B} are $\begin{pmatrix} 6 \\ 1 \\ -3 \end{pmatrix}$ and $\begin{pmatrix} 4 \\ -3 \\ -2 \end{pmatrix}$ respectively. The work done is

Solution:

Given

$$\text{Force } \mathbf{P} = \begin{pmatrix} 2 \\ -5 \\ 6 \end{pmatrix}, \mathbf{A} = \begin{pmatrix} 6 \\ 1 \\ -3 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 4 \\ -3 \\ -2 \end{pmatrix} \quad (1)$$

Work done is given by

$$\mathbf{P}^T (\mathbf{B} - \mathbf{A}) \quad (2)$$

$$\Rightarrow (2 \quad -5 \quad 6) \left(\begin{pmatrix} 4 \\ -3 \\ -2 \end{pmatrix} - \begin{pmatrix} 6 \\ 1 \\ -3 \end{pmatrix} \right) \quad (3)$$

$$\Rightarrow (2 \quad -5 \quad 6) \begin{pmatrix} -2 \\ -4 \\ 1 \end{pmatrix} \quad (4)$$

$$\Rightarrow -4 + 20 + 6 = 22 \quad (5)$$

\therefore The work done is 22 J.

3D Visualization of Force and Displacement

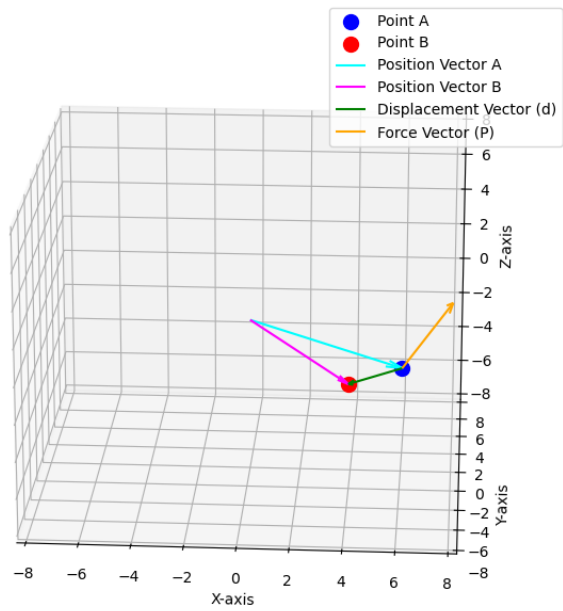


Fig. 1