EE25BTECH11049 - Sai Krishna Bakki

Question:

Solve the following system of linear equations.

$$5x + 2y = 4$$

$$7x + 3y = 5$$

Solution:

The equation of line L_1 is,

$$(5 \quad 2)\mathbf{x} = 4$$
 (1)

The equation of line L_2 is,

$$\begin{pmatrix} 7 & 3 \end{pmatrix} \mathbf{x} = 5 \tag{2}$$

On putting the equations in a matrix, we will get

$$\implies \begin{pmatrix} 5 & 2 \\ 7 & 3 \end{pmatrix} \mathbf{x} = \begin{pmatrix} 4 \\ 5 \end{pmatrix} \tag{3}$$

So the augmented matrix is,

$$\begin{pmatrix} 5 & 2 & | & 4 \\ 7 & 3 & | & 5 \end{pmatrix} \tag{4}$$

$$\begin{pmatrix} 5 & 2 & | & 4 \\ 7 & 3 & | & 5 \end{pmatrix} s \xrightarrow{R_2 \to R_2 - \frac{7}{5}R_1} \begin{pmatrix} 5 & 2 & | & 4 \\ 0 & \frac{1}{5} & | & \frac{-3}{5} \end{pmatrix}$$
 (5)

$$\begin{pmatrix} 5 & 2 & | & 4 \\ 0 & \frac{1}{5} & | & \frac{-3}{5} \end{pmatrix} \xrightarrow{R_2 \to 5R_2} \begin{pmatrix} 5 & 2 & | & 4 \\ 0 & 1 & | & -3 \end{pmatrix}$$
 (6)

$$\begin{pmatrix} 5 & 2 & | & 4 \\ 0 & 1 & | & -3 \end{pmatrix} \xrightarrow{R_1 \to R_1 - 2R_2} \begin{pmatrix} 5 & 0 & | & 10 \\ 0 & 1 & | & -3 \end{pmatrix} \tag{7}$$

$$\begin{pmatrix} 5 & 0 & 10 \\ 0 & 1 & -3 \end{pmatrix} \xrightarrow{R_1 \to \frac{1}{5}R_1} \begin{pmatrix} 1 & 0 & 2 \\ 0 & 1 & -3 \end{pmatrix}$$
 (8)

$$\implies \mathbf{x} = \begin{pmatrix} 2 \\ -3 \end{pmatrix} \tag{9}$$

Therefore the two lines will intersect at $\begin{pmatrix} 2 \\ -3 \end{pmatrix}$.

