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Fa19-bcs-125

G II

Assig#5

Q1. Compute the BoW model, TF model, and IDF model for each of the terms in the following three sentences.

Then calculate the TF.IDF values.

S1 “sunshine state enjoy sunshine”

S2 “brown fox jump high, brown fox run”

S3 “sunshine state fox run fast”

Q2. Compute the cosine similarity between S1 and S3.

Solution

Words:

S1 “sunshine state enjoy sunshine”

S2 “brown fox jump high, brown fox run”

S3 “sunshine state fox run fast”

Vocabulary

'brown', 'enjoy', 'fast', 'fox', 'high', 'jump', 'run', 'state', 'sunshine'

BOW model

	'brown'	'enjoy'	'fast'	'fox'	'high'	'jump'	'run'	'state'	'sunshine'	Total
S1	0	1	0	0	0	0	0	1	2	4
S2	2	0	0	2	1	1	1	0	0	7
S3	0	0	1	1	0	0	1	1	1	5

Term frequencies

$$Tf = Val/total$$

	'brown'	'enjoy'	'fast'	'fox'	'high'	'jump'	'run'	'state'	'sunshine'	Total
S1	0	1/4	0	0	0	0	0	1/4	2/4	4
S2	2/7	0	0	2/7	1/7	1/7	1/7	0	0	7
S3	0	0	1/5	1/5	0	0	1/5	1/5	1/5	5

IDF

$$Idf(\text{word}) = \log(\text{total}/\text{value of word})$$

S1: “sunshine state enjoy sunshine”

$$Idf(\text{“sunshine”}) = \log(3/2) = 0.176$$

$$Idf(\text{“state”}) = \log(3/2) = 0.176$$

$$Idf(\text{“enjoy”}) = \log(3/1) = 0.477$$

S2: “brown fox jump high, brown fox run”

$$Idf(\text{“brown”}) = \log(3/1) = 0.477$$

$$Idf(\text{“fox”}) = \log(3/2) = 0.176$$

$$Idf(\text{“jump”}) = \log(3/1) = 0.477$$

$$Idf(\text{“high”}) = \log(3/1) = 0.477$$

$$Idf(\text{“run”}) = \log(3/2) = 0.176$$

S3: “sunshine state fox run fast”

$$Idf(\text{“sunshine”}) = \log(3/2) = 0.176$$

$$Idf(\text{“state”}) = \log(3/2) = 0.176$$

$$Idf(\text{“fox”}) = \log(3/2) = 0.176$$

$$Idf(\text{“run”}) = \log(3/2) = 0.176$$

$$Idf(\text{“fast”}) = \log(3/1) = 0.477$$

	'brown'	'enjoy'	'fast'	'fox'	'high'	'jump'	'run'	'state'	'sunshine'	Total
S1	0	0.477	0	0	0	0	0	0.176	0.176	4
S2	0.477	0	0	0.176	0.477	0.477	0.176	0	0	7
S3	0	0	0.477	0.176	0	0	0.176	0.176	0.176	5

Tf-idf

	'brown'	'enjoy'	'fast'	'fox'	'high'	'jump'	'run'	'state'	'sunshine'	Total
S1	0	0.119	0	0	0	0	0	0.044	0.088	4
S2	0.136	0	0	0.050	0.068	0.068	0.025	0	0	7
S3	0	0	0.095	0.035	0	0	0.035	0.035	0.035	5

Q2

Cosine Similarity between S1 and S3

TF Vector:

S1= [2/4, 1/4, 1/4, 0, 0, 0, 0, 0, 0]

S3 = [1/5, 1/5, 0, 0, 1/5, 0, 0, 1/5, 1/5]

$S1 \cdot S3 = 2/4 * 1/5 + 1/4 * 1/5 + 1/4 * 0 + 0 * 0 + 0 * 1/5 + 0 * 0 + 0 * 0 + 0 * 1/5 + 0 * 1/5$

$S1.S3 = 0.15000$

$|S1| = (2/4 * 2/4 + 1/4 * 1/4 + 1/4 * 1/4 + 0 * 0 + 0 * 0 + 0 * 0 + 0 * 0 + 0 * 0 + 0 * 0)^{1/2}$

$|S1| = 0.61237$

$|S3| = (1/5 * 1/5 + 1/5 * 1/5 + 0 * 0 + 0 * 0 + 1/5 * 1/5 + 0 * 0 + 0 * 0 + 1/5 * 1/5 + 1/5 * 1/5)^{1/2}$

$|S3| = 0.44721$

The Cosine similarity between S1 and S3 are as below:

$COS(S1,S3) = 0.15/0.61237*0.44721$

$COS(S1,S3) = 0.54773$

