

## 5.2 Solve by means of Gaussian elimination

You should indicate the decomposition  $PA=LU$

$$\begin{cases} 4x_1 + 5x_2 + 6x_3 = 28 \\ 2x_1 - 7x_3 = 29 \\ -5x_1 - 8x_2 = -64 \end{cases} \xrightarrow{l_1 \leftrightarrow l_3} \left[ \begin{array}{ccc|c} -5 & -8 & 0 & -64 \\ 2 & 0 & -7 & 29 \\ 4 & 5 & 6 & 28 \end{array} \right] \xrightarrow{\begin{array}{l} l_2 \leftarrow l_2 + \frac{2}{5}l_1 \\ l_3 \leftarrow l_3 + \frac{4}{5}l_1 \end{array}} \left[ \begin{array}{ccc|c} -5 & -8 & 0 & -64 \\ 0 & -16/5 & -7/3 & 17/5 \\ 0 & -7/5 & 6 & -116/5 \end{array} \right]$$

$$\xrightarrow{l_3 \leftarrow l_3 - \frac{7}{16}l_2} \left[ \begin{array}{ccc|c} 5 & -8 & 0 & 64 \\ 0 & -16/5 & -7/3 & 17/5 \\ 0 & 0 & 47/16 & 395/16 \end{array} \right]$$

$$\begin{matrix} P & A & L & U \end{matrix}$$

$$\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix} \times \begin{bmatrix} 4 & 5 & 6 \\ 2 & 0 & -1 \\ -5 & -8 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ -2/5 & 1 & 0 \\ -4/5 & 7/16 & 1 \end{bmatrix} \times \begin{bmatrix} 5 & -8 & 0 \\ 0 & -16/5 & -7 \\ 0 & 0 & 47/16 \end{bmatrix}$$