

Linear Algebra Scalars

- `x = np.array(3.0)`
- `y = np.array(2.0)`
- `x + y, x * y, x / y, x ** y`
- o/p
- `(array(5.), array(6.), array(1.5), array(9.))`

Linear Algebra ... Matrices

- We have already discussed about length dimensionality and shape.
- `A = np.arange(20).`
- `reshape(5, 4)`
- `A`
- o/p

```
array([[ 0.,  1.,  2.,  3.],  
       [ 4.,  5.,  6.,  7.],  
       [ 8.,  9., 10., 11.],  
       [12., 13., 14., 15.],  
       [16., 17., 18., 19.]])
```

Linear Algebra ...

Matrices...Transpose of a Matrix

- A.T

```
array([[ 0.,  4.,  8., 12., 16.],  
       [ 1.,  5.,  9., 13., 17.],  
       [ 2.,  6., 10., 14., 18.],  
       [ 3.,  7., 11., 15., 19.]])
```

Linear Algebra ...

Transpose of a Matrix

- As a special type of the square matrix, a symmetric matrix A is equal to its transpose: $A = A^T$.
- `B = np.array([[1, 2, 3], [2, 0, 4], [3, 4, 5]])`
- `B`

```
array([[1., 2., 3.],  
       [2., 0., 4.],  
       [3., 4., 5.]])
```

Linear Algebra ...

Matrices...Transpose of a Matrix

- Now we compare B with its transpose.
- o/p

```
array([[ True,  True,  True],  
       [ True,  True,  True],  
       [ True,  True,  True]])
```

Linear Algebra

Basic Properties of Tensor Arithmetic

- Scalars, vectors, matrices, and tensors (“tensors” in this subsection refer to algebraic objects) of an arbitrary number of axes have some nice properties that often come in handy.
- For example
- Two tensors with the same shape, the result of any binary element wise operation will be a tensor of that same shape.

Linear Algebra

Basic Properties of Tensor Arithmetic....

- `A = np.arange(20).reshape(5, 4)`
- `B = A.copy()` # Assign a copy of `A` to `B` by allocating new memory
`A, A + B`

```
(array([[ 0.,  1.,  2.,  3.],  
       [ 4.,  5.,  6.,  7.],  
       [ 8.,  9., 10., 11.],  
       [12., 13., 14., 15.],  
       [16., 17., 18., 19.]]),  
 array([[ 0.,  2.,  4.,  6.],  
       [ 8., 10., 12., 14.],  
       [16., 18., 20., 22.],  
       [24., 26., 28., 30.],  
       [32., 34., 36., 38.]])
```

Linear Algebra

Sum and Dot Product

- `x = np.arange(4)` x,
- `x.sum()`
- o/p
- `(array([0., 1., 2., 3.]), array(6.))`

- `y = np.ones(4)`
- `x, y, np.dot(x, y)`
- o/p
- `(array([0., 1., 2., 3.]), array([1., 1., 1., 1.]), array(6.))`

Linear Algebra

Matrix-Vector Products

- $A=[1,2,3,4]$
- `np.dot(A,2)`
- o/p
- `array([2, 4, 6])`

Matrix-Matrix Multiplication

- $A=[1 \ 2 \ 3]$
- $B=[2,3,4]$
- `Np.dot(A,B)`
- o/p
- 20

$$C = AB = \begin{bmatrix} \mathbf{a}_1^\top \\ \mathbf{a}_2^\top \\ \vdots \\ \mathbf{a}_n^\top \end{bmatrix} \begin{bmatrix} \mathbf{b}_1 & \mathbf{b}_2 & \cdots & \mathbf{b}_m \end{bmatrix}$$

Matrix-Matrix Multiplication...

- `B = np.ones(shape=(4, 3))`
- `np.dot(A, B)`