

Deep Learning-I

by

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MODULE-2

Mathematical background for Deep learning:

- Data Manipulation**
- Data Preprocessing**
- Linear Algebra**
- Calculus**
- Probability**

Probabilty

- Machine learning is all about making predictions.
- We might want to predict the probability of a patient suffering a heart attack in the next year, given their clinical history.
- Distinguishing cats and dogs based on photographs.
- This might sound simple but it is actually a formidable challenge.
- The difficulty of the problem may depend on the resolution of the image.

Probabilty...



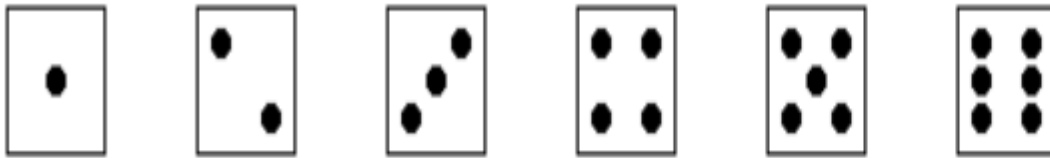
Images of varying resolutions (10×10 , 20×20 , 40×40 , 80×80 , and 160×160 pixels).

Probabilty...

- While it is easy for humans to recognize cats and dogs at the resolution of 160×160 pixels, it becomes challenging at 40×40 pixels and next to impossible at 10×10 pixels.
- Our ability to tell cats and dogs apart at a large distance (and thus low resolution) might approach uninformed guessing. Probability gives us a formal way of reasoning about our level of certainty.

Write a Python program which will roll a dice and decides the probability of it.

- All of the outcomes of this experiment are shown below pictorially.



- All of the outcomes of this experiment are shown below as a list.

If each face is represented by a numeral of the number of dots on the face; the following represents all of the outcomes:

$\{ 1, 2, 3, 4, 5, 6 \}$

Roll a dice and decides the probability of it....

```
• import random
    rolled = []
• rolledtimes = 0;
• biggest = []
•
    freq = int(input('How many times would you like to roll the dice? '))
•
    def roll():
•        rand = random.randrange(1,7)
•        return rand
• def probability():
•     for i in range(0,6):
•         print('Calculation of probability:')
•         percentage = "{:.2f}".format((count[i] / freq)*100)
•         percent = str(percentage) + '%'
```

Roll a dice and decides the probability of it....

- `def theoretical():`
 - `result = "{:.2f}".format((1/6)*freq)`
 - `denominator = "{:.2f}".format(((1/6)*freq)*6)`
 - `print('\nIn theory, each dice should roll {} out of {} times'.format(result, denominator))`
- `def findBiggest():`
- `for i in range(1, 7):`
 - `biggest.append(rolled.count(i))`
- `print('\n', 'The most times a dice is rolled is', max(biggest), 'times')`

Roll a dice and decides the probability of it....

- `def findSmallest():`
- `for i in range(1, 7):`
- `biggest.append(rolled.count(i))`
- `print('\n`
`n', 'The least times a dice is rolled is', min(biggest)`
`, 'times')`
- `for i in range(1, freq + 1):`
- `number = roll()`
- `rolled.append(number)`
- `rolledtimes+=1`

Roll a dice and decides the probability of it....

- `count = [rolled.count(1),rolled.count(2),rolled.count(3),rolled.count(4),rolled.count(5),rolled.count(6)]`
- `print('After being rolled {} times:\n\n1 is rolled {} times\n2 is rolled {} times\n3 is rolled {} times\n4 is rolled {} times\n5 is rolled {} times\n6 is rolled {} times\nn'.format(rolledtimes,count[0],count[1],count[2],count[3],count[4],count[5]))`
- `probability()`
- `findBiggest()`
- `findSmallest()`
- `theoretical()`

OUTPUT

```
How many times would you like to roll the dice? 1000  
After being rolled 1000 times:
```

```
1 is rolled 180 times  
2 is rolled 161 times  
3 is rolled 190 times  
4 is rolled 145 times  
5 is rolled 162 times  
6 is rolled 162 times
```

```
Calculation of probability:
```

```
1 : 18.00%
```

```
Calculation of probability:
```

```
2 : 16.10%
```

```
Calculation of probability:
```

```
3 : 19.00%
```

```
Calculation of probability:
```

```
4 : 14.50%
```

```
Calculation of probability:
```

```
5 : 16.20%
```

```
Calculation of probability:
```

```
6 : 16.20%
```

```
The most times a dice is rolled is 190 times
```

```
The least times a dice is rolled is 145 times
```

```
In theory, each dice should roll 166.67 out of 1000.00 times
```

Python code for finding the probability of tossing a coin

- `import collections`
- `import itertools`
- `from fractions import Fraction`
- `def fibonacci_nth(size):`
 - `store = collections.deque([0] * size, size)`
 - `store.append(1)`
 - `while True:`
 - `yield store[-1]`
 - `store.append(sum(store))`

Python code for finding the probability of tossing a coin

```
• def coin_chance(flips, streak):
•     if streak <= 0 or streak % 1:
•         raise ValueError("streak must be a positive integer")
•     if flips < 0 or flips % 1:
•         raise ValueError("flips must be a non-negative integer")
•     if streak == 1:
•         return Fraction(flips != 0, 1)
•     sequence = (
•         Fraction(2 * numerator, 2 ** exponent)
•         for exponent, numerator in enumerate(fibonacci_nth(streak - 1
•     ), streak)
•     )
•     return sum(itertools.islice(sequence, flips - streak + 1))
```

Conditional Probability

Bayes'theorem :Assume that $P(B)>0$

$$P(A | B) = \frac{P(B | A)P(A)}{P(B)}.$$

Expectation and Variance

$$E[X] = \sum_x xP(X = x).$$

$$\text{Var}[X] = E[(X - E[X])^2] = E[X^2] - E[X]^2.$$

Home work

- We conducted $m = 500$ groups of experiments where each group draws $n = 10$ samples. Vary m and n . Observe and analyze the experimental results.

Thank You!

