

Alex has a board game consisting of:

- A *chip* for marking his current location on the board.
- $n$  *fields* numbered from  $1$  to  $n$ . Each position  $i$  has a value,  $f_i$ , denoting the *next* position for the chip to jump to from that field.
- A *die* with  $m$  faces numbered from  $0$  to  $m - 1$ . Each face  $j$  has a probability,  $p_j$ , of being rolled.

Alex then performs the following actions:

- Begins the game by placing the chip at a position in a field randomly and with equiprobability.
- Takes  $k$  turns; during each turn he:
  - Rolls the die. We'll denote the number rolled during a turn as  $d$ .
  - Jumps the chip  $d$  times. Recall that each field contains a value denoting the *next* field number to jump to.
- After completing  $k$  turns, the game ends and he must calculate the respective probabilities for each field as to whether the game ended with the chip in that field.

Given  $n, m, k$ , the game board, and the probabilities for each *die* face, print  $n$  lines where each line  $i$  contains the probability that the chip is on field  $i$  at the end of the game.

**Note:** All the probabilities in this task are rational numbers modulo  $M = 998244353$ . That is, if the probability can be expressed as the irreducible fraction  $\frac{p}{q}$  where  $q \bmod M \neq 0$ , then it corresponds to the number  $(p \times q^{-1}) \bmod M$  (or, alternatively,  $p \times q^{-1} \equiv x \pmod{M}$ ). [Click here](#) to learn about *Modular Multiplicative Inverse*.

### Input Format

The first line contains three space-separated integers describing the respective values of  $n$  (the number of positions),  $m$  (the number of die faces), and  $k$  (the number of turns).

The second line contains  $n$  space-separated integers describing the respective values of each  $f_i$  (i.e., the index of the field that field  $i$  can transition to).

The third line contains  $m$  space-separated integers describing the respective values of each  $p_j$  (where  $0 \leq p_j < M$ ) describing the probabilities of the faces of the  $m$ -sided die.

### Constraints

- $1 \leq n \leq 6 \times 10^4$
- $4 \leq m \leq 10^5$
- $1 \leq k \leq 1000$
- $1 \leq i, f_i \leq n$
- $0 \leq p_j < M$
- The sum of  $p_j \bmod M$  is  $1$

**Note:** The time limit for this challenge is doubled for *all* languages. Read more about standard time limits at our [environment](#) page.

### Output Format

Print  $n$  lines of output in which each line  $i$  contains a single integer,  $x_i$  (where  $0 \leq x_i < M$ ), denoting the probability that the chip will be on field  $i$  after  $k$  turns.

### Sample Input 0

```
4 5 1
2 3 2 4
332748118 332748118 332748118 0 0
```

### Sample Output 0

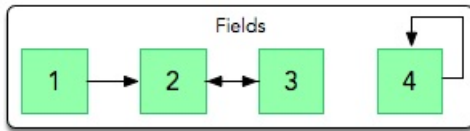
```
582309206
332748118
332748118
748683265
```

## Explanation 0

The diagram below depicts the respective probabilities of each *die* face being rolled:

Game Die					
Face	0	1	2	3	4
$p_j$	332748118	332748118	332748118	0	0
Probability	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	0	0

The diagram below depicts each field with an arrow pointing to the *next* field:



There are four equiprobable initial fields, so each field has a  $\frac{1}{4}$  probability of being the chip's initial location. Next, we calculate the probability that the chip will end up in each field after  $k = 1$  turn:

1. The only way the chip ends up in this field is if it never jumps from the field, which only happens if Alex rolls a **0**. So, this field's probability is  $\frac{1}{4} \cdot \frac{1}{3} = \frac{1}{12}$ . We then calculate and print the result of  $\frac{1}{12} \bmod 998244353 = 582309206$  on a new line.
2. The chip can end up in field **2** after one turn in the following scenarios:
  - Start in field **1** and roll a **1**, the probability for which is  $\frac{1}{4} \cdot \frac{1}{3} = \frac{1}{12}$ .
  - Start in field **2** and roll a **0** or a **2**, the probability for which is  $\frac{1}{4} \cdot \frac{2}{3} = \frac{2}{12}$ .
  - Start in field **3** and roll a **1**, the probability for which is  $\frac{1}{4} \cdot \frac{1}{3} = \frac{1}{12}$ .

After summing these probabilities, we get a total probability of  $\frac{1}{12} + \frac{2}{12} + \frac{1}{12} = \frac{1}{3}$  for the field. We then calculate and print the result of  $\frac{1}{3} \bmod 998244353 = 332748118$  on a new line.

3. The chip can end up in field **3** after one turn in the following scenarios:
  - Start in field **1** and roll a **2**, the probability for which is  $\frac{1}{4} \cdot \frac{1}{3} = \frac{1}{12}$ .
  - Start in field **2** and roll a **1**, the probability for which is  $\frac{1}{4} \cdot \frac{1}{3} = \frac{1}{12}$ .
  - Start in field **3** and roll a **0** or a **2**, the probability for which is  $\frac{1}{4} \cdot \frac{2}{3} = \frac{2}{12}$ .

After summing these probabilities, we get a total probability of  $\frac{1}{12} + \frac{1}{12} + \frac{2}{12} = \frac{1}{3}$  for the field. We then calculate and print the result of  $\frac{1}{3} \bmod 998244353 = 332748118$  on a new line.

4. If the chip is initially placed in field **4**, it will always end up in field **4** regardless of how many turns are taken (because this field loops back onto itself). Thus, this field's probability is  $\frac{1}{4}$ . We then calculate and print the result of  $\frac{1}{4} \bmod 998244353 = 748683265$  on a new line.