An <u>XOR</u> operation on a list is defined here as the xor ( $\oplus$ ) of all its elements (e.g.:  $XOR(\{A,B,C\}) = A \oplus B \oplus C$ ).

The XorSum of set arr is defined here as the sum of the XORs of all non-empty subsets of arr known as arr'. The set arr' can be expressed as:

$$XorSum(arr) = \sum_{i=1}^{2^n-1} XOR(arr_i') = XOR(arr_1') + XOR(arr_2') + \cdots + XOR(arr_{2^n-2}') + XOR(arr_{2^n-1}')$$

For example: Given set  $arr = \{n_1, n_2, n_3\}$ 

- The set of possible non-empty subsets is:  $arr'=\{\{n_1\},\{n_2\},\{n_3\},\{n_1,n_2\},\{n_1,n_3\},\{n_2,n_3\},\{n_1,n_2,n_3\}\}$
- The XorSum of these non-empty subsets is then calculated as follows:  $XorSum(arr) = n_1 + n_2 + n_3 + (n_1 \oplus n_2) + (n_1 \oplus n_3) + (n_2 \oplus n_3) + (n_1 \oplus n_2 \oplus n_3)$

Given a list of n space-separated integers, determine and print  $XorSum \% (10^9 + 7)$ .

For example,  $arr=\{3,4\}$ . There are three possible subsets,  $arr'=\{\{3\},\{4\},\{3,4\}\}$ . The XOR of arr'[1]=3, of arr'[2]=4 and of  $arr[3]=3\oplus 4=7$ . The XorSum is the sum of these: 3+4+7=14 and  $14\%(10^9+7)=14$ .

**Note:** The cardinality of powerset(n) is  $2^n$ , so the set of non-empty subsets of set arr of size n contains  $2^n - 1$  subsets.

## **Function Description**

Complete the *xoringNinja* function in the editor below. It should return an integer that represents the XorSum of the input array, modulo  $(10^9 + 7)$ .

xoringNinja has the following parameter(s):

• arr: an integer array

## **Input Format**

The first line contains an integer T, the number of test cases.

Each test case consists of two lines:

- The first line contains an integer n, the size of the set arr.
- The second line contains n space-separated integers arr[i].

## **Constraints**

$$1 \le T \le 5$$
  
 $1 \le n \le 10^5$   
 $0 \le arr[i] \le 10^9$ ,  $1 \le i \le n$ 

### **Output Format**

For each test case, print its  $XorSum \% (10^9 + 7)$  on a new line. The  $i^{th}$  line should contain the output for the  $i^{th}$  test case.

## Sample Input 0

1 3 1 2 3

### Sample Output 0

## **Explanation 0**

```
The input set, S=\{1,2,3\}, has 7 possible non-empty subsets: S'=\{\{1\},\{2\},\{3\},\{1,2\},\{2,3\},\{1,3\},\{1,2,3\}\}.
```

We then determine the  $\boldsymbol{XOR}$  of each subset in  $\boldsymbol{S'}$ :

```
XOR(\{1\}) = 1

XOR(\{2\}) = 2

XOR(\{3\}) = 3

XOR(\{1,2\}) = 1 \oplus 2 = 3

XOR(\{2,3\}) = 2 \oplus 3 = 1

XOR(\{1,3\} = 1 \oplus 3 = 2

XOR(\{1,2,3\} = 1 \oplus 2 \oplus 3 = 0
```

Then sum the results of the XOR of each individual subset in S', resulting in XorSum=12 and  $12\%(10^9+7)=12$ .

# **Sample Input 1**

2 4 1 2 4 8 5 1 2 3 5 100

# **Sample Output 1**

120 1648