

Matrix theory Assignment 11

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Abstract—This document contains the concept of sub space.

Download all python codes from

<https://github.com/saipranavkr/EE5609/codes>

and latex-tikz codes from

<https://github.com/saipranavkr/EE5609>

1 PROBLEM

Find the range, rank, null space, and nullity for the zero transformation and the identity transformation on a finite-dimensional space \mathbf{V} .

2 SOLUTION

Suppose vector space \mathbf{V} has $\dim(\mathbf{V}) = n$. Table 0 provides the properties of range, rank, null space and nullity of zero and identity transformation on a vector space \mathbf{V}

3 EXAMPLE

Let T_0, T_I be the zero and identity transformation on the vector space \mathbf{V} such that $\dim(\mathbf{V}) = 2$. Let,

$$\mathbf{v} = \begin{pmatrix} v_1 \\ v_2 \end{pmatrix}$$

be a vector in \mathbf{V} . Now,

$$T_0 \mathbf{v} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \quad (3.0.1)$$

From (3.0.1) we can tell that, it has range of $\{0\}$, Rank of Zero, Null space as \mathbf{V} and nullity as 2 ($\because \dim(\mathbf{V}) = 2$) Now,

$$T_I \mathbf{v} = \begin{pmatrix} v_1 \\ v_2 \end{pmatrix} \quad (3.0.2)$$

From (3.0.2) we can tell that, it has range of \mathbf{V} , Rank of 2, Null space as $\{0\}$ and nullity as $\mathbf{0}$ ($\because \dim(\mathbf{0}) = 0$). Because identity transformation is the transformation $T_I : \mathbf{R}_n \rightarrow \mathbf{R}_n$ defined by $T_I(x) = x$ for every vector x

Properties	Zero Transformation	Identity Transformation
Transformation	$T_0(\mathbf{v}) = \mathbf{0}$	$T_I(\mathbf{v}) = \mathbf{v}$
Range	Zero subspace $\{0\}$	\mathbf{V}
Rank	$\dim(\mathbf{0}) = 0$	$\dim(\mathbf{V}) = n$
Null space	\mathbf{V}	Zero subspace $\{0\}$
Nullity	$\dim(\mathbf{V}) = n$	$\dim(\mathbf{0}) = 0$

TABLE 0: Properties of Zero and Identity transformation