

$$2.31 \quad R^2 = 1 - \frac{SS_E}{SS_T}$$

$$SS_E = \sum_i (y_i - \hat{y}_i)^2$$

If there are diff values of y , then $SS_E > 0$. Hence $R^2 < 1$ always

$$2.32-a) \quad S(\beta_0, \beta_1) = \sum_{i=1}^n (y_i - \beta_0 - \beta_1 x_i)^2 \quad \hat{\beta}_0 = \beta_0$$

$$\left. \frac{\partial S}{\partial \beta_0} \right|_{\hat{\beta}_0, \hat{\beta}_1} = -2 \sum_{i=1}^n (y_i - \hat{\beta}_0 - \hat{\beta}_1 x_i) = 0$$

$$\left. \frac{\partial S}{\partial \beta_1} \right|_{\hat{\beta}_0, \hat{\beta}_1} = -2 \sum_{i=1}^n (y_i - \hat{\beta}_0 - \hat{\beta}_1 x_i) x_i = 0$$

$$n \hat{\beta}_0 + \hat{\beta}_1 \sum_{i=1}^n x_i = \sum_{i=1}^n y_i \quad \hat{\beta}_1 = \frac{\sum_{i=1}^n (y_i - \hat{\beta}_0) x_i}{\sum_{i=1}^n x_i^2}$$

1. $\hat{\beta}_1$ denotes Parameter

b)
$$\text{Var}(\hat{\beta}_1) = \frac{1}{\left(\sum_{i=1}^n x_i\right)^2} \text{Var}\left(\sum_{i=1}^n y_i x_i\right)$$

$$= \frac{1}{\left(\sum_{i=1}^n x_i\right)^2} \left(\sum_{i=1}^n x_i^2\right) \sigma^2$$

$$= \frac{\sigma^2}{\sum_{i=1}^n x_i^2}$$

c) t_{n-2} is approximately $\frac{\hat{\beta}_1 - \beta_1}{\sqrt{MSE / \sum_{i=1}^n x_i^2}}$

We get
$$\hat{\beta}_1 \pm t_{\frac{\alpha}{2}, n-2} \sqrt{\frac{MSE}{\sum_{i=1}^n x_i^2}}$$

In the above equation, the variability is significantly reduced.