



# ***More Data Mining with Weka***

Class 4 – Lesson 1

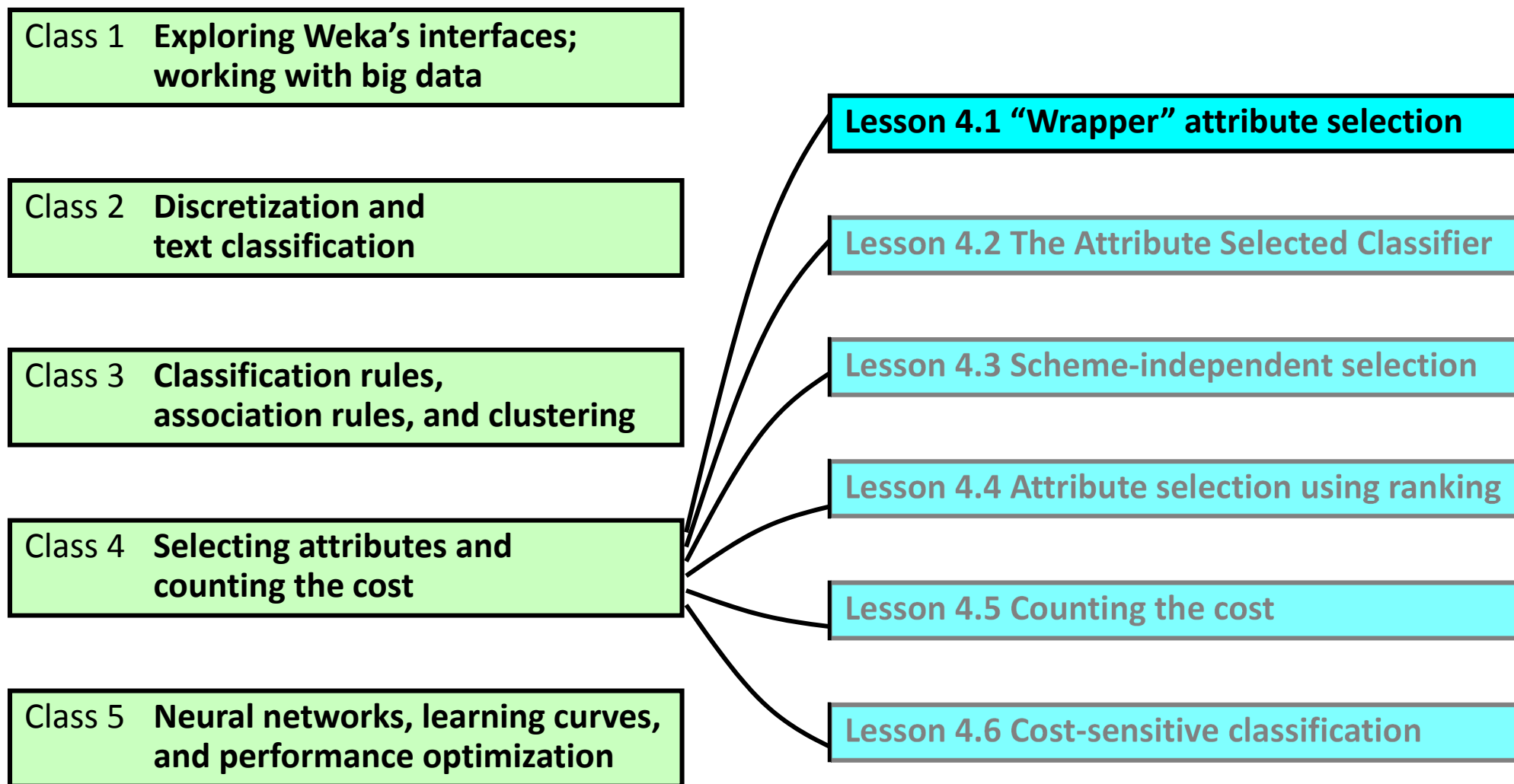
*Attribute selection using the “wrapper” method*

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# *Lesson 4.1: Attribute selection using the “wrapper” method*



# Lesson 4.1: Attribute selection using the “wrapper” method

## Fewer attributes, better classification

### ❖ Data Mining with Weka, Lesson 1.5

- Open *glass.arff*; run J48 (*trees>J48*): cross-validation classification accuracy 67%
- Remove all attributes except RI and Mg: 69%
- Remove all attributes except RI, Na, Mg, Ca, Ba: 74%

### ❖ “Select attributes” panel avoids laborious experimentation

- Open *glass.arff*; attribute evaluator *WrapperSubsetEval*  
select J48, 10-fold cross-validation, threshold = -1
- Search method: *BestFirst*; select Backward
- Get the same attribute subset: RI, Na, Mg, Ca, Ba: “merit” 0.74

### ❖ How much experimentation?

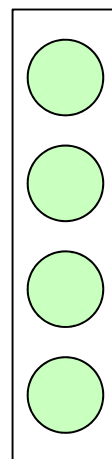
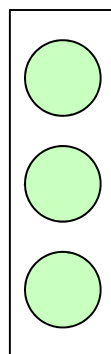
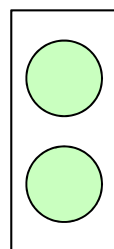
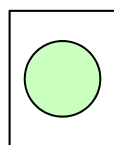
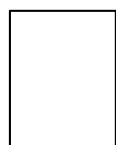
- Set *searchTermination* = 1
- Total number of subsets evaluated 36  
complete set (1 evaluation); remove one attribute (9); one more (8); one more (7); one more (6); plus one more (5) to check that removing a further attribute does not yield an improvement;  $1+9+8+7+6+5 = 36$

# Lesson 4.1: Attribute selection using the “wrapper” method

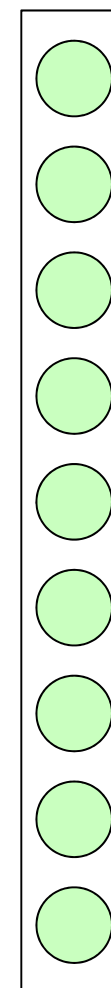
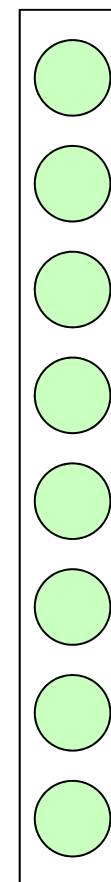
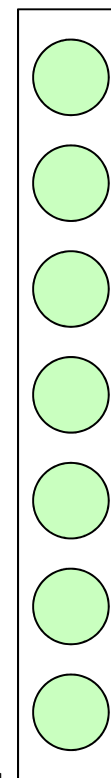
## Searching

- ❖ Exhaustive search:  $2^9 = 512$  subsets
- ❖ Searching forward, searching backward  
+ when to stop? (*searchTermination*)

0 attributes  
(ZeroR)



...



all 9  
attributes

forward  
search →

bidirectional  
search →

←  
backward  
search

# Lesson 4.1: Attribute selection using the “wrapper” method

## Trying different searches (*WrapperSubsetEval* folds = 10, threshold = -1)

- ❖ Backwards (*searchTermination* = 1): *Rl, Mg, K, Ba, Fe* (0.72)
  - *searchTermination* = 5 or more: *Rl, Na, Mg, Ca, Ba* (0.74)
- ❖ Forwards: *Rl, Al, Ca* (0.70)
  - *searchTermination* = 2 or more: *Rl, Na, Mg, Al, K, Ca* (0.72)
- ❖ Bi-directional: *Rl, Al, Ca* (0.70)
  - *searchTermination* = 2 or more: *Rl, Na, Mg, Al* (0.74)
  
- ❖ Note: local vs global optimum
  - *searchTermination* > 1 can traverse a valley
- ❖ Al is the best single attribute to use (as OneR will confirm)
  - thus forwards search results include Al
- ❖ (curiously) Al is the best single attribute to drop
  - thus backwards search results do not include Al

# Lesson 4.1: Attribute selection using the “wrapper” method

## Cross-validation

Backward (*searchTermination=5*)

number of folds (%)	attribute
10 (100 %)	1 RI
8 ( 80 %)	2 Na
10 (100 %)	3 Mg
3 ( 30 %)	4 Al
2 ( 20 %)	5 Si
2 ( 20 %)	6 K
7 ( 70 %)	7 Ca
10 (100 %)	8 Ba
4 ( 40 %)	9 Fe

In how many folds  
does that attribute  
appear in the final subset?

Definitely choose RI, Mg, Ba; probably Na, Ca; probably not Al, Si, K, Fe

But if we did forward search, would definitely choose Al!

# Lesson 4.1: Attribute selection using the “wrapper” method

## Gory details

(generally, Weka methods follow descriptions in the research literature)

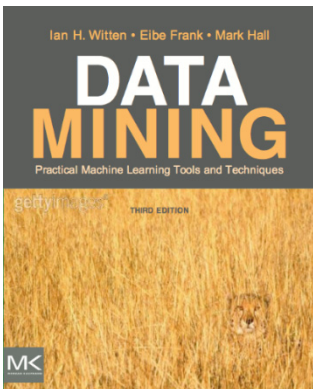
- ❖ *WrapperSubsetEval* attribute evaluator
  - Default: 5-fold cross-validation
  - Does at least 2 and up to 5 cross-validation runs and takes average accuracy
  - Stops when the standard deviation across the runs is less than the user-specified threshold times the mean (default: 1% of the mean)
  - Setting a negative threshold forces a single cross-validation
- ❖ *BestFirst* search method
  - *searchTermination* defaults to 5 for traversing valleys
- ❖ Choose *ClassifierSubsetEval* to use the wrapper method, but with a separate test set instead of cross-validation

# Lesson 4.1: Attribute selection using the “wrapper” method

- ❖ Use a classifier to find a good attribute set (“scheme-dependent”)
  - we used J48; in the associated Activity you will use ZeroR, OneR, IBk
- ❖ Wrap a classifier in a cross-validation loop
- ❖ Involves both an Attribute Evaluator and a Search Method
- ❖ Searching can be greedy forward, backward, or bidirectional
  - computationally intensive;  $m^2$  for  $m$  attributes
  - there’s also has an “exhaustive” search method ( $2^m$ ), used in the Activity
- ❖ Greedy searching finds a local optimum in the search space
  - you can traverse valleys by increasing the *searchTermination* parameter

## Course text

- ❖ Section 7.1 *Attribute selection*







# ***More Data Mining with Weka***

Class 4 – Lesson 2

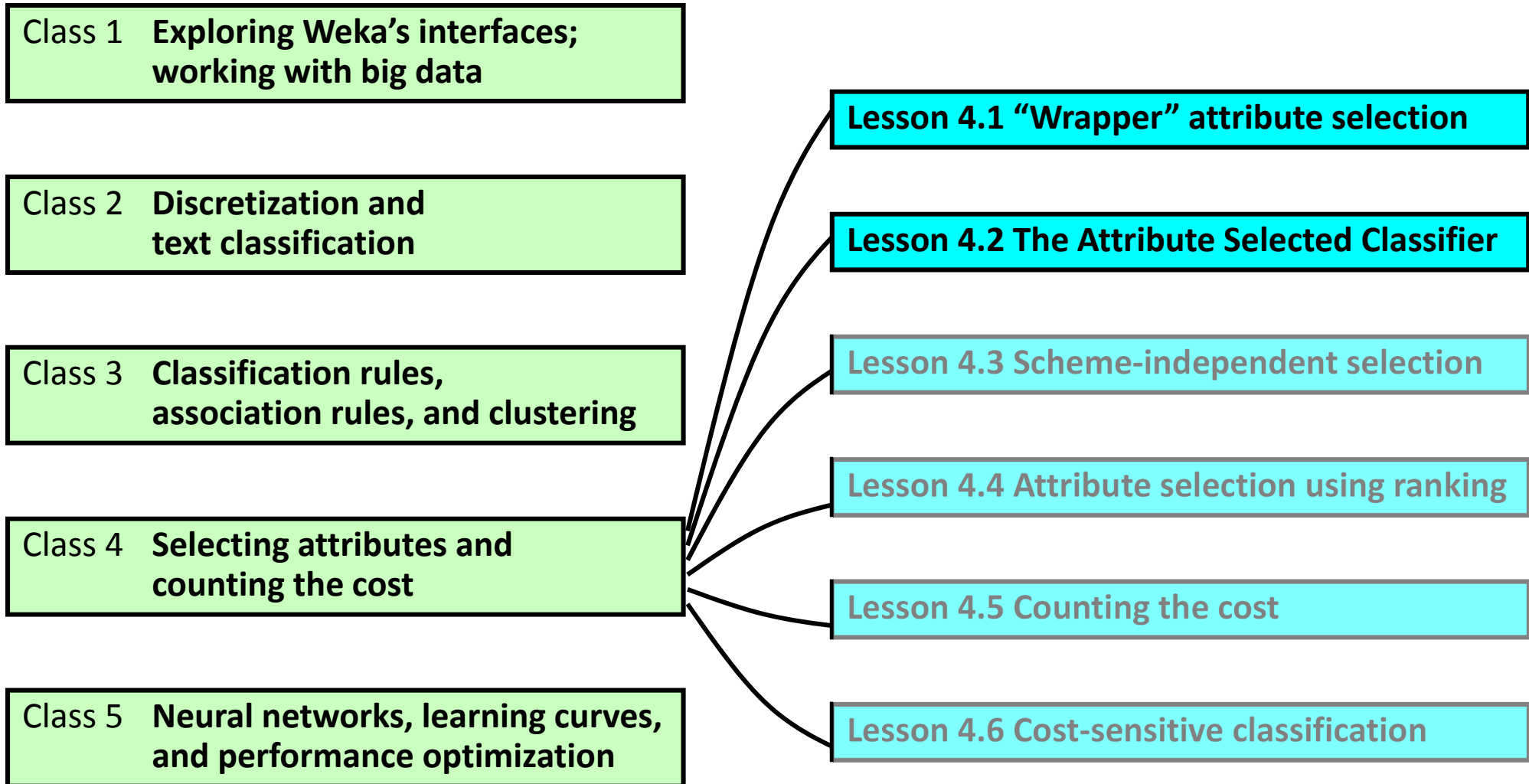
*The Attribute Selected Classifier*

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## ***Lesson 4.2: The Attribute Selected Classifier***



## Lesson 4.2: The Attribute Selected Classifier

### ❖ Select attributes and apply a classifier to the result

- *glass.arff* default parameters everywhere
- Wrapper selection with J48 {Rl, Mg, Al, K, Ba}
- with IBk {Rl, Mg, Al, K, Ca, Ba}

**J48**   **IBk**

67%   71%

71%

78%

### ❖ Is this cheating? – yes!

### ❖ AttributeSelectedClassifier (in *meta*)

- Select attributes based on training data only  
... then train the classifier and evaluate it on the test data
- like the FilteredClassifier used for supervised discretization (Lesson 2.2)
- Use AttributeSelectedClassifier to wrap J48
- Use AttributeSelectedClassifier to wrap IBk

72%

74%

69%

71%

(slightly  
surprising)

## Lesson 4.2: The Attribute Selected Classifier

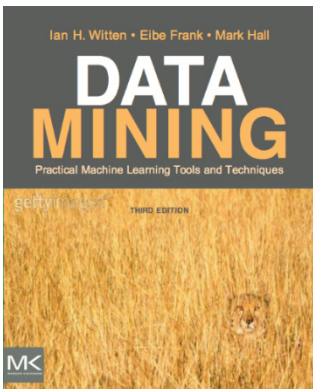
- |   | NaiveBayes        |
|---|-------------------|
| ❖ Check the effectiveness of the AttributeSelectedClassifier                    |                   |
| – <i>diabetes.arff</i>  | 76.3%             |
| – <i>AttributeSelectedClassifier, NaiveBayes, WrapperSubsetEval, NaiveBayes</i> | 75.7%             |
| ❖ Add copies of an attribute  |                   |
| – <i>Copy the first attribute (preg); NaiveBayes</i>                            | 75.7%             |
| – <i>AttributeSelectedClassifier as above</i>                                   | 75.7%             |
| – <i>Add 9 further copies of preg; NaiveBayes</i>                               | 68.9%             |
| – <i>AttributeSelectedClassifier as above</i>                                   | 75.7%             |
| – <i>Add further copies: NaiveBayes</i>   | <i>even worse</i> |
| – <i>AttributeSelectedClassifier as above</i>                                   | 75.7%             |
| ❖ Attribute selection does a good job of removing redundant attributes          |                   |

## Lesson 4.2: The Attribute Selected Classifier

- ❖ AttributeSelectedClassifier selects based on training set only
  - even when cross-validation is used for evaluation
  - this is the right way to do it!
  - we used J48; in the associated Activity you will use ZeroR, OneR, IBk
- ❖ (probably) Best to use the same classifier within the wrapper
  - e.g. wrap J48 to select attributes for J48
- ❖ One-off experiments in the Explorer may not be reliable
  - the associated Activity uses the Experimenter for more repetition

### Course text

- ❖ Section 7.1 *Attribute selection*





# ***More Data Mining with Weka***

Class 4 – Lesson 3

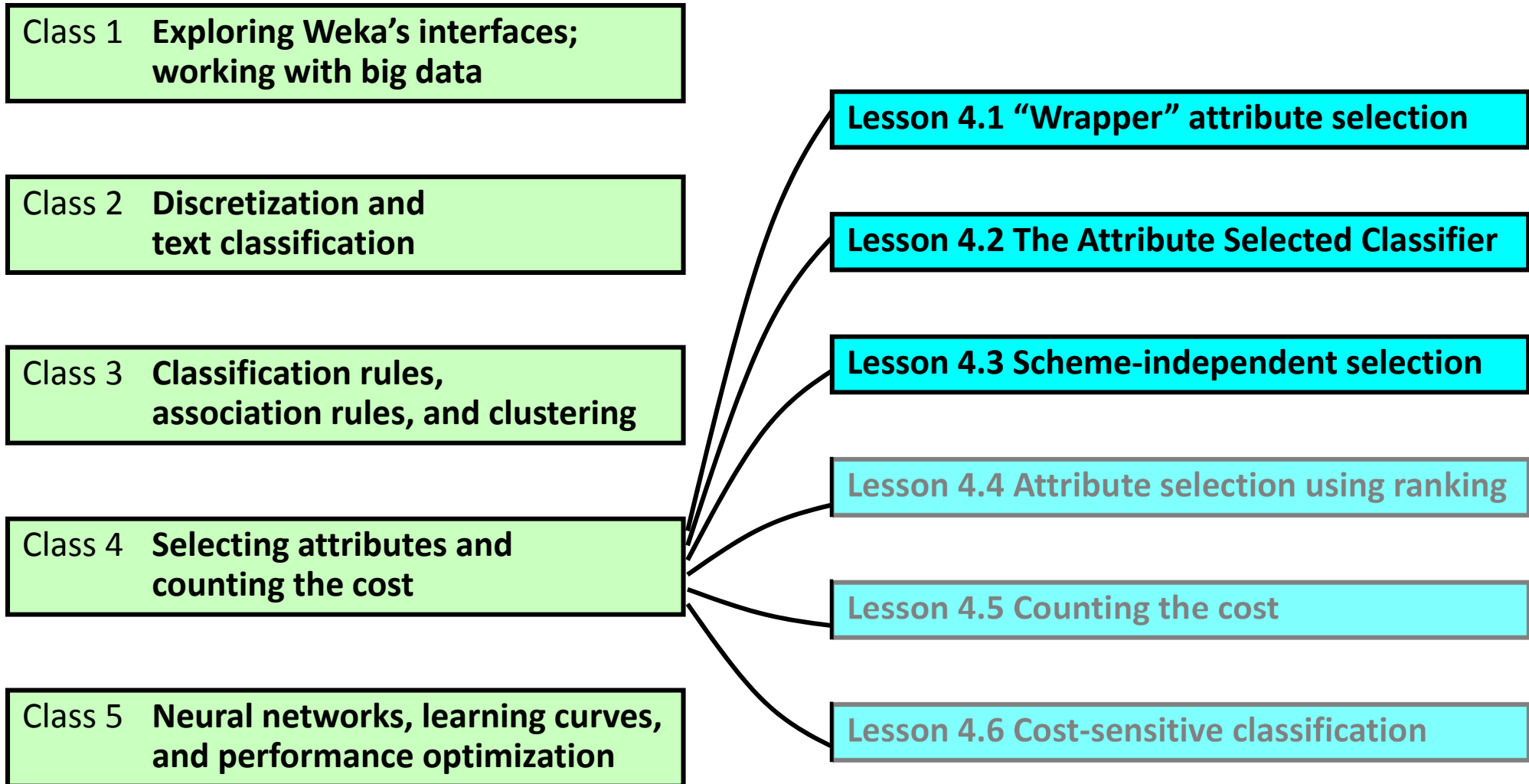
*Scheme-independent attribute selection*

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## ***Lesson 4.3: Scheme-independent attribute selection***



## Lesson 4.3: Scheme-independent attribute selection

Wrapper method is simple and direct – but slow

❖ Either:

1. use a single-attribute evaluator, with ranking (*Lesson 4.4*)
  - can eliminate **irrelevant** attributes
2. combine an attribute subset evaluator with a search method
  - can eliminate **redundant** attributes as well

❖ We've already looked at search methods (*Lesson 4.1*)

- greedy forward, backward, bidirectional

❖ Attribute subset evaluators

- wrapper methods are **scheme-dependent** attribute subset evaluators
- other subset evaluators are **scheme-independent**



## Lesson 4.3: Scheme-independent attribute selection

**CfsSubsetEval**: a scheme-independent attribute subset evaluator

- ❖ An attribute subset is good if the attributes it contains are
  - *highly correlated with the class attribute*
  - *not strongly correlated with one another*
- ❖ Goodness of an attribute subset = 
$$\frac{\sum_{\text{all attributes } x} C(x, \text{class})}{\sqrt{\sum_{\text{all attributes } x} \sum_{\text{all attributes } y} C(x, y)}}$$
- ❖  $C$  measures the correlation between two attributes
- ❖ An entropy-based metric called the “symmetric uncertainty” is used

## Lesson 4.3: Scheme-independent attribute selection

Compare CfsSubsetEval with Wrapper selection on **ionosphere.arff**

	<i>NaiveBayes</i>	<i>IBk</i>	<i>J48</i>
❖ No attribute selection	83%	86%	91%
❖ With attribute selection (using <b>AttributeSelectedClassifier</b> )			
– <b>CfsSubsetEval</b> (very fast)	89%	89%	90%
– <b>Wrapper</b> selection (very slow)	91%	89%	92%

*(the corresponding classifier is used in the wrapper, e.g. the wrapper for IBk uses IBk)*

❖ Conclusion: CfsSubsetEval is nearly as good as Wrapper, and much faster

## ***Lesson 4.3: Scheme-independent attribute selection***

### **Attribute subset evaluators in Weka**

#### **Scheme-dependent**

- ❖ WrapperSubsetEval (internal cross-validation)
- ❖ ClassifierSubsetEval (separate held-out test set)

#### **Scheme-independent**

- ❖ CfsSubsetEval
  - *consider predictive value of each attribute, along with the degree of inter-redundancy*
- ❖ ConsistencySubsetEval
  - *measures consistency in class values of training set with respect to the attributes*
  - *seek the smallest attribute set whose consistency is no worse than for the full set*

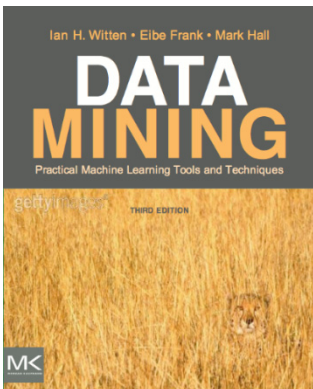
(There are also meta-evaluators, which incorporate other operations)

## Lesson 4.3: Scheme-independent attribute selection

- ❖ Attribute subset selection involves
  - a subset evaluation measure
  - a search method
- ❖ Some measures are scheme-dependent
  - e.g. the wrapper method; but very slow
- ❖ ... and others are scheme-independent
  - e.g. CfsSubsetEval; quite fast
- ❖ Even faster ... single-attribute evaluator, with ranking (*next lesson*)

### Course text

- ❖ Section 7.1 *Attribute selection*





# ***More Data Mining with Weka***

Class 4 – Lesson 4

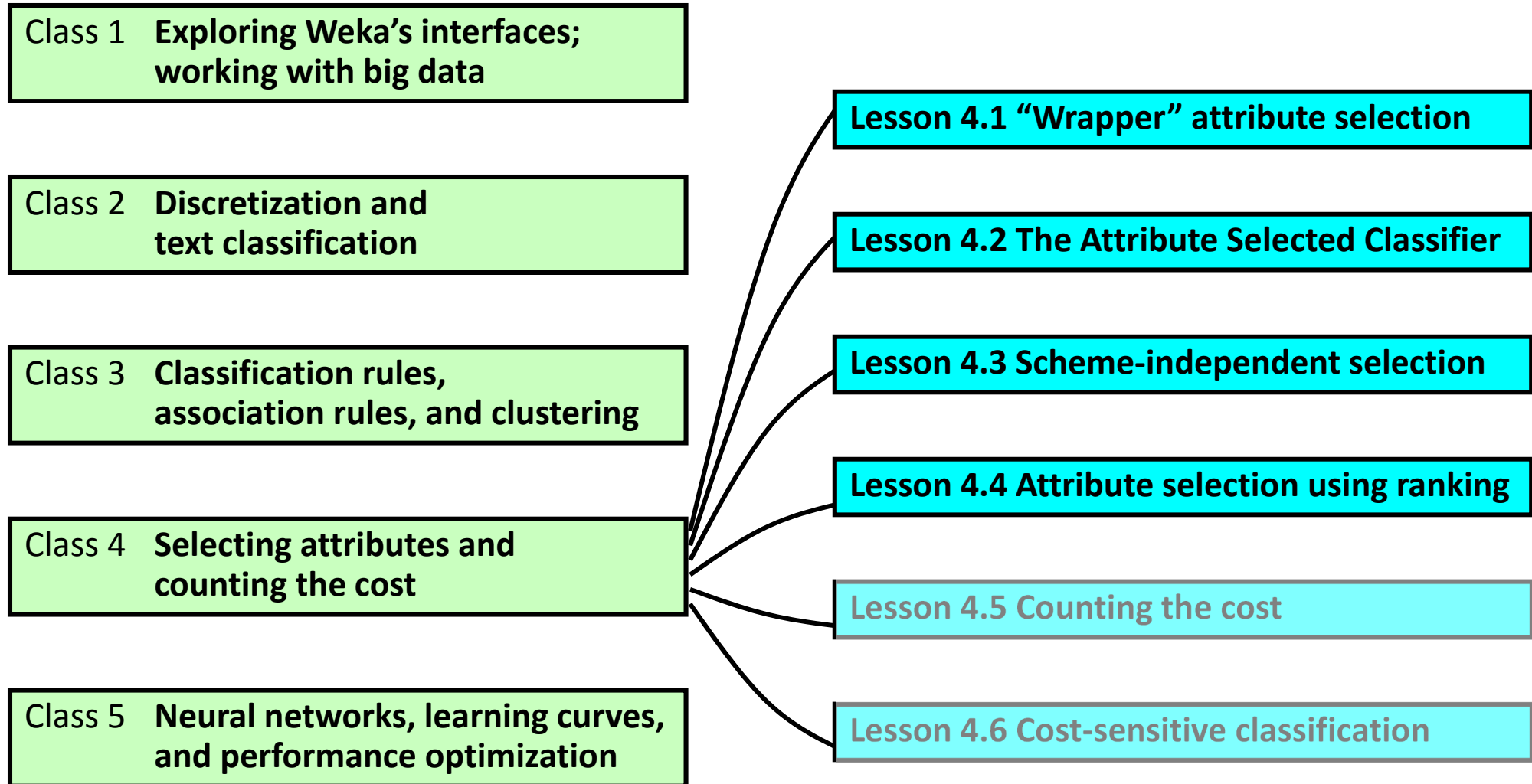
*Fast attribute selection using ranking*

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## *Lesson 4.4: Fast attribute selection using ranking*



## *Lesson 4.4: Fast attribute selection using ranking*

- ❖ Attribute subset selection involves:
  - subset evaluation measure
  - search method
- ❖ Searching is slow!
  
- ❖ Alternative: use a single-attribute evaluator, with ranking
  - can eliminate irrelevant attributes  
... but not redundant attributes
- ❖ Choose the “ranking” search method when selecting a single-attribute evaluator

## Lesson 4.4: Fast attribute selection using ranking

Metrics for evaluating attributes: we've seen some before

- ❖ OneR uses the accuracy of a single-attribute classifier OneRAttributeEval
- ❖ C4.5 (i.e. J48) uses information gain InfoGainAttributeEval  
... actually, it uses gain ratio GainRatioAttributeEval
- ❖ CfsSubsetEval uses “symmetric uncertainty” SymmetricalUncertAttributeEval

The “ranker” search method sorts attributes according to their evaluation

- ❖ parameters
  - *number of attributes to retain (default: retain all)*
  - *or discard attributes whose evaluation falls below a threshold (default:  $-\infty$ )*
  - *can specify a set of attributes to ignore*



## Lesson 4.4: Scheme-independent attribute selection

Compare **GainRatioAttributeEval** with others on **ionosphere.arff**

	<i>NaiveBayes</i>	<i>IBk</i>	<i>J48</i>
❖ No attribute selection	83%	86%	91%
❖ With attribute selection (using <b>AttributeSelectedClassifier</b> )			
– <b>CfsSubsetEval</b> (very fast)	89%	89%	92%
– <b>Wrapper</b> selection (very slow)	91%	89%	90%
<i>(the corresponding classifier is used in the wrapper, e.g. the wrapper for IBk uses IBk)</i>			
– <b>GainRatioAttributeEval</b> , retaining 7 attributes	90%	90%	91%
❖ Lightning fast ...			
but performance is sensitive to the number of attributes retained			

## *Lesson 4.4: Fast attribute selection using ranking*

### **Attribute evaluators in Weka**

- ❖ OneRAttributeEval
- ❖ InfoGainAttributeEval
- ❖ GainRatioAttributeEval
- ❖ SymmetricalUncertaintyAttributeEval

**plus**

- ❖ ChiSquaredAttributeEval – *compute the  $\chi^2$  statistic of each attribute wrt the class*
- ❖ SVMAttributeEval – *use SVM to determine the value of attributes*
- ❖ ReliefFAttributeEval – *instance-based attribute evaluator*
- ❖ PrincipalComponents – *principal components transform, choose largest eigenvectors*
- ❖ LatentSemanticAnalysis – *performs latent semantic analysis and transformation*

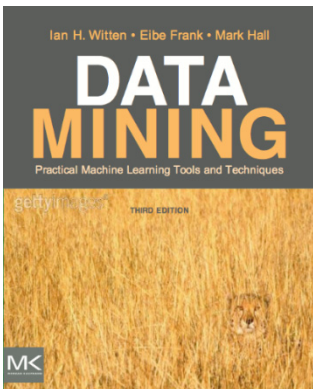
(There are also meta-evaluators, which incorporate other operations)

## *Lesson 4.4: Fast attribute selection using ranking*

- ❖ Attribute subset evaluation
  - involves searching and is bound to be slow
- ❖ Single-attribute evaluation
  - involves ranking, which is far faster
  - difficult to specify a suitable number of attributes to retain (involves experimentation)
  - does not cope with redundant attributes (e.g. copies of an attribute will be repeatedly selected)
- ❖ Many single-attribute evaluators are based on ML methods

### **Course text**

- ❖ Section 7.1 *Attribute selection*





# ***More Data Mining with Weka***

Class 4 – Lesson 5

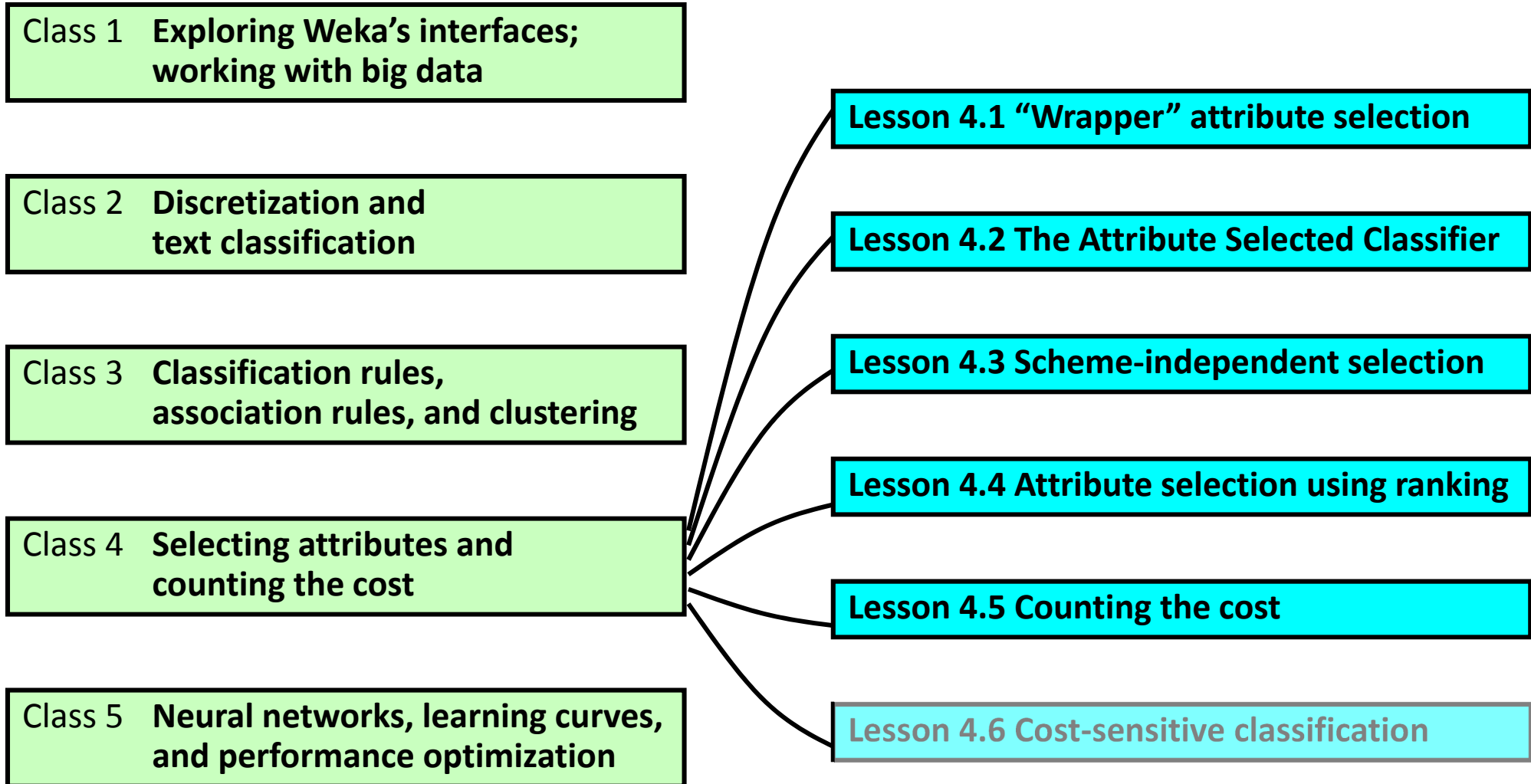
*Counting the cost*

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# *Lesson 4.5: Counting the cost*



## Lesson 4.5: Counting the cost

### What is success?

- ❖ So far, the classification rate  
*(measured by test set, holdout, cross-validation)*
- ❖ Different kinds of error may have different costs
- ❖ Minimizing total errors is inappropriate  
*With 2-class classification, the ROC curve summarizes different tradeoffs*
- ❖ Credit dataset **credit-g.arff**  
*It's worse to class a customer as good when they are bad  
than to class a customer as bad when they are good*
- ❖ Economic model: error cost of 5 vs. 1

# Lesson 4.5: Counting the cost

## Weka: Cost-sensitive *evaluation*

- ❖ Credit dataset **credit-g.arff**
- ❖ **J48** (70%)

a	b	<-- classified as
588	112	a = good
183	117	b = bad

cost: 295 incorrectly  
classified instances

- ❖ Classify Panel “More options”: **Cost-sensitive evaluation**

Cost matrix: 

0	1
5	0

 $\rightarrow$  cost:  $183 \times 5 + 112 \times 1$   
 $= 1027$  (1.027/instance)

- ❖ Baseline (**ZeroR**)

a	b	<-- classified as
700	0	a = good
300	0	b = bad

cost:  $300 \times 5 = 1500$

- ❖ if you were to classify everything as *bad* the total cost would be only 700

## Lesson 4.5: Counting the cost

### Weka: cost-sensitive *classification*

- ❖ The classifier should know the costs when learning!
- ❖ `meta > CostSensitiveClassifier`
- ❖ Select **J48**
- ❖ Define cost matrix:  $\begin{matrix} 0 & 1 \\ 5 & 0 \end{matrix}$
- ❖ Worse classification error (61% vs. 70%)
- ❖ Lower average cost (0.66 vs. 1.027)
- ❖ Effect of error on confusion matrix
- ❖ **ZeroR**: average cost 0.7

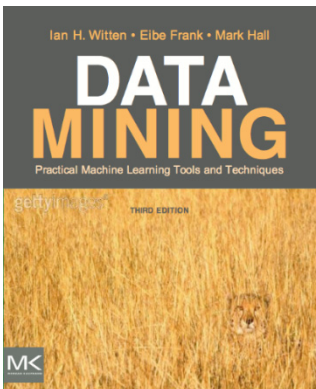
		old	
a	b		
588	112		a = good
183	117		b = bad

		new	
a	b		
372	328		a = good
66	234		b = bad



## Lesson 4.5: Counting the cost

- ❖ Is classification accuracy the best measure?
- ❖ Economic model: cost of errors
  - or consider the tradeoff between error rates – the ROC curve
- ❖ Cost-sensitive *evaluation*
- ❖ Cost-sensitive *classification*
- ❖ `meta > CostSensitiveClassifier`
  - makes any classifier cost-sensitive
- ❖ Section 5.7 *Counting the cost*





# ***More Data Mining with Weka***

Class 4 – Lesson 6

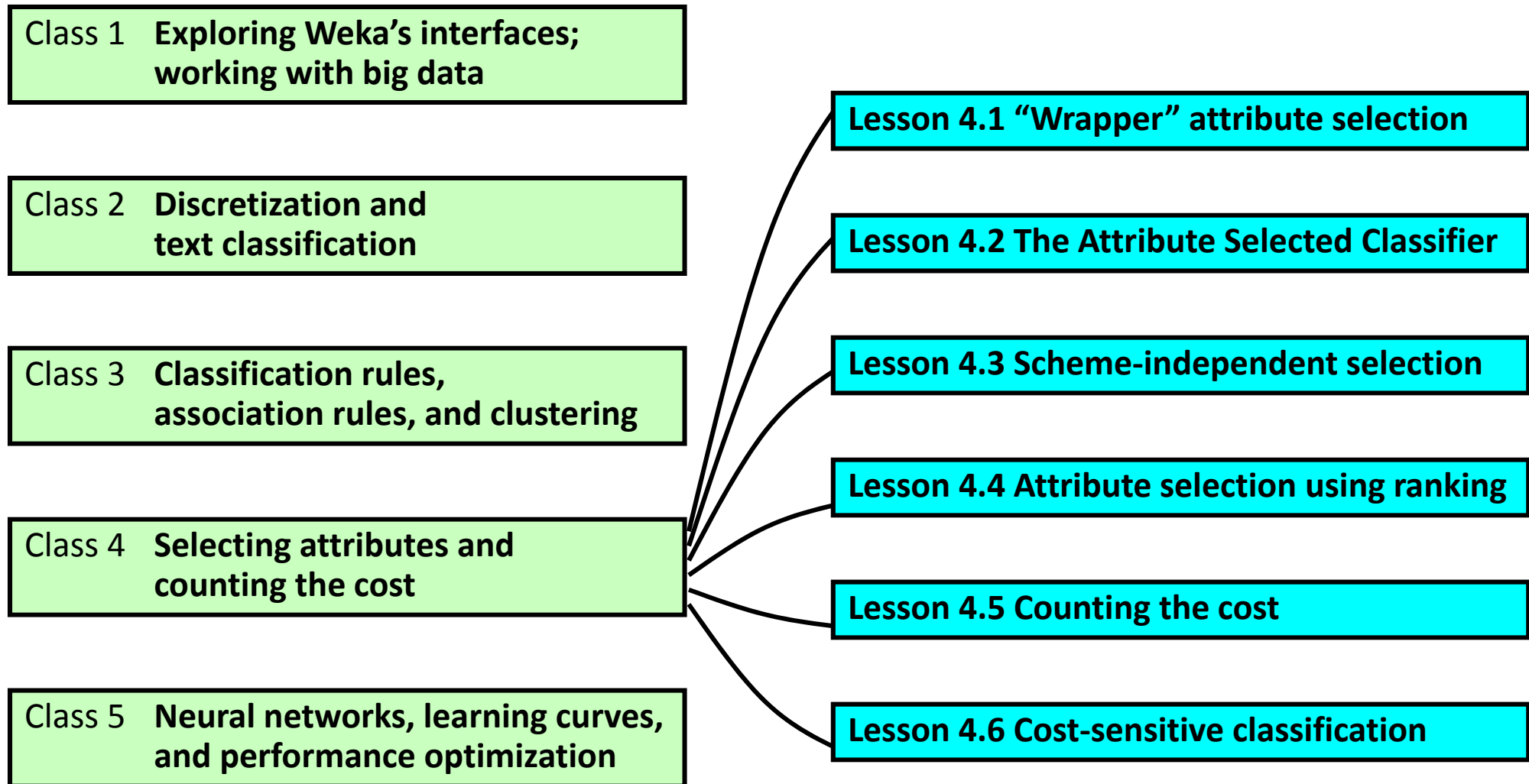
*Cost-sensitive classification vs. cost-sensitive learning*

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## *Lesson 4.6: Cost-sensitive classification vs. cost-sensitive learning*



# Lesson 4.6: Cost-sensitive classification vs. cost-sensitive learning

## Making a classifier cost-sensitive: Method 1: Cost-sensitive *classification*

Adjust a classifier's output  
by recalculating the probability threshold

- ❖ Credit dataset **credit-g.arff**
- ❖ **NaiveBayes, Output predictions**

a	b	<-- classified as
605	95	a = good
151	149	b = bad

- ❖ Threshold: 0.5
  - predicts 756 *good*, with 151 mistakes
  - 244 *bad*, with 95 mistakes



	actual	predicted	$p_{\text{good}}$
0	good	good	0.999
50	good	good	0.991
100	good	good	0.983
150	good	good	0.975
200	good	good	0.965
250	bad	good	0.951
300	bad	good	0.934
350	good	good	0.917
400	good	good	0.896
450	good	good	0.873
500	good	good	0.836
550	good	good	0.776
600	bad	good	0.715
650	good	good	0.663
700	good	good	0.587
750	bad	good	0.508
800	good	bad	0.416
850	bad	bad	0.297
900	good	bad	0.184
950	bad	bad	0.04

# Lesson 4.6: Cost-sensitive classification vs. cost-sensitive learning

## Recalculating the probability threshold

❖ Cost matrix

	a	b	
0	1	a = good	
5	0	b = bad	

❖ Threshold =  $5/6 = 0.833$

a	b	<-- classified as
448	252	a = good
53	247	b = bad

total cost 517 (vs. 850)

❖ General cost matrix:

0	$\lambda$
$\mu$	0

❖ To minimize expected cost, classify as *good* if

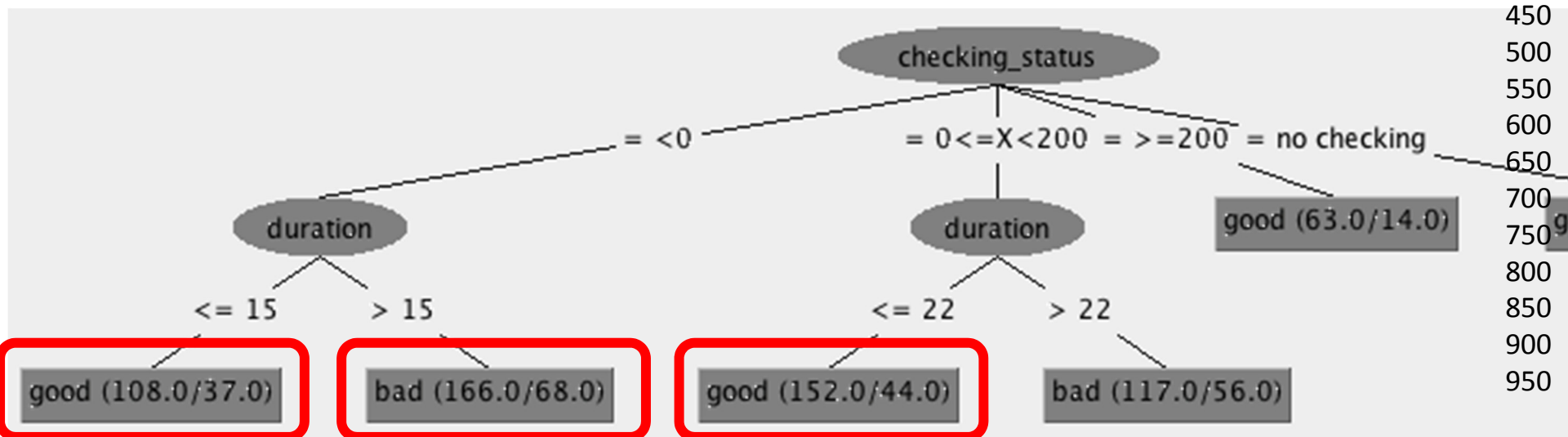
$$p_{\text{good}} > \frac{\mu}{\lambda + \mu}$$

	actual	predicted	$p_{\text{good}}$
0	good	good	0.999
50	good	good	0.991
100	good	good	0.983
150	good	good	0.975
200	good	good	0.965
250	bad	good	0.951
300	bad	good	0.934
350	good	good	0.917
400	good	good	0.896
450	good	good	0.873
500	good	good	0.836
550	good	good	0.776
600	bad	good	0.715
650	good	good	0.663
700	good	good	0.587
750	bad	good	0.508
800	good	bad	0.416
850	bad	bad	0.297
900	good	bad	0.184
950	bad	bad	0.04

# Lesson 4.6: Cost-sensitive classification vs. cost-sensitive learning

What about methods that don't produce probabilities?

- ❖ They (almost) all do 😊
- ❖ **J48** with **minNumObj** = 100 (to get small tree)
- ❖ from tree,  
 $1 - 37/108 = 0.657$ ,  $68/166 = 0.410$ ,  $1 - 44/152 = 0.711$ , etc
- ❖ Other methods (e.g. rules) are similar



↓

	actual	predicted	$p_{\text{good}}$
0	good	good	0.883
50	good	good	0.883
100	good	good	0.883
150	good	good	0.883
200	good	good	0.883
250	good	good	0.883
300	good	good	0.883
350	good	good	0.883
400	good	good	0.778
450	bad	good	0.778
500	bad	good	0.711
550	good	good	0.711
600	good	good	0.711
650	good	good	0.657
700	bad	good	0.657
750	good	bad	0.479
800	good	bad	0.479
850	bad	bad	0.410
900	good	bad	0.410
950	bad	bad	0.410

# Lesson 4.6: Cost-sensitive classification vs. cost-sensitive learning

## CostSensitiveClassifier with minimizeExpectedCost = true

❖ Credit dataset **credit-g.arff**; **J48**

❖ Cost matrix

a	b
0	1   a = good
5	0   b = bad

a	b	<-- classified as
588	112	a = good
183	117	b = bad

cost 1027

❖ **meta > CostSensitiveClassifier; minimizeExpectedCost = true; set cost matrix**

❖ **select J48**

a	b	<-- classified as
455	245	a = good
105	195	b = bad

cost 770

❖ use bagging (Data Mining with Weka, Lesson 4.6)

*... J48 produces a restricted set of probs*

❖ **bagged J48**

a	b	<-- classified as
367	333	a = good
54	246	b = bad

cost 603

# Lesson 4.6: Cost-sensitive classification vs. cost-sensitive learning

## Method 2: Cost-sensitive *learning*

- ❖ Cost-sensitive ***classification*** adjusts the output of a classifier
- ❖ Cost-sensitive ***learning*** learns a different classifier
- ❖ Create a new dataset with some instances replicated
- ❖ To simulate the cost matrix

a	b	
0	1	a = good
5	0	b = bad
- ❖ add 4 copies of every *bad* instance

*Dataset credit-g has 700 good and 300 bad instances (1000)*  
*→ new version has 700 good and 1500 bad (2200)*  
... and re-learn!
- ❖ In practice, re-weight the instances, don't copy them



# Lesson 4.6: Cost-sensitive classification vs. cost-sensitive learning

## Cost-sensitive learning in Weka:

**CostSensitiveClassifier** with **minimizeExpectedCost = false** (default)

- ❖ Credit dataset, cost matrix as before **credit-g.arff**; **J48**
- ❖ **meta > CostSensitiveClassifier**; **minimizeExpectedCost = false**

❖ **NaïveBayes**

a	b	<-- classified as	cost 530
445	255	a = good	
55	245	b = bad	

❖ **J48**

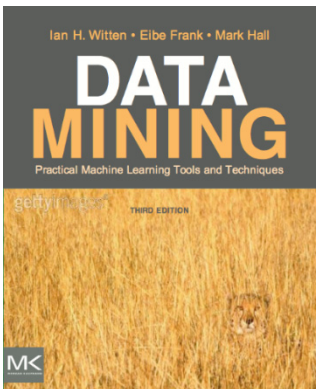
a	b	<-- classified as	cost 658
372	328	a = good	
66	234	b = bad	

❖ **bagged J48**

a	b	<-- classified as	cost 581
404	296	a = good	
57	243	b = bad	

# Lesson 4.6: Cost-sensitive classification vs. cost-sensitive learning

- ❖ Cost-sensitive **classification**: adjust a classifier's output
- ❖ Cost-sensitive **learning**: learn a new classifier
  - by duplicating instances appropriately (inefficient!)
  - or by internally reweighting the original instances
- ❖ **meta > CostSensitiveClassifier**
  - implements both cost-sensitive classification and cost-sensitive learning
- ❖ Cost matrix can be stored and loaded automatically
  - e.g. `german-credit.cost`
- ❖ Section 5.7 *Counting the cost*





# ***More Data Mining with Weka***

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