EAS508-HW4

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Lab Code Homework

5.3 Cross Validation Labs

5.3.1 Validation Set Approach

```
# Setting the seed and loading the data
library(ISLR2)
## Warning: package 'ISLR2' was built under R version 4.0.5
set.seed(1)
train <- sample(392,196)</pre>
# Fitting a linear regression on the train data using subset option
lm.fit <- lm(mpg ~ horsepower, data = Auto, subset = train)</pre>
# Predicting the estimates for the 392 observations and calculate the MSE for 192 observations
mean((Auto$mpg - predict(lm.fit, Auto))[-train]^2)
## [1] 23.26601
# Fitting cubic regression and calculating the MSE
lm.fit2 <- lm(mpg ~poly(horsepower, 2), data = Auto, subset = train)</pre>
mean((Auto$mpg - predict(lm.fit2, Auto))[-train]^2)
## [1] 18.71646
# Fitting uadratic regression and calculating the MSE
lm.fit3 <- lm(mpg ~ poly(horsepower, 3), data = Auto, subset = train)</pre>
mean((Auto$mpg - predict(lm.fit3, Auto))[-train]^2)
```

```
## [1] 18.79401
# Using different seed and calculating the values for all the three regressions - will result into dif
set.seed(2)
train <- sample(392,196)</pre>
# Linear regression MSE
lm.fit <- lm(mpg ~ horsepower, data = Auto, subset = train)</pre>
mean((Auto$mpg - predict(lm.fit, Auto))[-train]^2)
## [1] 25.72651
# Cubic regression MSE
lm.fit2 <- lm(mpg ~poly(horsepower, 2), data = Auto, subset = train)</pre>
mean((Auto$mpg - predict(lm.fit2, Auto))[-train]^2)
## [1] 20.43036
# Quadratic regression MSE
lm.fit3 <- lm(mpg ~poly(horsepower, 3), data = Auto, subset = train)</pre>
mean((Auto$mpg - predict(lm.fit3, Auto))[-train]^2)
## [1] 20.38533
5.3.2 Leave One-Out Cross-Validation
# LOOCV using glm() package
glm.fit <- glm(mpg ~ horsepower, data = Auto)</pre>
coef(glm.fit)
## (Intercept) horsepower
## 39.9358610 -0.1578447
# LOOCV using normal lm() function
```

lm.fit <- lm(mpg ~ horsepower, data = Auto)</pre>

coef(lm.fit)

```
## (Intercept) horsepower
## 39.9358610 -0.1578447
# Cross-validation error using glm() package
library(boot)
## Warning: package 'boot' was built under R version 4.0.5
glm.fit <- glm(mpg ~ horsepower, data = Auto)</pre>
cv.err <- cv.glm(Auto, glm.fit)</pre>
cv.err$delta
## [1] 24.23151 24.23114
# Calculating CV error for for polynomial of order 1 to 10 using a for loop.
cv.error \leftarrow rep(0,10)
for (i in 1:10) {
  glm.fit <- glm(mpg ~ poly(horsepower, i), data = Auto)</pre>
 cv.error[i] <- cv.glm(Auto, glm.fit)$delta[1]</pre>
}
cv.error
## [1] 24.23151 19.24821 19.33498 19.42443 19.03321 18.97864 18.83305 18.96115
```

[9] 19.06863 19.49093

5.3.3 k-Fold Cross Validation

```
# Calculating k-fold CV error for for polynomial of order 1 to 10 with k = 10
set.seed(17)
cv.error.10 <- rep(0,10)

for (i in 1:10) {
    glm.fit <- glm(mpg ~ poly(horsepower, i), data = Auto)
    cv.error.10[i] <- cv.glm(Auto, glm.fit, K = 10)$delta[1]
}
cv.error.10</pre>
```

```
## [1] 24.27207 19.26909 19.34805 19.29496 19.03198 18.89781 19.12061 19.14666
## [9] 18.87013 20.95520
```

$6.5.3~\mathrm{PCR}$ and PLS Regression