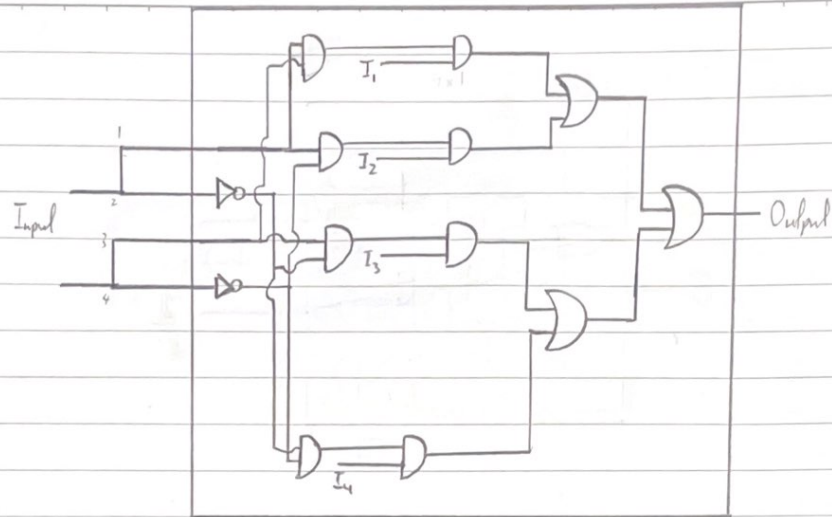


CSCI113-Lab 1

1) 4x1 multiplexer:

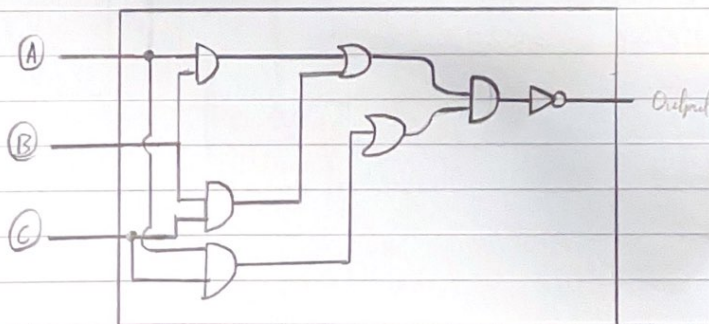


2)

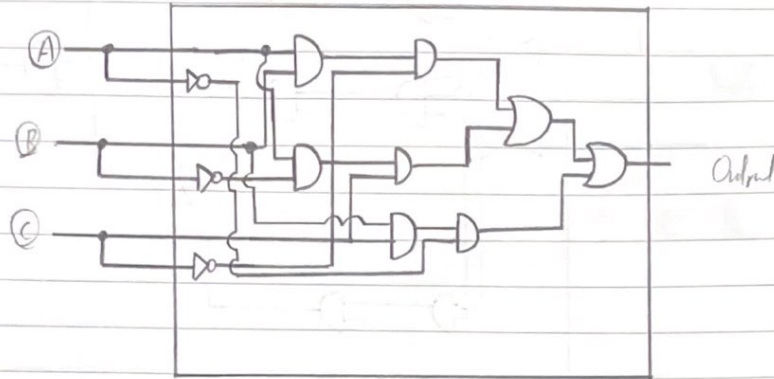
x_2	x_1	x_0	F_1	F_2	F_3	F_4
0	0	0	0	0	1	0
0	0	1	0	1	1	0
0	1	0	0	1	1	0
0	1	1	1	0	1	0
1	0	0	0	1	0	1
1	0	1	1	0	0	1
1	1	0	1	0	0	1
1	1	1	0	1	0	1

$$\begin{array}{r} 111 \\ 000 \\ +1 \\ \hline 001 \end{array} \quad \begin{array}{r} 110 \\ 001 \\ +1 \\ \hline 011 \end{array}$$

3) $E = ((A \cdot B) + (A \cdot C) + (B \cdot C)) \cdot (A \cdot B \cdot C)$



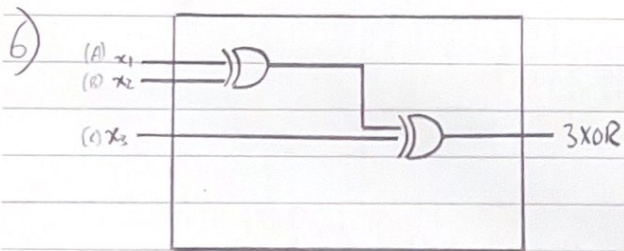
$$E = (A \cdot B \cdot \bar{C}) + (A \cdot \bar{B} \cdot C) + (\bar{A} \cdot B \cdot C)$$



$E = (A \cdot B \cdot \bar{C}) + (A \cdot \bar{B} \cdot C) + (\bar{A} \cdot B \cdot C)$ seems to be more efficient among the two terms.

$$\begin{aligned} 4) E &= ((A \cdot B) + (A \cdot C) + (B \cdot C)) \cdot (\bar{A} \cdot \bar{B} \cdot \bar{C}) = (A \cdot B) \cdot (\bar{A} + \bar{B} + \bar{C}) + (A \cdot C) \cdot (\bar{A} + \bar{B} + \bar{C}) + (B \cdot C) \cdot (\bar{A} + \bar{B} + \bar{C}) \\ &= (A \cdot B) \cdot (\bar{C}) + (A \cdot C) \cdot (\bar{B}) + (B \cdot C) \cdot (\bar{A}) = (A \cdot B \cdot \bar{C}) + (A \cdot \bar{B} \cdot C) + (\bar{A} \cdot B \cdot C) \neq \end{aligned}$$

$$\begin{aligned} 5) \text{XOR} &= (A + B) \cdot (\bar{A} \cdot \bar{B}) = (A + B) \cdot (\bar{A} + \bar{B}) = ((A + B) \cdot \bar{A}) + ((A + B) \cdot \bar{B}) \\ &= (\bar{A} \cdot B) + (A \cdot \bar{B}) = (A \cdot \bar{B}) + (\bar{A} \cdot B) \end{aligned}$$



A	B	C	$A \oplus B \oplus C$
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

$$\begin{aligned} E &= \bar{A} \cdot \bar{B} \cdot \bar{C} + \bar{A} \cdot \bar{B} \cdot C + \bar{A} \cdot B \cdot \bar{C} + \bar{A} \cdot B \cdot C \\ &\quad + A \cdot \bar{B} \cdot \bar{C} + A \cdot \bar{B} \cdot C + A \cdot B \cdot \bar{C} + A \cdot B \cdot C \end{aligned}$$