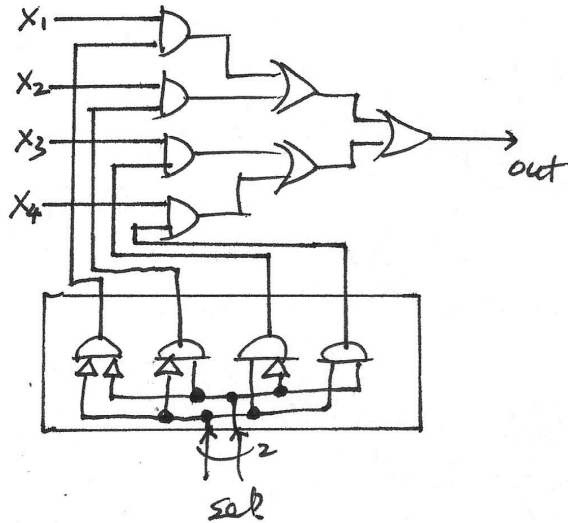


Assignment 1 key

#1 4x1 Mux using only 3 gates (AND, OR, NOT).



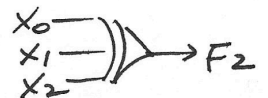
#2

Truth table

X_2	X_1	X_0	F_1	F_2	F_3	F_4
0	0	0	0	0	1	0
0	0	1	0	1	1	0
0	1	0	0	1	1	0
0	1	1	1	0	1	0
1	0	0	0	1	0	1
1	0	1	1	0	0	1
1	1	0	1	0	0	1
1	1	1	0	1	0	1

Rewrite F_2

$$F_2 = X_2 \oplus X_1 \oplus X_0$$



$$F_1 = \bar{X}_2 \cdot X_1 \cdot X_0 + X_2 \cdot \bar{X}_1 \cdot X_0 + X_2 \cdot X_1 \cdot \bar{X}_0$$

$$F_2 = \bar{X}_2 \cdot \bar{X}_1 \cdot X_0 + \bar{X}_2 \cdot X_1 \cdot \bar{X}_0 + X_2 \cdot \bar{X}_1 \cdot \bar{X}_0 + X_2 \cdot X_1 \cdot X_0$$

$$F_3 = \bar{X}_2 \cdot \bar{X}_1 \cdot \bar{X}_0 + \bar{X}_2 \cdot \bar{X}_1 \cdot X_0 + \bar{X}_2 \cdot X_1 \cdot \bar{X}_0 + \bar{X}_2 \cdot X_1 \cdot X_0$$

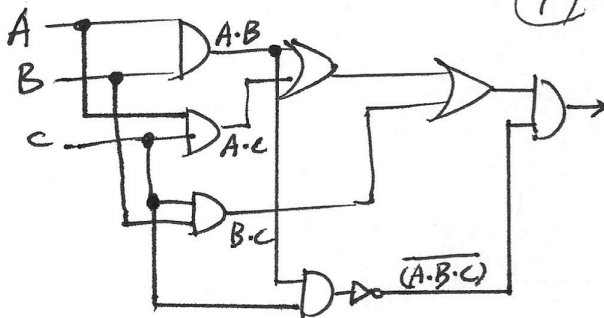
$$\text{or, } F_3 = \bar{X}_2$$

$$F_4 = \bar{X}_2 \cdot \bar{X}_1 \cdot \bar{X}_0 + X_2 \cdot \bar{X}_1 \cdot X_0 + X_2 \cdot X_1 \cdot \bar{X}_0 + X_2 \cdot X_1 \cdot X_0$$

$$\text{or, } F_4 = X_2$$

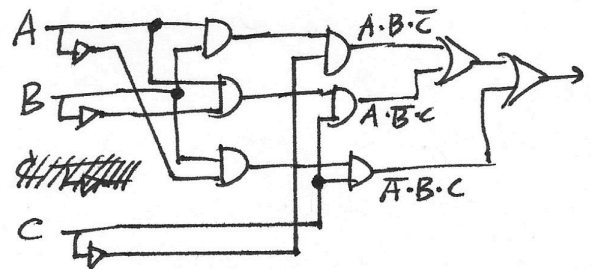
#3

$$E = ((A \cdot B) + (A \cdot C) + (B \cdot C)) \cdot \overline{(A \cdot B \cdot C)} \quad \text{vs.} \quad E = (A \cdot B \cdot \bar{C}) + (A \cdot \bar{B} \cdot C) + (\bar{A} \cdot B \cdot C)$$



(7)

8



#4

$$\begin{aligned}
 E &= ((A \cdot B) + (A \cdot C) + (B \cdot C)) \cdot \overline{(A \cdot B \cdot C)} \\
 &= ((A \cdot B) + (A \cdot C) + (B \cdot C)) \cdot (\bar{A} + \bar{B} + \bar{C}) \quad \text{—by De Morgan's law} \\
 &= ((A \cdot B) \cdot (\bar{A} + \bar{B} + \bar{C})) + ((A \cdot C) \cdot (\bar{A} + \bar{B} + \bar{C})) + ((B \cdot C) \cdot (\bar{A} + \bar{B} + \bar{C})) \quad \text{—by distributive law} \\
 &= \begin{pmatrix} \underbrace{(A \cdot B \cdot \bar{A})}_{\phi} + \underbrace{(A \cdot B \cdot \bar{B})}_{\phi} + \underbrace{(A \cdot B \cdot \bar{C})}_{\phi} \\ + \underbrace{(A \cdot C \cdot \bar{A})}_{\phi} + \underbrace{(A \cdot C \cdot \bar{B})}_{\phi} + \underbrace{(A \cdot C \cdot \bar{C})}_{\phi} \\ + \underbrace{(B \cdot C \cdot \bar{A})}_{\phi} + \underbrace{(B \cdot C \cdot \bar{B})}_{\phi} + \underbrace{(B \cdot C \cdot \bar{C})}_{\phi} \end{pmatrix} \\
 &= (A \cdot B \cdot \bar{C}) + (A \cdot C \cdot \bar{B}) + (B \cdot C \cdot \bar{A}) \\
 \therefore E &= ((A \cdot B) + (A \cdot C) + (B \cdot C)) \cdot \overline{(A \cdot B \cdot C)} \\
 &\text{and } E = (A \cdot B \cdot \bar{C}) + (A \cdot \bar{B} \cdot C) + (\bar{A} \cdot B \cdot C) \text{ are equivalent.}
 \end{aligned}$$

$$\begin{aligned}
 \text{ref} \\
 (X \cdot \bar{X}) &= \phi \\
 (\phi + X) &= X
 \end{aligned}$$

#5

proof $X \circ Y = (A \cdot \bar{B}) + (\bar{A} \cdot B) = (A + B) \cdot \overline{(A \cdot B)}$

start from $(A + B) \cdot \overline{(A \cdot B)}$

$$= (A + B) \cdot (\bar{A} + \bar{B})$$

$$= ((A + B) \cdot \bar{A}) + ((A + B) \cdot \bar{B})$$

$$= (A \cdot \bar{A}) + (B \cdot \bar{A}) + (A \cdot \bar{B}) + (B \cdot \bar{B})$$

$$= (B \cdot \bar{A}) + (A \cdot \bar{B}) = \underline{(A \cdot \bar{B}) + (\bar{A} \cdot B)} \quad \checkmark$$

#6

3-input XOR — True if # of Truthts is odd.

X_1	X_2	X_3	XOR
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

Logic Eg:

$$\text{XOR} = (\overline{X_1} \cdot \overline{X_2} \cdot X_3) + (\overline{X_1} \cdot X_2 \cdot \overline{X_3}) + (X_1 \cdot \overline{X_2} \cdot \overline{X_3}) + (X_1 \cdot X_2 \cdot X_3)$$

— Using the idea of

