TAFL- Theory of Automata and Formal Language TAFL: Automata theory is a subject which describes the behaviour of automatic machines mathematically.

Applications!-

- Digital circuit design
- Compiler design
- For designing the reduced mathematical model
- · Circuit design is possible if mathematical model exists.
 - · Language: Means of communication
 - · Program : sequence of instructions
 - · String: sequence of symbols
 - · Sentence/instructions: An ordered combination of word on string that makes complete sense

why do we study theory?

Theory provides concepts and principles that help us understand the general nature of discipline

Alphabet Set (E): Set of consisting of symbols or characters.

Eq: E = {0,13 = (0+1)

length of string (IWI): w=abbcde, IWI=6 Null string (& OH); The string of length 0. 1 WI=0 (2 = 2)

Cocatenation: W1=010 W2 = 1011 w= w2 w1 = 1011010 -> cocatenation of string does not support commutative property but support associative property. L1. L2 = { W1. W2 / W1 EL, & W2 EL2} Kleen Chrule (E*): (all possible string) E* = Universal language over alphabet E | E* | = ∞ Positive Closure (E+) E+= E* - 567 MOTE: (01)* = & E, 01, 0101, 010101,} W=010 (010)0 = 8 length=0 (010) = 010 length = 3 $(010)^2 = 010010$ length = 6 * Symbol (* on +) with & is universal 1 = W given 1W1 = M Find not longth of w = mxn Revolse w = a1, a2, a3 ... an WR = an, an-1, a2, a1

W= XY WR = (XY)R = YRXR

Palindyome W=1011 wwr -> even 10111101 W=101 · w#wr-odd 10101 ™ Swbstning Any sequence of consecutive symbols from w (anystring) w = dog sublus" = { &, d, o, q, do, og, dog } s But dg is not a part of sub-string. It will be a part of power set. Non-null sub-string: Set of substring of any string we except never string 1.6. (Sub(w) - {E} {d,0,9,d0,09,d0g} PHOPEN Substring: Set of all possible substring of w except string sub(w) - {w} { E, d, o, g, do, og} Non-null Proper substring; sub(w) - & &, w} 20,0,9,do,og} Number of Substring-1. Symbols are distinct Q(Q+1) +1 Q = 1 +1 9b = 3+1 abc = 6+1

2. Symbols are some a = 1+1 1+1 aa= 2+1 900=3+1 Prefix and Suffix Pregix of ong string is nothing but set of conjugate symbol from left to night in given string. Prefix (w) = 28, d, do, dog } (1+1) Suffex (w) = { E, g, og, dog} I no. of suffix & prefix El co are present in both Power of string w' = w'.w° = w'.8 = w $\omega^2 = \omega_1 \cdot \omega_1 = \omega \cdot \omega$ $\omega^3 = \omega^2 \cdot \omega_1 = \omega \omega \cdot \omega$ Operations on longuages: L1 = {0,10,11} L2 = {11, 101, 110} LIUL2 = \$0, 10, 11, 101, 110} $L_{1} \cap L_{2} = \{11\}$ L1 = E* - L1 = (0+1)* - L, {€, 1, 01, 00,∞} LIR = {WR, WEL} LR = { 11, 101, 011}

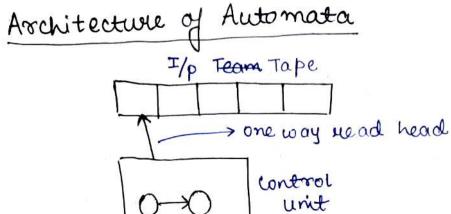
L= L1L2 = & W1W1 / W1EL1 & W1EL2 }

[L1L2 | < | L1| | L2|

Finite Automata

Architecture of Automata

T/p Team Tape



Finite Automata (FA) is a quin(5) tuple machine. (Q, E, δ, Q_0, F)

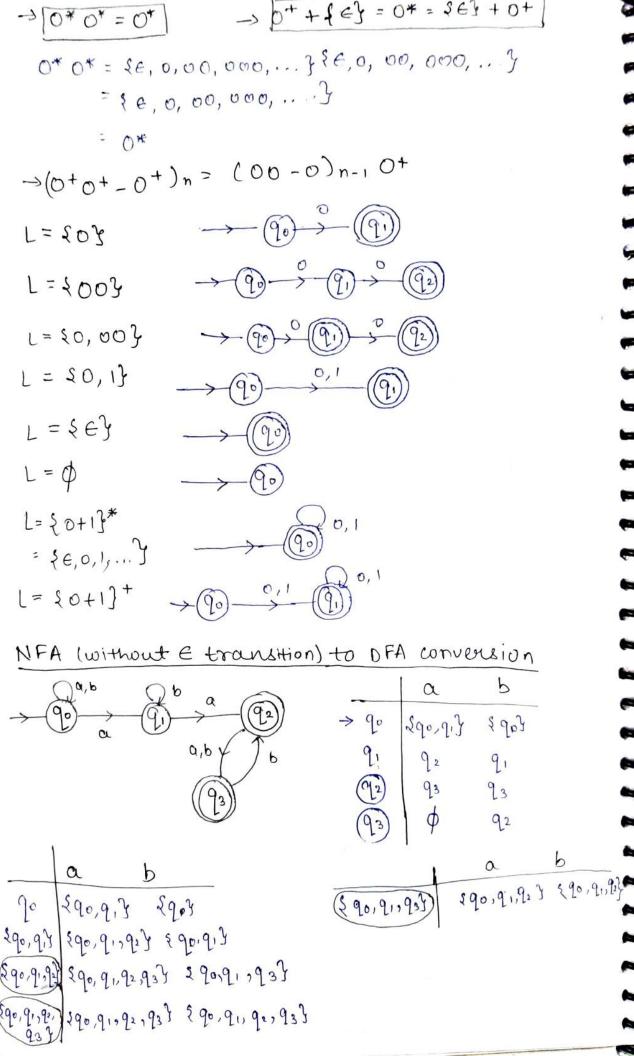
where Q > Finite set of state E > Finite set of character

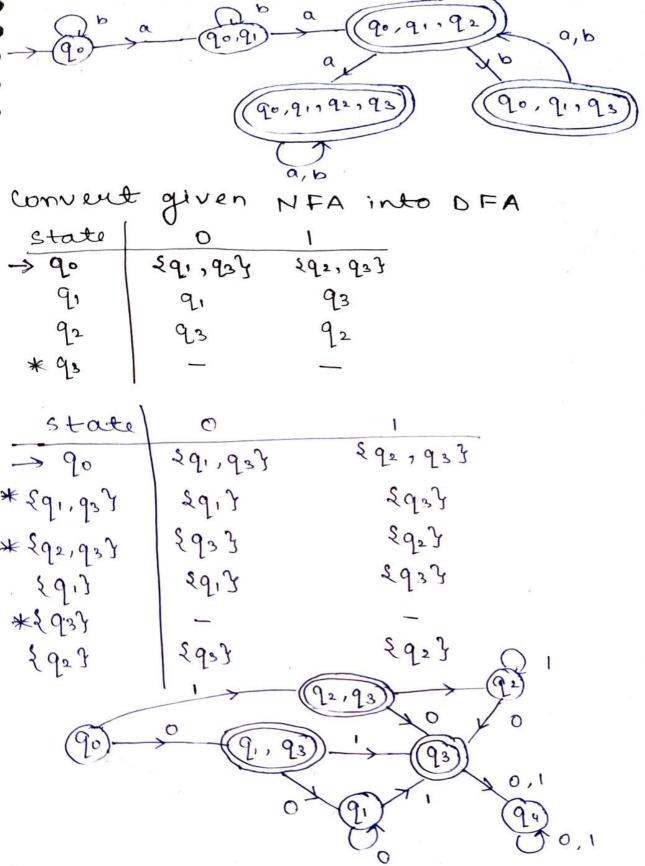
F → Finite set of Final State

F ⊆ (Q)

S: (90, a) -> 92 S: (90,b) -> 91 91 -> Qo 92 S! (91,a) -> 91 S: (911b) -> 91 91 91 9, S: (q2,a) -> q2 * 92 92 92 S: (91,b) -> 92 Difference b/w nfa and afa (i) choices are allowed (1) No choices due allowed. (1) E-transition not allowed in E-transition are allowed (11) Dead configuration is (iii) Dead configuration is not allowed. allowed. The Maximum & Minimum language over E. E = 20,19 Maximum language = €* = \$0,19*=(0,1)* = (0+1)* -Minimum langhage = 0 = (Max L)c * Cascading of transition function \$ (q0,0111) = 8(8(8(8(90,0),1),1),1) Practices for da 2 nfa Ex1: construct a finite automata for the language over alphabet $\mathcal{E} = \{0,1\}$ which consist string of exactly length 1. E = 80,13 L= 20, 13 = (0+1)

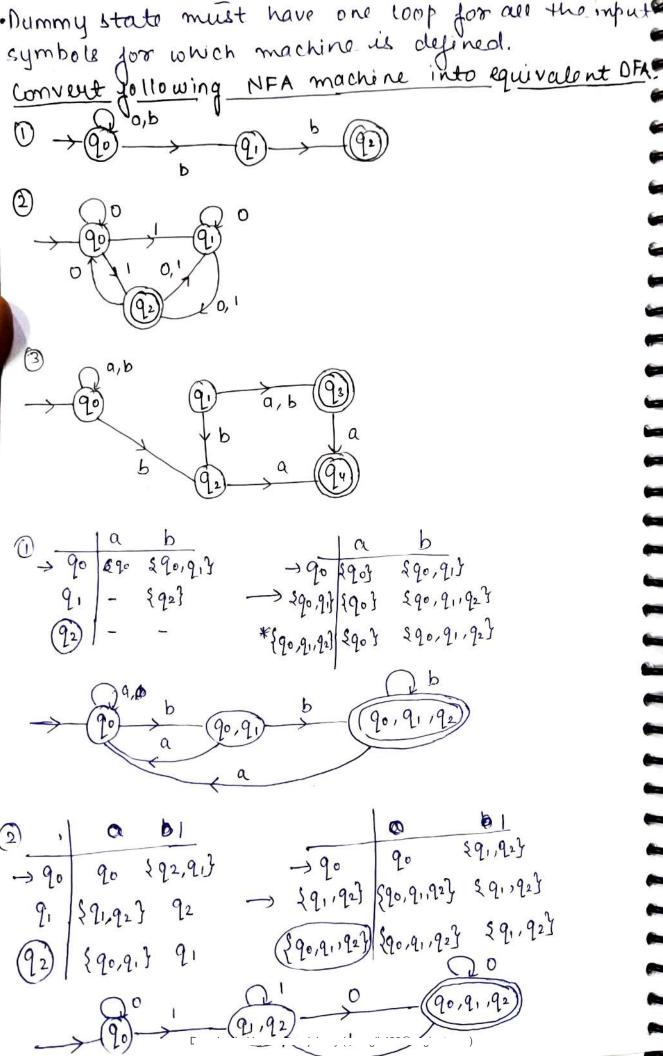
(P) → (P) Valid machine Invalid machine 🍑 つ L= 🛡 (90) (nga/dya) $(q_0) \rightarrow (q_0) \leftarrow (q_1)$ Final state are not there on final state are not reachable from initial state. EX2: Construct a finite automata for the language over alphabet \== \$0, if in which every string must start from symbol o. £ = \$0,13 L = {0,00,01,000,001,010,011,...} 92R O, 1 Je dumny state L = 0. (0+1)* = {0} { €, 0, 1, 00.} = 20,00,01,....} → 0* = \$ €, 0,00,000,0000,} 0+ = {0,00,000,} 00*=0*0=000 If the base of the language is m & you are looking Joh universal language over that base Z, thon counting of any random le length string is given by mn

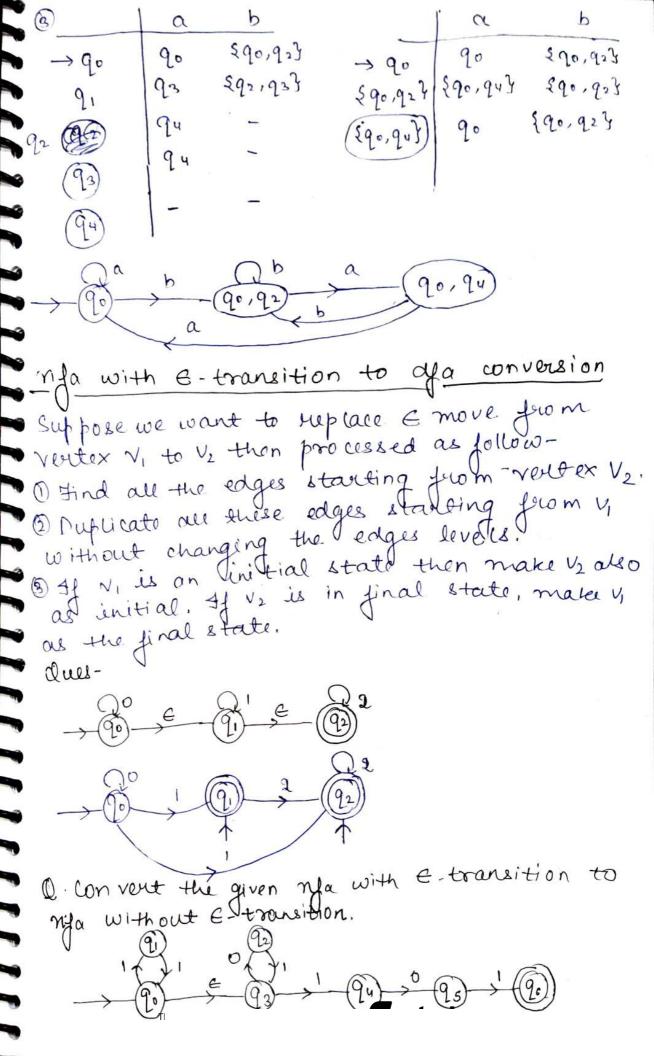




Dummy on trap state

· Dummy state will always be in dja. Dummy state will always be exactly one state in any machine. Dummy state will be non-initial knon-linel any machine. Dummy state will be non-initial knon-linel





Drow a da. for the larguage accepting string prow a da. for ab over approbet $\xi = \{a, b\}$ z = 2ab, aba, abb, abao,} Stanting with prow a dya for the language over alphabets E=80,13 such that every string of have on as a substring. £ = 20,19 (0+1)*00(0+1)* = \$00,000, 100,001,:...} 890,9,3 3903 → 90 | {qo,qi} 90 → {90,91} {90,91,923,90 (90,9,92) +90,9,,923 +90,923 (390,923) 390,91,923 390,923 0,1 90,91,90)

> 50-closeure (90) = 870,71,923 >] 1 - closure (90) = 29,,924 590,91,927 591,927 5923 (2 - cusure (203 = {923 A > (90,91,92) € (0 - clusure (q1) = 0 \$q1, q2} \$q2} (91, 92 } 5923 1 - closeure (9,1) = 29,1923 c · 2 - cropine (d1) = 2 d5 } (0 - closure (q2) = φ 1- clo sure (9,) = \$ (2 - closure (92) = {92} €-closure (90)=8(90, €) = { 90, 9, 92} 0-closure (90, 91, 92) = 0-closuro (90) U 6-closure (q1) U 0-closure (92) = 290,91,92)U = {90,91,92} 0,1 0,1,2 for the given rifa equivalent de Q. Find o-closure of A = EA, B, C3 1-closure of A = SA, B, C3 0- closure of B = SA, B, C3

So-closure of C=&C3 e-chosure (A) = \$1,B,Cy qe (\$A, B, C3) \$A, B, C3 \$A, B, C3 convert the given ma machine into equivalent and de maciline. 0-closure of A = &B,C} 1-closure of A = &A,B,C} 0-closure of B = {c} o-closure of c = ECY 1-closure of c = & c } € closure (A) = &A,B,C3 0 \$ B, C & & A, B, C } 2 → (\$ A, B, C3) १८५. १८५ १८५ १८५ 9, (88, 69) 92 (3 () 20,1

Minimalization of all ala There is two algorithms to minimise any given aga-(1) Poutitioning method (ii) My hill marrodo narrodo method Partitioning Method > Distinguishable & Indistinguishable state Two or mode than two states (in any machine) are indistinguishable if for the same input,.
we are getting output - all final or all non-final Otherwise states are distinguishable. Eg: of got que indistingues hable for input co 6(90, W) = F7/NF 8(q1, w) = F 1/NF But if they are distinguishable for some input, we will get - $\delta (q_0, \omega) = NF \int /F \delta (q_1, \omega) = F \int /NF$ K-equivalence Two or more than two states will, k-equivalent if and only if up to the length K for all possible string, states must be indistingui--shable & it is denoted by Tk... Q. Construct a min state automata equivalent to da whose transition table is defined State a → 90 - 91 - 92 by -91 - 94- 93

94 - 97 - 96 95-93-96 96 - 96 - 96 97 - 94 - 96 Inveacrable or dead state or inaccessible state In any finite automata, if any state is not In any finite automata, if any state then it is not reachable from starting state then it is reachable fiveachable /dead/inaccessible state. No = { 290,91,98,95,96,973, 293,9433 17,= { 990, 96 }, 891, 923, 898, 943, 295, 9,33 Ma= { 2903, 2963, 29,023, 293,943, 295,9733 173 = { \$90}, \$96}, \$91,92}, \$95, 943, \$95,973} 9,2 A 90 96 £9,,923 296,978 96 (893,943) 893,944 96 \$ 95,973 Q. Minimise the given d'a 0

Mo = & { A,B,F}, {C,D,E}} TI, = { { A, B}, } F}, { C, D, E}} $\Pi_2 = \{\{A,B\}, \{F\}, \{C, b, E\}\}$

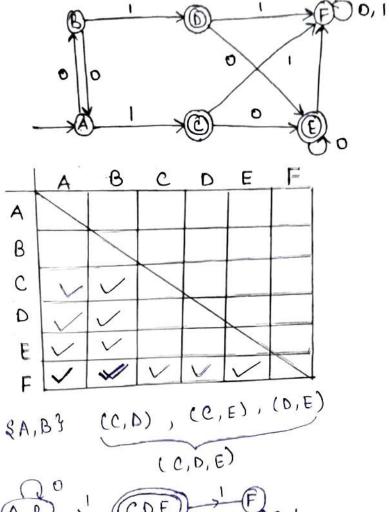
| | 0 | 1 |
|-------------|-------|----------|
| 7A,B3 | (0,A) | ₹ c, o } |
| SFY (CO, O) | { E} | 3 F3 |
| { C, D, E } | \$ E3 | {F} |

effa minimisation by Ma Hill Navode Theorem

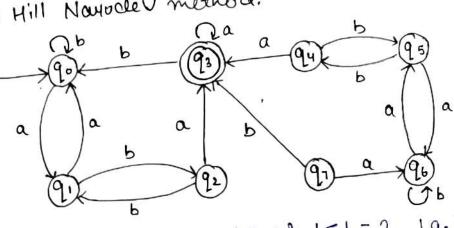
- · Draw a table for all poins of states p, 2.

 · Make all point where PEFAQFF
- · If there are any unmarked pair P, Q such that $\delta(p, x)$, $\delta(Q, x)$ is already marked then

- · Repeat this process until no marking can be
- combine all unmark paire & make them are a
- single state. Q. Minimise the given dya by using Ma Hill Narode Theorem.

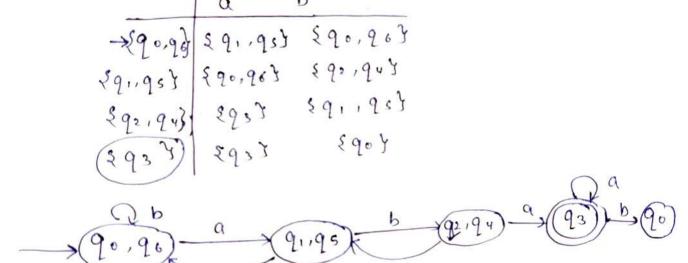


O Minimise the given du by using pautioning & Ma Hill Nayvole method.



 $|F| = \{1\}, |Q| = 8, \le = \{a, b\}, |E| = 2, |q_0| = 1$

 $\eta_{0} = \xi \xi q_{0}, q_{1}, q_{2}, q_{4}, q_{5}, q_{6}\xi, \xi q_{3}\xi$ $\eta_{1} = \xi \xi q_{0}, q_{1}, q_{5}, q_{6}\xi, \xi q_{2}, q_{4}\xi, \xi q_{3}\xi$ $\eta_{1} = \xi \xi q_{0}, q_{1}, q_{5}, q_{6}\xi, \xi q_{2}, q_{4}\xi, \xi q_{3}\xi$ $\eta_{2} = \xi \xi q_{0}, q_{6}\xi, \xi q_{1}, q_{5}\xi, \xi q_{2}, q_{4}\xi, \xi q_{3}\xi$ $\eta_{3} = \xi \xi q_{0}, q_{6}\xi, \xi q_{1}, q_{5}\xi, \xi q_{2}, q_{4}\xi, \xi q_{3}\xi$



O. Minimise the given afa by partioning & Ma Hill Nauvode method.

