Chapter-6 Lines And Angles

Exercise 6.1

In the below figure, lines AB and CD intersect at 0. If $\angle AOC + \angle BOE = 70^\circ$ and angle $\angle BOD = 40^\circ$. Find $\angle BOE$ and neflex

Solution:

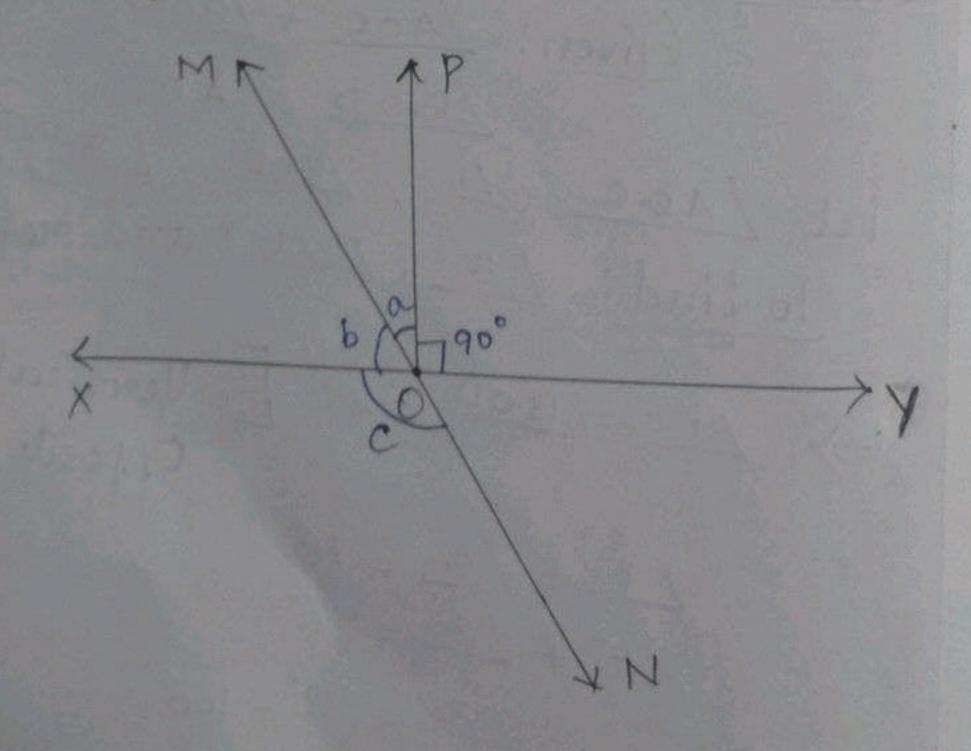
$$\frac{1}{40^{\circ} + 23} = 70^{\circ}$$

$$\frac{1}{40^{\circ} + 23} = 70^{\circ}$$

$$\frac{1}{40^{\circ} + 23} = 70^{\circ} - 40^{\circ}$$

 $/3 = 30^{\circ}$. $\Rightarrow /BOE = 30^{\circ}$. [: AOB is a straight line]. $/L + /2 + /3 = 180^{\circ}$. $(/L + /2) + /2 = 180^{\circ}$. $/2 + 70^{\circ} = 180^{\circ}$. $/2 = 110^{\circ}$.

2) In this figure, lines XY and MN intersect at 0. If LPOX = 90° and a: b = 2:3, find c



Solution :-

Given / POY = 90°
a:b = 2:3

> let angles à and it be 22, 32.

[: XY is a line], $(XOP + POY = 180^{\circ})$ [Linear Pain $(XOP = 180^{\circ} - POY)$ Angles] $= 180^{\circ} - 90^{\circ}$ $\Rightarrow (XOP = 90^{\circ})$

 $\frac{1 \times OP}{90} = a + b \left[\frac{1 \times OP}{1 \times OP} = \frac{1 \times OM}{1 \times OP} \right]$

5x = 90°

x = 90°

 $\Rightarrow x = 18^{\circ}$. $\alpha = 2x = 2 \times 18^{\circ} = 36^{\circ}$

b = 3x = 3 x 18° = 54°.

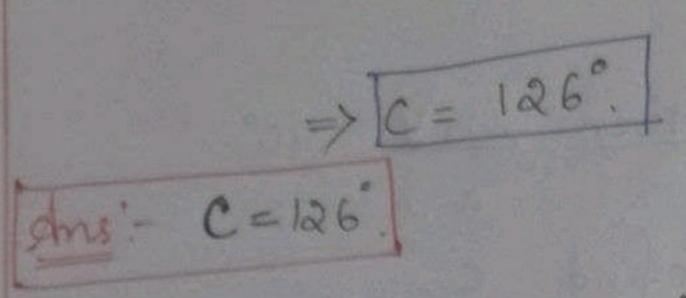
[:MN vis a line];

MEX + XON = 180° [Linear Pair Angles]

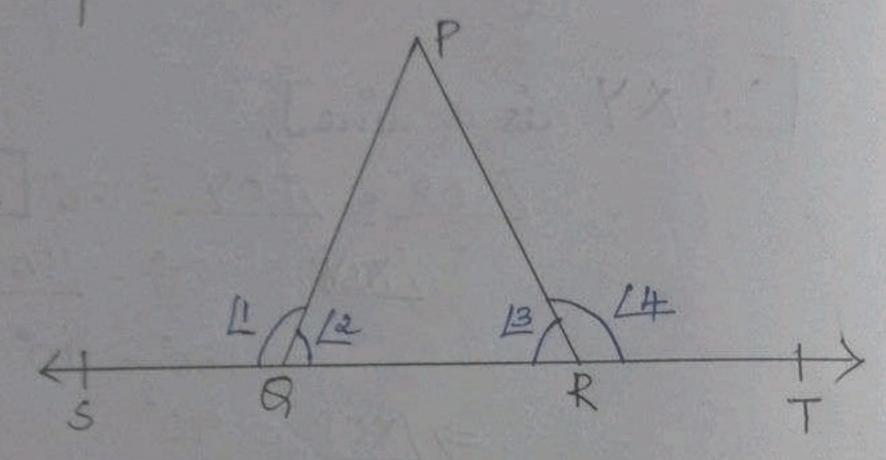
b + C = 180° [from the figure].

54° + C = 180°

C = 180° - 54°.



3) In the below figure, LPRR = LPRR. - LPRR. - LPRR. - LPRR.



Detution.

Let IPBR = 12, IPBS = 11,

IPBR = 13, [PRT = 14.

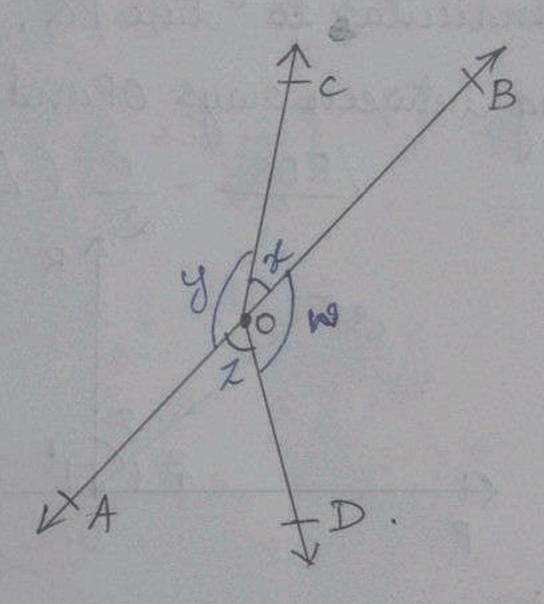
Given 12 = 13.

Toprove 11 = 14.

Firstie a straight line], LI+L2=180° ? [Linear Pain L3+L4=180°] Angles]

·. L1+12= L3+ L4 [: Both sums L1+13= L3+ L4 [: Given 12=13]

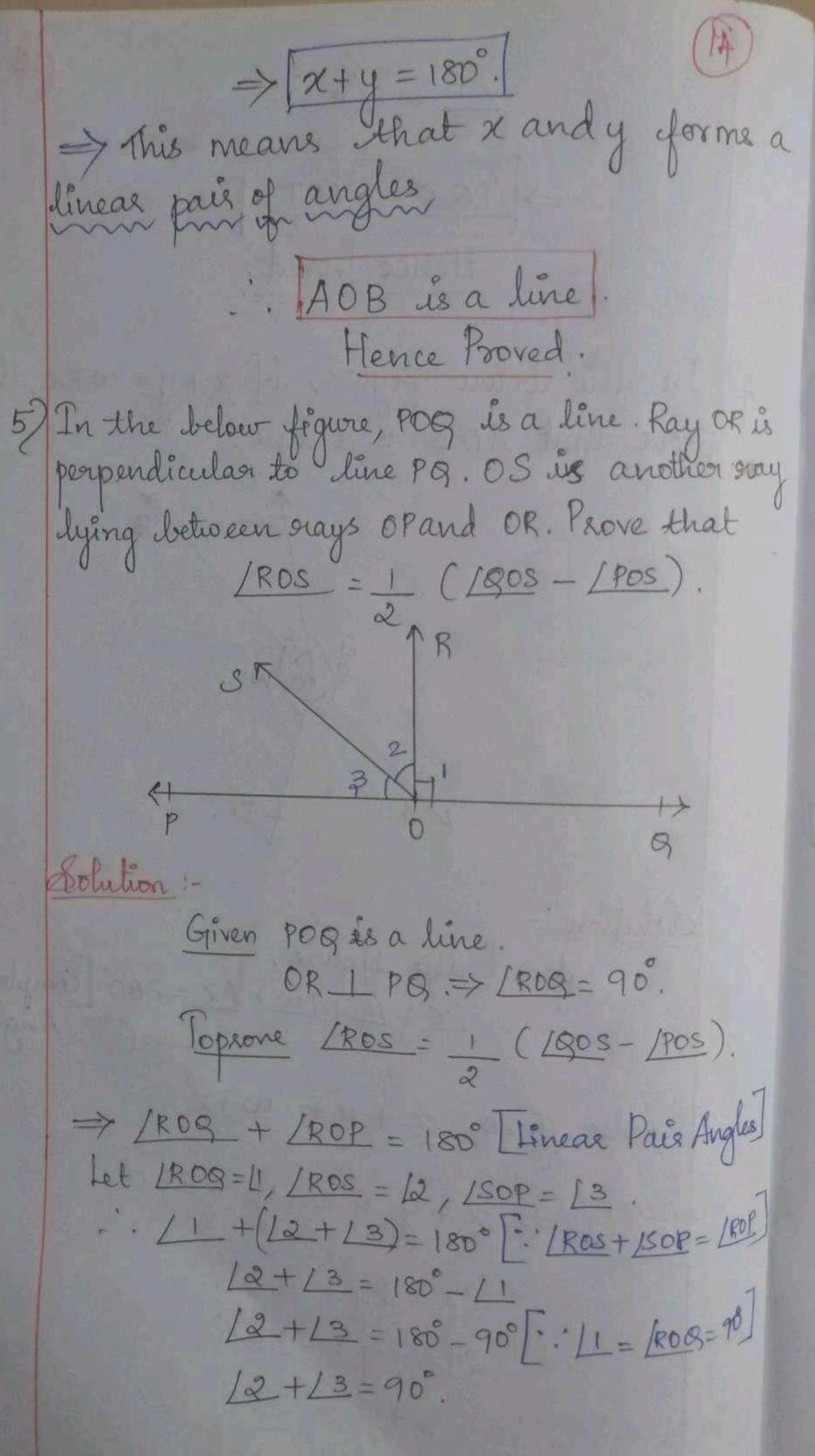
A In the below figure, if x+y=w+z, then prove that AOB is a line.



Solution :-

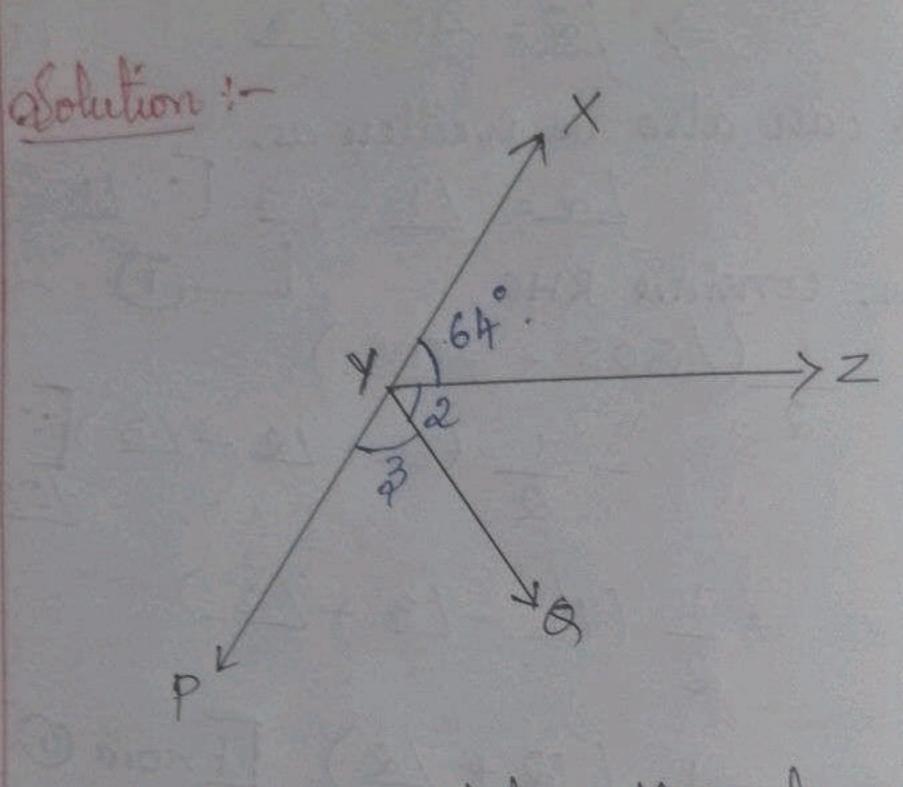
Also, given x + y = w+z

$$2x + 2y = 360^{\circ}$$
.
 $2(x + y) = 360^{\circ}$.
 $2(x + y) = 360^{\circ}$.



=> 12= 96- L3. This can also be weither as, [:11 =96]. Now, consider RHS, L-0 = 1 (11+12-13)[:180s= = 1 (11-13+12) = 1 (12+12) [From 0]. = 1 (2 /3) = 12 = /ROS > LROS = 1 (1805 - 1905) Hence Proved.

produced to point P. Dnaw a figure from
the given Information. If may 19 bisects
(ZYP) find LXYS and reflex 194P.



From the given data, the above figure is drawn.

Given /XYZ = 64°. [: XP is a line], /XYZ + /ZYP = 180° [Linear Pair L (1) aarion

Also, Given gray YQ drisects (ZYP,

[248 = 12, 1949 = 13.

-> 12 = 13 - 2.

-> 1xyz + 12 + 13 = 180° [2249 =

[248 + 1489]

64° + 12 + 13 = 180°

64° + 2 L2 = 180° [from @]
2 L2 = 180° - 64°
2 L2 = 116°

12 = 116°

(17)

12 = 58 12=13=58°. · . /xyg = /xyz + /zyg = /x4z + /2 = 64° +580 => (XYB = 122°) Reflex LBYP = R [3 = 360 - 13 = 360° - 58° => R (QYP = 302°)

Ans: LXYB = 122°, R 184P = 302°.

Exercise 6.2

2 In the figure, find the values of x and y and then show that ABIICD.

Solution:



Gjiven:
* The figure. * values of x andy * Prove that ABILCE. -> The teans versal intersects 2 lines AB and CA such that, 2+50°=180°. L'hear Pair & xiom $\Rightarrow \chi = 180^{\circ} - 50^{\circ}$ x = 130° .. y = 130° [: Vertically Opposite
Angles]. => Lx = 4y = 130° L'Alliernate Interior and alternate interior angles are equal, then the 2 lines will be parallel. Ans! - Lx = Ly = 130° => ABIICA is proved.

2) In the figure, if ABIICA, CAIIFF and y: Z=3:7, findx.

Solution:

Given: ABIICD

CDIIFF

y:Z=3:7

Pofind: - x.

⇒ Let the transversal meet at G, H, I the lines AB, CD, EF respectively. Let y = 3a, Z = Ta.

".' LCHG= y >> LDHI = y [Ventically Opposite
Angles]

DHI + LFIH = 180° [Angles on the same side of the leansversal]

:, y + Z = 180° [LDHI = y, LFIH = Z]

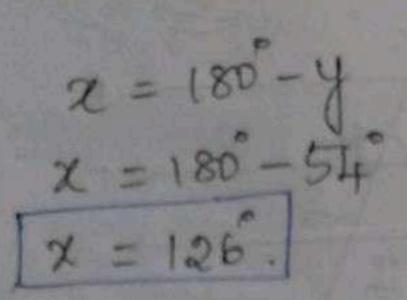
3 a + 7 a = 180°

10a=180°

 $y = 3a = 3 \times 18^{\circ} = 54^{\circ}$ $z = 7a = 7 \times 18^{\circ} = 126^{\circ}$

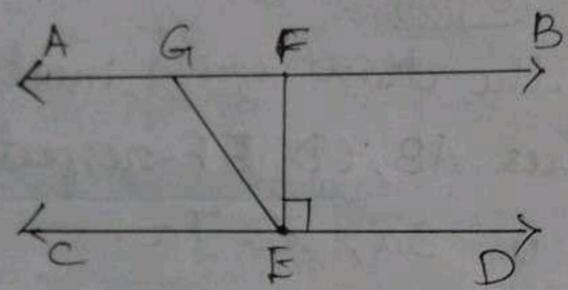
=>]y=54°, z=126°.

x + y = 180° [Angles on the same side of the trans versal]



dns: 2=126°

37 In the figure, & ABIICD, EFLCD and GED=126°, find AGE, GEF and IFGE.



Solution

Given ABICD EFLCD.

GED= 126.

Tofind LAGE, LGEF, LFGE.

=> LAGE = LGED [Allernate Angles]
- LAGE = 126]

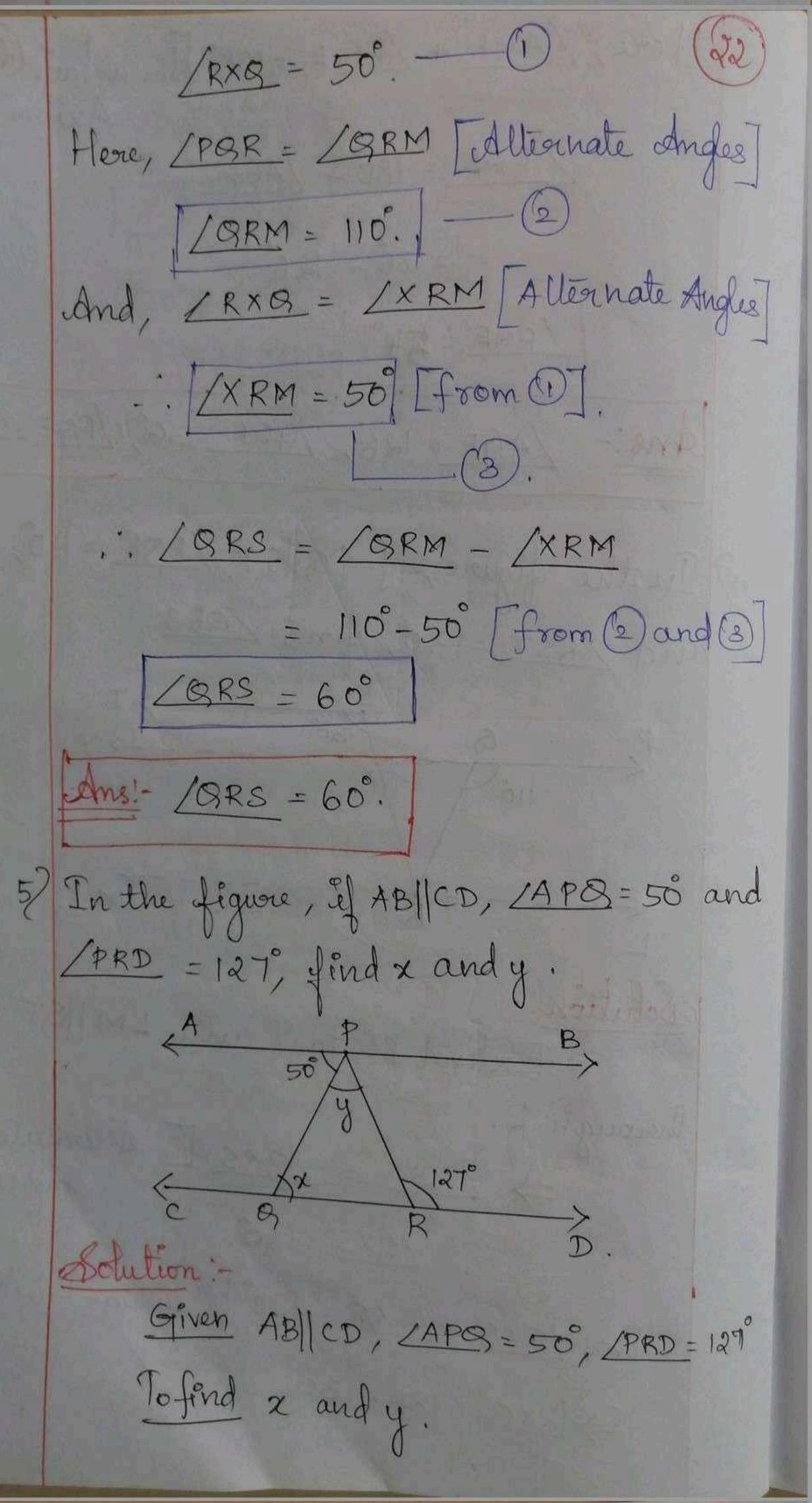
Also, LGED = LGEF + LFED

126 = [GIEF + 90° [. [FED = 90°].

/GFF = 126°-90°

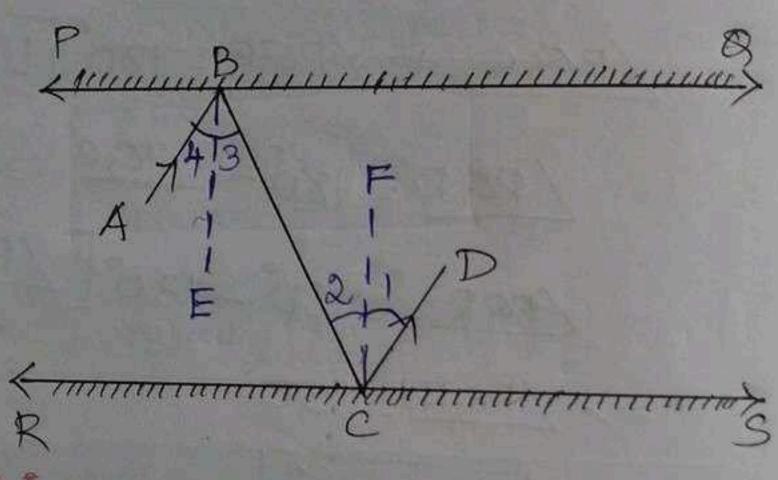
/GFF = 36°.

Hore, LAGE + LFGIF = 180° [Linear Pair (21) Axiom]. LFGF = 180 - LAGIE = 186 - 126° LFGE = 54° dns:- [AGE = 126°, [GEF = 36°, [FGE = 54°] 47 In the figure, if PallsT, LPQR = 110, and LRSI = 130°, find LQRS. P_ 8 ---> T Extend PQ to Y and LM 1/ST thorough R. => ITSX = LOXS [: Alternate dingles] .'. LBXS = 130°. Also, 19xs + 1RXB = 180° [. Linear Pais Angles => [RXB = 180 - 130



=> LAPB + LPBC = 180° Pair of consecutive interior angles = 180 50°+ 1980° [Given 1APQ=50] 1990 = 180° - 50° [PBC = 130°. LPBC + LPBR = 180° Lineage Paige Azion [PAR = 1800 - [PBC [PBR = 180° - 130° [LPAC = 130] > LPBR = 50° => 2 = 50° Here, x+y=127° [Exterior Angle of a touangle = sum of 2 Enterior opposite angles y=127°-2 y=127°-50° [x=50] => 1 = 77° Ans: - 2 = 50° and y = 77°

To the figure, PR and RS one 2 (24)
misorors placed parallel to each other, In
incident may AB strikes the misoror PR
at B, the neflected may moves along the
path BC and strikes the misoror RS at C
and again neflects back along CD. Prove
that AB | CD.



Solution:

At point B, down BFIPB and at point C, down CFIRS.

$$\angle 1 = \angle 2 \rightarrow 0$$
 ? [Angle of incidence $\angle 3 = \angle 4 \rightarrow \odot$] = Angle of reflection]
$$\angle 2 = \angle 3 \rightarrow \odot$$
 [A llearnate Angles]
from \odot , \odot , \odot ,
$$\angle 1 = \angle 4 \rightarrow \odot$$

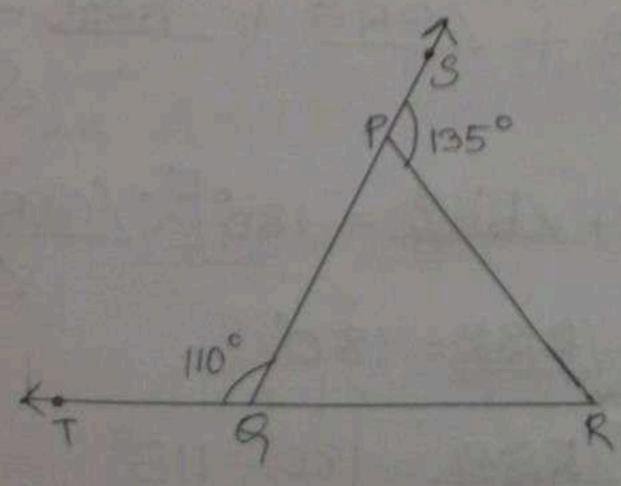
Add a and A, 11+12=13+14. ... LABC = LBCD. Donce Alternate Angles are equal, ABUCD. coms: ABICD Hence Proved.

Exercise 6.3

17 In the figure, sides Of and RB of a APBR.

ORE produced to points Sand Tonespectively.

If LSPR = 135° and LPBI = 110°, find LPRB.



Dobution:

(26)

Given LSPR = 135°, LPBT = 110° Tofind LPRR.

Here, LSPR + LBPR = 180 [Lineau Paign Axiom

135° + 180° - Given 1SPR = 180° - Given 1SPR

180°-135°

19PR = 45°

Also, 1PBT + 1PBR = 180 [Linear Pain Axion

110° + LPBR = 180° [: Given LPBT]

LPBR = 180°-110° = 110°]

[PBR = 70°

Now, In triangle PBR,

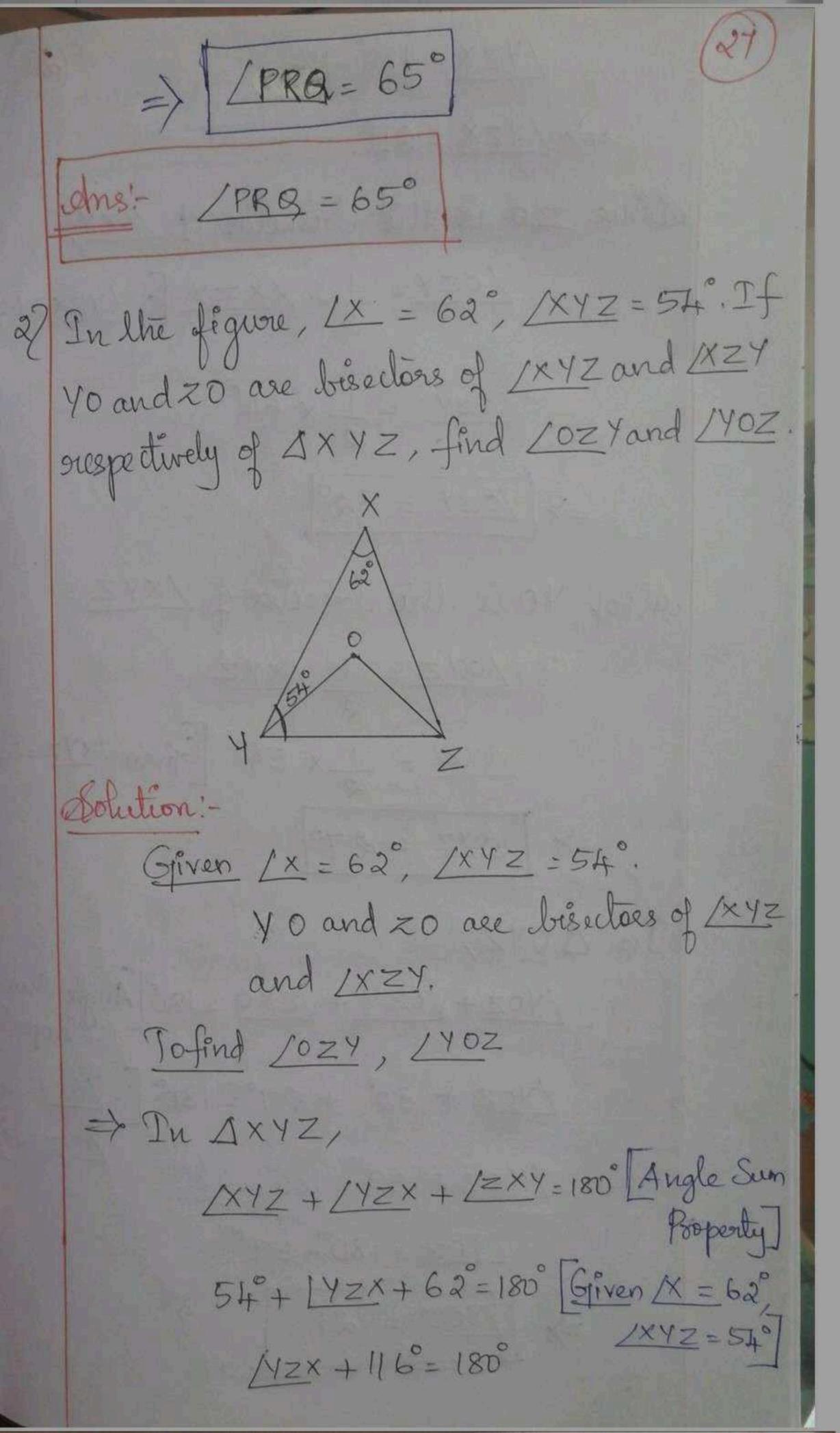
180 Angle 180 Angle

Sum Proporty

45° + 70° + LPRQ = 180° [: LAPR = 45° and
115° 180° [: LAPR = 45° and
115° 180° [: LAPR = 10°]

115°+ LPRQ = 180°

LPR9 = 180°-115°



[YZX = 180°-116

=> LYZX = 64°.

Since 20 is the bisector of XZY,

LOZY = 1 /XZX [: /4ZX = 64]

 $\angle 02Y = \frac{1}{2} \times 64^{\circ}$

> 1024 = 32°

Also, 40 is the bisector of /XYZ

. . LOYZ = 1 /xYZ

1042 = 1 x 54° Given 1x42=54°

=> LOYZ = 270

In DOYZ,

140z+10zy+1zyo=180 Angle Sum
Respertly

LYOZ + 32° + 27° = 180° [:/024=32° 104Z=27

140z + 59° = 180°

140Z = 180°-59°

> / LYOZ = 121°

dns: - Lozy = 32° and Moz=121° 3) In the figure, if AB||DE, LBAC = 35° and [CDE = 53°, find DCE. Solution: Given 1BAC = 35°, 1CDE = 53°, ABILDE Tofind LDCE > BAC = CED = 35° [Allornate In A CDE, LCDE + IDEC + LECD = 180° Angle Sum Property 53°+35°+ LECD = 180° [:/CDE = 53°, /ECD + 88° = 180° [ECD = 180°-88° => LECD = 92° Ans: IDCE = 92°.

12 In the figure, if lines PB, and RS intersect at point T such that LPRT = 40°, /RPI = 95° and / ISQ = 75°, find 1505T. Given IPRT = 40, LRPT = 95° [TS9 = 75° To-find 158T > In APTR, LRPT+ LPRT+ LPTR = 180 Angle Sum 95°+40°+ LPTR = 180° [: Given /PRT LPTR + 135°= 180° = 40°, LRPT LPTR = 180°-135° => 1PTR = 45° Since, LPTR = LSTB, [Vertically Opposite Angles

In ASTB, 1STB+ 1TSB+ 1SBT=180° [Angle Surr Property A5° + 75° + LSBT = 180° [from 0) > and Given Msg=75 /S9T+120=180° 159T = 180°-120° 159T=60° Ans:- 158T = 60° 57 In the figure, if PT LPS, PRIISR, 1503R=28°; and LORT = 65°, then find the values of x and y. Griven PT_LPS, PB/ISR, LSBR = 28° /BRT = 65° Tofind Lz, 4

