Cambridge International AS & A Level

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MATHEMATICS

9709/53

Paper 5 Probability & Statistics 1 May/June 2022

1 hour 15 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

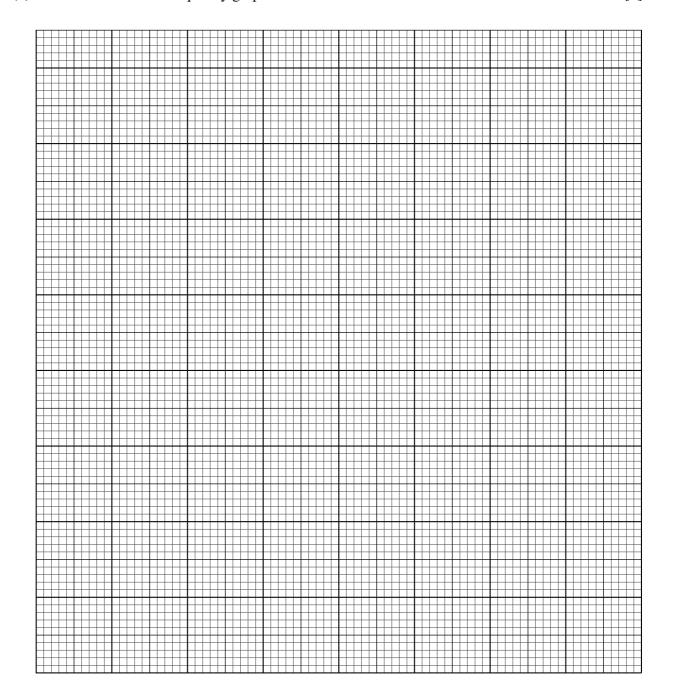
This document has 12 pages.

1 The time taken, t minutes, to complete a puzzle was recorded for each of 150 students. These times are summarised in the table.

| Time taken (t minutes) | <i>t</i> ≤ 25 | <i>t</i> ≤ 50 | <i>t</i> ≤ 75 | <i>t</i> ≤ 100 | <i>t</i> ≤ 150 | <i>t</i> ≤ 200 |
|------------------------|---------------|---------------|---------------|----------------|----------------|----------------|
| Cumulative frequency | 16 | 44 | 86 | 104 | 132 | 150 |

(a) Draw a cumulative frequency graph to illustrate the data.

[2]



| (b) | Use your graph to estimate the 20th percentile of the data. | [1] |
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2

as follows.

Twenty children were asked to estimate the height of a particular tree. Their estimates, in metres, were

| | 4.1 | 4.2 | 4.4 | 4.5 | 4.6 | 4.8 | 5.0 | 5.2 | 5.3 | 5.4 | |
|------------|-------------------------------|------------|----------------------|----------------------|-----------|-------------|-----------|----------|-------------|------------|----------|
| | 5.5 | 5.8 | 6.0 | 6.2 | 6.3 | 6.4 | 6.6 | 6.8 | 6.9 | 19.4 | |
| (a) | Find the mea | an of the | estimate | ed heigh | ts. | | | | | | [1] |
| | | | | | | | | | | | |
| | ••••• | •••••• | •••••• | ••••• | ••••• | ••••••• | ••••••• | • | •••••• | •••••• | •••••• |
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| | ••••• | ••••••• | •••••• | ••••• | ••••• | ••••••••••• | •••••••• | • | ••••••• | | •••••• |
| | | ••••••• | •••••• | •••••• | ••••• | •••••••••• | •••••• | | ••••••• | | •••••• |
| | ••••• | •••••• | •••••• | •••••• | ••••• | ••••••• | •••••• | ••••• | •••••• | ••••• | •••••• |
| | | •••••• | ••••• | ••••• | ••••• | ••••••• | ••••••• | | ••••••••••• | ••••••• | •••••• |
| (b) | Find the med | dian of tl | he estim | ated heig | ghts. | | | | | | [1] |
| | ••••• | | ••••• | ••••• | ••••• | | | | | | |
| | | | •••••• | ••••• | ••••• | | | | | | |
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| | | | ••••• | ••••• | ••••• | | | | | | |
| (c) | Give a reaso central tende | on why to | he medi this info | an is lik rmation | ely to be | e more s | uitable t | than the | mean a | s a measur | e of the |
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| | | | ••••• | ••••• | ••••• | | •••••• | •••••• | •••••• | | |
| | | ••••• | ••••• | ••••• | ••••• | •••••• | •••••• | •••••• | •••••• | | |
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3

| (a) | Draw up the probability distribution table for X , giving the probabilities as numerical fractions. [3] |
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| (b) | Find $E(X)$ and $Var(X)$. |
| (b) | |
| (b) | |
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| (b) | |
| (b) | |
| (b) | |
| (b) | |

| | esh throws an ordinary fair 6-sided die. | |
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|) | Find the probability that he obtains a 4 for the first time on his 8th throw. | [1] |
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|) | Find the probability that it takes no more than 5 throws for Ramesh to obtain a 4. | [2] |
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| e tv | esh now repeatedly throws two ordinary fair 6-sided dice at the same time. Each to wo numbers that he obtains. For 10 randomly chosen throws of the two dice, find the probability that Ramesh obtains. | tains a total |
| e tv | wo numbers that he obtains. | tains a total |
| e tv | wo numbers that he obtains. For 10 randomly chosen throws of the two dice, find the probability that Ramesh ob | tains a total [4] |
| t | wo numbers that he obtains. For 10 randomly chosen throws of the two dice, find the probability that Ramesh ob of less than 4 on at least three throws. | otains a total [4] |
| t | wo numbers that he obtains. For 10 randomly chosen throws of the two dice, find the probability that Ramesh ob of less than 4 on at least three throws. | otains a total [4] |
| t | wo numbers that he obtains. For 10 randomly chosen throws of the two dice, find the probability that Ramesh ob of less than 4 on at least three throws. | otains a total [4] |
| t | wo numbers that he obtains. For 10 randomly chosen throws of the two dice, find the probability that Ramesh ob of less than 4 on at least three throws. | otains a total [4] |
| t | wo numbers that he obtains. For 10 randomly chosen throws of the two dice, find the probability that Ramesh ob of less than 4 on at least three throws. | otains a total [4] |
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| e tv | wo numbers that he obtains. For 10 randomly chosen throws of the two dice, find the probability that Ramesh ob of less than 4 on at least three throws. | otains a total |

5

Farmer Jones grows apples. The weights, in grams, of the apples grown this year are normally

| | Find the probability that a randomly chosen apple grown by Farmer Jones this year is sold to the |
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| | supermarket. [4] |
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Farmer Jones sells the apples to the supermarket at \$0.24 each. He sells apples that weigh more than 205 grams to a local shop at \$0.30 each. He does not sell apples that weigh less than 142 grams.

The total number of apples grown by Farmer Jones this year is 20000.

| 1 | Calculate an estimate for his total income from this year's apples. | [3] |
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| n | ner Tan also grows apples. The weights, in grams, of the apples grown this ribution $N(182, 20^2)$. 72% of these apples have a weight more than w grams. | year follow the |
| tr | ner Tan also grows apples. The weights, in grams, of the apples grown this ribution N(182, 20^2). 72% of these apples have a weight more than w grams. Find the value of w . | |
| tr | ribution N(182, 20^2). 72% of these apples have a weight more than w grams. | |
| r | ribution N(182, 20^2). 72% of these apples have a weight more than w grams. | [3] |
| r | Find the value of w . | [3] |
| r | Find the value of w . | [3] |
| r | Find the value of w . | [3] |
| r | Find the value of w . | [3] |
| r | Find the value of w . | [3] |
| r | Find the value of w . | [3] |
| tr | Find the value of w . | [3] |

6 Sajid is practising for a long jump competition. He counts any jump that is longer than 6 m as a success. On any day, the probability that he has a success with his first jump is 0.2. For any subsequent jump, the probability of a success is 0.3 if the previous jump was a success and 0.1 otherwise. Sajid makes three jumps.

(a) Draw a tree diagram to illustrate this information, showing all the probabilities. [2]

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- 7 A group of 15 friends visit an adventure park. The group consists of four families.
 - Mr and Mrs Kenny and their four children
 - Mr and Mrs Lizo and their three children
 - Mrs Martin and her child
 - Mr and Mrs Nantes

The group travel to the park in three cars, one containing 6 people, one containing 5 people and one containing 4 people. The cars are driven by Mr Lizo, Mrs Martin and Mr Nantes respectively.

| (a) | In how many different ways can the remaining 12 members of the group be divided between the three cars? [3] |
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| The | e group enter the park by walking through a gate one at a time. |
| (b) | In how many different orders can the 15 friends go through the gate if Mr Lizo goes first and each family stays together? [3] |
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In the park, the group enter a competition which requires a team of 4 adults and 3 children.

| | erent familie | | | | | | [2] |
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| In how included | | can the tear | n be chose | en so that at | least one of Mi | r Kenny or N | Ar Lizo is |
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Additional Page

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