

**[Turn over**

- 1** Two fair coins are thrown at the same time repeatedly until a pair of heads is obtained. The number of throws taken is denoted by the random variable  $X$ .

**(a)** State the value of  $E(X)$ . [1]

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**(b)** Find the probability that exactly 5 throws are required to obtain a pair of heads. [1]

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**(c)** Find the probability that fewer than 7 throws are required to obtain a pair of heads. [2]

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- Use an approximation to find the probability that, of the 120 voters, between 36 and 54 inclusive voted for Anil. [5]

This image shows a single page of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

- (a)** Given that  $P(X = 4) = 3P(X = 2)$ , find the value of  $a$  and the value of  $k$ . [4]

This image shows a full page of white paper with horizontal dashed lines, typical of primary school writing paper. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

- (b) Draw up the probability distribution table for  $X$ , giving the probabilities as numerical fractions. [1]

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- (c) Given that  $E(X) = 3.2$ , find  $\text{Var}(X)$ . [2]

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- 4 The times taken, in minutes, to complete a cycle race by 19 cyclists from each of two clubs, the Cheetahs and the Panthers, are represented in the following back-to-back stem-and-leaf diagram.

Cheetahs						Panthers				
9 8					7	4				
8	7	3	2	0	8	6 8				
9 8 7					9	1 7 8 9 9				
6	5	3	3	1	10	2 3 4 4 5 6				
9 8 2					11	1 2 8				
4					12	0 6				

Key: 7 | 9 | 1 means 97 minutes for Cheetahs and 91 minutes for Panthers

- (a) Find the median and the interquartile range of the times of the Cheetahs. [3]

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The median and interquartile range for the Panthers are 103 minutes and 14 minutes respectively.

- (b) Make two comparisons between the times taken by the Cheetahs and the times taken by the Panthers. [2]

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Another cyclist, Kenny, from the Cheetahs also took part in the race. The mean time taken by the 20 cyclists from the Cheetahs was 99 minutes.

- (c) Find the time taken by Kenny to complete the race. [3]

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- 5 Jasmine throws two ordinary fair 6-sided dice at the same time and notes the numbers on the uppermost faces. The events  $A$  and  $B$  are defined as follows.

$A$ : The sum of the two numbers is less than 6.

$B$ : The difference between the two numbers is at most 2.

- (a) Determine whether or not the events  $A$  and  $B$  are independent. [4]

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- (b) Find  $P(B \mid A')$ . [3]

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- 6** The mass of grapes sold per day by a large shop can be modelled by a normal distribution with mean 28 kg. On 10% of days less than 16 kg of grapes are sold.

(a) Find the standard deviation of the mass of grapes sold per day. [3]

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The mass of grapes sold on any day is independent of the mass sold on any other day.

(b) 12 days are chosen at random.

Find the probability that less than 16 kg of grapes are sold on more than 2 of these 12 days. [3]

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(c) In a random sample of 365 days, on how many days would you expect the mass of grapes sold to be within 1.3 standard deviations of the mean? [4]

**[Turn over**

- 7 (a) Find the number of different arrangements of the 10 letters in the word CASABLANCA in which the two Cs are **not** together. [3]

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- (b) Find the number of different arrangements of the 10 letters in the word CASABLANCA which have an A at the beginning, an A at the end and exactly 3 letters between the 2 Cs. [3]

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Five letters are selected from the 10 letters in the word CASABLANCA.

- (c) Find the number of different selections in which the five letters include at least two As and at most one C. [3]

This image shows a full page of white paper with horizontal dotted lines. The lines are evenly spaced and run across the width of the page, providing a guide for handwriting practice. There are no margins, text, or other markings on the page.

## Additional Page

If you use the following lined page to complete the answer(s) to any question(s), the question number(s) must be clearly shown.

[illegible]

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