

# 7

## Microarchitecture

With contributions from Matthew Watkins

### 7.1 INTRODUCTION

In this chapter, you will learn how to piece together a MIPS microprocessor. Indeed, you will puzzle out three different versions, each with different trade-offs between performance, cost, and complexity.

To the uninitiated, building a microprocessor may seem like black magic. But it is actually relatively straightforward, and by this point you have learned everything you need to know. Specifically, you have learned to design combinational and sequential logic given functional and timing specifications. You are familiar with circuits for arithmetic and memory. And you have learned about the MIPS architecture, which specifies the programmer's view of the MIPS processor in terms of registers, instructions, and memory.

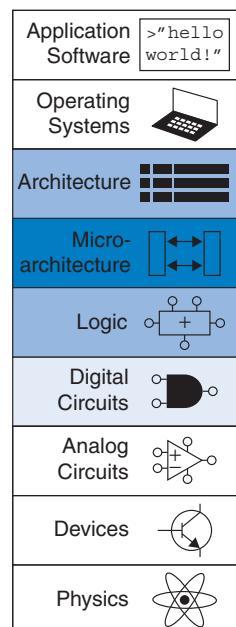
This chapter covers *microarchitecture*, which is the connection between logic and architecture. Microarchitecture is the specific arrangement of registers, ALUs, finite state machines (FSMs), memories, and other logic building blocks needed to implement an architecture. A particular architecture, such as MIPS, may have many different microarchitectures, each with different trade-offs of performance, cost, and complexity. They all run the same programs, but their internal designs vary widely. We will design three different microarchitectures in this chapter to illustrate the trade-offs.

This chapter draws heavily on David Patterson and John Hennessy's classic MIPS designs in their text *Computer Organization and Design*. They have generously shared their elegant designs, which have the virtue of illustrating a real commercial architecture while being relatively simple and easy to understand.

#### 7.1.1 Architectural State and Instruction Set

Recall that a computer architecture is defined by its instruction set and *architectural state*. The architectural state for the MIPS processor consists

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David Patterson was the first in his family to graduate from college (UCLA, 1969). He has been a professor of computer science at UC Berkeley since 1977, where he co-invented RISC, the Reduced Instruction Set Computer. In 1984, he developed the SPARC architecture used by Sun Microsystems. He is also the father of RAID (*Redundant Array of Inexpensive Disks*) and NOW (*Network of Workstations*).

John Hennessy is president of Stanford University and has been a professor of electrical engineering and computer science there since 1977. He co-invented RISC. He developed the MIPS architecture at Stanford in 1984 and cofounded MIPS Computer Systems. As of 2004, more than 300 million MIPS microprocessors have been sold.

In their copious free time, these two modern paragons write textbooks for recreation and relaxation.

of the program counter and the 32 registers. Any MIPS microarchitecture must contain all of this state. Based on the current architectural state, the processor executes a particular instruction with a particular set of data to produce a new architectural state. Some microarchitectures contain additional *nonarchitectural state* to either simplify the logic or improve performance; we will point this out as it arises.

To keep the microarchitectures easy to understand, we consider only a subset of the MIPS instruction set. Specifically, we handle the following instructions:

- ▶ R-type arithmetic/logic instructions: add, sub, and, or, slt
- ▶ Memory instructions: lw, sw
- ▶ Branches: beq

After building the microarchitectures with these instructions, we extend them to handle addi and j. These particular instructions were chosen because they are sufficient to write many interesting programs. Once you understand how to implement these instructions, you can expand the hardware to handle others.

### 7.1.2 Design Process

We will divide our microarchitectures into two interacting parts: the *datapath* and the *control*. The datapath operates on words of data. It contains structures such as memories, registers, ALUs, and multiplexers. MIPS is a 32-bit architecture, so we will use a 32-bit datapath. The control unit receives the current instruction from the datapath and tells the datapath how to execute that instruction. Specifically, the control unit produces multiplexer select, register enable, and memory write signals to control the operation of the datapath.

A good way to design a complex system is to start with hardware containing the state elements. These elements include the memories and the architectural state (the program counter and registers). Then, add blocks of combinational logic between the state elements to compute the new state based on the current state. The instruction is read from part of memory; load and store instructions then read or write data from another part of memory. Hence, it is often convenient to partition the overall memory into two smaller memories, one containing instructions and the other containing data. Figure 7.1 shows a block diagram with the four state elements: the program counter, register file, and instruction and data memories.

In Figure 7.1, heavy lines are used to indicate 32-bit data busses. Medium lines are used to indicate narrower busses, such as the 5-bit address busses on the register file. Narrow blue lines are used to indicate

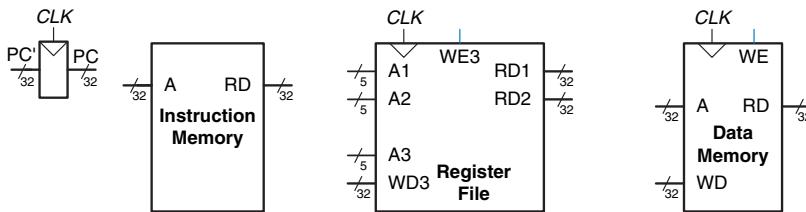


Figure 7.1 State elements of MIPS processor

control signals, such as the register file write enable. We will use this convention throughout the chapter to avoid cluttering diagrams with bus widths. Also, state elements usually have a reset input to put them into a known state at start-up. Again, to save clutter, this reset is not shown.

The *program counter* is an ordinary 32-bit register. Its output, *PC*, points to the current instruction. Its input, *PC'*, indicates the address of the next instruction.

The *instruction memory* has a single read port.<sup>1</sup> It takes a 32-bit instruction address input, *A*, and reads the 32-bit data (i.e., instruction) from that address onto the read data output, *RD*.

The 32-element × 32-bit *register file* has two read ports and one write port. The read ports take 5-bit address inputs, *A1* and *A2*, each specifying one of  $2^5 = 32$  registers as source operands. They read the 32-bit register values onto read data outputs *RD1* and *RD2*, respectively. The write port takes a 5-bit address input, *A3*; a 32-bit write data input, *WD*; a write enable input, *WE3*; and a clock. If the write enable is 1, the register file writes the data into the specified register on the rising edge of the clock.

The *data memory* has a single read/write port. If the write enable, *WE*, is 1, it writes data *WD* into address *A* on the rising edge of the clock. If the write enable is 0, it reads address *A* onto *RD*.

The instruction memory, register file, and data memory are all read *combinatorially*. In other words, if the address changes, the new data appears at *RD* after some propagation delay; no clock is involved. They are written only on the rising edge of the clock. In this fashion, the state of the system is changed only at the clock edge. The address, data, and write enable must setup sometime before the clock edge and must remain stable until a hold time after the clock edge.

Because the state elements change their state only on the rising edge of the clock, they are synchronous sequential circuits. The microprocessor

#### Resetting the PC

At the very least, the program counter must have a reset signal to initialize its value when the processor turns on. MIPS processors initialize the PC to `0xBFC00000` on reset and begin executing code to start up the operating system (OS). The OS then loads an application program at `0x00400000` and begins executing it. For simplicity in this chapter, we will reset the PC to `0x00000000` and place our programs there instead.

<sup>1</sup> This is an oversimplification used to treat the instruction memory as a ROM; in most real processors, the instruction memory must be writable so that the OS can load a new program into memory. The multicycle microarchitecture described in Section 7.4 is more realistic in that it uses a combined memory for instructions and data that can be both read and written.

is built of clocked state elements and combinational logic, so it too is a synchronous sequential circuit. Indeed, the processor can be viewed as a giant finite state machine, or as a collection of simpler interacting state machines.

### 7.1.3 MIPS Microarchitectures

In this chapter, we develop three microarchitectures for the MIPS processor architecture: single-cycle, multicycle, and pipelined. They differ in the way that the state elements are connected together and in the amount of nonarchitectural state.

The *single-cycle microarchitecture* executes an entire instruction in one cycle. It is easy to explain and has a simple control unit. Because it completes the operation in one cycle, it does not require any nonarchitectural state. However, the cycle time is limited by the slowest instruction.

The *multicycle microarchitecture* executes instructions in a series of shorter cycles. Simpler instructions execute in fewer cycles than complicated ones. Moreover, the multicycle microarchitecture reduces the hardware cost by reusing expensive hardware blocks such as adders and memories. For example, the adder may be used on several different cycles for several purposes while carrying out a single instruction. The multicycle microprocessor accomplishes this by adding several nonarchitectural registers to hold intermediate results. The multicycle processor executes only one instruction at a time, but each instruction takes multiple clock cycles.

The *pipelined microarchitecture* applies pipelining to the single-cycle microarchitecture. It therefore can execute several instructions simultaneously, improving the throughput significantly. Pipelining must add logic to handle dependencies between simultaneously executing instructions. It also requires nonarchitectural pipeline registers. The added logic and registers are worthwhile; all commercial high-performance processors use pipelining today.

We explore the details and trade-offs of these three microarchitectures in the subsequent sections. At the end of the chapter, we briefly mention additional techniques that are used to get even more speed in modern high-performance microprocessors.

## 7.2 PERFORMANCE ANALYSIS

As we mentioned, a particular processor architecture can have many microarchitectures with different cost and performance trade-offs. The cost depends on the amount of hardware required and the implementation technology. Each year, CMOS processes can pack more transistors on a chip for the same amount of money, and processors take advantage

of these additional transistors to deliver more performance. Precise cost calculations require detailed knowledge of the implementation technology, but in general, more gates and more memory mean more dollars. This section lays the foundation for analyzing performance.

There are many ways to measure the performance of a computer system, and marketing departments are infamous for choosing the method that makes their computer look fastest, regardless of whether the measurement has any correlation to real-world performance. For example, Intel and Advanced Micro Devices (AMD) both sell compatible microprocessors conforming to the x86 architecture. Intel Pentium III and Pentium 4 microprocessors were largely advertised according to clock frequency in the late 1990s and early 2000s, because Intel offered higher clock frequencies than its competitors. However, Intel's main competitor, AMD, sold Athlon microprocessors that executed programs faster than Intel's chips at the same clock frequency. What is a consumer to do?

The only gimmick-free way to measure performance is by measuring the execution time of a program of interest to you. The computer that executes your program fastest has the highest performance. The next best choice is to measure the total execution time of a collection of programs that are similar to those you plan to run; this may be necessary if you haven't written your program yet or if somebody else who doesn't have your program is making the measurements. Such collections of programs are called *benchmarks*, and the execution times of these programs are commonly published to give some indication of how a processor performs.

The execution time of a program, measured in seconds, is given by Equation 7.1.

$$\text{Execution Time} = \left( \# \text{ instructions} \right) \left( \frac{\text{cycles}}{\text{instruction}} \right) \left( \frac{\text{seconds}}{\text{cycle}} \right) \quad (7.1)$$

The number of instructions in a program depends on the processor architecture. Some architectures have complicated instructions that do more work per instruction, thus reducing the number of instructions in a program. However, these complicated instructions are often slower to execute in hardware. The number of instructions also depends enormously on the cleverness of the programmer. For the purposes of this chapter, we will assume that we are executing known programs on a MIPS processor, so the number of instructions for each program is constant, independent of the microarchitecture.

The number of cycles per instruction, often called *CPI*, is the number of clock cycles required to execute an average instruction. It is the reciprocal of the throughput (instructions per cycle, or *IPC*). Different microarchitectures have different CPIs. In this chapter, we will assume

we have an ideal memory system that does not affect the CPI. In [Chapter 8](#), we examine how the processor sometimes has to wait for the memory, which increases the CPI.

The number of seconds per cycle is the clock period,  $T_c$ . The clock period is determined by the critical path through the logic on the processor. Different microarchitectures have different clock periods. Logic and circuit designs also significantly affect the clock period. For example, a carry-lookahead adder is faster than a ripple-carry adder. Manufacturing advances have historically doubled transistor speeds every 4–6 years, so a microprocessor built today will be much faster than one from last decade, even if the microarchitecture and logic are unchanged.

The challenge of the microarchitect is to choose the design that minimizes the execution time while satisfying constraints on cost and/or power consumption. Because microarchitectural decisions affect both CPI and  $T_c$  and are influenced by logic and circuit designs, determining the best choice requires careful analysis.

There are many other factors that affect overall computer performance. For example, the hard disk, the memory, the graphics system, and the network connection may be limiting factors that make processor performance irrelevant. The fastest microprocessor in the world doesn't help surfing the Internet on a dial-up connection. But these other factors are beyond the scope of this book.

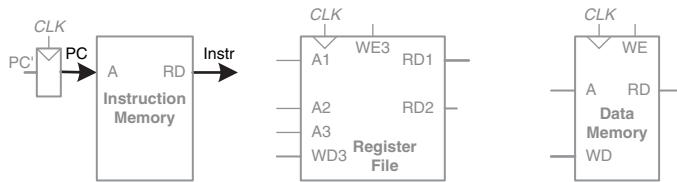
## 7.3 SINGLE-CYCLE PROCESSOR

We first design a MIPS microarchitecture that executes instructions in a single cycle. We begin constructing the datapath by connecting the state elements from [Figure 7.1](#) with combinational logic that can execute the various instructions. Control signals determine which specific instruction is carried out by the datapath at any given time. The controller contains combinational logic that generates the appropriate control signals based on the current instruction. We conclude by analyzing the performance of the single-cycle processor.

### 7.3.1 Single-Cycle Datapath

This section gradually develops the single-cycle datapath, adding one piece at a time to the state elements from [Figure 7.1](#). The new connections are emphasized in black (or blue, for new control signals), while the hardware that has already been studied is shown in gray.

The program counter (PC) register contains the address of the instruction to execute. The first step is to read this instruction from instruction memory. [Figure 7.2](#) shows that the PC is simply connected to the address input of the instruction memory. The instruction memory reads out, or *fetches*, the 32-bit instruction, labeled *Instr*.

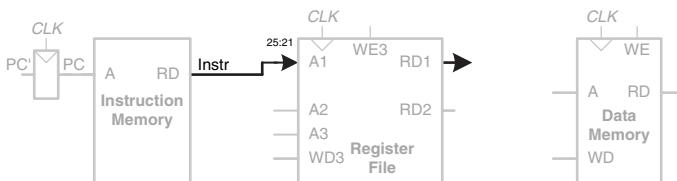


**Figure 7.2** Fetch instruction from memory

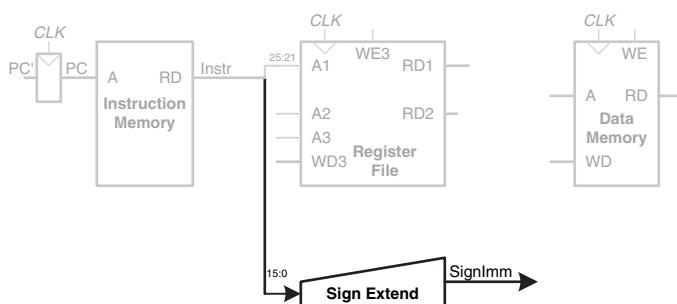
The processor's actions depend on the specific instruction that was fetched. First we will work out the datapath connections for the `lw` instruction. Then we will consider how to generalize the datapath to handle the other instructions.

For a `lw` instruction, the next step is to read the source register containing the base address. This register is specified in the `rs` field of the instruction,  $Instr_{25:21}$ . These bits of the instruction are connected to the address input of one of the register file read ports,  $A1$ , as shown in Figure 7.3. The register file reads the register value onto  $RD1$ .

The `lw` instruction also requires an offset. The offset is stored in the immediate field of the instruction,  $Instr_{15:0}$ . Because the 16-bit immediate might be either positive or negative, it must be sign-extended to 32 bits, as shown in Figure 7.4. The 32-bit sign-extended value is called *SignImm*. Recall from Section 1.4.6 that sign extension simply copies the sign bit (most significant bit) of a short input into all of the upper bits of the longer output. Specifically,  $SignImm_{15:0} = Instr_{15:0}$  and  $SignImm_{31:16} = Instr_{15}$ .



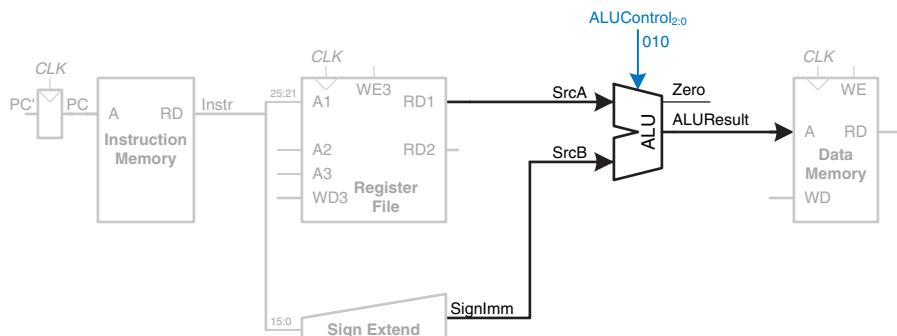
**Figure 7.3** Read source operand from register file



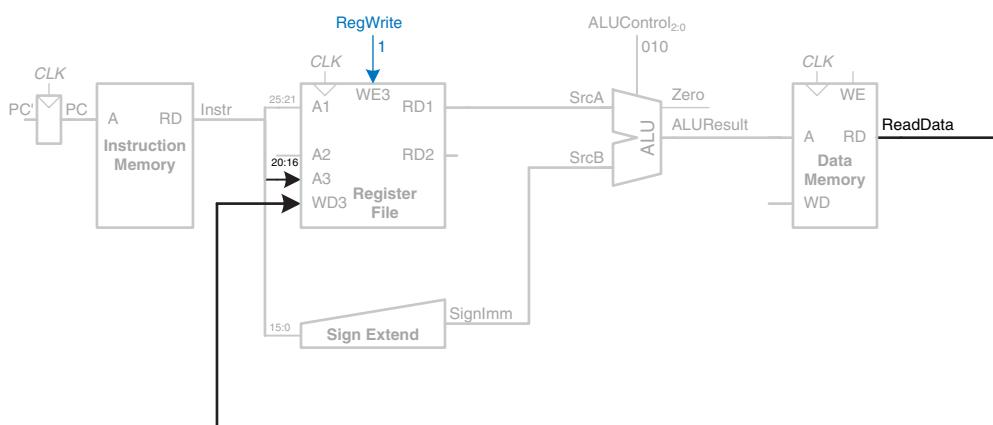
**Figure 7.4** Sign-extend the immediate

The processor must add the base address to the offset to find the address to read from memory. Figure 7.5 introduces an ALU to perform this addition. The ALU receives two operands, *SrcA* and *SrcB*. *SrcA* comes from the register file, and *SrcB* comes from the sign-extended immediate. The ALU can perform many operations, as was described in Section 5.2.4. The 3-bit *ALUControl* signal specifies the operation. The ALU generates a 32-bit *ALUResult* and a *Zero* flag, that indicates whether  $ALUResult == 0$ . For a  $lw$  instruction, the *ALUControl* signal should be set to 010 to add the base address and offset. *ALUResult* is sent to the data memory as the address for the load instruction, as shown in Figure 7.5.

The data is read from the data memory onto the *ReadData* bus, then written back to the destination register in the register file at the end of the cycle, as shown in Figure 7.6. Port 3 of the register file is the write port.



**Figure 7.5** Compute memory address



**Figure 7.6** Write data back to register file

The destination register for the `lw` instruction is specified in the  $rt$  field,  $Instr_{20:16}$ , which is connected to the port 3 address input,  $A_3$ , of the register file. The  $ReadData$  bus is connected to the port 3 write data input,  $WD_3$ , of the register file. A control signal called  $RegWrite$  is connected to the port 3 write enable input,  $WE_3$ , and is asserted during a `lw` instruction so that the data value is written into the register file. The write takes place on the rising edge of the clock at the end of the cycle.

While the instruction is being executed, the processor must compute the address of the next instruction,  $PC'$ . Because instructions are 32 bits = 4 bytes, the next instruction is at  $PC + 4$ . Figure 7.7 uses another adder to increment the PC by 4. The new address is written into the program counter on the next rising edge of the clock. This completes the datapath for the `lw` instruction.

Next, let us extend the datapath to also handle the `sw` instruction. Like the `lw` instruction, the `sw` instruction reads a base address from port 1 of the register file and sign-extends an immediate. The ALU adds the base address to the immediate to find the memory address. All of these functions are already supported by the datapath.

The `sw` instruction also reads a second register from the register file and writes it to the data memory. Figure 7.8 shows the new connections for this function. The register is specified in the  $rt$  field,  $Instr_{20:16}$ . These bits of the instruction are connected to the second register file read port,  $A_2$ . The register value is read onto the  $RD_2$  port. It is connected to the write data port of the data memory. The write enable port of the data memory,  $WE$ , is controlled by  $MemWrite$ . For a `sw` instruction,  $MemWrite = 1$ , to write the data to memory;  $ALUControl = 010$ , to add the base address and offset; and  $RegWrite = 0$ , because nothing should

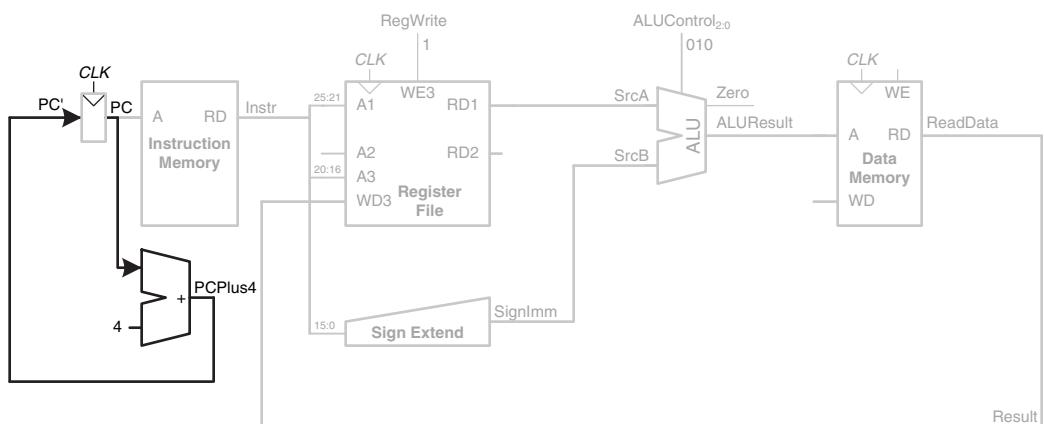
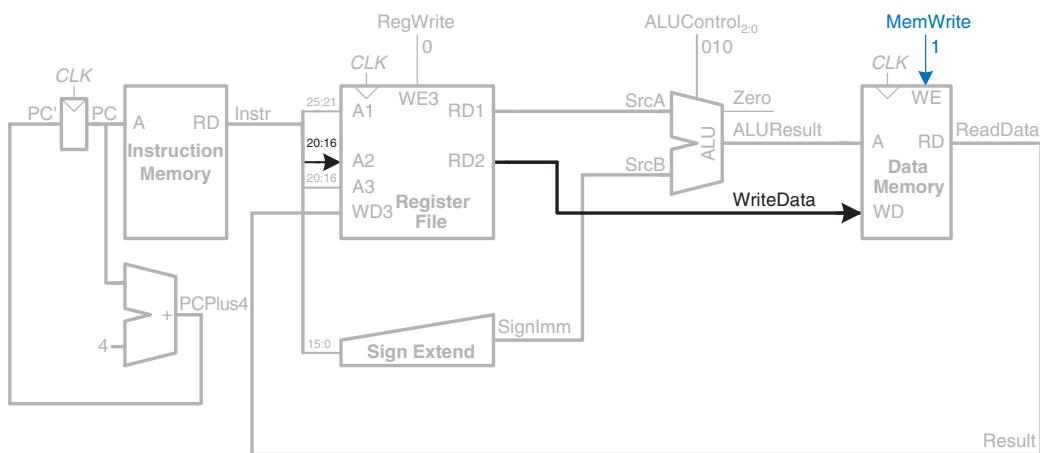


Figure 7.7 Determine address of next instruction for PC



**Figure 7.8 Write data to memory for SW instruction**

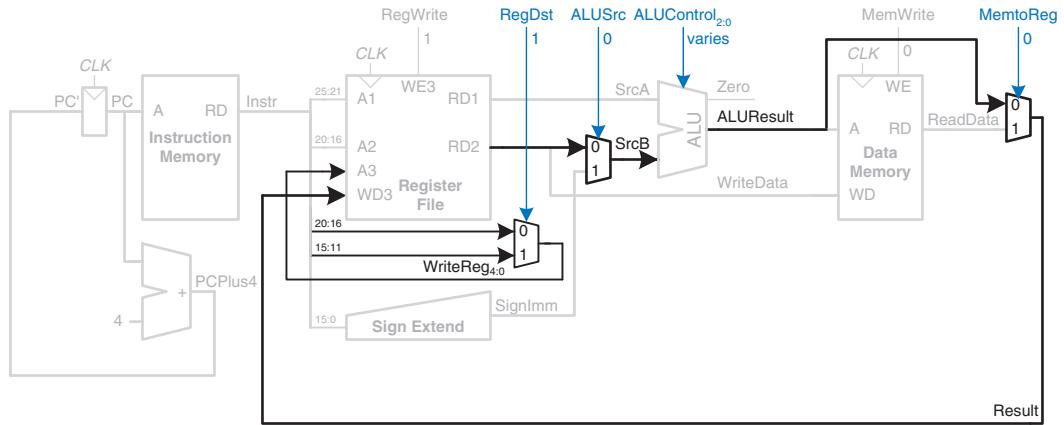
be written to the register file. Note that data is still read from the address given to the data memory, but that this *ReadData* is ignored because *RegWrite* = 0.

Next, consider extending the datapath to handle the R-type instructions add, sub, and, or, and slt. All of these instructions read two registers from the register file, perform some ALU operation on them, and write the result back to a third register file. They differ only in the specific ALU operation. Hence, they can all be handled with the same hardware, using different *ALUControl* signals.

Figure 7.9 shows the enhanced datapath handling R-type instructions. The register file reads two registers. The ALU performs an operation on these two registers. In Figure 7.8, the ALU always received its *SrcB* operand from the sign-extended immediate (*SignImm*). Now, we add a multiplexer to choose *SrcB* from either the register file *RD2* port or *SignImm*.

The multiplexer is controlled by a new signal, *ALUSrc*. *ALUSrc* is 0 for R-type instructions to choose *SrcB* from the register file; it is 1 for lw and sw to choose *SignImm*. This principle of enhancing the datapath's capabilities by adding a multiplexer to choose inputs from several possibilities is extremely useful. Indeed, we will apply it twice more to complete the handling of R-type instructions.

In Figure 7.8, the register file always got its write data from the data memory. However, R-type instructions write the *ALUResult* to the register file. Therefore, we add another multiplexer to choose between *ReadData* and *ALUResult*. We call its output *Result*. This multiplexer is controlled by another new signal, *MemtoReg*. *MemtoReg* is 0 for R-type



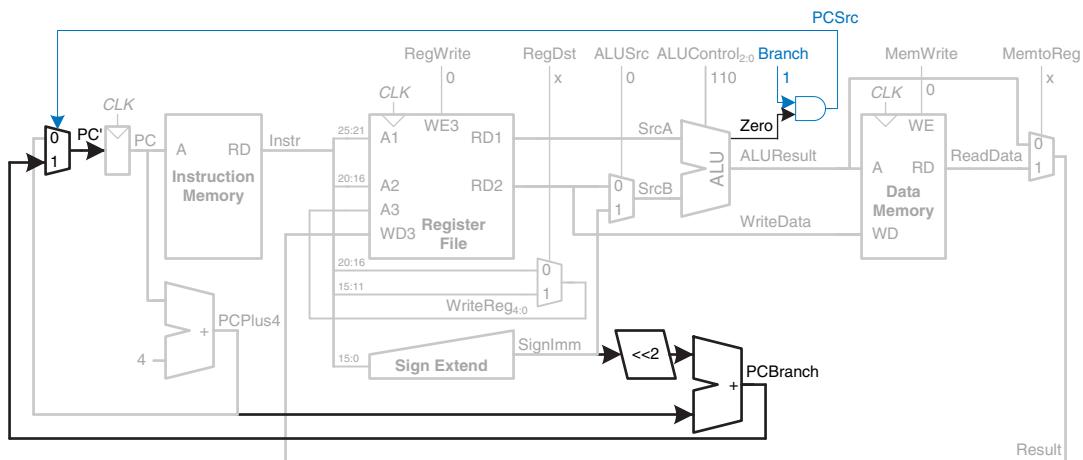
**Figure 7.9** Datapath enhancements for R-type instruction

instructions to choose *Result* from the *ALUResult*; it is 1 for *lw* to choose *ReadData*. We don't care about the value of *MemtoReg* for *sw*, because *sw* does not write to the register file.

Similarly, in Figure 7.8, the register to write was specified by the *rt* field of the instruction, *Instr*<sub>20:16</sub>. However, for R-type instructions, the register is specified by the *rd* field, *Instr*<sub>15:11</sub>. Thus, we add a third multiplexer to choose *WriteReg* from the appropriate field of the instruction. The multiplexer is controlled by *RegDst*. *RegDst* is 1 for R-type instructions to choose *WriteReg* from the *rd* field, *Instr*<sub>15:11</sub>; it is 0 for *lw* to choose the *rt* field, *Instr*<sub>20:16</sub>. We don't care about the value of *RegDst* for *sw*, because *sw* does not write to the register file.

Finally, let us extend the datapath to handle *beq*. *beq* compares two registers. If they are equal, it takes the branch by adding the branch offset to the program counter. Recall that the offset is a positive or negative number, stored in the *imm* field of the instruction, *Instr*<sub>15:0</sub>. The offset indicates the number of instructions to branch past. Hence, the immediate must be sign-extended and multiplied by 4 to get the new program counter value:  $PC' = PC + 4 + SignImm \times 4$ .

Figure 7.10 shows the datapath modifications. The next *PC* value for a taken branch, *PCBranch*, is computed by shifting *SignImm* left by 2 bits, then adding it to *PCPlus4*. The left shift by 2 is an easy way to multiply by 4, because a shift by a constant amount involves just wires. The two registers are compared by computing *SrcA - SrcB* using the ALU. If *ALUResult* is 0, as indicated by the *Zero* flag from the ALU, the registers are equal. We add a multiplexer to choose *PC'* from either *PCPlus4* or *PCBranch*. *PCBranch* is selected if the instruction is a branch



**Figure 7.10** Datapath enhancements for `beq` instruction

and the *Zero* flag is asserted. Hence, *Branch* is 1 for `beq` and 0 for other instructions. For `beq`,  $ALUControl = 110$ , so the ALU performs a subtraction.  $ALUSrc = 0$  to choose *SrcB* from the register file.  $RegWrite$  and  $MemWrite$  are 0, because a branch does not write to the register file or memory. We don't care about the values of  $RegDst$  and  $MemtoReg$ , because the register file is not written.

This completes the design of the single-cycle MIPS processor datapath. We have illustrated not only the design itself, but also the design process in which the state elements are identified and the combinational logic connecting the state elements is systematically added. In the next section, we consider how to compute the control signals that direct the operation of our datapath.

### 7.3.2 Single-Cycle Control

The control unit computes the control signals based on the opcode and funct fields of the instruction,  $Instr_{31:26}$  and  $Instr_{5:0}$ . Figure 7.11 shows the entire single-cycle MIPS processor with the control unit attached to the datapath.

Most of the control information comes from the opcode, but R-type instructions also use the funct field to determine the ALU operation. Thus, we will simplify our design by factoring the control unit into two blocks of combinational logic, as shown in Figure 7.12. The main decoder computes most of the outputs from the opcode. It also determines a 2-bit  $ALUOp$  signal. The ALU decoder uses this  $ALUOp$  signal in conjunction with the funct field to compute  $ALUControl$ . The meaning of the  $ALUOp$  signal is given in Table 7.1.

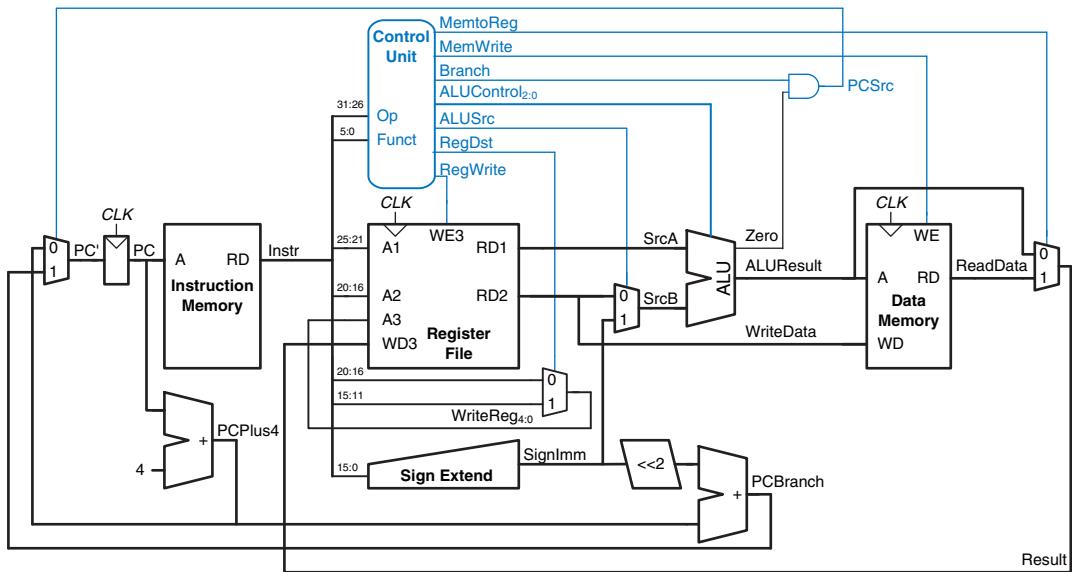


Figure 7.11 Complete single-cycle MIPS processor

Table 7.1 ALUOp encoding

ALUOp	Meaning
00	add
01	subtract
10	look at funct field
11	n/a

Table 7.2 is a truth table for the ALU decoder. Recall that the meanings of the three *ALUControl* signals were given in Table 5.1. Because *ALUOp* is never 11, the truth table can use don't care's X1 and 1X instead of 01 and 10 to simplify the logic. When *ALUOp* is 00 or 01, the ALU should add or subtract, respectively. When *ALUOp* is 10, the decoder examines the *funct* field to determine the *ALUControl*. Note that, for the R-type instructions we implement, the first two bits of the *funct* field are always 10, so we may ignore them to simplify the decoder.

The control signals for each instruction were described as we built the datapath. Table 7.3 is a truth table for the main decoder that summarizes the control signals as a function of the opcode. All R-type instructions use the same main decoder values; they differ only in the

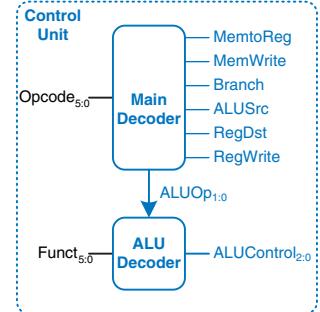


Figure 7.12 Control unit internal structure

**Table 7.2 ALU decoder truth table**

ALUOp	Funct	ALUControl
00	X	010 (add)
X1	X	110 (subtract)
1X	100000 (add)	010 (add)
1X	100010 (sub)	110 (subtract)
1X	100100 (and)	000 (and)
1X	100101 (or)	001 (or)
1X	101010 (slt)	111 (set less than)

**Table 7.3 Main decoder truth table**

Instruction	Opcode	RegWrite	RegDst	ALUSrc	Branch	MemWrite	MemtoReg	ALUOp
R-type	000000	1	1	0	0	0	0	10
lw	100011	1	0	1	0	0	1	00
sw	101011	0	X	1	0	1	X	00
beq	000100	0	X	0	1	0	X	01

ALU decoder output. Recall that, for instructions that do not write to the register file (e.g., `sw` and `beq`), the *RegDst* and *MemtoReg* control signals are don't cares (X); the address and data to the register write port do not matter because *RegWrite* is not asserted. The logic for the decoder can be designed using your favorite techniques for combinational logic design.

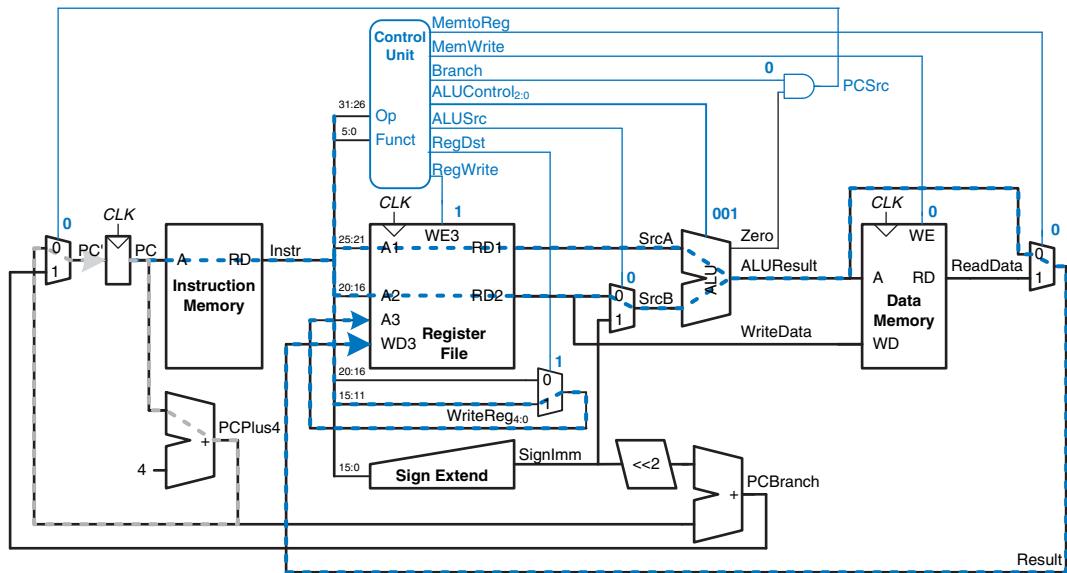
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#### Example 7.1 SINGLE-CYCLE PROCESSOR OPERATION

Determine the values of the control signals and the portions of the datapath that are used when executing an `or` instruction.

**Solution:** Figure 7.13 illustrates the control signals and flow of data during execution of the `or` instruction. The PC points to the memory location holding the instruction, and the instruction memory fetches this instruction.

The main flow of data through the register file and ALU is represented with a dashed blue line. The register file reads the two source operands specified by  $Instr_{25:21}$  and  $Instr_{20:16}$ .  $SrcB$  should come from the second port of the register file



**Figure 7.13** Control signals and data flow while executing `or` instruction

(not *SignImm*), so *ALUSrc* must be 0. `or` is an R-type instruction, so *ALUOp* is 10, indicating that *ALUControl* should be determined from the *funct* field to be 001. *Result* is taken from the ALU, so *MemtoReg* is 0. The result is written to the register file, so *RegWrite* is 1. The instruction does not write memory, so *MemWrite* = 0.

The selection of the destination register is also shown with a dashed blue line. The destination register is specified in the *rd* field,  $Instr_{15:11}$ , so *RegDst* = 1.

The updating of the PC is shown with the dashed gray line. The instruction is not a branch, so *Branch* = 0 and, hence, *PCSrc* is also 0. The PC gets its next value from *PCPlus4*.

Note that data certainly does flow through the nonhighlighted paths, but that the value of that data is unimportant for this instruction. For example, the immediate is sign-extended and data is read from memory, but these values do not influence the next state of the system.

### 7.3.3 More Instructions

We have considered a limited subset of the full MIPS instruction set. Adding support for the `addi` and `j` instructions illustrates the principle of how to handle new instructions and also gives us a sufficiently rich instruction set to write many interesting programs. We will see that

supporting some instructions simply requires enhancing the main decoder, whereas supporting others also requires more hardware in the datapath.

---

#### Example 7.2 addi INSTRUCTION

The add immediate instruction, `addi`, adds the value in a register to the immediate and writes the result to another register. The datapath already is capable of this task. Determine the necessary changes to the controller to support `addi`.

**Solution:** All we need to do is add a new row to the main decoder truth table showing the control signal values for `addi`, as given in Table 7.4. The result should be written to the register file, so `RegWrite` = 1. The destination register is specified in the `rt` field of the instruction, so `RegDst` = 0. `SrcB` comes from the immediate, so `ALUSrc` = 1. The instruction is not a branch, nor does it write memory, so `Branch` = `MemWrite` = 0. The result comes from the ALU, not memory, so `MemtoReg` = 0. Finally, the ALU should add, so `ALUOp` = 00.

---

**Table 7.4** Main decoder truth table enhanced to support `addi`

Instruction	Opcode	RegWrite	RegDst	ALUSrc	Branch	MemWrite	MemtoReg	ALUOp
R-type	000000	1	1	0	0	0	0	10
lw	100011	1	0	1	0	0	1	00
sw	101011	0	X	1	0	1	X	00
beq	000100	0	X	0	1	0	X	01
addi	001000	1	0	1	0	0	0	00

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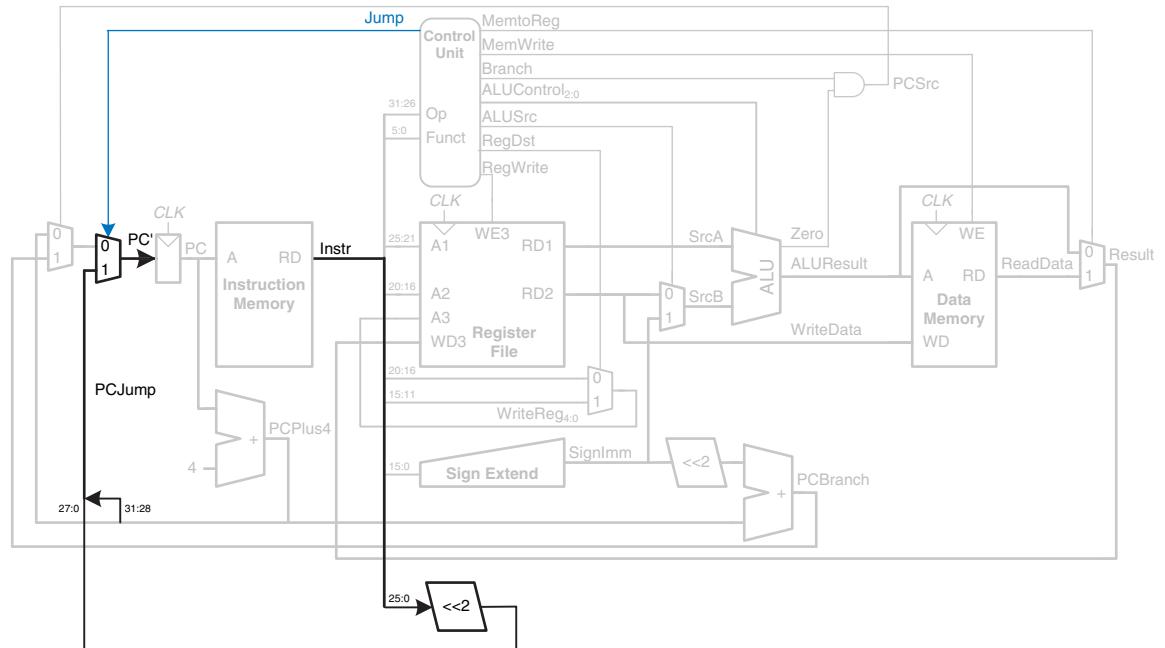
#### Example 7.3 j INSTRUCTION

The jump instruction, `j`, writes a new value into the PC. The two least significant bits of the PC are always 0, because the PC is word aligned (i.e., always a multiple of 4). The next 26 bits are taken from the jump address field in  $Instr_{25:0}$ . The upper four bits are taken from the old value of the PC.

The existing datapath lacks hardware to compute  $PC'$  in this fashion. Determine the necessary changes to both the datapath and controller to handle `j`.

**Solution:** First, we must add hardware to compute the next PC value,  $PC'$ , in the case of a `j` instruction and a multiplexer to select this next PC, as shown in Figure 7.14. The new multiplexer uses the new `Jump` control signal.

Now we must add a row to the main decoder truth table for the *j* instruction and a column for the *Jump* signal, as shown in [Table 7.5](#). The *Jump* control signal is 1 for the *j* instruction and 0 for all others. *j* does not write the register file or memory, so *RegWrite* = *MemWrite* = 0. Hence, we don't care about the computation done in the datapath, and *RegDst* = *ALUSrc* = *Branch* = *MemtoReg* = *ALUOp* = *X*.



**Figure 7.14** Single-cycle MIPS datapath enhanced to support the *j* instruction

**Table 7.5** Main decoder truth table enhanced to support *j*

Instruction	Opcode	RegWrite	RegDst	ALUSrc	Branch	MemWrite	MemtoReg	ALUOp	Jump
R-type	000000	1	1	0	0	0	0	10	0
lw	100011	1	0	1	0	0	1	00	0
sw	101011	0	X	1	0	1	X	00	0
beq	000100	0	X	0	1	0	X	01	0
addi	001000	1	0	1	0	0	0	00	0
j	000010	0	X	X	X	0	X	XX	1

### 7.3.4 Performance Analysis

Each instruction in the single-cycle processor takes one clock cycle, so the CPI is 1. The critical path for the  $\text{l}_w$  instruction is shown in Figure 7.15 with a heavy dashed blue line. It starts with the PC loading a new address on the rising edge of the clock. The instruction memory reads the next instruction. The register file reads  $SrcA$ . While the register file is reading, the immediate field is sign-extended and selected at the  $ALUSrc$  multiplexer to determine  $SrcB$ . The ALU adds  $SrcA$  and  $SrcB$  to find the effective address. The data memory reads from this address. The  $MemtoReg$  multiplexer selects  $ReadData$ . Finally,  $Result$  must setup at the register file before the next rising clock edge, so that it can be properly written. Hence, the cycle time is

$$T_c = t_{pcq\_PC} + t_{mem} + \max[t_{RFread}, t_{sext} + t_{mux}] \\ + t_{ALU} + t_{mem} + t_{mux} + t_{RFsetup} \quad (7.2)$$

In most implementation technologies, the ALU, memory, and register file accesses are substantially slower than other operations. Therefore, the cycle time simplifies to

$$T_c = t_{pcq\_PC} + 2t_{mem} + t_{RFread} + t_{ALU} + t_{mux} + t_{RFsetup} \quad (7.3)$$

The numerical values of these times will depend on the specific implementation technology.

Other instructions have shorter critical paths. For example, R-type instructions do not need to access data memory. However, we are

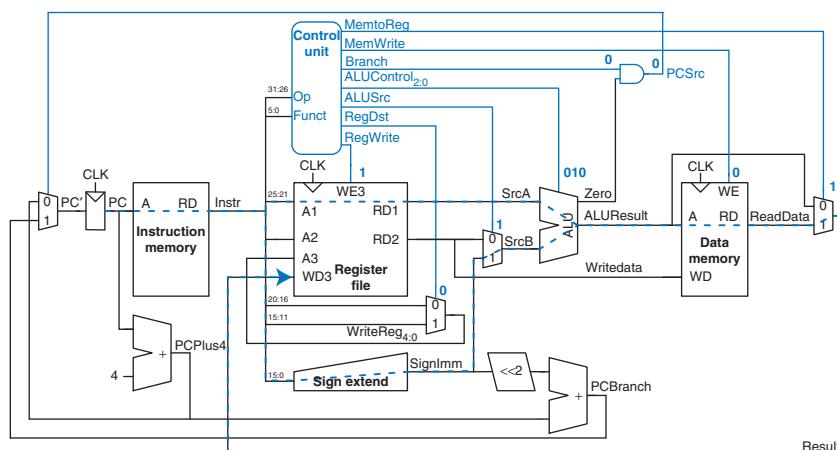


Figure 7.15 Critical path for  $\text{l}_w$  instruction

disciplining ourselves to synchronous sequential design, so the clock period is constant and must be long enough to accommodate the slowest instruction.

#### Example 7.4 SINGLE-CYCLE PROCESSOR PERFORMANCE

Ben Bitdiddle is contemplating building the single-cycle MIPS processor in a 65 nm CMOS manufacturing process. He has determined that the logic elements have the delays given in Table 7.6. Help him compute the execution time for a program with 100 billion instructions.

**Solution:** According to Equation 7.3, the cycle time of the single-cycle processor is  $T_{c1} = 30 + 2(250) + 150 + 200 + 25 + 20 = 925$  ps. We use the subscript “1” to distinguish it from subsequent processor designs. According to Equation 7.1, the total execution time is  $T_1 = (100 \times 10^9 \text{ instructions}) (1 \text{ cycle/instruction}) (925 \times 10^{-12} \text{ s/cycle}) = 92.5$  seconds.

**Table 7.6 Delays of circuit elements**

Element	Parameter	Delay (ps)
register clk-to-Q	$t_{pcq}$	30
register setup	$t_{\text{setup}}$	20
multiplexer	$t_{\text{mux}}$	25
ALU	$t_{\text{ALU}}$	200
memory read	$t_{\text{mem}}$	250
register file read	$t_{RF\text{read}}$	150
register file setup	$t_{RF\text{setup}}$	20

## 7.4 MULTICYCLE PROCESSOR

The single-cycle processor has three primary weaknesses. First, it requires a clock cycle long enough to support the slowest instruction ( $\lceil w \rceil$ ), even though most instructions are faster. Second, it requires three adders (one in the ALU and two for the PC logic); adders are relatively expensive circuits, especially if they must be fast. And third, it has separate instruction and data memories, which may not be realistic. Most computers have a single large memory that holds both instructions and data and that can be read and written.

The multicycle processor addresses these weaknesses by breaking an instruction into multiple shorter steps. In each short step, the processor

can read or write the memory or register file or use the ALU. Different instructions use different numbers of steps, so simpler instructions can complete faster than more complex ones. The processor needs only one adder; this adder is reused for different purposes on various steps. And the processor uses a combined memory for instructions and data. The instruction is fetched from memory on the first step, and data may be read or written on later steps.

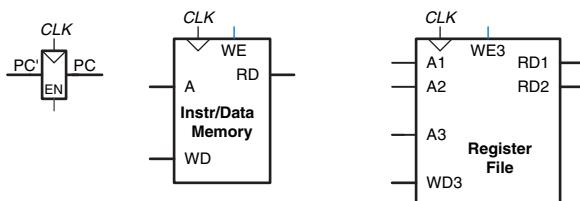
We design a multicycle processor following the same procedure we used for the single-cycle processor. First, we construct a datapath by connecting the architectural state elements and memories with combinational logic. But, this time, we also add nonarchitectural state elements to hold intermediate results between the steps. Then we design the controller. The controller produces different signals on different steps during execution of a single instruction, so it is now a finite state machine rather than combinational logic. We again examine how to add new instructions to the processor. Finally, we analyze the performance of the multicycle processor and compare it to the single-cycle processor.

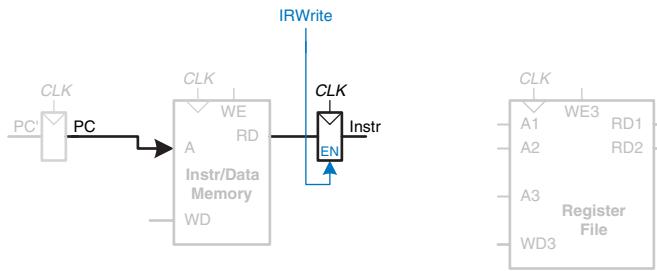
#### 7.4.1 Multicycle Datapath

Again, we begin our design with the memory and architectural state of the MIPS processor, shown in Figure 7.16. In the single-cycle design, we used separate instruction and data memories because we needed to read the instruction memory and read or write the data memory all in one cycle. Now, we choose to use a combined memory for both instructions and data. This is more realistic, and it is feasible because we can read the instruction in one cycle, then read or write the data in a separate cycle. The PC and register file remain unchanged. We gradually build the datapath by adding components to handle each step of each instruction. The new connections are emphasized in black (or blue, for new control signals), whereas the hardware that has already been studied is shown in gray.

The PC contains the address of the instruction to execute. The first step is to read this instruction from instruction memory. Figure 7.17 shows that the PC is simply connected to the address input of the instruction memory. The instruction is read and stored in a new nonarchitectural

**Figure 7.16** State elements with unified instruction/data memory





**Figure 7.17** Fetch instruction from memory

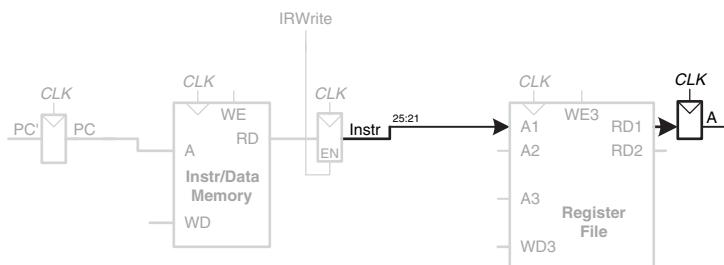
Instruction Register so that it is available for future cycles. The Instruction Register receives an enable signal, called *IRWrite*, that is asserted when it should be updated with a new instruction.

As we did with the single-cycle processor, we will work out the data-path connections for the `lw` instruction. Then we will enhance the data-path to handle the other instructions. For a `lw` instruction, the next step is to read the source register containing the base address. This register is specified in the *rs* field of the instruction, *Instr*<sub>25:21</sub>. These bits of the instruction are connected to one of the address inputs, *A*<sub>1</sub>, of the register file, as shown in Figure 7.18. The register file reads the register onto *RD*<sub>1</sub>. This value is stored in another nonarchitectural register, *A*.

The `lw` instruction also requires an offset. The offset is stored in the immediate field of the instruction, *Instr*<sub>15:0</sub>, and must be sign-extended to 32 bits, as shown in Figure 7.19. The 32-bit sign-extended value is called *SignImm*. To be consistent, we might store *SignImm* in another nonarchitectural register. However, *SignImm* is a combinational function of *Instr* and will not change while the current instruction is being processed, so there is no need to dedicate a register to hold the constant value.

The address of the load is the sum of the base address and offset. We use an ALU to compute this sum, as shown in Figure 7.20. *ALUControl* should be set to 010 to perform an addition. *ALUResult* is stored in a nonarchitectural register called *ALUOut*.

The next step is to load the data from the calculated address in the memory. We add a multiplexer in front of the memory to choose the



**Figure 7.18** Read source operand from register file

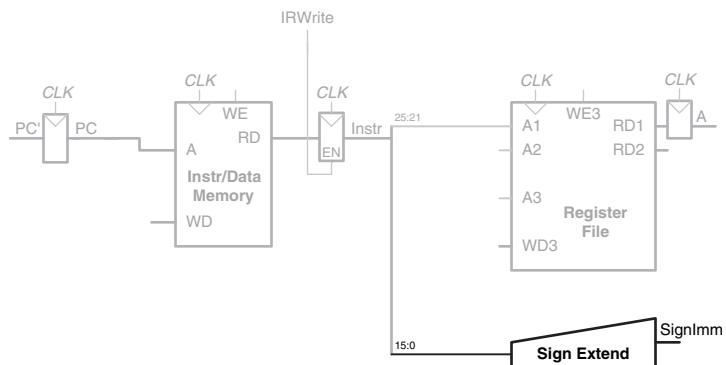


Figure 7.19 Sign-extend the immediate

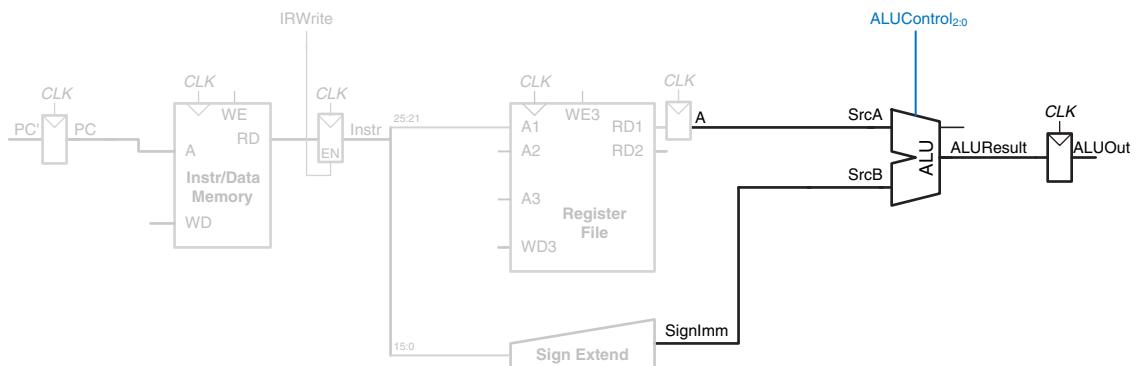


Figure 7.20 Add base address to offset

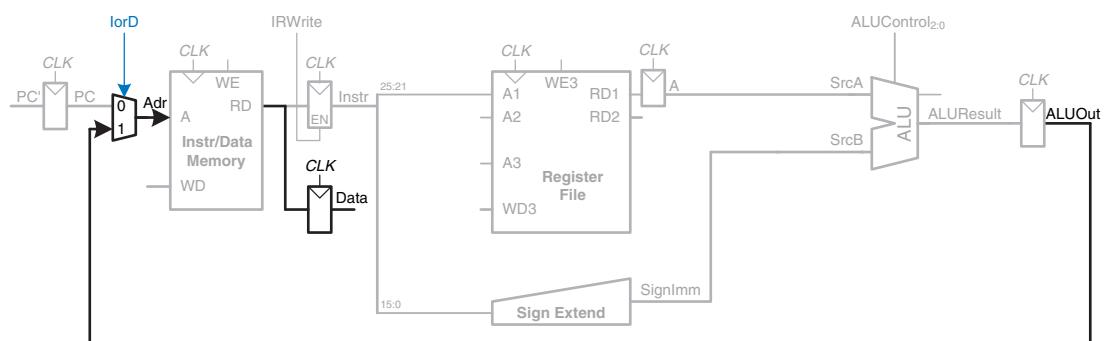


Figure 7.21 Load data from memory

memory address,  $Adr$ , from either the PC or  $ALUOut$ , as shown in Figure 7.21. The multiplexer select signal is called  $IorD$ , to indicate either an instruction or data address. The data read from the memory is stored in another nonarchitectural register, called  $Data$ . Notice that the address multiplexer permits us to reuse the memory during the  $lw$  instruction. On the first step, the address is taken from the PC to fetch the instruction. On a later step, the address is taken from  $ALUOut$  to load the data. Hence,  $IorD$  must have different values on different steps. In Section 7.4.2, we develop the FSM controller that generates these sequences of control signals.

Finally, the data is written back to the register file, as shown in Figure 7.22. The destination register is specified by the  $rt$  field of the instruction,  $Instr_{20:16}$ .

While all this is happening, the processor must update the program counter by adding 4 to the old PC. In the single-cycle processor, a separate adder was needed. In the multicycle processor, we can use the existing ALU on one of the steps when it is not busy. To do so, we must insert source multiplexers to choose the PC and the constant 4 as ALU inputs, as shown in Figure 7.23. A two-input multiplexer controlled by  $ALUSrcA$  chooses either the PC or register  $A$  as  $SrcA$ . A four-input multiplexer controlled by  $ALUSrcB$  chooses either 4 or  $SignImm$  as  $SrcB$ . We use the other two multiplexer inputs later when we extend the datapath to handle other instructions. (The numbering of inputs to the multiplexer is arbitrary.) To update the PC, the ALU adds  $SrcA$  ( $PC$ ) to  $SrcB$  (4), and the result is written into the program counter register. The  $PCWrite$  control signal enables the PC register to be written only on certain cycles.

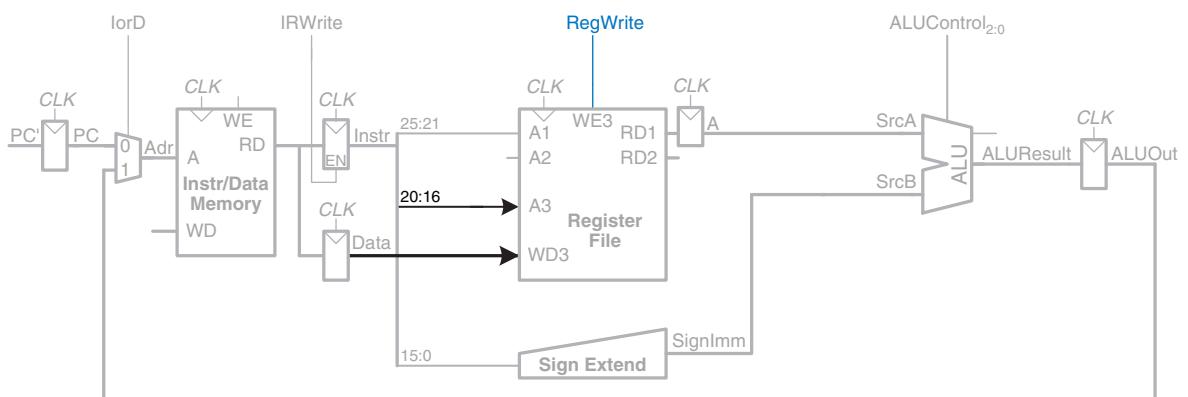


Figure 7.22 Write data back to register file

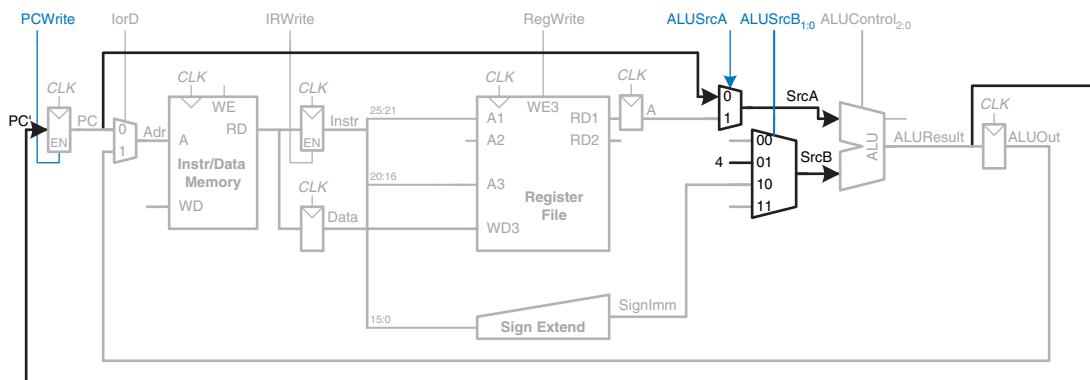


Figure 7.23 Increment PC by 4

This completes the datapath for the `lw` instruction. Next, let us extend the datapath to also handle the `sw` instruction. Like the `lw` instruction, the `sw` instruction reads a base address from port 1 of the register file and sign-extends the immediate. The ALU adds the base address to the immediate to find the memory address. All of these functions are already supported by existing hardware in the datapath.

The only new feature of `sw` is that we must read a second register from the register file and write it into the memory, as shown in Figure 7.24. The register is specified in the `rt` field of the instruction, `Instr20:16`, which is connected to the second port of the register file. When the register is read, it is stored in a nonarchitectural register, `B`. On the next step, it is sent to the write data port (`WD`) of the data memory to be written. The memory receives an additional `MemWrite` control signal to indicate that the write should occur.

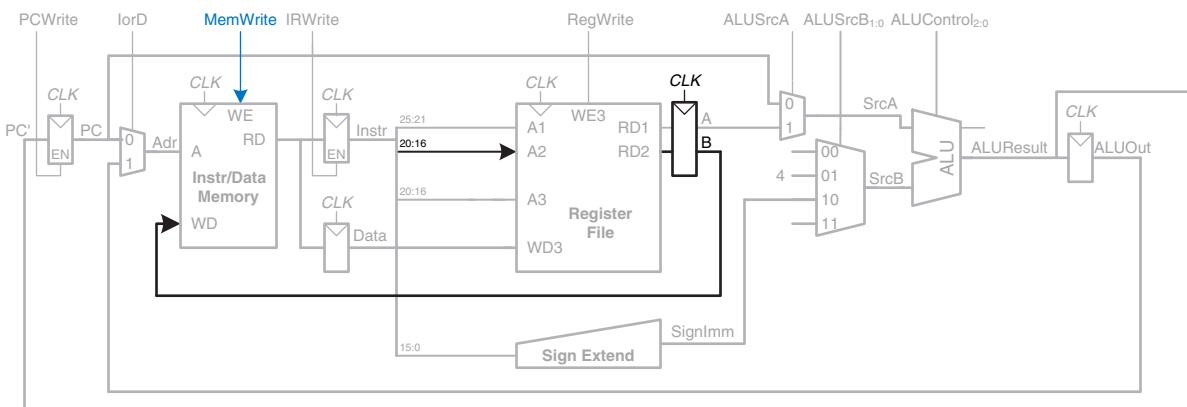
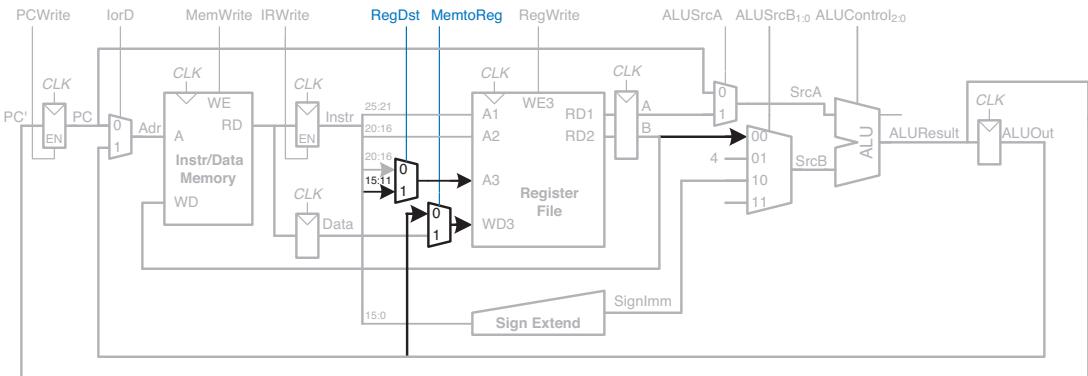


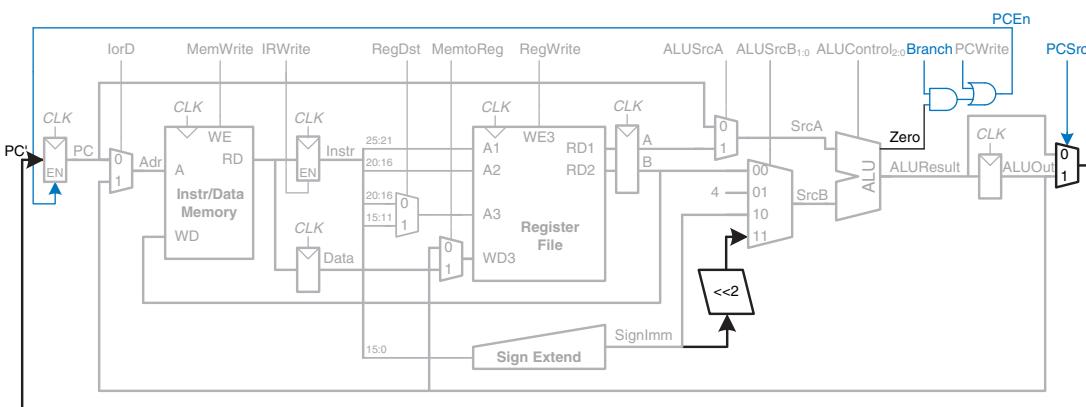
Figure 7.24 Enhanced datapath for SW instruction



**Figure 7.25 Enhanced datapath for R-type instructions**

For R-type instructions, the instruction is again fetched, and the two source registers are read from the register file.  $ALUSrcB_{1:0}$ , the control input of the  $SrcB$  multiplexer, is used to choose register  $B$  as the second source register for the ALU, as shown in Figure 7.25. The ALU performs the appropriate operation and stores the result in  $ALUOut$ . On the next step,  $ALUOut$  is written back to the register specified by the  $rd$  field of the instruction,  $Instr_{15:11}$ . This requires two new multiplexers. The  $MemtoReg$  multiplexer selects whether  $WD3$  comes from  $ALUOut$  (for R-type instructions) or from  $Data$  (for  $lw$ ). The  $RegDst$  instruction selects whether the destination register is specified in the  $rt$  or  $rd$  field of the instruction.

For the  $beq$  instruction, the instruction is again fetched, and the two source registers are read from the register file. To determine whether the registers are equal, the ALU subtracts the registers and, upon a zero result, sets the *Zero* flag. Meanwhile, the datapath must compute the next value of the PC if the branch is taken:  $PC' = PC + 4 + SignImm \times 4$ . In the single-cycle processor, yet another adder was needed to compute the branch address. In the multicycle processor, the ALU can be reused again to save hardware. On one step, the ALU computes  $PC + 4$  and writes it back to the program counter, as was done for other instructions. On another step, the ALU uses this updated PC value to compute  $PC + SignImm \times 4$ .  $SignImm$  is left-shifted by 2 to multiply it by 4, as shown in Figure 7.26. The  $SrcB$  multiplexer chooses this value and adds it to the PC. This sum represents the destination of the branch and is stored in  $ALUOut$ . A new multiplexer, controlled by  $PCSrc$ , chooses what signal should be sent to  $PC'$ . The program counter should be written either when  $PCWrite$  is asserted or when a branch is taken. A new control signal,  $Branch$ , indicates that the  $beq$  instruction is being executed. The branch is taken if *Zero* is also asserted. Hence, the datapath computes a new PC write enable,



**Figure 7.26 Enhanced datapath for beq instruction**

called *PCEn*, which is TRUE either when *PCWrite* is asserted or when both *Branch* and *Zero* are asserted.

This completes the design of the multicycle MIPS processor datapath. The design process is much like that of the single-cycle processor in that hardware is systematically connected between the state elements to handle each instruction. The main difference is that the instruction is executed in several steps. Nonarchitectural registers are inserted to hold the results of each step. In this way, the ALU can be reused several times, saving the cost of extra adders. Similarly, the instructions and data can be stored in one shared memory. In the next section, we develop an FSM controller to deliver the appropriate sequence of control signals to the datapath on each step of each instruction.

### 7.4.2 Multicycle Control

As in the single-cycle processor, the control unit computes the control signals based on the opcode and funct fields of the instruction,  $Instr_{31:26}$  and  $Instr_{5:0}$ . Figure 7.27 shows the entire multicycle MIPS processor with the control unit attached to the datapath. The datapath is shown in black, and the control unit is shown in blue.

As in the single-cycle processor, the control unit is partitioned into a main controller and an ALU decoder, as shown in Figure 7.28. The ALU decoder is unchanged and follows the truth table of Table 7.2. Now, however, the main controller is an FSM that applies the proper control signals on the proper cycles or steps. The sequence of control signals depends on the instruction being executed. In the remainder of this section, we will develop the FSM state transition diagram for the main controller.

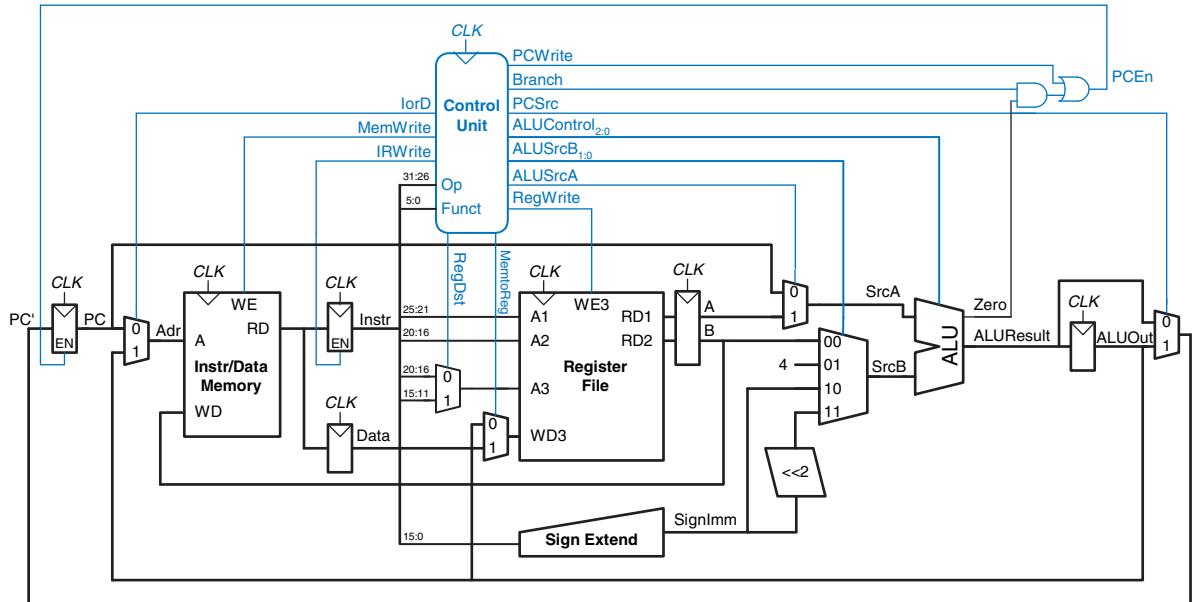


Figure 7.27 Complete multicycle MIPS processor

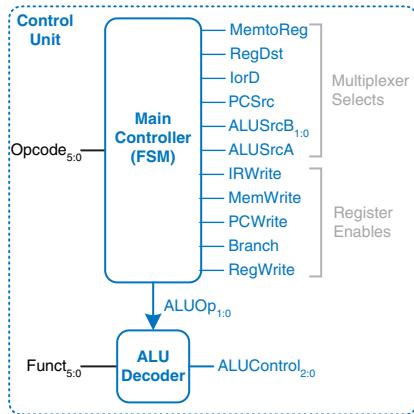


Figure 7.28 Control unit internal structure

The main controller produces multiplexer select and register enable signals for the datapath. The select signals are *MemtoReg*, *RegDst*, *IorD*, *PCSrc*, *ALUSrcB*, and *ALUSrcA*. The enable signals are *IRWrite*, *MemWrite*, *PCWrite*, *Branch*, and *RegWrite*.

To keep the following state transition diagrams readable, only the relevant control signals are listed. Select signals are listed only when their value matters; otherwise, they are don't cares. Enable signals are listed only when they are asserted; otherwise, they are 0.

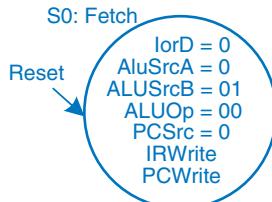


Figure 7.29 Fetch

The first step for any instruction is to fetch the instruction from memory at the address held in the PC. The FSM enters this state on reset. To read memory,  $IorD = 0$ , so the address is taken from the PC.  $IRWrite$  is asserted to write the instruction into the instruction register, IR. Meanwhile, the PC should be incremented by 4 to point to the next instruction. Because the ALU is not being used for anything else, the processor can use it to compute  $PC + 4$  at the same time that it fetches the instruction.  $ALUSrcA = 0$ , so  $SrcA$  comes from the PC.  $ALUSrcB = 01$ , so  $SrcB$  is the constant 4.  $ALUOp = 00$ , so the ALU decoder produces  $ALUControl = 010$  to make the ALU add. To update the PC with this new value,  $PCSrc = 0$ , and  $PCWrite$  is asserted. These control signals are shown in Figure 7.29. The data flow on this step is shown in Figure 7.30, with the instruction fetch shown using the dashed blue line and the PC increment shown using the dashed gray line.

The next step is to read the register file and decode the instruction. The register file always reads the two sources specified by the  $rs$  and  $rt$  fields of the instruction. Meanwhile, the immediate is sign-extended. Decoding involves examining the opcode of the instruction to determine what to do next. No control signals are necessary to decode the instruction, but the FSM must wait 1 cycle for the reading and decoding to complete, as shown in Figure 7.31. The new state is highlighted in blue. The data flow is shown in Figure 7.32.

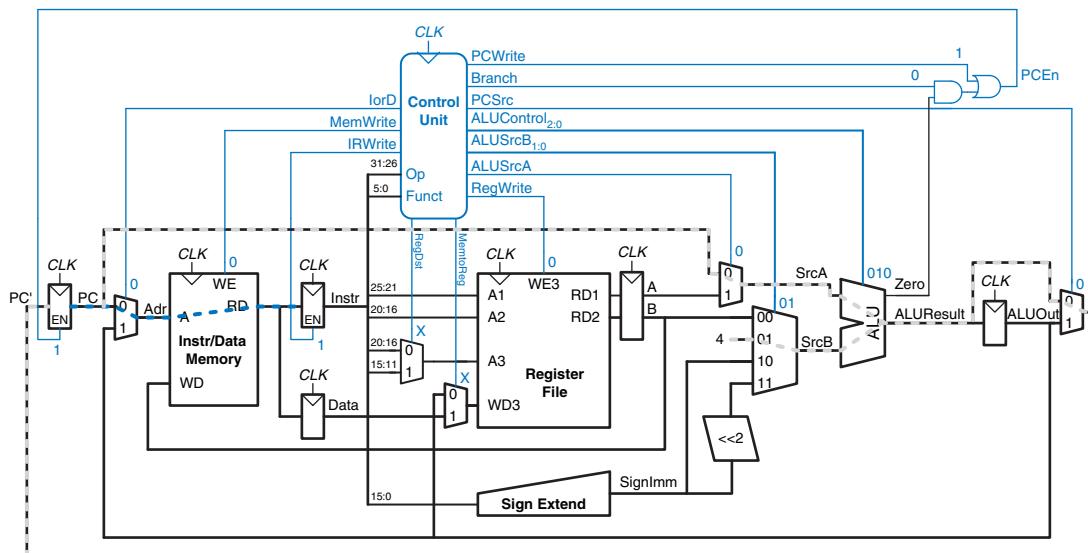


Figure 7.30 Data flow during the fetch step

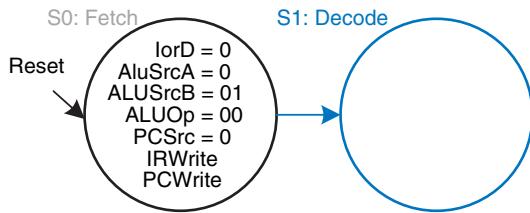


Figure 7.31 Decode

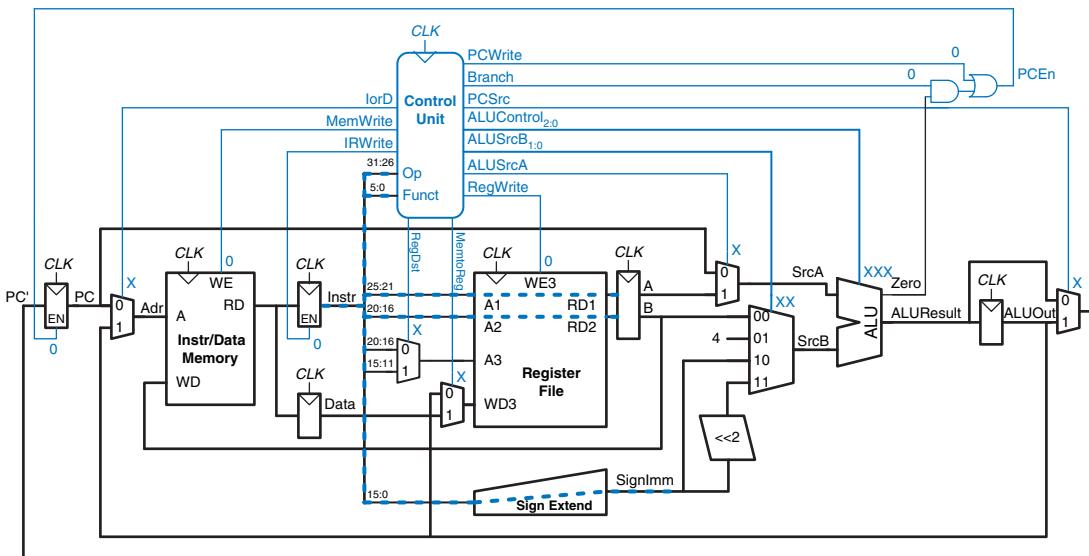
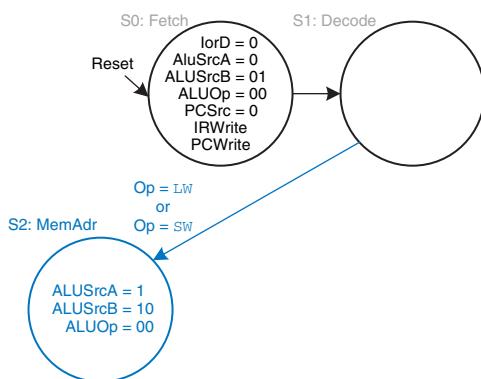


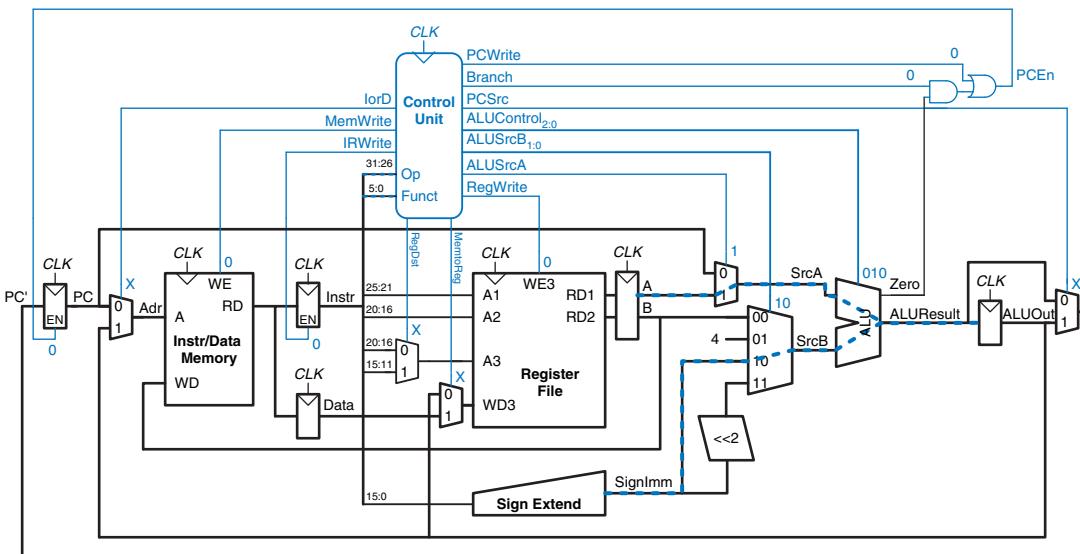
Figure 7.32 Data flow during the decode step

Now the FSM proceeds to one of several possible states, depending on the opcode. If the instruction is a memory load or store (`lw` or `sw`), the multicycle processor computes the address by adding the base address to the sign-extended immediate. This requires  $ALUSrcA = 1$  to select register A and  $ALUSrcB = 10$  to select  $SignImm$ .  $ALUOp = 00$ , so the ALU adds. The effective address is stored in the  $ALUOut$  register for use on the next step. This FSM step is shown in Figure 7.33, and the data flow is shown in Figure 7.34.

If the instruction is `lw`, the multicycle processor must next read data from memory and write it to the register file. These two steps are shown in Figure 7.35. To read from memory,  $IorD = 1$  to select the memory address that was just computed and saved in  $ALUOut$ . This address in memory is read and saved in the Data register during step S3. On the next step, S4,  $Data$  is written to the register file.  $MemtoReg = 1$  to select



**Figure 7.33** Memory address computation



**Figure 7.34** Data flow during memory address computation

*Data*, and *RegDst* = 0 to pull the destination register from the *rt* field of the instruction. *RegWrite* is asserted to perform the write, completing the *lw* instruction. Finally, the FSM returns to the initial state, S0, to fetch the next instruction. For these and subsequent steps, try to visualize the data flow on your own.

From state S2, if the instruction is *sw*, the data read from the second port of the register file is simply written to memory. In state S3, *IorD* = 1 to select the address computed in S2 and saved in *ALUOut*. *MemWrite* is asserted to write the memory. Again, the FSM returns to S0 to fetch the next instruction. The added step is shown in Figure 7.36.

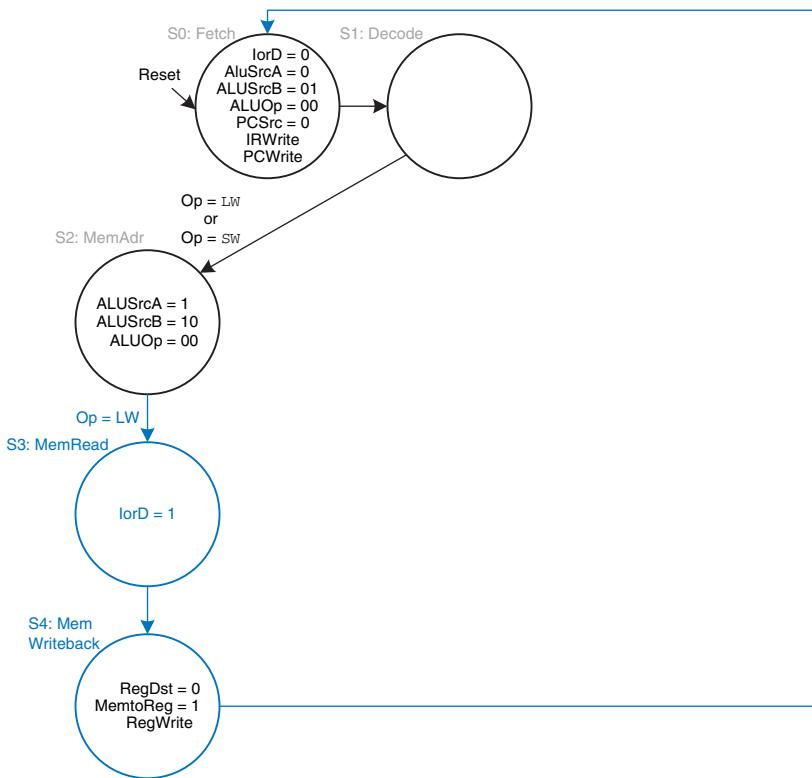
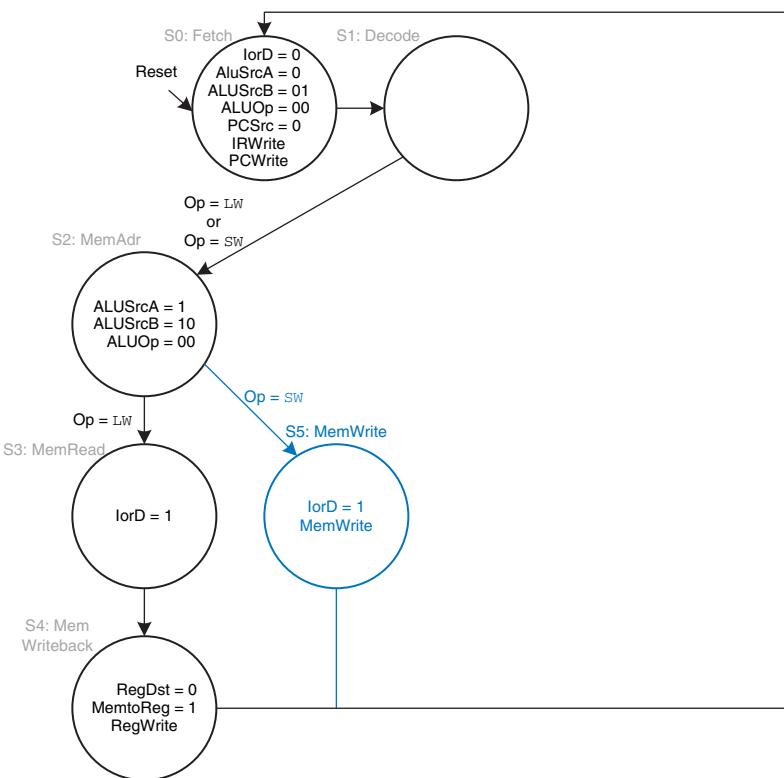


Figure 7.35 Memory read

If the opcode indicates an R-type instruction, the multicycle processor must calculate the result using the ALU and write that result to the register file. Figure 7.37 shows these two steps. In S6, the instruction is executed by selecting the A and B registers ( $ALUSrcA = 1$ ,  $ALUSrcB = 00$ ) and performing the ALU operation indicated by the funct field of the instruction.  $ALUOp = 10$  for all R-type instructions. The  $ALUResult$  is stored in  $ALUOut$ . In S7,  $ALUOut$  is written to the register file,  $RegDst = 1$ , because the destination register is specified in the rd field of the instruction.  $MemoReg = 0$  because the write data,  $WD3$ , comes from  $ALUOut$ .  $RegWrite$  is asserted to write the register file.

For a beq instruction, the processor must calculate the destination address and compare the two source registers to determine whether the branch should be taken. This requires two uses of the ALU and hence might seem to demand two new states. Notice, however, that the ALU was not used during S1 when the registers were being read. The processor might as well use the ALU at that time to compute the destination address by adding the incremented PC,  $PC + 4$ , to  $SignImm \times 4$ , as shown in Figure 7.38 (see page 404).  $ALUSrcA = 0$  to select the incremented PC,

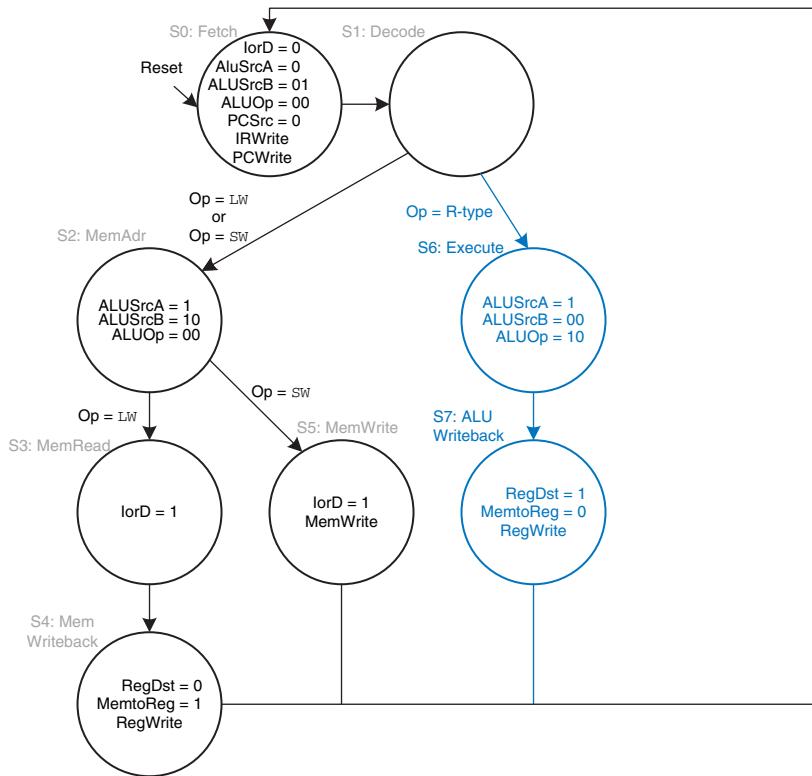


**Figure 7.36** Memory write

$ALUSrcB = 11$  to select  $SignImm \times 4$ , and  $ALUOp = 00$  to add. The destination address is stored in  $ALUOut$ . If the instruction is not `beq`, the computed address will not be used in subsequent cycles, but its computation was harmless. In S8, the processor compares the two registers by subtracting them and checking to determine whether the result is 0. If it is, the processor branches to the address that was just computed.  $ALUSrcA = 1$  to select register A;  $ALUSrcB = 00$  to select register B;  $ALUOp = 01$  to subtract;  $PCSrc = 1$  to take the destination address from  $ALUOut$ , and  $Branch = 1$  to update the PC with this address if the ALU result is 0.<sup>2</sup>

Putting these steps together, Figure 7.39 shows the complete main controller state transition diagram for the multicycle processor (see page 405). Converting it to hardware is a straightforward but tedious task using the techniques of Chapter 3. Better yet, the FSM can be coded in an HDL and synthesized using the techniques of Chapter 4.

<sup>2</sup> Now we see why the  $PCSrc$  multiplexer is necessary to choose  $PC'$  from either  $ALUResult$  (in S0) or  $ALUOut$  (in S8).



**Figure 7.37** Execute R-type operation

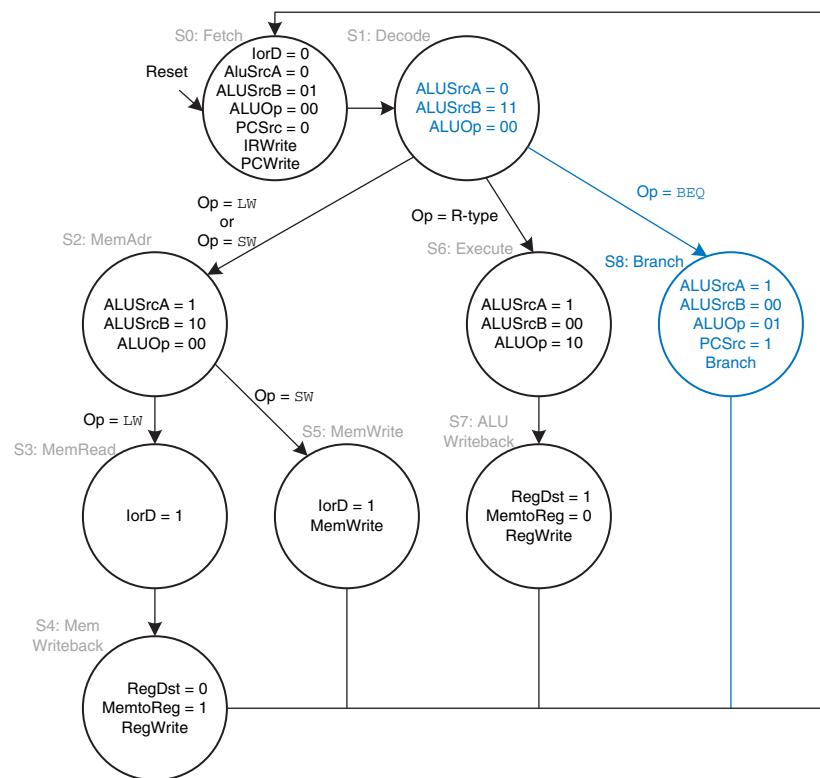
### 7.4.3 More Instructions

As we did in Section 7.3.3 for the single-cycle processor, let us now extend the multicycle processor to support the addi and j instructions. The next two examples illustrate the general design process to support new instructions.

#### Example 7.5 addi INSTRUCTION

Modify the multicycle processor to support addi.

**Solution:** The datapath is already capable of adding registers to immediates, so all we need to do is add new states to the main controller FSM for addi, as shown in Figure 7.40 (see page 406). The states are similar to those for R-type instructions. In S9, register A is added to *SignImm* ( $ALUSrcA = 1$ ,  $ALUSrcB = 10$ ,  $ALUOp = 00$ ) and the result, *ALUResult*, is stored in *ALUOut*. In S10, *ALUOut* is written



**Figure 7.38** Branch

to the register specified by the *rt* field of the instruction (*RegDst* = 0, *MemtoReg* = 0, *RegWrite* asserted). The astute reader may notice that S2 and S9 are identical and could be merged into a single state.

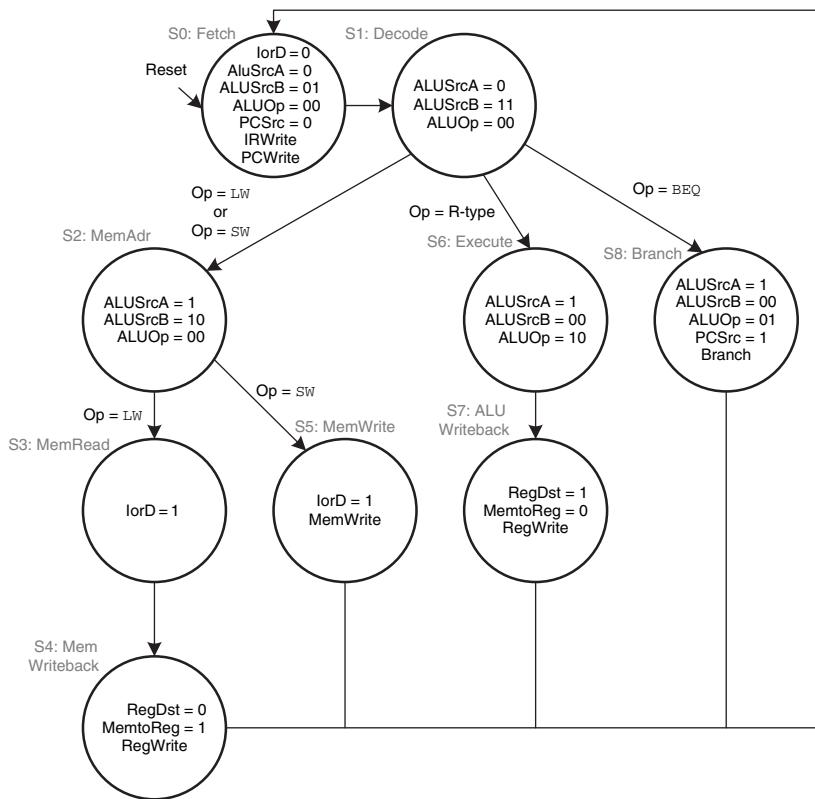
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#### Example 7.6 j INSTRUCTION

Modify the multicycle processor to support *j*.

**Solution:** First, we must modify the datapath to compute the next PC value in the case of a *j* instruction. Then we add a state to the main controller to handle the instruction.

Figure 7.41 shows the enhanced datapath (see page 407). The jump destination address is formed by left-shifting the 26-bit *addr* field of the instruction by two bits, then prepending the four most significant bits of the already incremented PC. The *PCSrc* multiplexer is extended to take this address as a third input.



**Figure 7.39** Complete multicycle control FSM

Figure 7.42 shows the enhanced main controller (see page 408). The new state, S11, simply selects  $PC'$  as the  $PCJump$  value ( $PCSrc = 10$ ) and writes the PC. Note that the  $PCSrc$  select signal is extended to two bits in S0 and S8 as well.

#### 7.4.4 Performance Analysis

The execution time of an instruction depends on both the number of cycles it uses and the cycle time. Whereas the single-cycle processor performed all instructions in one cycle, the multicycle processor uses varying numbers of cycles for the various instructions. However, the multicycle processor does less work in a single cycle and, thus, has a shorter cycle time.

The multicycle processor requires three cycles for `beq` and `j` instructions, four cycles for `sw`, `addi`, and R-type instructions, and five cycles for `lw` instructions. The CPI depends on the relative likelihood that each instruction is used.

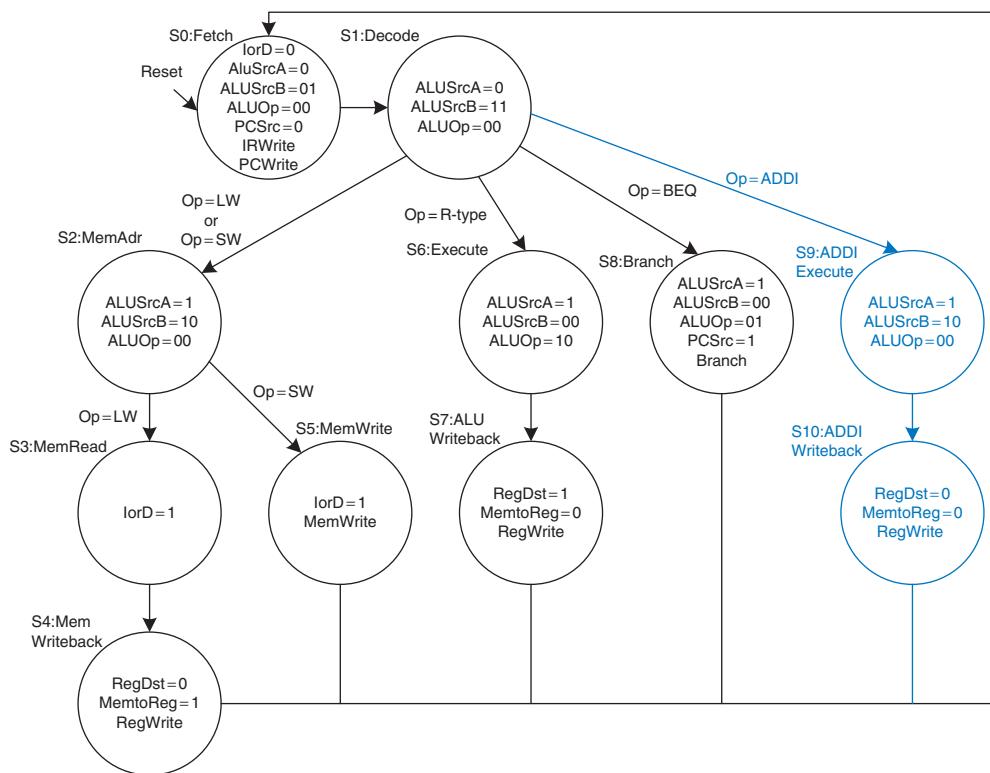


Figure 7.40 Main controller states for addi

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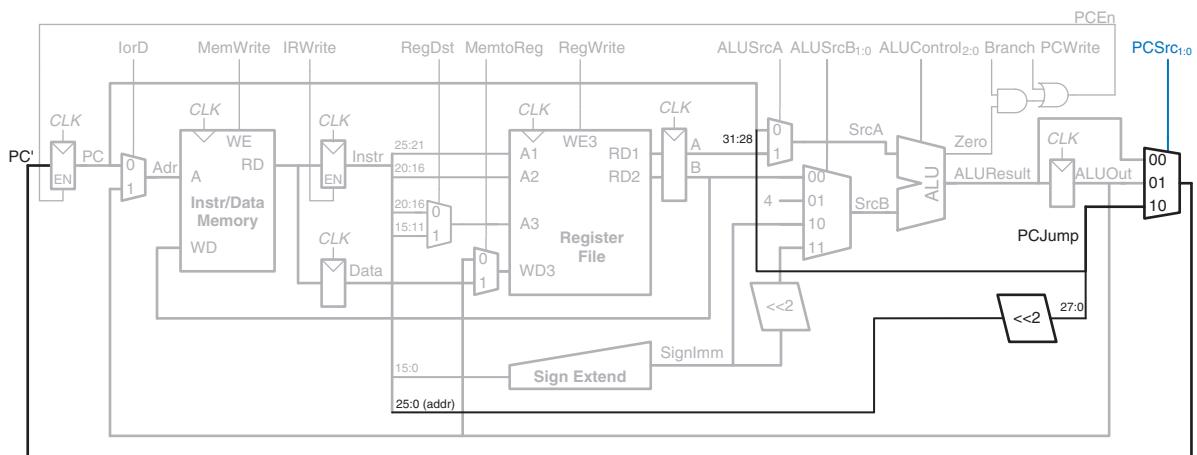
#### Example 7.7 MULTICYCLE PROCESSOR CPI

The SPECINT2000 benchmark consists of approximately 25% loads, 10% stores, 11% branches, 2% jumps, and 52% R-type instructions.<sup>3</sup> Determine the average CPI for this benchmark.

**Solution:** The average CPI is the sum over each instruction of the CPI for that instruction multiplied by the fraction of the time that instruction is used. For this benchmark,  $\text{Average CPI} = (0.11 + 0.02)(3) + (0.52 + 0.10)(4) + (0.25)(5) = 4.12$ . This is better than the worst-case CPI of 5, which would be required if all instructions took the same time.

---

<sup>3</sup> Data from Patterson and Hennessy, *Computer Organization and Design*, 4th Edition, Morgan Kaufmann, 2011.



**Figure 7.41** Multicycle MIPS datapath enhanced to support the `j` instruction

Recall that we designed the multicycle processor so that each cycle involved one ALU operation, memory access, or register file access. Let us assume that the register file is faster than the memory and that writing memory is faster than reading memory. Examining the datapath reveals two possible critical paths that would limit the cycle time:

$$T_c = t_{pcq} + t_{mux} + \max(t_{ALU} + t_{mux}, t_{mem}) + t_{\text{setup}} \quad (7.4)$$

The numerical values of these times will depend on the specific implementation technology.

## **Example 7.8** PROCESSOR PERFORMANCE COMPARISON

Ben Bitdiddle is wondering whether he would be better off building the multicycle processor instead of the single-cycle processor. For both designs, he plans on using a 65 nm CMOS manufacturing process with the delays given in [Table 7.6](#). Help him compare each processor's execution time for 100 billion instructions from the SPECINT2000 benchmark (see [Example 7.7](#)).

**Solution:** According to Equation 7.4, the cycle time of the multicycle processor is  $T_{c2} = 30 + 25 + 250 + 20 = 325$  ps. Using the CPI of 4.12 from Example 7.7, the total execution time is  $T_2 = (100 \times 10^9 \text{ instructions})(4.12 \text{ cycles/instruction})(325 \times 10^{-12} \text{ s/cycle}) = 133.9$  seconds. According to Example 7.4, the single-cycle processor had a cycle time of  $T_{c1} = 925$  ps, a CPI of 1, and a total execution time of 92.5 seconds.

One of the original motivations for building a multicycle processor was to avoid making all instructions take as long as the slowest one. Unfortunately, this

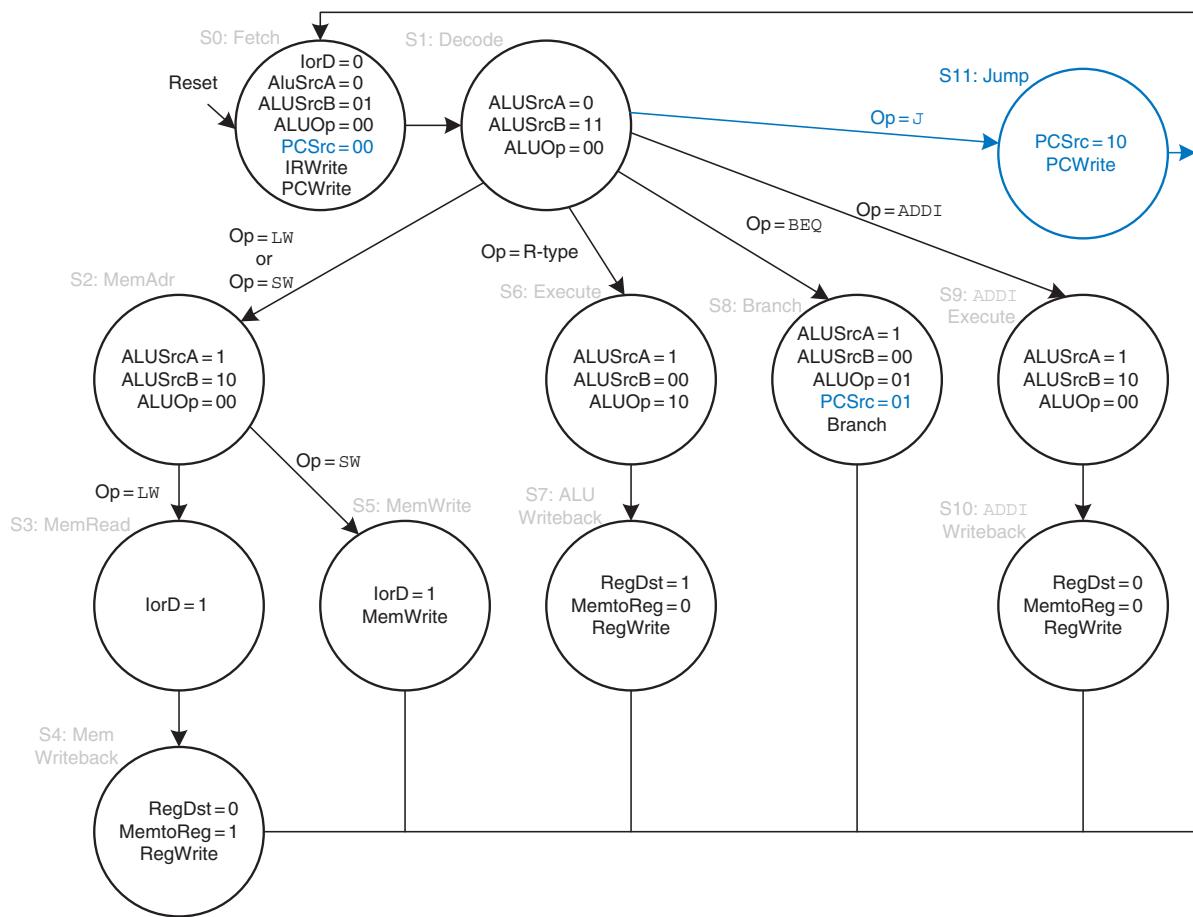


Figure 7.42 Main controller state for  $j$

example shows that the multicycle processor is slower than the single-cycle processor given the assumptions of CPI and circuit element delays. The fundamental problem is that even though the slowest instruction,  $\text{l}_w$ , was broken into five steps, the multicycle processor cycle time was not nearly improved five-fold. This is partly because not all of the steps are exactly the same length, and partly because the 50-ps sequencing overhead of the register clk-to-Q and setup time must now be paid on every step, not just once for the entire instruction. In general, engineers have learned that it is difficult to exploit the fact that some computations are faster than others unless the differences are large.

Compared with the single-cycle processor, the multicycle processor is likely to be less expensive because it eliminates two adders and combines the instruction and data memories into a single unit. It does, however, require five nonarchitectural registers and additional multiplexers.

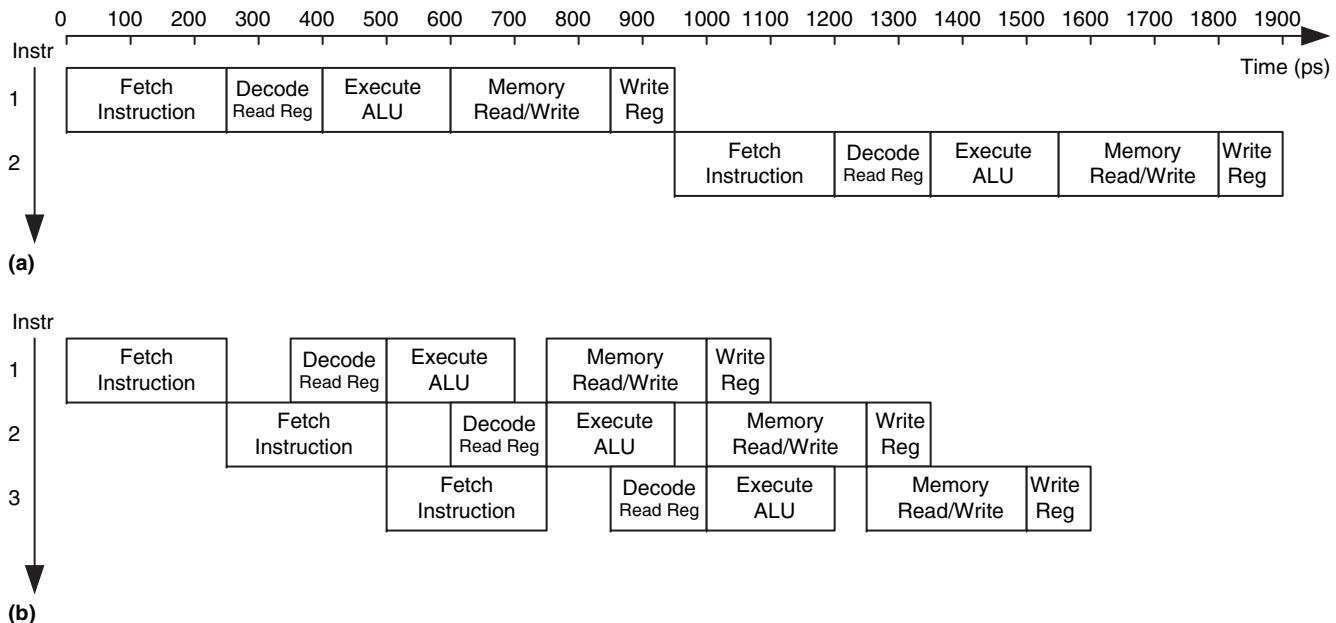
## 7.5 PIPELINED PROCESSOR

Pipelining, introduced in [Section 3.6](#), is a powerful way to improve the throughput of a digital system. We design a pipelined processor by subdividing the single-cycle processor into five pipeline stages. Thus, five instructions can execute simultaneously, one in each stage. Because each stage has only one-fifth of the entire logic, the clock frequency is almost five times faster. Hence, the latency of each instruction is ideally unchanged, but the throughput is ideally five times better. Microprocessors execute millions or billions of instructions per second, so throughput is more important than latency. Pipelining introduces some overhead, so the throughput will not be quite as high as we might ideally desire, but pipelining nevertheless gives such great advantage for so little cost that all modern high-performance microprocessors are pipelined.

Reading and writing the memory and register file and using the ALU typically constitute the biggest delays in the processor. We choose five pipeline stages so that each stage involves exactly one of these slow steps. Specifically, we call the five stages *Fetch*, *Decode*, *Execute*, *Memory*, and *Writeback*. They are similar to the five steps that the multi-cycle processor used to perform `lw`. In the *Fetch* stage, the processor reads the instruction from instruction memory. In the *Decode* stage, the processor reads the source operands from the register file and decodes the instruction to produce the control signals. In the *Execute* stage, the processor performs a computation with the ALU. In the *Memory* stage, the processor reads or writes data memory. Finally, in the *Writeback* stage, the processor writes the result to the register file, when applicable.

[Figure 7.43](#) shows a timing diagram comparing the single-cycle and pipelined processors. Time is on the horizontal axis, and instructions are on the vertical axis. The diagram assumes the logic element delays from [Table 7.6](#) but ignores the delays of multiplexers and registers. In the single-cycle processor, [Figure 7.43\(a\)](#), the first instruction is read from memory at time 0; next the operands are read from the register file; and then the ALU executes the necessary computation. Finally, the data memory may be accessed, and the result is written back to the register file by 950 ps. The second instruction begins when the first completes. Hence, in this diagram, the single-cycle processor has an instruction latency of  $250 + 150 + 200 + 250 + 100 = 950$  ps and a throughput of 1 instruction per 950 ps (1.05 billion instructions per second).

In the pipelined processor, [Figure 7.43\(b\)](#), the length of a pipeline stage is set at 250 ps by the slowest stage, the memory access (in the Fetch or Memory stage). At time 0, the first instruction is fetched from memory. At 250 ps, the first instruction enters the Decode stage, and a



**Figure 7.43** Timing diagrams: (a) single-cycle processor, (b) pipelined processor

second instruction is fetched. At 500 ps, the first instruction executes, the second instruction enters the Decode stage, and a third instruction is fetched. And so forth, until all the instructions complete. The instruction latency is  $5 \times 250 = 1250$  ps. The throughput is 1 instruction per 250 ps (4 billion instructions per second). Because the stages are not perfectly balanced with equal amounts of logic, the latency is slightly longer for the pipelined than for the single-cycle processor. Similarly, the throughput is not quite five times as great for a five-stage pipeline as for the single-cycle processor. Nevertheless, the throughput advantage is substantial.

Figure 7.44 shows an abstracted view of the pipeline in operation in which each stage is represented pictorially. Each pipeline stage is represented with its major component—instruction memory (IM), register file (RF) read, ALU execution, data memory (DM), and register file write-back—to illustrate the flow of instructions through the pipeline. Reading across a row shows the clock cycles in which a particular instruction is in each stage. For example, the `sub` instruction is fetched in cycle 3 and executed in cycle 5. Reading down a column shows what the various pipeline stages are doing on a particular cycle. For example, in cycle 6, the `or` instruction is being fetched from instruction memory, while `$s1` is being read from the register file, the ALU is computing `$t5 AND $t6`, the data memory is idle, and the register file is writing a sum to `$s3`. Stages are shaded to indicate when they are used. For example, the data memory is used by `lw` in cycle 4 and by `sw` in cycle 8. The instruction memory and ALU are used in every cycle. The register file is written by every

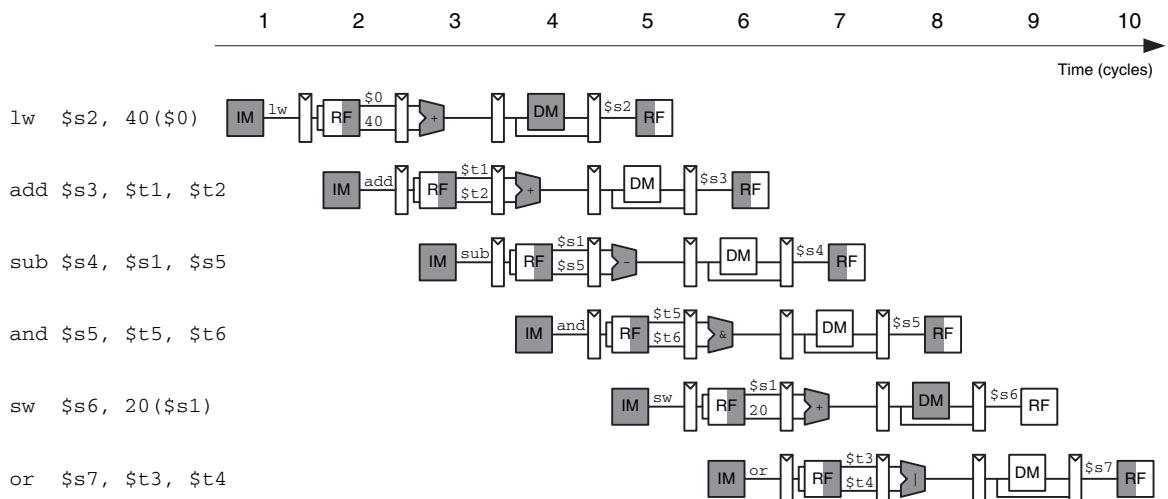


Figure 7.44 Abstract view of pipeline in operation

instruction except `sw`. In the pipelined processor, the register file is written in the first part of a cycle and read in the second part, as suggested by the shading. This way, data can be written and read back within a single cycle.

A central challenge in pipelined systems is handling *hazards* that occur when the results of one instruction are needed by a subsequent instruction before the former instruction has completed. For example, if the `add` in [Figure 7.44](#) used `$s2` rather than `$t2`, a hazard would occur because the `$s2` register has not been written by the `lw` by the time it is read by the `add`. This section explores *forwarding*, *stalls*, and *flushes* as methods to resolve hazards. Finally, this section revisits performance analysis considering sequencing overhead and the impact of hazards.

### 7.5.1 Pipelined Datapath

The pipelined datapath is formed by chopping the single-cycle datapath into five stages separated by pipeline registers. [Figure 7.45\(a\)](#) shows the single-cycle datapath stretched out to leave room for the pipeline registers. [Figure 7.45\(b\)](#) shows the pipelined datapath formed by inserting four pipeline registers to separate the datapath into five stages. The stages and their boundaries are indicated in blue. Signals are given a suffix (F, D, E, M, or W) to indicate the stage in which they reside.

The register file is peculiar because it is read in the Decode stage and written in the Writeback stage. It is drawn in the Decode stage, but the write address and data come from the Writeback stage. This feedback will lead to pipeline hazards, which are discussed in [Section 7.5.3](#). The register file in the pipelined processor writes on the falling edge of `CLK`, when `WD3` is stable.

One of the subtle but critical issues in pipelining is that all signals associated with a particular instruction must advance through the pipeline in unison. [Figure 7.45\(b\)](#) has an error related to this issue. Can you find it?

The error is in the register file write logic, which should operate in the Writeback stage. The data value comes from `ResultW`, a Writeback stage signal. But the address comes from `WriteRegE`, an Execute stage signal. In the pipeline diagram of [Figure 7.44](#), during cycle 5, the result of the `lw` instruction would be incorrectly written to `$s4` rather than `$s2`.

[Figure 7.46](#) shows a corrected datapath. The `WriteReg` signal is now pipelined along through the Memory and Writeback stages, so it remains in sync with the rest of the instruction. `WriteRegW` and `ResultW` are fed back together to the register file in the Writeback stage.

The astute reader may notice that the `PC'` logic is also problematic, because it might be updated with a Fetch or a Memory stage signal (`PCPlus4F` or `PCBranchM`). This control hazard will be fixed in [Section 7.5.3](#).

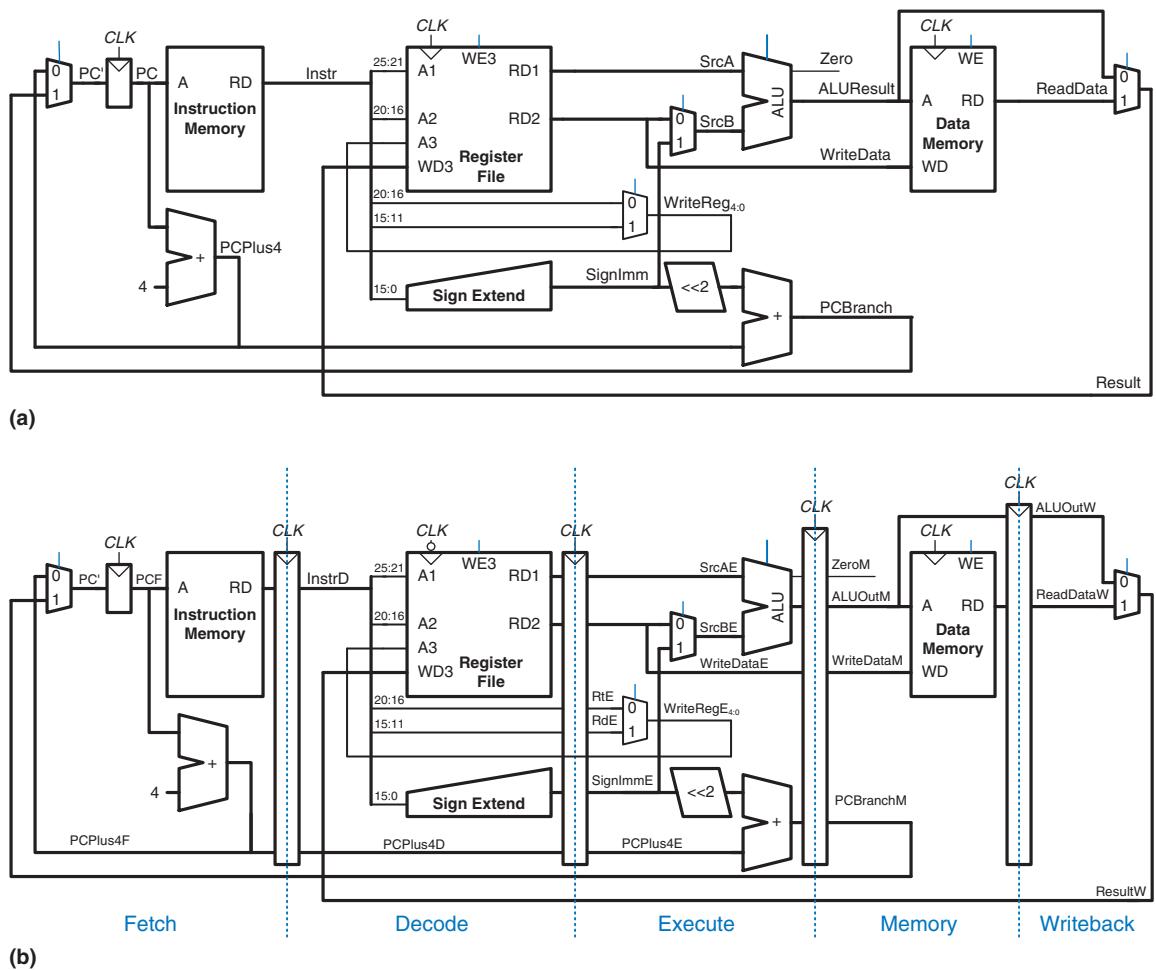


Figure 7.45 Single-cycle and pipelined datapaths

### 7.5.2 Pipelined Control

The pipelined processor takes the same control signals as the single-cycle processor and therefore uses the same control unit. The control unit examines the `opcode` and `funct` fields of the instruction in the Decode stage to produce the control signals, as was described in Section 7.3.2. These control signals must be pipelined along with the data so that they remain synchronized with the instruction.

The entire pipelined processor with control is shown in Figure 7.47. `RegWrite` must be pipelined into the Writeback stage before it feeds back to the register file, just as `WriteReg` was pipelined in Figure 7.46.

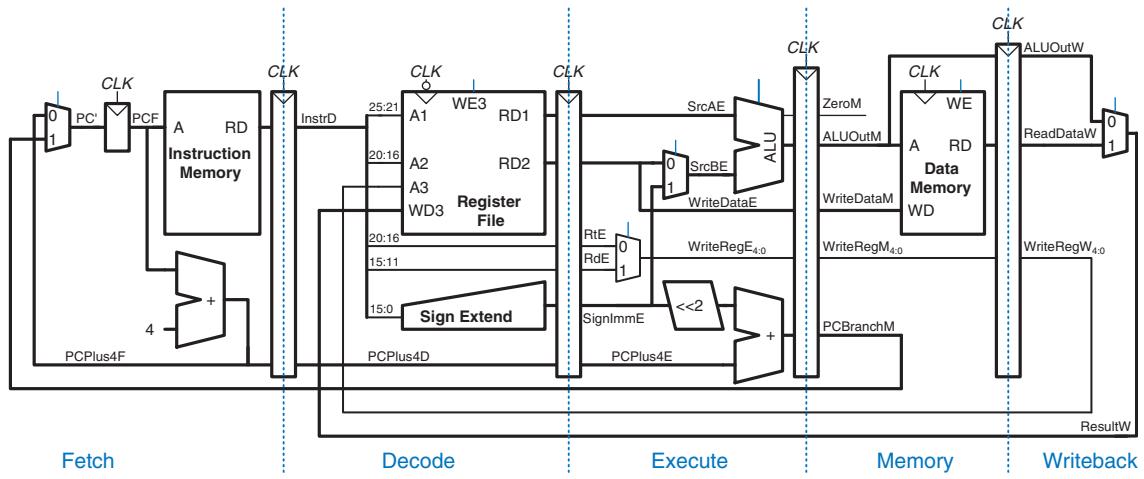


Figure 7.46 Corrected pipelined datapath

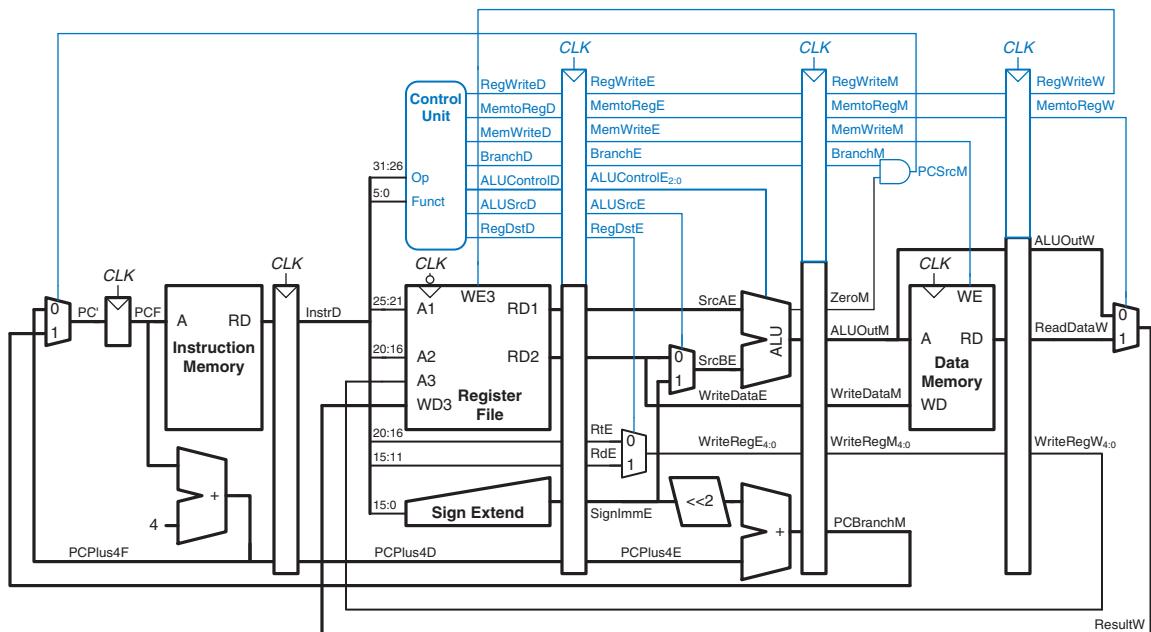
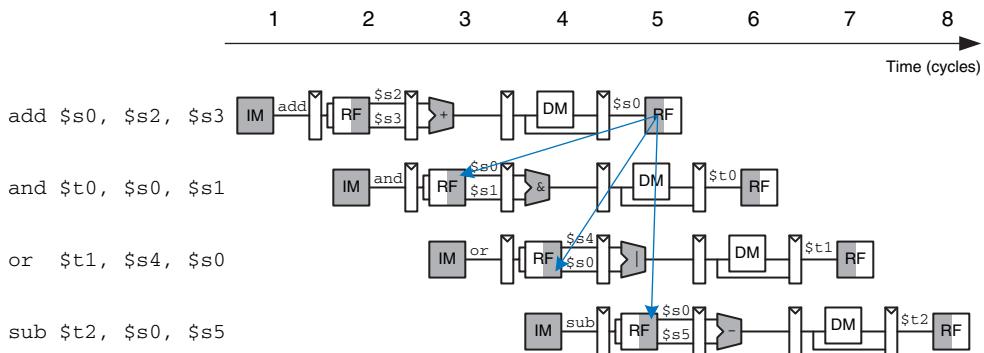


Figure 7.47 Pipelined processor with control

### 7.5.3 Hazards

In a pipelined system, multiple instructions are handled concurrently. When one instruction is *dependent* on the results of another that has not yet completed, a *hazard* occurs.



**Figure 7.48** Abstract pipeline diagram illustrating hazards

The register file can be read and written in the same cycle. The write takes place during the first half of the cycle and the read takes place during the second half of the cycle, so a register can be written and read back in the same cycle without introducing a hazard.

Figure 7.48 illustrates hazards that occur when one instruction writes a register ( $\$s0$ ) and subsequent instructions read this register. This is called a *read after write (RAW)* hazard. The add instruction writes a result into  $\$s0$  in the first half of cycle 5. However, the and instruction reads  $\$s0$  on cycle 3, obtaining the wrong value. The or instruction reads  $\$s0$  on cycle 4, again obtaining the wrong value. The sub instruction reads  $\$s0$  in the second half of cycle 5, obtaining the correct value, which was written in the first half of cycle 5. Subsequent instructions also read the correct value of  $\$s0$ . The diagram shows that hazards may occur in this pipeline when an instruction writes a register and either of the two subsequent instructions read that register. Without special treatment, the pipeline will compute the wrong result.

On closer inspection, however, observe that the sum from the add instruction is computed by the ALU in cycle 3 and is not strictly needed by the and instruction until the ALU uses it in cycle 4. In principle, we should be able to forward the result from one instruction to the next to resolve the RAW hazard without slowing down the pipeline. In other situations explored later in this section, we may have to stall the pipeline to give time for a result to be produced before the subsequent instruction uses the result. In any event, something must be done to solve hazards so that the program executes correctly despite the pipelining.

Hazards are classified as data hazards or control hazards. A *data hazard* occurs when an instruction tries to read a register that has not yet been written back by a previous instruction. A *control hazard* occurs when the decision of what instruction to fetch next has not been made by the time the fetch takes place. In the remainder of this section, we will

enhance the pipelined processor with a hazard unit that detects hazards and handles them appropriately, so that the processor executes the program correctly.

### Solving Data Hazards with Forwarding

Some data hazards can be solved by *forwarding* (also called *bypassing*) a result from the Memory or Writeback stage to a dependent instruction in the Execute stage. This requires adding multiplexers in front of the ALU to select the operand from either the register file or the Memory or Writeback stage. Figure 7.49 illustrates this principle. In cycle 4, \$s0 is forwarded from the Memory stage of the add instruction to the Execute stage of the dependent and instruction. In cycle 5, \$s0 is forwarded from the Writeback stage of the add instruction to the Execute stage of the dependent or instruction.

Forwarding is necessary when an instruction in the Execute stage has a source register matching the destination register of an instruction in the Memory or Writeback stage. Figure 7.50 modifies the pipelined processor to support forwarding. It adds a *hazard detection unit* and two forwarding multiplexers. The hazard detection unit receives the two source registers from the instruction in the Execute stage and the destination registers from the instructions in the Memory and Writeback stages. It also receives the *RegWrite* signals from the Memory and Writeback stages to know whether the destination register will actually be written (for example, the sw and beq instructions do not write results to the register file and hence do not need to have their results forwarded). Note that the *RegWrite* signals are *connected by name*. In other words, rather than cluttering up the diagram with long wires running from the control signals at the top to the hazard unit at the bottom, the connections are indicated by a short stub of wire labeled with the control signal name to which it is connected.

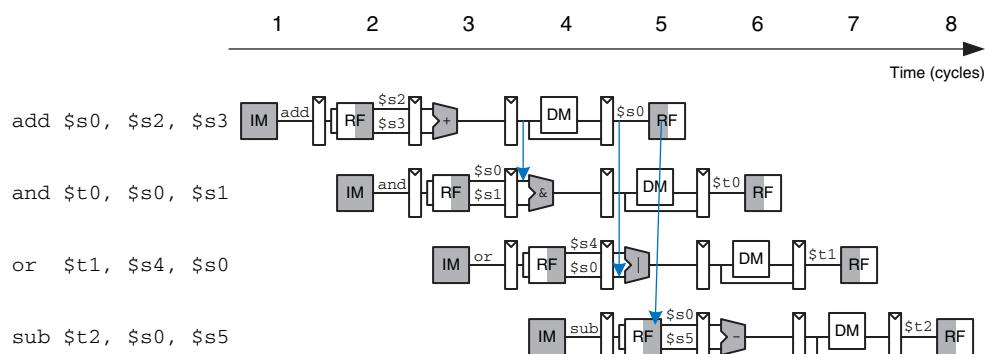


Figure 7.49 Abstract pipeline diagram illustrating forwarding

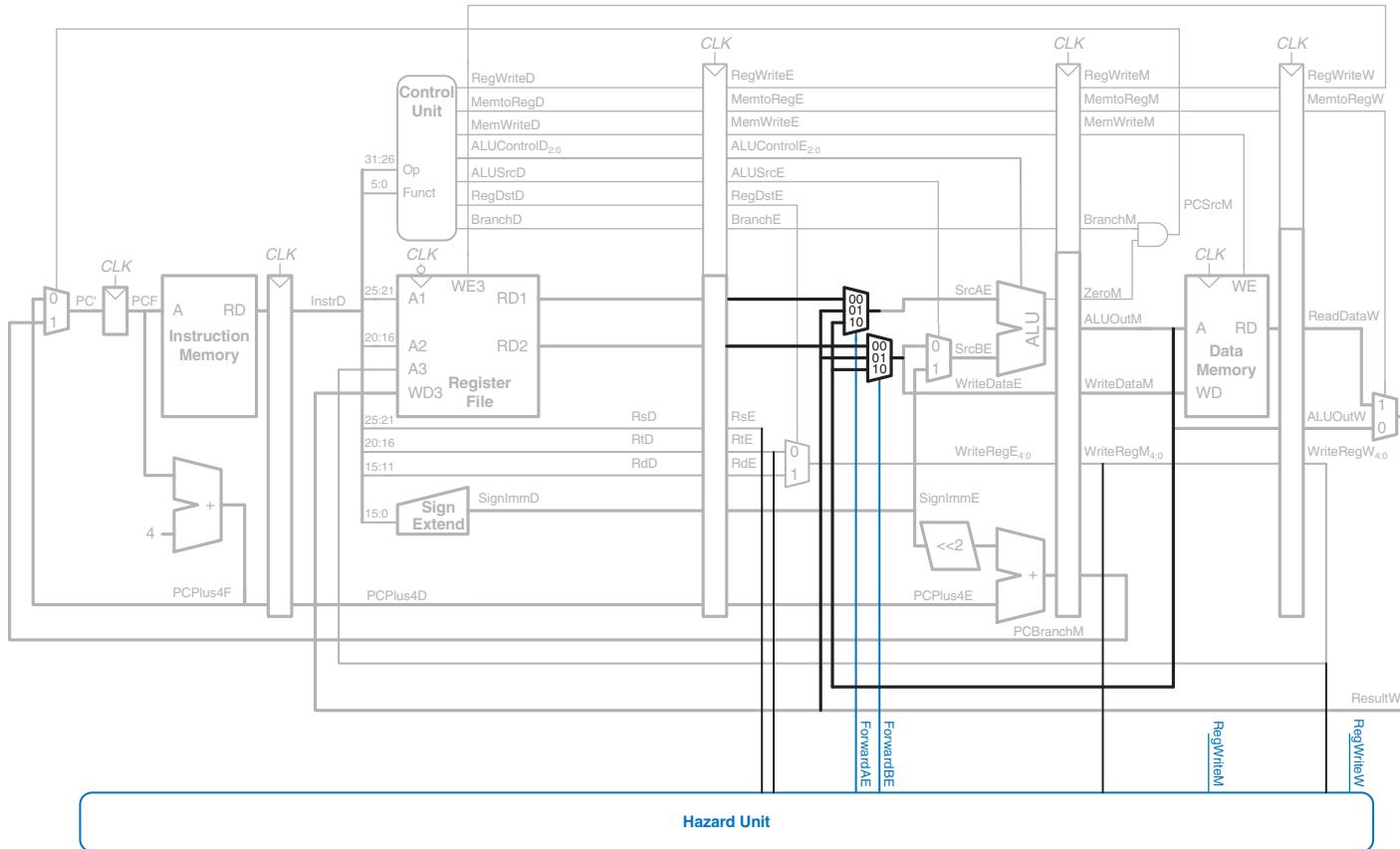


Figure 7.50 Pipelined processor with forwarding to solve hazards

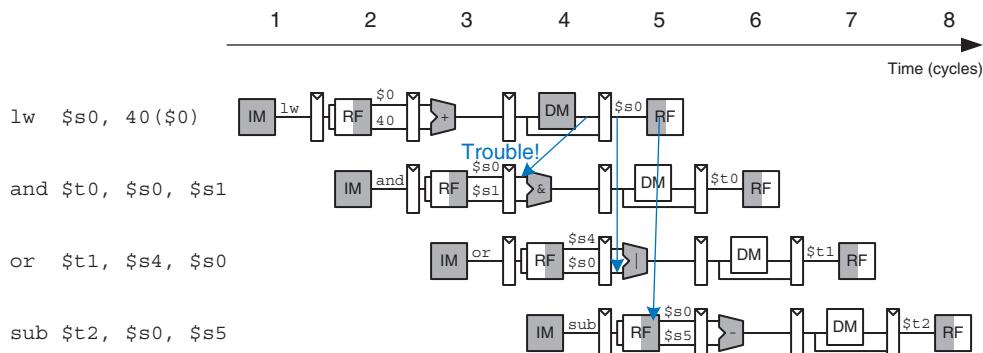
The hazard detection unit computes control signals for the forwarding multiplexers to choose operands from the register file or from the results in the Memory or Writeback stage. It should forward from a stage if that stage will write a destination register and the destination register matches the source register. However, \$0 is hardwired to 0 and should never be forwarded. If both the Memory and Writeback stages contain matching destination registers, the Memory stage should have priority, because it contains the more recently executed instruction. In summary, the function of the forwarding logic for *SrcA* is given below. The forwarding logic for *SrcB* (*ForwardBE*) is identical except that it checks *rt* rather than *rs*.

```

if      ((rsE != 0) AND (rsE == WriteRegM) AND RegWriteM) then
        ForwardAE = 10
else if ((rsE != 0) AND (rsE == WriteRegW) AND RegWriteW) then
        ForwardAE = 01
else
        ForwardAE = 00
    
```

### Solving Data Hazards with Stalls

Forwarding is sufficient to solve RAW data hazards when the result is computed in the Execute stage of an instruction, because its result can then be forwarded to the Execute stage of the next instruction. Unfortunately, the *lw* instruction does not finish reading data until the end of the Memory stage, so its result cannot be forwarded to the Execute stage of the next instruction. We say that the *lw* instruction has a *two-cycle latency*, because a dependent instruction cannot use its result until two cycles later. Figure 7.51 shows this problem. The *lw* instruction receives data from memory at the end of cycle 4. But the *and* instruction needs that data as a source operand at the beginning of cycle 4. There is no way to solve this hazard with forwarding.



**Figure 7.51** Abstract pipeline diagram illustrating trouble forwarding from *lw*

The alternative solution is to *stall* the pipeline, holding up operation until the data is available. Figure 7.52 shows stalling the dependent instruction (*and*) in the Decode stage, and enters the Decode stage in cycle 3 and stalls there through cycle 4. The subsequent instruction (*or*) must remain in the Fetch stage during both cycles as well, because the Decode stage is full.

In cycle 5, the result can be forwarded from the Writeback stage of *lw* to the Execute stage of *and*. In cycle 5, source \$s0 of the *or* instruction is read directly from the register file, with no need for forwarding.

Notice that the Execute stage is unused in cycle 4. Likewise, Memory is unused in Cycle 5 and Writeback is unused in cycle 6. This unused stage propagating through the pipeline is called a *bubble*, and it behaves like a *nop* instruction. The bubble is introduced by zeroing out the Execute stage control signals during a Decode stall so that the bubble performs no action and changes no architectural state.

In summary, stalling a stage is performed by disabling the pipeline register, so that the contents do not change. When a stage is stalled, all previous stages must also be stalled, so that no subsequent instructions are lost. The pipeline register directly after the stalled stage must be cleared to prevent bogus information from propagating forward. Stalls degrade performance, so they should only be used when necessary.

Figure 7.53 modifies the pipelined processor to add stalls for *lw* data dependencies. The hazard unit examines the instruction in the Execute stage. If it is *lw* and its destination register (*rtE*) matches either source operand of the instruction in the Decode stage (*rsD* or *rtD*), that instruction must be stalled in the Decode stage until the source operand is ready.

Stalls are supported by adding enable inputs (*EN*) to the Fetch and Decode pipeline registers and a synchronous reset/clear (*CLR*) input to the Execute pipeline register. When a *lw* stall occurs, *StallD* and *StallF*

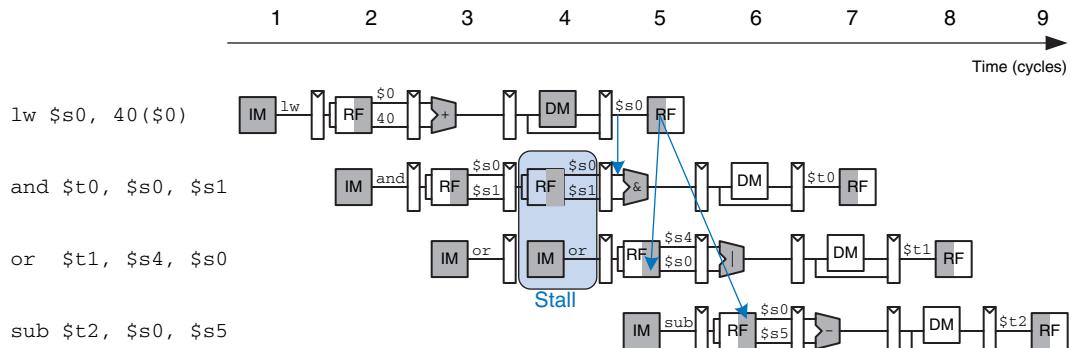


Figure 7.52 Abstract pipeline diagram illustrating stall to solve hazards

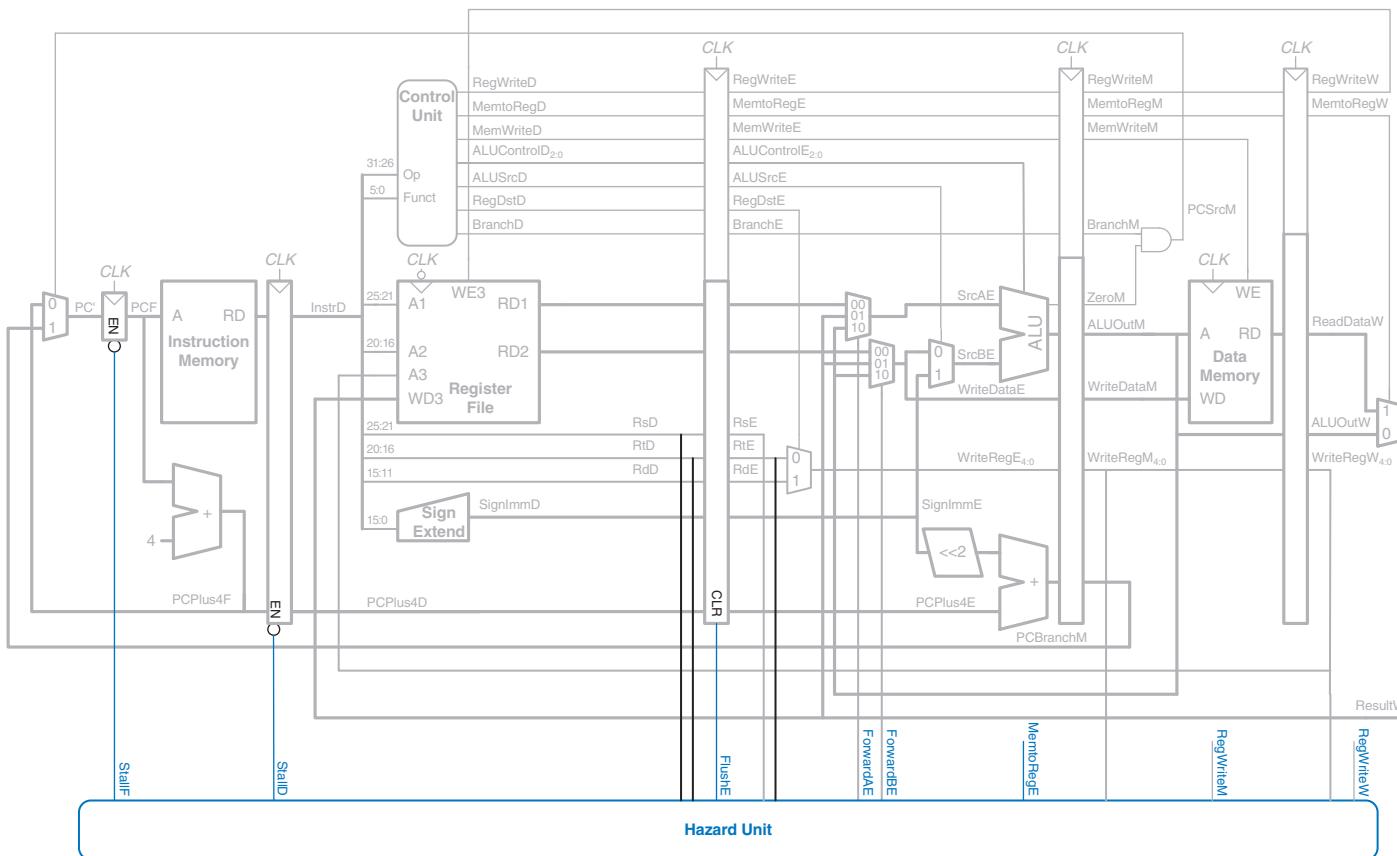


Figure 7.53 Pipelined processor with stalls to solve 1w data hazard

are asserted to force the Decode and Fetch stage pipeline registers to hold their old values. *FlushE* is also asserted to clear the contents of the Execute stage pipeline register, introducing a bubble.<sup>4</sup>

The *MemtoReg* signal is asserted for the *lw* instruction. Hence, the logic to compute the stalls and flushes is

```
lwstall = ((rsD == rtE) OR (rdD == rtE)) AND MemtoRegE  
StallF = StallD = FlushE = lwstall
```

### Solving Control Hazards

The *beq* instruction presents a control hazard: the pipelined processor does not know what instruction to fetch next, because the branch decision has not been made by the time the next instruction is fetched.

One mechanism for dealing with the control hazard is to stall the pipeline until the branch decision is made (i.e., *PCSrc* is computed). Because the decision is made in the Memory stage, the pipeline would have to be stalled for three cycles at every branch. This would severely degrade the system performance.

An alternative is to predict whether the branch will be taken and begin executing instructions based on the prediction. Once the branch decision is available, the processor can throw out the instructions if the prediction was wrong. In particular, suppose that we predict that branches are not taken and simply continue executing the program in order. If the branch should have been taken, the three instructions following the branch must be *flushed* (discarded) by clearing the pipeline registers for those instructions. These wasted instruction cycles are called the *branch misprediction penalty*.

Figure 7.54 shows such a scheme, in which a branch from address 20 to address 64 is taken. The branch decision is not made until cycle 4, by which point the *and*, *or*, and *sub* instructions at addresses 24, 28, and 2C have already been fetched. These instructions must be flushed, and the *slt* instruction is fetched from address 64 in cycle 5. This is somewhat of an improvement, but flushing so many instructions when the branch is taken still degrades performance.

We could reduce the branch misprediction penalty if the branch decision could be made earlier. Making the decision simply requires comparing the values of two registers. Using a dedicated equality comparator is much faster than performing a subtraction and zero detection. If the comparator is fast enough, it could be moved back into the Decode stage, so that the operands are read from the register file and compared to determine the next PC by the end of the Decode stage.

---

<sup>4</sup> Strictly speaking, only the register designations (*RsE*, *RtE*, and *RdE*) and the control signals that might update memory or architectural state (*RegWrite*, *MemWrite*, and *Branch*) need to be cleared; as long as these signals are cleared, the bubble can contain random data that has no effect.

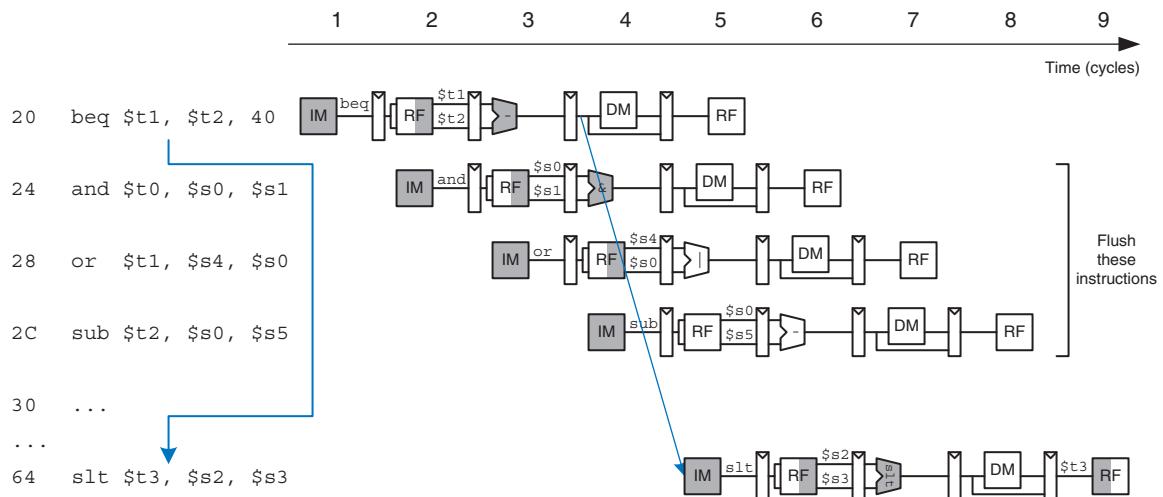


Figure 7.54 Abstract pipeline diagram illustrating flushing when a branch is taken

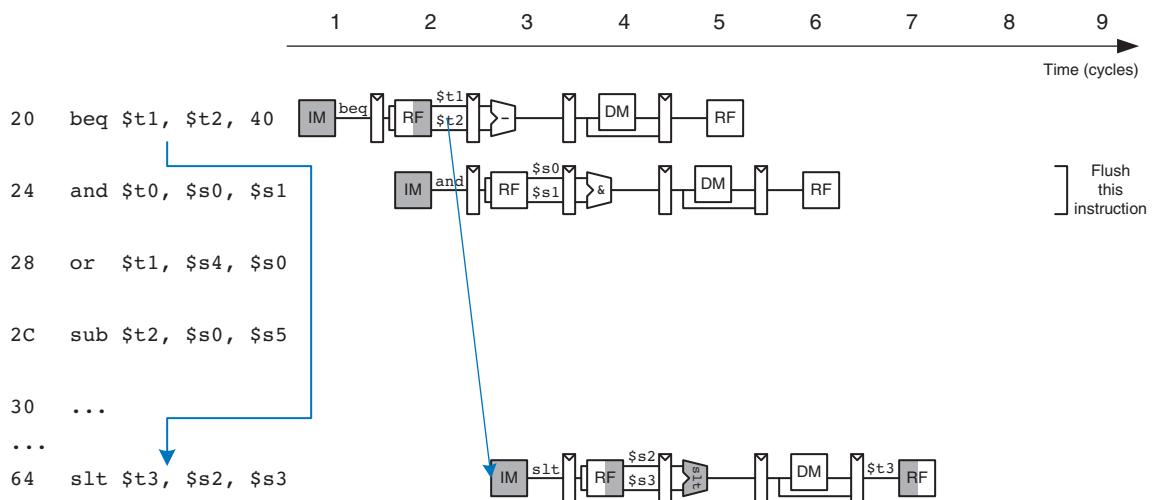


Figure 7.55 Abstract pipeline diagram illustrating earlier branch decision

Figure 7.55 shows the pipeline operation with the early branch decision being made in cycle 2. In cycle 3, the and instruction is flushed and the slt instruction is fetched. Now the branch misprediction penalty is reduced to only one instruction rather than three.

Figure 7.56 modifies the pipelined processor to move the branch decision earlier and handle control hazards. An equality comparator is added to the Decode stage and the *PCSrc* AND gate is moved earlier,

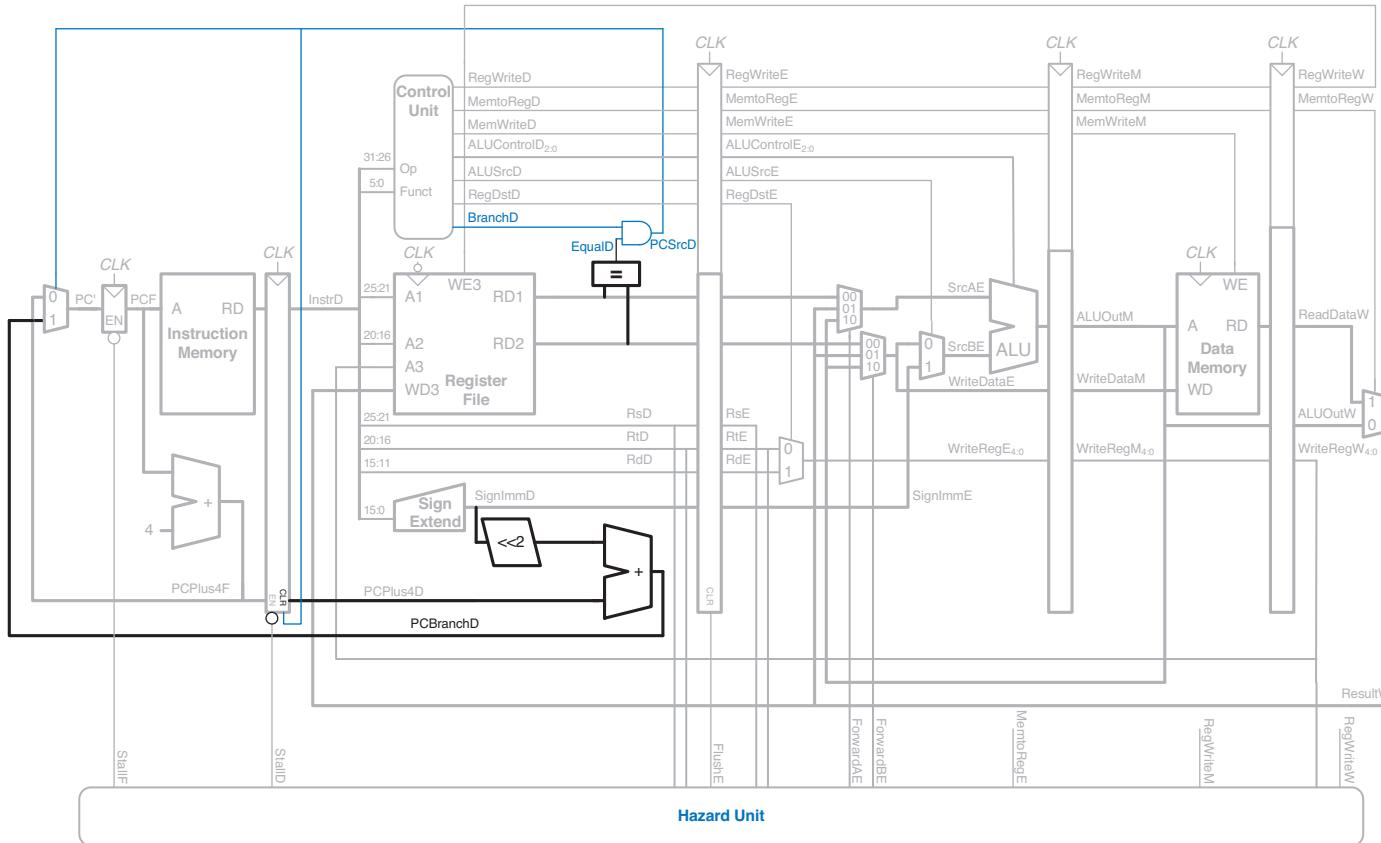


Figure 7.56 Pipelined processor handling branch control hazard

so that  $PCSrc$  can be determined in the Decode stage rather than the Memory stage. The  $PCBranch$  adder must also be moved into the Decode stage so that the destination address can be computed in time. The synchronous clear input ( $CLR$ ) connected to  $PCSrcD$  is added to the Decode stage pipeline register so that the incorrectly fetched instruction can be flushed when a branch is taken.

Unfortunately, the early branch decision hardware introduces a new RAW data hazard. Specifically, if one of the source operands for the branch was computed by a previous instruction and has not yet been written into the register file, the branch will read the wrong operand value from the register file. As before, we can solve the data hazard by forwarding the correct value if it is available or by stalling the pipeline until the data is ready.

[Figure 7.57](#) shows the modifications to the pipelined processor needed to handle the Decode stage data dependency. If a result is in the Writeback stage, it will be written in the first half of the cycle and read during the second half, so no hazard exists. If the result of an ALU instruction is in the Memory stage, it can be forwarded to the equality comparator through two new multiplexers. If the result of an ALU instruction is in the Execute stage or the result of a  $lw$  instruction is in the Memory stage, the pipeline must be stalled at the Decode stage until the result is ready.

The function of the Decode stage forwarding logic is given below.

$$\begin{aligned} \text{ForwardAD} &= (\text{rsD} \neq 0) \text{ AND } (\text{rsD} == \text{WriteRegM}) \text{ AND } \text{RegWriteM} \\ \text{ForwardBD} &= (\text{rtD} \neq 0) \text{ AND } (\text{rtD} == \text{WriteRegM}) \text{ AND } \text{RegWriteM} \end{aligned}$$

The function of the stall detection logic for a branch is given below. The processor must make a branch decision in the Decode stage. If either of the sources of the branch depends on an ALU instruction in the Execute stage or on a  $lw$  instruction in the Memory stage, the processor must stall until the sources are ready.

$$\begin{aligned} \text{branchstall} = & \\ & \text{BranchD AND RegWriteE AND } (\text{WriteRegE} == \text{rsD OR WriteRegE} == \text{rtD}) \\ & \quad \text{OR} \\ & \text{BranchD AND MemtoRegM AND } (\text{WriteRegM} == \text{rsD OR WriteRegM} == \text{rtD}) \end{aligned}$$

Now the processor might stall due to either a load or a branch hazard:

$$\text{StallF} = \text{StallD} = \text{FlushE} = \text{lwstall OR branchstall}$$

### Hazard Summary

In summary, RAW data hazards occur when an instruction depends on the result of another instruction that has not yet been written into the register file. The data hazards can be resolved by forwarding if the result is computed soon enough; otherwise, they require stalling the pipeline until the result is available. Control hazards occur when the decision of what instruction to fetch has not been made by the time the next instruction

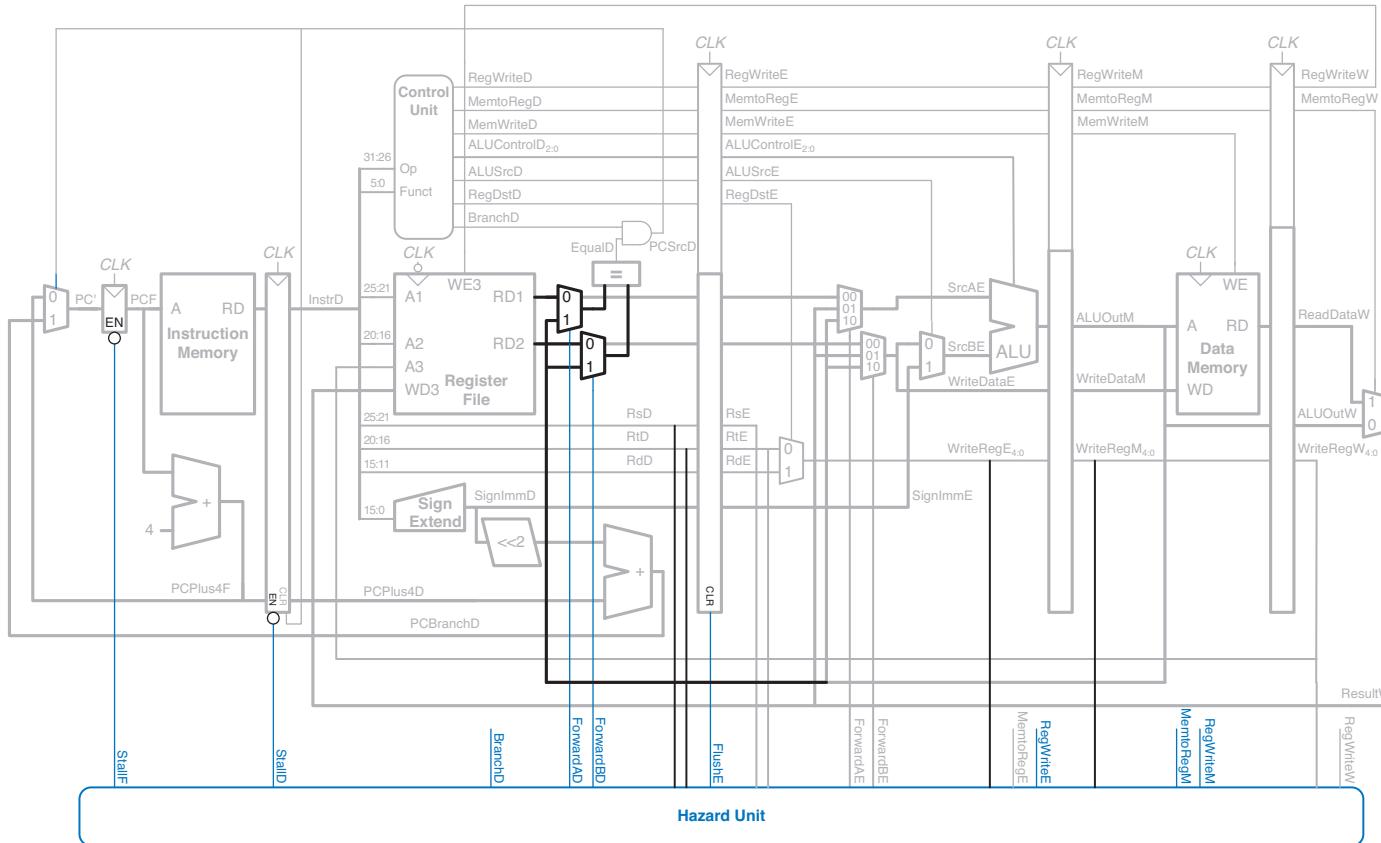


Figure 7.57 Pipelined processor handling data dependencies for branch instructions

must be fetched. Control hazards are solved by predicting which instruction should be fetched and flushing the pipeline if the prediction is later determined to be wrong. Moving the decision as early as possible minimizes the number of instructions that are flushed on a misprediction. You may have observed by now that one of the challenges of designing a pipelined processor is to understand all the possible interactions between instructions and to discover all the hazards that may exist. Figure 7.58 shows the complete pipelined processor handling all of the hazards.

#### 7.5.4 More Instructions

Supporting new instructions in the pipelined processor is much like supporting them in the single-cycle processor. However, new instructions may introduce hazards that must be detected and solved.

In particular, supporting addi and j instructions in the pipelined processor requires enhancing the controller, exactly as was described in Section 7.3.3, and adding a jump multiplexer to the datapath after the branch multiplexer. Like a branch, the jump takes place in the Decode stage, so the subsequent instruction in the Fetch stage must be flushed. Designing this flush logic is left as Exercise 7.35.

#### 7.5.5 Performance Analysis

The pipelined processor ideally would have a CPI of 1, because a new instruction is issued every cycle. However, a stall or a flush wastes a cycle, so the CPI is slightly higher and depends on the specific program being executed.

---

##### Example 7.9 PIPELINED PROCESSOR CPI

The SPECINT2000 benchmark considered in Example 7.7 consists of approximately 25% loads, 10% stores, 11% branches, 2% jumps, and 52% R-type instructions. Assume that 40% of the loads are immediately followed by an instruction that uses the result, requiring a stall, and that one quarter of the branches are mispredicted, requiring a flush. Assume that jumps always flush the subsequent instruction. Ignore other hazards. Compute the average CPI of the pipelined processor.

**Solution:** The average CPI is the sum over each instruction of the CPI for that instruction multiplied by the fraction of time that instruction is used. Loads take one clock cycle when there is no dependency and two cycles when the processor must stall for a dependency, so they have a CPI of  $(0.6)(1) + (0.4)(2) = 1.4$ . Branches take one clock cycle when they are predicted properly and two when they are not, so they have a CPI of  $(0.75)(1) + (0.25)(2) = 1.25$ . Jumps always have a CPI of 2. All other instructions have a CPI of 1. Hence, for this benchmark, Average CPI =  $(0.25)(1.4) + (0.1)(1) + (0.11)(1.25) + (0.02)(2) + (0.52)(1) = 1.15$ .

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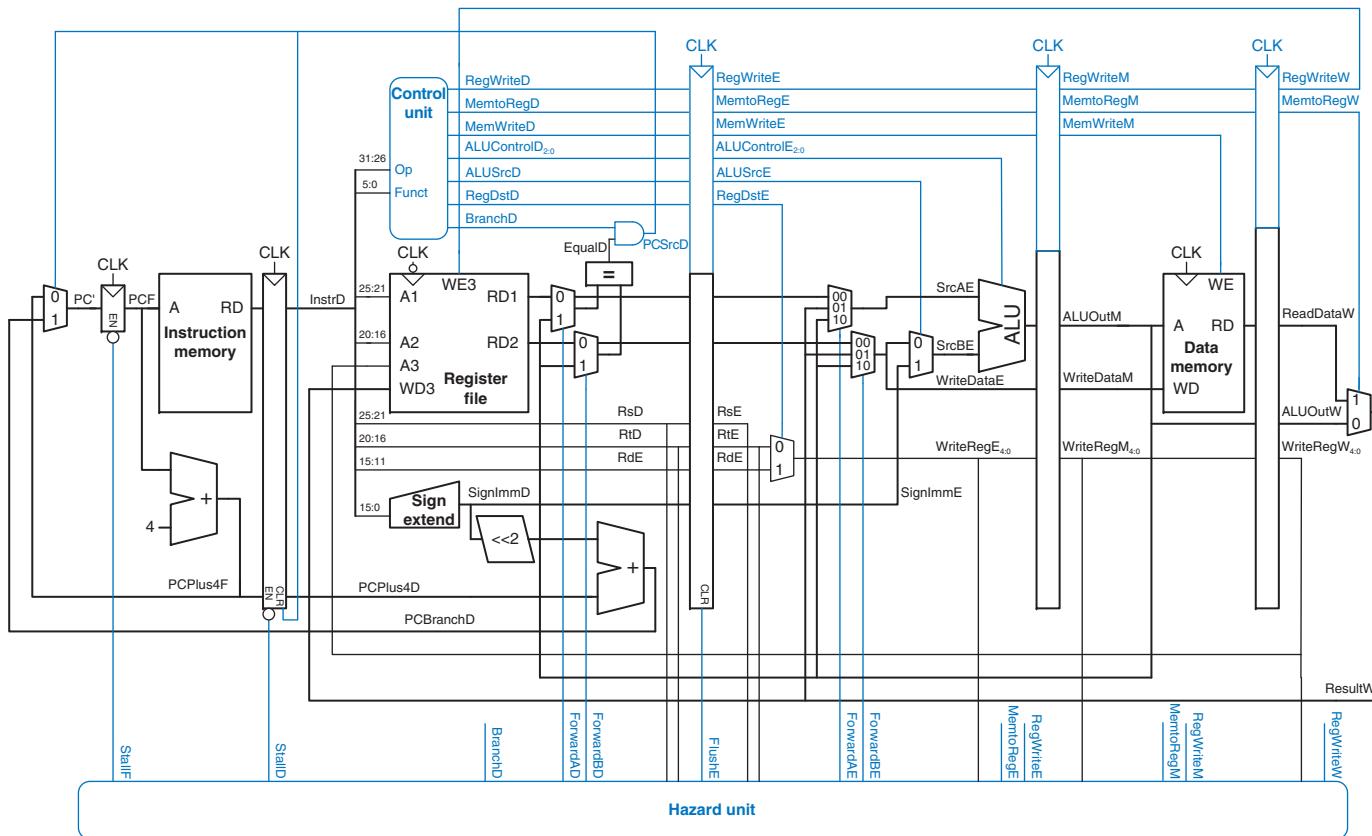


Figure 7.58 Pipelined processor with full hazard handling

We can determine the cycle time by considering the critical path in each of the five pipeline stages shown in Figure 7.58. Recall that the register file is written in the first half of the Writeback cycle and read in the second half of the Decode cycle. Therefore, the cycle time of the Decode and Writeback stages is twice the time necessary to do the half-cycle of work.

$$T_c = \max \left( \begin{array}{l} t_{pcq} + t_{mem} + t_{setup} \\ 2(t_{RFread} + t_{mux} + t_{eq} + t_{AND} + T_{mux} + t_{setup}) \\ t_{pcq} + t_{mux} + t_{mux} + t_{ALU} + t_{setup} \\ t_{pcq} + t_{memwrite} + t_{setup} \\ 2(t_{pcq} + t_{mux} + t_{RFwrite}) \end{array} \right) \quad \begin{array}{l} \text{Fetch} \\ \text{Decode} \\ \text{Execute} \\ \text{Memory} \\ \text{Writeback} \end{array} \quad (7.5)$$

### Example 7.10 PROCESSOR PERFORMANCE COMPARISON

Ben Bitdiddle needs to compare the pipelined processor performance to that of the single-cycle and multicycle processors considered in Example 7.8. Most of the logic delays were given in Table 7.6. The other element delays are 40 ps for an equality comparator, 15 ps for an AND gate, 100 ps for a register file write, and 220 ps for a memory write. Help Ben compare the execution time of 100 billion instructions from the SPECINT2000 benchmark for each processor.

**Solution:** According to Equation 7.5, the cycle time of the pipelined processor is  $T_{c3} = \max[30 + 250 + 20, 2(150 + 25 + 40 + 15 + 25 + 20), 30 + 25 + 25 + 200 + 20, 30 + 220 + 20, 2(30 + 25 + 100)] = 550$  ps. According to Equation 7.1, the total execution time is  $T_3 = (100 \times 10^9 \text{ instructions})(1.15 \text{ cycles/instruction})(550 \times 10^{-12} \text{ s/cycle}) = 63.3$  seconds. This compares to 92.5 seconds for the single-cycle processor and 133.9 seconds for the multicycle processor.

The pipelined processor is substantially faster than the others. However, its advantage over the single-cycle processor is nowhere near the fivefold speedup one might hope to get from a five-stage pipeline. The pipeline hazards introduce a small CPI penalty. More significantly, the sequencing overhead (clk-to-Q and setup times) of the registers applies to every pipeline stage, not just once to the overall datapath. Sequencing overhead limits the benefits one can hope to achieve from pipelining.

The careful reader might observe that the Decode stage is substantially slower than the others, because the register file read and branch comparison must both happen in half a cycle. Perhaps moving the branch comparison to the Decode stage was not such a good idea. If branches were resolved in the Execute stage instead, the CPI would increase slightly, because a mispredict would flush two instructions, but the cycle time would decrease substantially, giving an overall speedup.

The pipelined processor is similar in hardware requirements to the single-cycle processor, but it adds a substantial number of pipeline registers, along with multiplexers and control logic to resolve hazards.

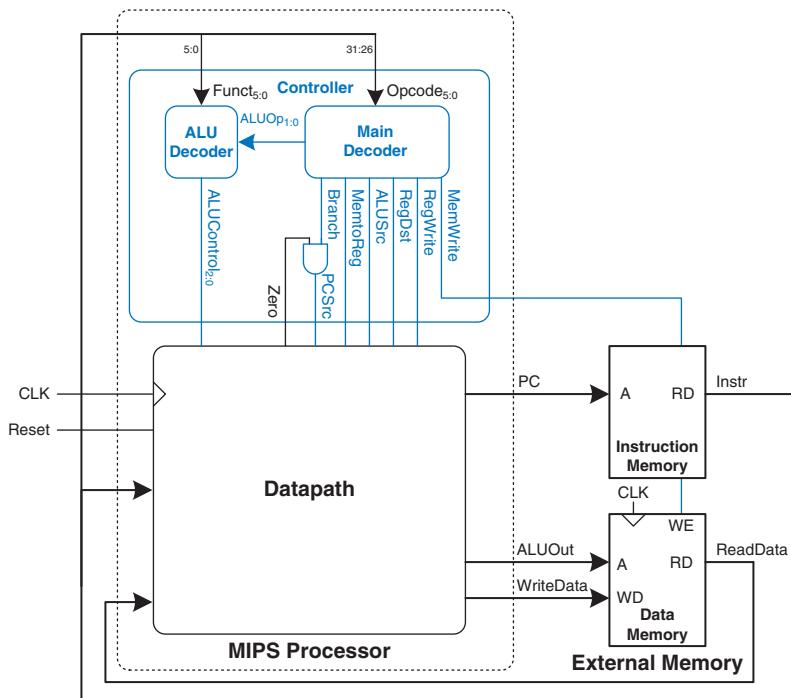
## 7.6 HDL REPRESENTATION\*

This section presents HDL code for the single-cycle MIPS processor supporting all of the instructions discussed in this chapter, including addi and j. The code illustrates good coding practices for a moderately complex system. HDL code for the multicycle processor and pipelined processor are left to [Exercises 7.25 and 7.40](#).

In this section, the instruction and data memories are separated from the main processor and connected by address and data busses. This is more realistic, because most real processors have external memory. It also illustrates how the processor can communicate with the outside world.

The processor is composed of a datapath and a controller. The controller, in turn, is composed of the main decoder and the ALU decoder. [Figure 7.59](#) shows a block diagram of the single-cycle MIPS processor interfaced to external memories.

The HDL code is partitioned into several sections. [Section 7.6.1](#) provides HDL for the single-cycle processor datapath and controller. [Section 7.6.2](#) presents the generic building blocks, such as registers and multiplexers, that are used by any microarchitecture. [Section 7.6.3](#) introduces the



**Figure 7.59** MIPS single-cycle processor interfaced to external memory

testbench and external memories. The HDL is available in electronic form on this book's website (see the preface).

### 7.6.1 Single-Cycle Processor

The main modules of the single-cycle MIPS processor module are given in the following HDL examples.

#### HDL Example 7.1 SINGLE-CYCLE MIPS PROCESSOR

##### SystemVerilog

```
module mips(input logic      clk, reset,
            output logic [31:0] pc,
            input logic [31:0] instr,
            output logic      memwrite,
            output logic [31:0] aluout, writedata,
            input logic [31:0] readdata);

    logic      memtoreg, alusrc, regdst,
               regwrite, jump, psrc, zero;
    logic [2:0] alucontrol;

    controller c(instr[31:26], instr[5:0], zero,
                  memtoreg, memwrite, psrc,
                  alusrc, regdst, regwrite, jump,
                  alucontrol);
    datapath dp(clk, reset, memtoreg, psrc,
                alusrc, regdst, regwrite, jump,
                alucontrol,
                zero, pc, instr,
                aluout, writedata, readdata);
endmodule
```

##### VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity mips is -- single cycle MIPS processor
    port(clk, reset:      in STD_LOGIC;
          pc:           out STD_LOGIC_VECTOR(31 downto 0);
          instr:        in STD_LOGIC_VECTOR(31 downto 0);
          memwrite:     out STD_LOGIC;
          aluout, writedata: out STD_LOGIC_VECTOR(31 downto 0);
          readdata:     in STD_LOGIC_VECTOR(31 downto 0));
end;

architecture struct of mips is
    component controller
        port(op, funct:      in STD_LOGIC_VECTOR(5 downto 0);
              zero:         in STD_LOGIC;
              memtoreg, memwrite: out STD_LOGIC;
              psrc, alusrc:   out STD_LOGIC;
              regdst, regwrite: out STD_LOGIC;
              jump:          out STD_LOGIC;
              alucontrol:    out STD_LOGIC_VECTOR(2 downto 0));
    end component;
    component datapath
        port(clk, reset:      in STD_LOGIC;
              memtoreg, psrc: in STD_LOGIC;
              alusrc, regdst: in STD_LOGIC;
              regwrite, jump: in STD_LOGIC;
              alucontrol:    in STD_LOGIC_VECTOR(2 downto 0);
              zero:          out STD_LOGIC;
              pc:            buffer STD_LOGIC_VECTOR(31 downto 0);
              instr:          in STD_LOGIC_VECTOR(31 downto 0);
              aluout, writedata: buffer STD_LOGIC_VECTOR(31 downto 0);
              readdata:       in STD_LOGIC_VECTOR(31 downto 0));
    end component;
    signal memtoreg, alusrc, regdst, regwrite, jump, psrc: STD_LOGIC;
    signal zero: STD_LOGIC;
    signal alucontrol: STD_LOGIC_VECTOR(2 downto 0);
begin
    begin
        cont: controller port map(instr(31 downto 26),
                                  instr(5 downto 0), zero, memtoreg,
                                  memwrite, psrc, alusrc, regdst,
                                  regwrite, jump, alucontrol);
        dp: datapath port map(clk, reset, memtoreg, psrc, alusrc,
                              regdst, regwrite, jump, alucontrol,
                              zero, pc, instr, aluout, writedata,
                              readdata);
    end;
```

---

**HDL Example 7.2 CONTROLLER**
**SystemVerilog**

```
module controller(input logic [5:0] op, funct,
                  input logic      zero,
                  output logic     memtoreg, memwrite,
                  output logic     pcsrc, alusrc,
                  output logic     regdst, regwrite,
                  output logic     jump,
                  output logic [2:0] alucontrol);

  logic [1:0] aluop;
  logic       branch;

  maindec md(op, memtoreg, memwrite, branch,
             alusrc, regdst, regwrite, jump, aluop);
  aludec ad(funct, aluop, alucontrol);

  assign pcsr=branch & zero;
endmodule
```

**VHDL**

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity controller is -- single cycle control decoder
  port(op, funct:      in STD_LOGIC_VECTOR(5 downto 0);
        zero:          in STD_LOGIC;
        memtoreg, memwrite: out STD_LOGIC;
        pcsr, alusrc:   out STD_LOGIC;
        regdst, regwrite: out STD_LOGIC;
        jump:           out STD_LOGIC;
        alucontrol:    out STD_LOGIC_VECTOR(2 downto 0));
end;

architecture struct of controller is
  component maindec
    port(op:      in STD_LOGIC_VECTOR(5 downto 0);
          memtoreg, memwrite: out STD_LOGIC;
          branch, alusrc:   out STD_LOGIC;
          regdst, regwrite: out STD_LOGIC;
          jump:           out STD_LOGIC;
          aluop:          out STD_LOGIC_VECTOR(1 downto 0));
  end component;
  component aludec
    port(funct:      in STD_LOGIC_VECTOR(5 downto 0);
          aluop:       in STD_LOGIC_VECTOR(1 downto 0);
          alucontrol:  out STD_LOGIC_VECTOR(2 downto 0));
  end component;
  signal aluop: STD_LOGIC_VECTOR(1 downto 0);
  signal branch: STD_LOGIC;
begin
  md: maindec port map(op, memtoreg, memwrite, branch,
                        alusrc, regdst, regwrite, jump, aluop);
  ad: aludec port map(funct, aluop, alucontrol);

  pcsr <= branch and zero;
end;
```

---

## HDL Example 7.3 MAIN DECODER

### SystemVerilog

```
module maindec(input logic [5:0] op,
               output logic      memtoreg, memwrite,
               output logic      branch, alusrc,
               output logic      regdst, regwrite,
               output logic      jump,
               output logic [1:0] aluop);

  logic [8:0] controls;

  assign {regwrite, regdst, alusrc, branch, memwrite,
         memtoreg, jump, aluop} = controls;

  always_comb
    case(op)
      6'b000000: controls <= 9'b110000010; // RTYPE
      6'b100011: controls <= 9'b101001000; // LW
      6'b101011: controls <= 9'b001010000; // SW
      6'b000100: controls <= 9'b000100001; // BEQ
      6'b001000: controls <= 9'b101000000; // ADDI
      6'b000010: controls <= 9'b0000000100; // J
      default:   controls <= 9'bxxxxxxxxx; // illegal op
    endcase
endmodule
```

### VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity maindec is -- main control decoder
  port(op:           in STD_LOGIC_VECTOR(5 downto 0);
       memtoreg, memwrite: out STD_LOGIC;
       branch, alusrc:   out STD_LOGIC;
       regdst, regwrite: out STD_LOGIC;
       jump:             out STD_LOGIC;
       aluop:            out STD_LOGIC_VECTOR(1 downto 0));
end;

architecture behave of maindec is
  signal controls: STD_LOGIC_VECTOR(8 downto 0);
begin
  process(all) begin
    case op is
      when "000000" => controls <= "110000010"; -- RTYPE
      when "100011" => controls <= "101001000"; -- LW
      when "101011" => controls <= "001010000"; -- SW
      when "000100" => controls <= "000100001"; -- BEQ
      when "001000" => controls <= "101000000"; -- ADDI
      when "000010" => controls <= "000000100"; -- J
      when others => controls <= "-----"; -- illegal op
    end case;
  end process;

  (regwrite, regdst, alusrc, branch, memwrite,
   memtoreg, jump, aluop(1 downto 0)) <= controls;
end;
```

---

## HDL Example 7.4 ALU DECODER

### SystemVerilog

```
module aludec(input logic [5:0] funct,
               input logic [1:0] aluop,
               output logic [2:0] alucontrol);

  always_comb
    case(aluop)
      2'b00: alucontrol <= 3'b010; // add (for lw/sw/addi)
      2'b01: alucontrol <= 3'b110; // sub (for beq)
      default: case(funct)          // R-type instructions
        6'b100000: alucontrol <= 3'b010; // add
        6'b100010: alucontrol <= 3'b110; // sub
        6'b100100: alucontrol <= 3'b000; // and
        6'b100101: alucontrol <= 3'b001; // or
        6'b101010: alucontrol <= 3'b111; // slt
        default:   alucontrol <= 3'bxxx; // ???
    endcase
  endcase
endmodule
```

### VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity aludec is -- ALU control decoder
  port(funct:   in STD_LOGIC_VECTOR(5 downto 0);
       aluop:    in STD_LOGIC_VECTOR(1 downto 0);
       alucontrol: out STD_LOGIC_VECTOR(2 downto 0));
end;

architecture behave of aludec is
begin
  process(all) begin
    case aluop is
      when "00" => alucontrol <= "010"; -- add (for lw/sw/addi)
      when "01" => alucontrol <= "110"; -- sub (for beq)
      when others => case funct is          -- R-type instructions
                      when "100000" => alucontrol <= "010"; -- add
                      when "100010" => alucontrol <= "110"; -- sub
                      when "100100" => alucontrol <= "000"; -- and
                      when "100101" => alucontrol <= "001"; -- or
                      when "101010" => alucontrol <= "111"; -- slt
                      when others => alucontrol <= "---"; -- ???
        end case;
    end case;
  end process;
end;
```

---

**HDL Example 7.5 DATAPATH**
**SystemVerilog**

```

module datapath(input logic          clk, reset,
                 input logic          memtoreg, pcsrc,
                 input logic          alusrc, regdst,
                 input logic          regwrite, jump,
                 input logic [2:0]    alucontrol,
                 output logic         zero,
                 output logic [31:0]  pc,
                 input logic [31:0]  instr,
                 output logic [31:0]  aluout, writedata,
                 input logic [31:0]  readdata);

logic [4:0] writereg;
logic [31:0] pcnext, pcnextbr, pcplus4, pcbranch;
logic [31:0] signimm, signimmsh;
logic [31:0] srca, srcb;
logic [31:0] result;

// next PC logic
flopr #(32) pcreg(clk, reset, pcnext, pc);
adder      pcadd1(pc, 32'b100, pcplus4);
s12        immsh(signimm, signimmsh);
adder      pcadd2(pcplus4, signimmsh, pcbranch);
mux2 #(32) pcbrmux(pcplus4, pcbranch, pcsrc, pcnextbr);
mux2 #(32) pcmux(pcnextbr, {pcplus4[31:28],
                           instr[25:0], 2'b00}, jump, pcnext);

// register file logic
regfile   rf(clk, regwrite, instr[25:21], instr[20:16],
            writereg, result, srca, writedata);
mux2 #(5) wrmux(instr[20:16], instr[15:11],
                regdst, writereg);
mux2 #(32) resmux(aluout, readdata, memtoreg, result);
signext   se(instr[15:0], signimm);

// ALU logic
mux2 #(32) srcbmux(writedata, signimm, alusrc, srcb);
alu       alu(srca, srcb, alucontrol, aluout, zero);
endmodule

```

**VHDL**

```

library IEEE; use IEEE.STD_LOGIC_1164.all;
use IEEE.STD_LOGIC_ARITH.all;

entity datapath is -- MIPS datapath
  port(clk, reset:     in STD_LOGIC;
        memtoreg, pcsrc: in STD_LOGIC;
        alusrc, regdst: in STD_LOGIC;
        regwrite, jump:  in STD_LOGIC;
        alucontrol:     in STD_LOGIC_VECTOR(2 downto 0);
        zero:           out STD_LOGIC;
        pc:              buffer STD_LOGIC_VECTOR(31 downto 0);
        instr:           in STD_LOGIC_VECTOR(31 downto 0);
        aluout, writedata: buffer STD_LOGIC_VECTOR(31 downto 0);
        readdata:        in STD_LOGIC_VECTOR(31 downto 0));
end;

architecture struct of datapath is
  component alu
    port(a, b:      in STD_LOGIC_VECTOR(31 downto 0);
         alucontrol: in STD_LOGIC_VECTOR(2 downto 0);
         result:     buffer STD_LOGIC_VECTOR(31 downto 0);
         zero:       out STD_LOGIC);
  end component;
  component regfile
    port(clk:      in STD_LOGIC;
         we3:      in STD_LOGIC;
         ral, ra2, wa3: in STD_LOGIC_VECTOR(4 downto 0);
         wd3:      in STD_LOGIC_VECTOR(31 downto 0);
         rd1, rd2:  out STD_LOGIC_VECTOR(31 downto 0));
  end component;
  component adder
    port(a, b: in STD_LOGIC_VECTOR(31 downto 0);
         y:   out STD_LOGIC_VECTOR(31 downto 0));
  end component;
  component s12
    port(a: in STD_LOGIC_VECTOR(31 downto 0);
         y: out STD_LOGIC_VECTOR(31 downto 0));
  end component;
  component signext
    port(a: in STD_LOGIC_VECTOR(15 downto 0);
         y: out STD_LOGIC_VECTOR(31 downto 0));
  end component;
  component flop generic(width: integer);
    port(clk, reset: in STD_LOGIC;
         d:          in STD_LOGIC_VECTOR(width-1 downto 0);
         q:          out STD_LOGIC_VECTOR(width-1 downto 0));
  end component;
  component mux2 generic(width: integer);
    port(d0, d1: in STD_LOGIC_VECTOR(width-1 downto 0);
         s:      in STD_LOGIC;
         y:      out STD_LOGIC_VECTOR(width-1 downto 0));
  end component;
  signal writereg:      STD_LOGIC_VECTOR(4 downto 0);
  signal pcjump, pcnext,
        pcnextbr, pcplus4,
        pcbranch:      STD_LOGIC_VECTOR(31 downto 0);

```

```
signal signimm, signimmsh: STD_LOGIC_VECTOR(31 downto 0);
signal srca, srcb, result: STD_LOGIC_VECTOR(31 downto 0);
begin
    -- next PC logic
    pcjump <= pcplus4(31 downto 28) & instr(25 downto 0) & "00";
    pcreg: flop generic map(32) port map(clk, reset, pcnext, pc);
    pcadd1: adder port map(pc, X"00000004", pcplus4);
    immsh: s12 port map(signimm, signimmsh);
    pcadd2: adder port map(pcplus4, signimmsh, pcbranch);
    pcbrmux: mux2 generic map(32) port map(pcplus4, pcbranch,
                                             pcsrc, pcnextbr);
    pcmux: mux2 generic map(32) port map(pcnextbr, pcjump, jump,
                                             pcnext);
    -- register file logic
    rf: regfile port map(clk, regwrite, instr(25 downto 21),
                           instr(20 downto 16), writereg, result, srca,
                           writedata);
    wrmux: mux2 generic map(5) port map(instr(20 downto 16),
                                         instr(15 downto 11),
                                         regdst, writereg);
    resmux: mux2 generic map(32) port map(aluout, readdata,
                                         memtoreg, result);
    se: signext port map(instr(15 downto 0), signimm);
    -- ALU logic
    srcbmux: mux2 generic map(32) port map(writedata, signimm,
                                             alusrc, srcb);
    mainalu: alu port map(srca, srcb, alucontrol, aluout, zero);
end;
```

### 7.6.2 Generic Building Blocks

This section contains generic building blocks that may be useful in any MIPS microarchitecture, including a register file, adder, left shift unit, sign-extension unit, resettable flip-flop, and multiplexer. The HDL for the ALU is left to [Exercise 5.9](#).

---

**HDL Example 7.6 REGISTER FILE**
**SystemVerilog**

```
module regfile(input logic      clk,
               input logic      we3,
               input logic [4:0] ra1, ra2, wa3,
               input logic [31:0] wd3,
               output logic [31:0] rd1, rd2);

  logic [31:0] rf[31:0];

  // three ported register file
  // read two ports combinationaly
  // write third port on rising edge of clk
  // register 0 hardwired to 0
  // note: for pipelined processor, write third port
  // on falling edge of clk

  always_ff @(posedge clk)
    if (we3) rf[wa3] <= wd3;

  assign rd1=(ra1 != 0) ? rf[ra1] : 0;
  assign rd2=(ra2 != 0) ? rf[ra2] : 0;
endmodule
```

**VHDL**

```
library IEEE; use IEEE.STD_LOGIC_1164.all;
use IEEE.NUMERIC_STD_UNSIGNED.all;

entity regfile is -- three-port register file
  port(clk:      in STD_LOGIC;
        we3:      in STD_LOGIC;
        ra1, ra2, wa3: in STD_LOGIC_VECTOR(4 downto 0);
        wd3:      in STD_LOGIC_VECTOR(31 downto 0);
        rd1, rd2:  out STD_LOGIC_VECTOR(31 downto 0));
end;

architecture behave of regfile is
  type ramtype is array (31 downto 0) of STD_LOGIC_VECTOR(31
                                         downto 0);
  signal mem: ramtype;
begin
  -- three-ported register file
  -- read two ports combinationaly
  -- write third port on rising edge of clk
  -- register 0 hardwired to 0
  -- note: for pipelined processor, write third port
  -- on falling edge of clk
  process(clk) begin
    if rising_edge(clk) then
      if we3='1' then mem(to_integer(wa3)) <= wd3;
    end if;
  end if;
  end process;
  process(all) begin
    if (to_integer(ra1)=0) then rd1 <= X"00000000";
      -- register 0 holds 0
    else rd1 <= mem(to_integer(ra1));
    end if;
    if (to_integer(ra2)=0) then rd2 <= X"00000000";
    else rd2 <= mem(to_integer(ra2));
    end if;
  end process;
end;
```

---

**HDL Example 7.7 ADDER**
**SystemVerilog**

```
module adder(input logic [31:0] a, b,
              output logic [31:0] y);

  assign y=a+b;
endmodule
```

**VHDL**

```
library IEEE; use IEEE.STD_LOGIC_1164.all;
use IEEE.NUMERIC_STD_UNSIGNED.all;

entity adder is -- adder
  port(a, b: in STD_LOGIC_VECTOR(31 downto 0);
       y:   out STD_LOGIC_VECTOR(31 downto 0));
end;

architecture behave of adder is
begin
  y <= a+b;
end;
```

**HDL Example 7.8 LEFT SHIFT (MULTIPLY BY 4)****SystemVerilog**

```
module sl2(input logic [31:0] a,
            output logic [31:0] y);
    // shift left by 2
    assign y={a[29:0], 2'b00};
endmodule
```

**VHDL**

```
library IEEE; use IEEE.STD_LOGIC_1164.all;
entity sl2 is -- shift left by 2
    port(a: in STD_LOGIC_VECTOR(31 downto 0);
         y: out STD_LOGIC_VECTOR(31 downto 0));
end;

architecture behave of sl2 is
begin
    y <= a(29 downto 0) & "00";
end;
```

**HDL Example 7.9 SIGN EXTENSION****SystemVerilog**

```
module signext(input logic [15:0] a,
                output logic [31:0] y);
    assign y={(16{a[15]}), a};
endmodule
```

**VHDL**

```
library IEEE; use IEEE.STD_LOGIC_1164.all;
entity signext is -- sign extender
    port(a: in STD_LOGIC_VECTOR(15 downto 0);
         y: out STD_LOGIC_VECTOR(31 downto 0));
end;

architecture behave of signext is
begin
    y <= X"ffff" & a when a(15) else X"0000" & a;
end;
```

**HDL Example 7.10 RESETTABLE FLIP-FLOP****SystemVerilog**

```
module flopr #(parameter WIDTH=8)
    (input logic          clk, reset,
     input logic [WIDTH-1:0] d,
     output logic [WIDTH-1:0] q);

    always_ff @(posedge clk, posedge reset)
        if (reset) q <= 0;
        else       q <= d;
endmodule
```

**VHDL**

```
library IEEE; use IEEE.STD_LOGIC_1164.all;
use IEEE.STD_LOGIC_ARITH.all;
entity flopr is -- flip-flop with synchronous reset
    generic(width: integer);
    port(clk, reset: in STD_LOGIC;
          d:           in STD_LOGIC_VECTOR(width-1 downto 0);
          q:           out STD_LOGIC_VECTOR(width-1 downto 0));
end;

architecture asynchronous of flopr is
begin
    process(clk, reset) begin
        if reset then q <= (others => '0');
        elsif rising_edge(clk) then
            q <= d;
        end if;
    end process;
end;
```

---

**HDL Example 7.11 2:1 MULTIPLEXER**
**SystemVerilog**

```
module mux2 #(parameter WIDTH=8)
    (input logic [WIDTH-1:0] d0, d1,
     input logic          s,
     output logic [WIDTH-1:0] y);

    assign y = s ? d1 : d0;
endmodule
```

**VHDL**

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity mux2 is -- two-input multiplexer
    generic(width: integer := 8);
    port(d0, d1: in STD_LOGIC_VECTOR(width-1 downto 0);
         s:      in STD_LOGIC;
         y:      out STD_LOGIC_VECTOR(width-1 downto 0));
end;

architecture behave of mux2 is
begin
    y <= d1 when s else d0;
end;
```

### 7.6.3 Testbench

The MIPS testbench loads a program into the memories. The program in Figure 7.60 exercises all of the instructions by performing a computation that should produce the correct answer only if all of the instructions are functioning properly. Specifically, the program will write the value 7 to address 84 if it runs correctly, and is unlikely to do so if the hardware is buggy. This is an example of *ad hoc* testing.

```
# mipsest.asm
# David_Harris@hmc.edu, Sarah_Harris@hmc.edu 31 March 2012
#
# Test the MIPS processor.
# add, sub, and, or, slt, addi, lw, sw, beq, j
# If successful, it should write the value 7 to address 84
```

#	Assembly	Description	Address	Machine	
main:	addi \$2, \$0, 5	# initialize \$2 = 5	0	20020005	20020005
	addi \$3, \$0, 12	# initialize \$3 = 12	4	2003000c	2003000c
	addi \$7, \$3, -9	# initialize \$7 = 3	8	2067fff7	2067fff7
	or \$4, \$7, \$2	# \$4 = (3 OR 5) = 7	c	00e22025	00e22025
	and \$5, \$3, \$4	# \$5 = (12 AND 7) = 4	10	00642824	00642824
	add \$5, \$5, \$4	# \$5 = 4 + 7 = 11	14	00a42820	00a42820
	beq \$5, \$7, end	# shouldn't be taken	18	10a7000a	10a7000a
	slt \$4, \$3, \$4	# \$4 = 12 < 7 = 0	1c	0064202a	0064202a
	beq \$4, \$0, around	# should be taken	20	10800001	10800001
	addi \$5, \$0, 0	# shouldn't happen	24	20050000	20050000
around:	slt \$4, \$7, \$2	# \$4 = 3 < 5 = 1	28	00e2202a	00e2202a
	add \$7, \$4, \$5	# \$7 = 1 + 11 = 12	2c	00853820	00853820
	sub \$7, \$7, \$2	# \$7 = 12 - 5 = 7	30	00e23822	00e23822
	sw \$7, 68(\$3)	# [80] = 7	34	ac670044	ac670044
	lw \$2, 80(\$0)	# \$2 = [80] = 7	38	8c020050	8c020050
	j end	# should be taken	3c	08000011	08000011
	addi \$2, \$0, 1	# shouldn't happen	40	20020001	20020001
end:	sw \$2, 84(\$0)	# write mem[84] = 7	44	ac020054	ac020054

**Figure 7.60** Assembly and machine code for MIPS test program

**Figure 7.61** Contents of  
memfile.dat

The machine code is stored in a hexadecimal file called `memfile.dat` (see [Figure 7.61](#)), which is loaded by the testbench during simulation. The file consists of the machine code for the instructions, one instruction per line.

The testbench, top-level MIPS module, and external memory HDL code are given in the following examples. The memories in this example hold 64 words each.

### HDL Example 7.12 MIPS TESTBENCH

#### SystemVerilog

```
module testbench();
    logic clk;
    logic reset;

    logic [31:0] writedata, dataaddr;
    logic memwrite;

    // instantiate device to be tested
    top dut (clk, reset, writedata, dataaddr, memwrite);

    // initialize test
    initial
    begin
        reset <= 1; # 22; reset <= 0;
    end

    // generate clock to sequence tests
    always
    begin
        clk <= 1; # 5; clk <= 0; # 5;
    end

    // check results
    always @ (negedge clk)
    begin
        if (memwrite) begin
            if (dataaddr === 84 & writedata === 7) begin
                $display("$Simulation succeeded");
                $stop;
            end else if (dataaddr !== 80) begin
                $display("Simulation failed");
                $stop;
            end
        end
    end
endmodule
```

#### VHDL

```
library IEEE;
use IEEE.STD_LOGIC_1164.all; use IEEE.NUMERIC_STD_UNSIGNED.all;
entity testbench is
end;

architecture test of testbench is
component top
    port(clk, reset:      in STD_LOGIC;
         writedata, dataaddr: out STD_LOGIC_VECTOR(31 downto 0);
         memwrite:           out STD_LOGIC);
end component;
signal writedata, dataaddr: STD_LOGIC_VECTOR(31 downto 0);
signal clk, reset, memwrite: STD_LOGIC;
begin

    -- instantiate device to be tested
    dut: top port map(clk, reset, writedata, dataaddr, memwrite);

    -- Generate clock with 10 ns period
    process begin
        clk <= '1';
        wait for 5 ns;
        clk <= '0';
        wait for 5 ns;
    end process;

    -- Generate reset for first two clock cycles
    process begin
        reset <= '1';
        wait for 22 ns;
        reset <= '0';
        wait;
    end process;

    -- check that 7 gets written to address 84 at end of program
    process(clk) begin
        if (clk'event and clk = '0' and memwrite = '1') then
            if (to_integer(dataaddr) = 84 and to_integer
                (writedata) = 7) then
                report "NO ERRORS: Simulation succeeded" severity failure;
            elsif (dataaddr /= 80) then
                report "Simulation failed" severity failure;
            end if;
        end process;
    end;
```

---

## HDL Example 7.13 MIPS TOP-LEVEL MODULE

### SystemVerilog

```
module top(input logic      clk, reset,
            output logic [31:0] writedata, dataaddr,
            output logic          memwrite);

    logic [31:0] pc, instr, readdata;

    // instantiate processor and memories
    mips mips(clk, reset, pc, instr, memwrite, dataaddr,
              writedata, readdata);
    imem imem(pc[7:2], instr);
    dmem dmem(clk, memwrite, dataaddr, writedata, readdata);
endmodule
```

### VHDL

```
library IEEE;
use IEEE.STD_LOGIC_1164.all; use IEEE.NUMERIC_STD_UNSIGNED.all;

entity top is -- top-level design for testing
    port(clk, reset:      in STD_LOGIC;
          writedata, dataaddr: buffer STD_LOGIC_VECTOR(31 downto 0);
          memwrite:           buffer STD_LOGIC);
end;

architecture test of top is
    component mips
        port(clk, reset:      in STD_LOGIC;
              pc:          out STD_LOGIC_VECTOR(31 downto 0);
              instr:       in STD_LOGIC_VECTOR(31 downto 0);
              memwrite:   out STD_LOGIC;
              aluout, writedata: out STD_LOGIC_VECTOR(31 downto 0);
              readdata:   in STD_LOGIC_VECTOR(31 downto 0));
    end component;
    component imem
        port(a: in STD_LOGIC_VECTOR(5 downto 0);
              rd: out STD_LOGIC_VECTOR(31 downto 0));
    end component;
    component dmem
        port(clk, we: in STD_LOGIC;
              a, wd:  in STD_LOGIC_VECTOR(31 downto 0);
              rd:    out STD_LOGIC_VECTOR(31 downto 0));
    end component;
    signal pc, instr,
          readdata: STD_LOGIC_VECTOR(31 downto 0);
begin
    -- instantiate processor and memories
    mips1: mips port map(clk, reset, pc, instr, memwrite,
                          dataaddr, writedata, readdata);
    imem1: imem port map(pc(7 downto 2), instr);
    dmem1: dmem port map(clk, memwrite, dataaddr, writedata, readdata);
end;
```

---

## HDL Example 7.14 MIPS DATA MEMORY

### SystemVerilog

```
module dmem(input logic      clk, we,
            input logic [31:0] a, wd,
            output logic [31:0] rd);

    logic [31:0] RAM[63:0];
    assign rd=RAM[a[31:2]]; // word aligned

    always_ff @(posedge clk)
        if (we) RAM[a[31:2]] <= wd;
endmodule
```

### VHDL

```
library IEEE;
use IEEE.STD_LOGIC_1164.all; use STD.TEXTIO.all;
use IEEE.NUMERIC_STD_UNSIGNED.all;

entity dmem is -- data memory
    port(clk, we: in STD_LOGIC;
          a, wd:  in STD_LOGIC_VECTOR(31 downto 0);
          rd:    out STD_LOGIC_VECTOR(31 downto 0));
end;

architecture behave of dmem is
begin
    process is
        type ramtype is array (63 downto 0) of
            STD_LOGIC_VECTOR(31 downto 0);
        variable mem: ramtype;
    begin
        -- read or write memory
        loop
            if rising_edge(clk) then
                if (we='1') then mem(to_integer(a(7 downto 2))) := wd;
                end if;
            end if;
            rd <= mem(to_integer(a(7 downto 2)));
            wait on clk, a;
        end loop;
    end process;
end;
```

---

**HDL Example 7.15 MIPS INSTRUCTION MEMORY**
**SystemVerilog**

```
module imem(input logic [5:0] a,
            output logic [31:0] rd);

    logic [31:0] RAM[63:0];

    initial
        $readmemh("memfile.dat", RAM);

    assign rd=RAM[a]; // word aligned
endmodule
```

**VHDL**

```
library IEEE;
use IEEE.STD_LOGIC_1164.all; use STD.TEXTIO.all;
use IEEE.NUMERIC_STD_UNSIGNED.all;

entity imem is -- instruction memory
    port(a: in STD_LOGIC_VECTOR(5 downto 0);
         rd: out STD_LOGIC_VECTOR(31 downto 0));
end;

architecture behave of imem is
begin
    process is
        file mem_file: TEXT;
        variable L: line;
        variable ch: character;
        variable i, index, result: integer;
        type ramtype is array (63 downto 0) of
            STD_LOGIC_VECTOR(31 downto 0);
        variable mem: ramtype;
    begin
        -- initialize memory from file
        for i in 0 to 63 loop -- set all contents low
            mem(i) := (others => '0');
        end loop;
        index := 0;
        FILE_OPEN (mem_file, "C:/docs/DDCA2e/hdl/memfile.dat",
                   READ_MODE);
        while not endfile(mem_file) loop
            readline(mem_file, L);
            result := 0;
            for i in 1 to 8 loop
                read (L, ch);
                if '0' <= ch and ch <= '9' then
                    result := character'pos(ch) - character'pos('0');
                elsif 'a' <= ch and ch <= 'f' then
                    result := character'pos(ch) - character'pos('a')+10;
                else report "Format error on line" & integer'
                    image(index) severity error;
                end if;
                mem(index)(35-i*4 downto 32-i*4) :=
                    to_std_logic_vector(result,4);
            end loop;
            index := index+1;
        end loop;
        -- read memory
        loop
            rd <= mem(to_integer(a));
            wait on a;
        end loop;
    end process;
end;
```

## 7.7 EXCEPTIONS\*

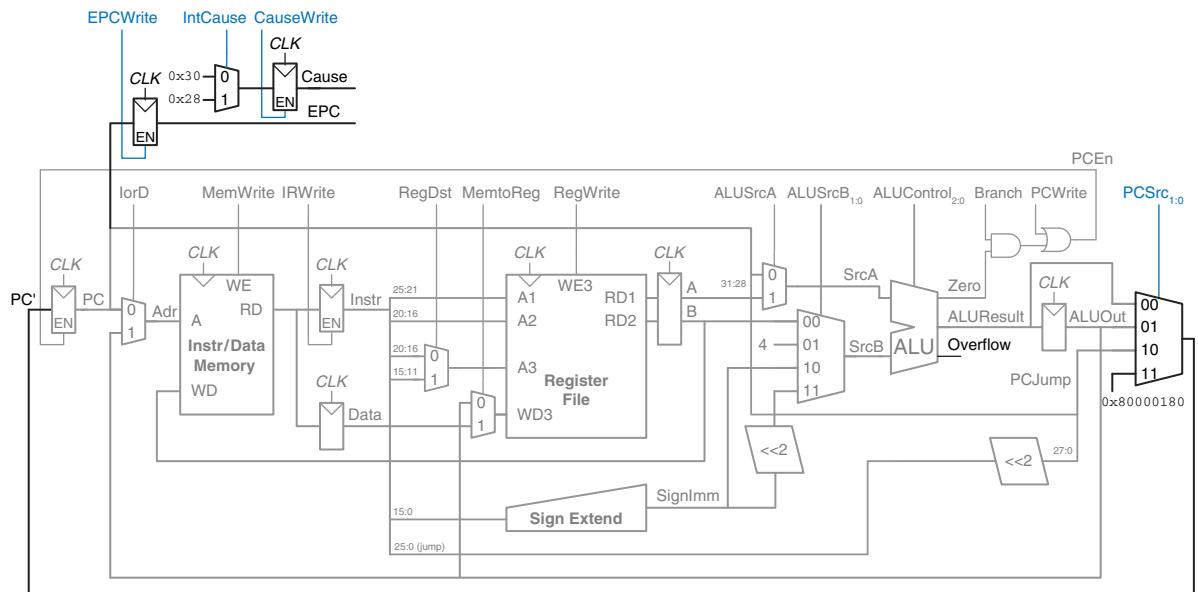
Section 6.7.2 introduced exceptions, which cause unplanned changes in the flow of a program. In this section, we enhance the multicycle processor to support two types of exceptions: undefined instructions and

arithmetic overflow. Supporting exceptions in other microarchitectures follows similar principles.

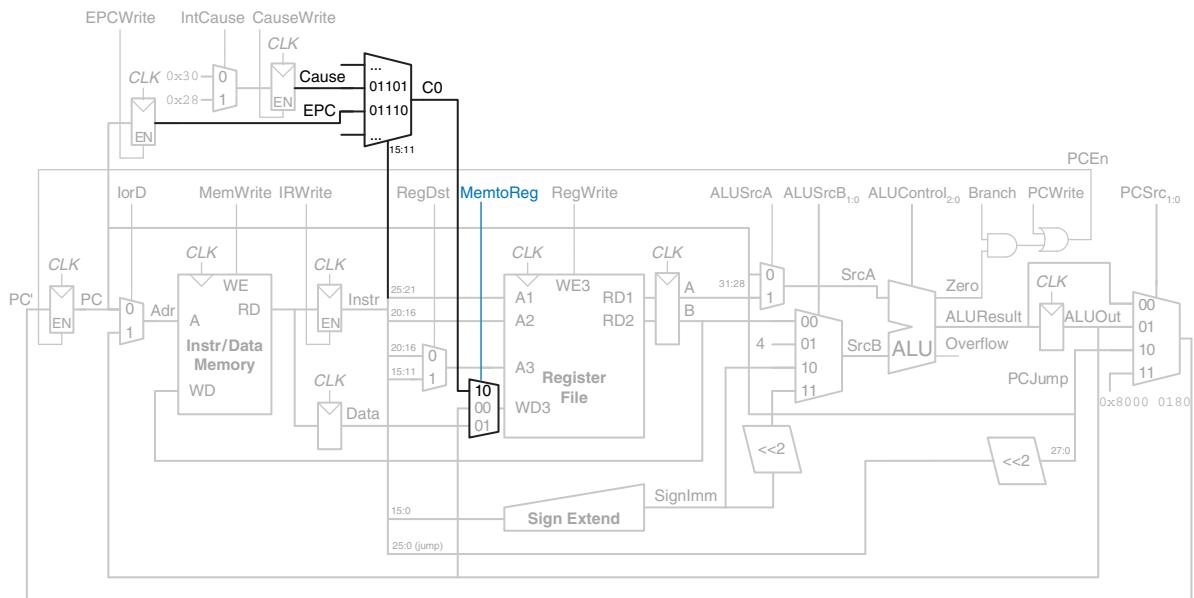
As described in [Section 6.7.2](#), when an exception takes place, the processor copies the PC to the EPC register and stores a code in the Cause register indicating the source of the exception. Exception causes include 0x28 for undefined instructions and 0x30 for overflow (see [Table 6.7](#)). The processor then jumps to the exception handler at memory address 0x80000180. The exception handler is code that responds to the exception. It is part of the operating system.

Also as discussed in [Section 6.7.2](#), the exception registers are part of *Coprocessor 0*, a portion of the MIPS processor that is used for system functions. Coprocessor 0 defines up to 32 special-purpose registers, including Cause and EPC. The exception handler may use the `mfc0` (move from coprocessor 0) instruction to copy these special-purpose registers into a general-purpose register in the register file; the Cause register is Coprocessor 0 register 13, and EPC is register 14.

To handle exceptions, we must add EPC and Cause registers to the datapath and extend the *PCSrc* multiplexer to accept the exception handler address, as shown in [Figure 7.62](#). The two new registers have write enables, *EPCWrite* and *CauseWrite*, to store the PC and exception cause when an exception takes place. The cause is generated by a multiplexer



**Figure 7.62** Datapath supporting overflow and undefined instruction exceptions



**Figure 7.63** Datapath supporting  $mfc_0$

that selects the appropriate code for the exception. The ALU must also generate an overflow signal, as was discussed in Section 5.2.4.<sup>5</sup>

To support the  $mfc_0$  instruction, we also add a way to select the Coprocessor 0 registers and write them to the register file, as shown in Figure 7.63. The  $mfc_0$  instruction specifies the Coprocessor 0 register by  $Instr_{15:11}$ ; in this diagram, only the Cause and EPC registers are supported. We add another input to the *MemtoReg* multiplexer to select the value from Coprocessor 0.

The modified controller is shown in Figure 7.64. The controller receives the overflow flag from the ALU. It generates three new control signals: one to write the EPC, a second to write the Cause register, and a third to select the Cause. It also includes two new states to support the two exceptions and another state to handle  $mfc_0$ .

If the controller receives an undefined instruction (one that it does not know how to handle), it proceeds to S12, saves the PC in EPC, writes 0x28 to the Cause register, and jumps to the exception handler. Similarly, if the controller detects arithmetic overflow on an add or sub instruction, it proceeds to S13, saves the PC in EPC, writes 0x30 in the Cause register,

<sup>5</sup> Strictly speaking, the ALU should assert overflow only for add and sub, not for other ALU instructions.

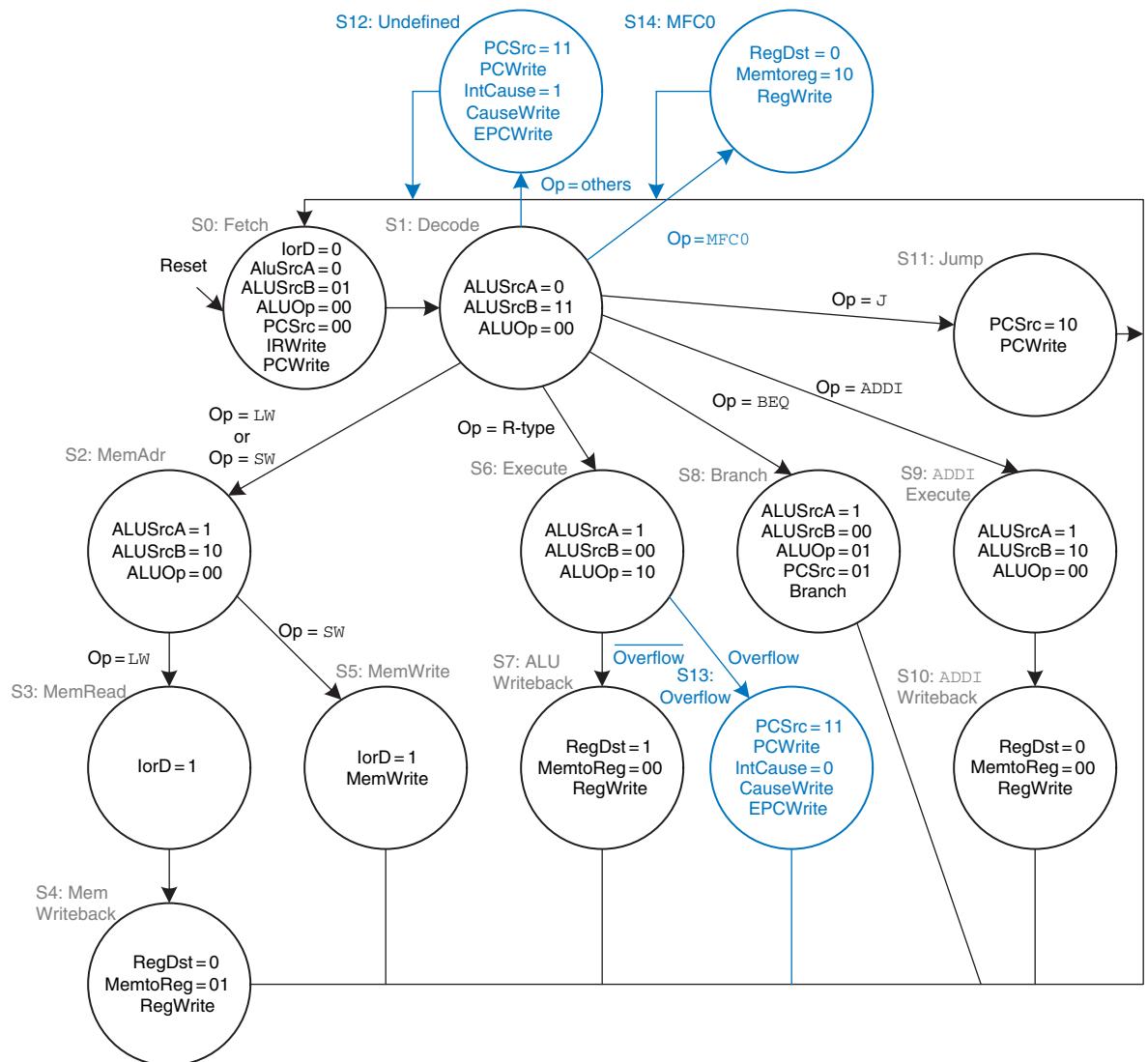


Figure 7.64 Controller supporting exceptions and mfc0

and jumps to the exception handler. Note that, when an exception occurs, the instruction is discarded and the register file is not written. When a `mfc0` instruction is decoded, the processor goes to S14 and writes the appropriate Coprocessor 0 register to the main register file.

## 7.8 ADVANCED MICROARCHITECTURE\*

High-performance microprocessors use a wide variety of techniques to run programs faster. Recall that the time required to run a program is proportional to the period of the clock and to the number of clock cycles per instruction (CPI). Thus, to increase performance we would like to speed up the clock and/or reduce the CPI. This section surveys some existing speedup techniques. The implementation details become quite complex, so we will focus on the concepts. Hennessy & Patterson's *Computer Architecture* text is a definitive reference if you want to fully understand the details.

Every 2 to 3 years, advances in CMOS manufacturing reduce transistor dimensions by 30% in each direction, doubling the number of transistors that can fit on a chip. A manufacturing process is characterized by its *feature size*, which indicates the smallest transistor that can be reliably built. Smaller transistors are faster and generally consume less power. Thus, even if the microarchitecture does not change, the clock frequency can increase because all the gates are faster. Moreover, smaller transistors enable placing more transistors on a chip. Microarchitects use the additional transistors to build more complicated processors or to put more processors on a chip. Unfortunately, power consumption increases with the number of transistors and the speed at which they operate (see [Section 1.8](#)). Power consumption is now an essential concern. Microprocessor designers have a challenging task juggling the trade-offs among speed, power, and cost for chips with billions of transistors in some of the most complex systems that humans have ever built.

### 7.8.1 Deep Pipelines

Aside from advances in manufacturing, the easiest way to speed up the clock is to chop the pipeline into more stages. Each stage contains less logic, so it can run faster. This chapter has considered a classic five-stage pipeline, but 10 to 20 stages are now commonly used.

The maximum number of pipeline stages is limited by pipeline hazards, sequencing overhead, and cost. Longer pipelines introduce more dependencies. Some of the dependencies can be solved by forwarding, but others require stalls, which increase the CPI. The pipeline registers between each stage have sequencing overhead from their setup time and clk-to-Q delay (as well as clock skew). This sequencing overhead makes adding more pipeline stages give diminishing returns. Finally, adding more stages increases the cost because of the extra pipeline registers and hardware required to handle hazards.

---

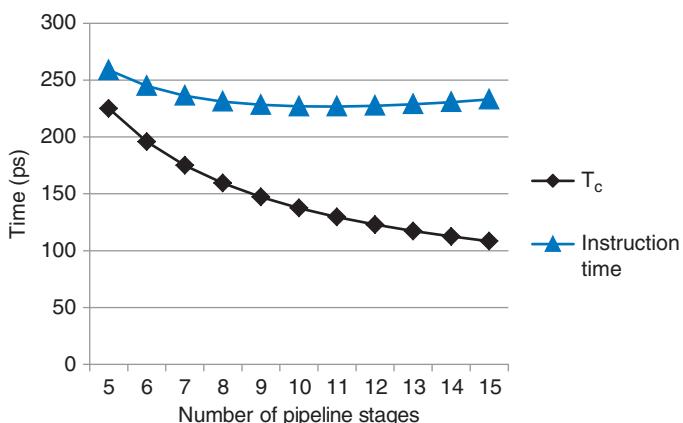
**Example 7.11 DEEP PIPELINES**

Consider building a pipelined processor by chopping up the single-cycle processor into  $N$  stages ( $N \geq 5$ ). The single-cycle processor has a propagation delay of 875 ps through the combinational logic. The sequencing overhead of a register is 50 ps. Assume that the combinational delay can be arbitrarily divided into any number of stages and that pipeline hazard logic does not increase the delay. The five-stage pipeline in [Example 7.9](#) has a CPI of 1.15. Assume that each additional stage increases the CPI by 0.1 because of branch mispredictions and other pipeline hazards. How many pipeline stages should be used to make the processor execute programs as fast as possible?

**Solution:** If the 875 ps combinational logic delay is divided into  $N$  stages and each stage also pays 50 ps of sequencing overhead for its pipeline register, the cycle time is  $T_c = (875/N + 50)$  ps. The CPI is  $1.15 + 0.1(N - 5)$ . The time per instruction, or instruction time, is the product of the cycle time and the CPI. [Figure 7.65](#) plots the cycle time and instruction time versus the number of stages. The instruction time has a minimum of 227 ps at  $N = 11$  stages. This minimum is only slightly better than the 245 ps per instruction achieved with a six-stage pipeline.

In the late 1990s and early 2000s, microprocessors were marketed largely based on clock frequency ( $1/T_c$ ). This pushed microprocessors to use very deep pipelines (20 to 31 stages on the Pentium 4) to maximize the clock frequency, even if the benefits for overall performance were questionable. Power is proportional to clock frequency and also increases with the number of pipeline registers, so now that power consumption is so important, pipeline depths are decreasing.

---



**Figure 7.65** Cycle time and instruction time versus the number of pipeline stages

### 7.8.2 Branch Prediction

An ideal pipelined processor would have a CPI of 1. The branch misprediction penalty is a major reason for increased CPI. As pipelines get deeper, branches are resolved later in the pipeline. Thus, the branch misprediction penalty gets larger, because all the instructions issued after the mispredicted branch must be flushed. To address this problem, most pipelined processors use a *branch predictor* to guess whether the branch should be taken. Recall that our pipeline from [Section 7.5.3](#) simply predicted that branches are never taken.

Some branches occur when a program reaches the end of a loop (e.g., a `for` or `while` statement) and branches back to repeat the loop. Loops tend to be executed many times, so these backward branches are usually taken. The simplest form of branch prediction checks the direction of the branch and predicts that backward branches should be taken. This is called *static branch prediction*, because it does not depend on the history of the program.

Forward branches are difficult to predict without knowing more about the specific program. Therefore, most processors use *dynamic branch predictors*, which use the history of program execution to guess whether a branch should be taken. Dynamic branch predictors maintain a table of the last several hundred (or thousand) branch instructions that the processor has executed. The table, sometimes called a *branch target buffer*, includes the destination of the branch and a history of whether the branch was taken.

To see the operation of dynamic branch predictors, consider the following loop code from [Code Example 6.20](#). The loop repeats 10 times, and the `beq` out of the loop is taken only on the last time.

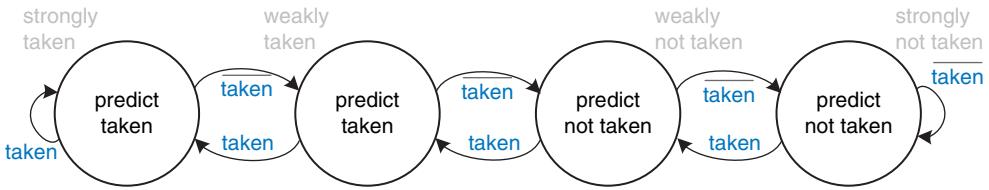
```

add $s1, $0, $0      # sum=0
addi $s0, $0, 0       # i=0
addi $t0, $0, 10      # $t0=10

for:
    beq    $s0, $t0, done    # if i == 10, branch to done
    add    $s1, $s1, $s0      # sum=sum+i
    addi   $s0, $s0, 1        # increment i
    j      for
done:

```

A *one-bit dynamic branch predictor* remembers whether the branch was taken the last time and predicts that it will do the same thing the next time. While the loop is repeating, it remembers that the `beq` was not taken last time and predicts that it should not be taken next time. This is a correct prediction until the last branch of the loop, when the branch does get taken. Unfortunately, if the loop is run again, the branch predictor remembers that the last branch was taken. Therefore, it incorrectly



**Figure 7.66** 2-bit branch predictor state transition diagram

predicts that the branch should be taken when the loop is first run again. In summary, a 1-bit branch predictor mispredicts the first and last branches of a loop.

A 2-bit dynamic branch predictor solves this problem by having four states: *strongly taken*, *weakly taken*, *weakly not taken*, and *strongly not taken*, as shown in Figure 7.66. When the loop is repeating, it enters the “strongly not taken” state and predicts that the branch should not be taken next time. This is correct until the last branch of the loop, which is taken and moves the predictor to the “weakly not taken” state. When the loop is first run again, the branch predictor correctly predicts that the branch should not be taken and reenters the “strongly not taken” state. In summary, a 2-bit branch predictor mispredicts only the last branch of a loop.

As one can imagine, branch predictors may be used to track even more history of the program to increase the accuracy of predictions. Good branch predictors achieve better than 90% accuracy on typical programs.

The branch predictor operates in the Fetch stage of the pipeline so that it can determine which instruction to execute on the next cycle. When it predicts that the branch should be taken, the processor fetches the next instruction from the branch destination stored in the branch target buffer. By keeping track of both branch and jump destinations in the branch target buffer, the processor can also avoid flushing the pipeline during jump instructions.

### 7.8.3 Superscalar Processor

A *superscalar processor* contains multiple copies of the datapath hardware to execute multiple instructions simultaneously. Figure 7.67 shows a block diagram of a two-way superscalar processor that fetches and executes two instructions per cycle. The datapath fetches two instructions at a time from the instruction memory. It has a six-ported register file to read four source operands and write two results back in each cycle. It also contains two ALUs and a two-ported data memory to execute the two instructions at the same time.

A *scalar* processor acts on one piece of data at a time. A *vector* processor acts on several pieces of data with a single instruction. A *superscalar* processor issues several instructions at a time, each of which operates on one piece of data.

Our MIPS pipelined processor is a scalar processor. Vector processors were popular for supercomputers in the 1980s and 1990s because they efficiently handled the long vectors of data common in scientific computations. Modern high-performance microprocessors are superscalar, because issuing several independent instructions is more flexible than processing vectors.

However, modern processors also include hardware to handle short vectors of data that are common in multimedia and graphics applications. These are called *single instruction multiple data (SIMD)* units.

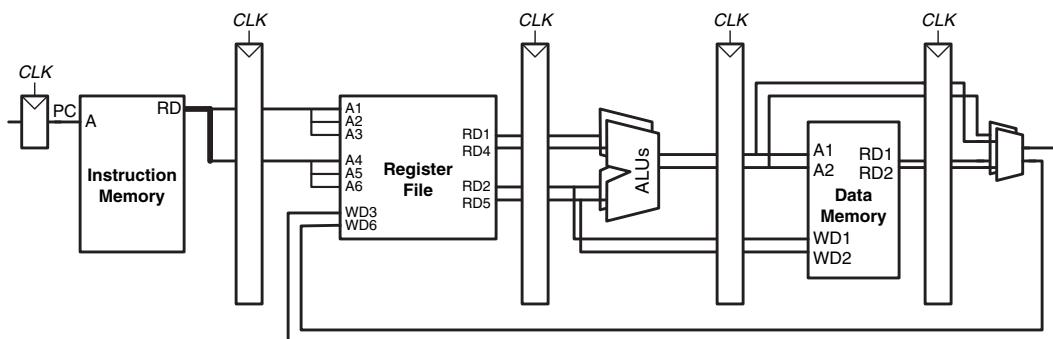


Figure 7.67 Superscalar datapath

Figure 7.68 shows a pipeline diagram illustrating the two-way superscalar processor executing two instructions on each cycle. For this program, the processor has a CPI of 0.5. Designers commonly refer to the reciprocal of the CPI as the *instructions per cycle*, or *IPC*. This processor has an IPC of 2 on this program.

Executing many instructions simultaneously is difficult because of dependencies. For example, Figure 7.69 shows a pipeline diagram running a program with data dependencies. The dependencies in the code are shown in blue. The add instruction is dependent on \$t0, which is produced by the `lw` instruction, so it cannot be issued at the same time as `lw`. Indeed, the add instruction stalls for yet another cycle so that `lw` can forward \$t0 to add in cycle 5. The other dependencies (between `sub` and `and`

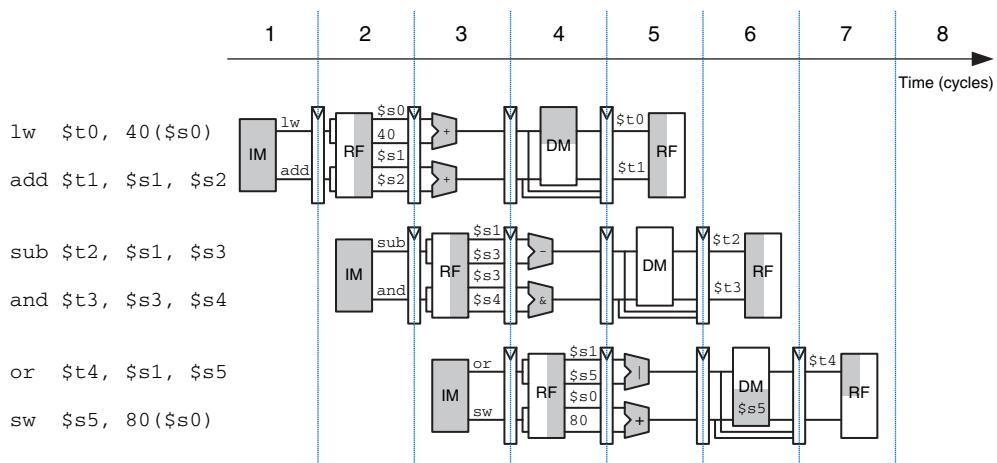


Figure 7.68 Abstract view of a superscalar pipeline in operation

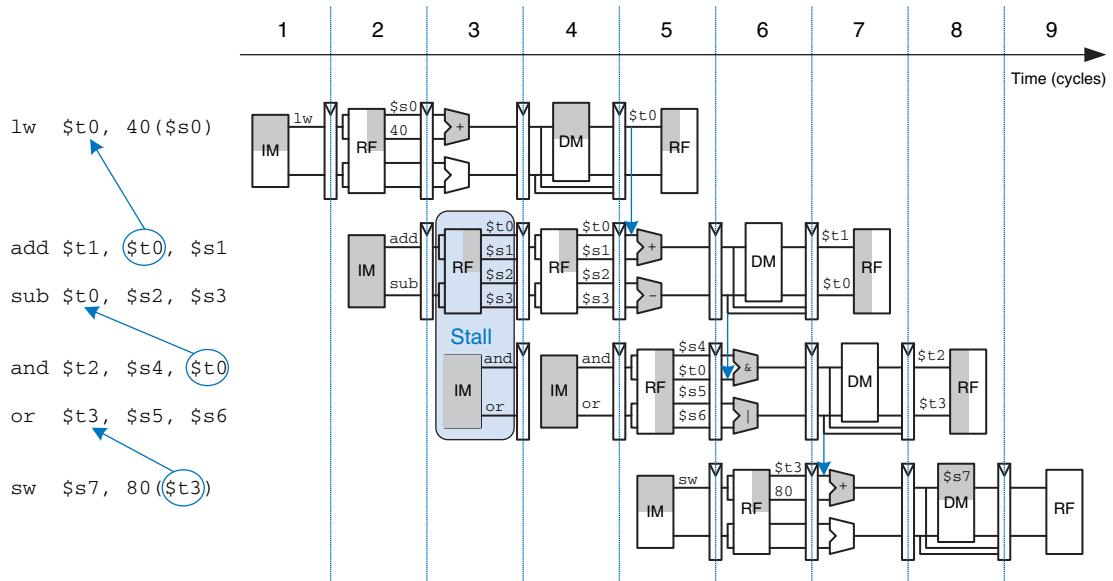


Figure 7.69 Program with data dependencies

based on  $\$t0$ , and between  $or$  and  $sw$  based on  $\$t3$ ) are handled by forwarding results produced in one cycle to be consumed in the next. This program, also given below, requires five cycles to issue six instructions, for an IPC of 1.17.

```
lw $t0, 40($s0)
add $t1, $t0, $s1
sub $t0, $s2, $s3
and $t2, $s4, $t0
or $t3, $s5, $s6
sw $s7, 80($t3)
```

Recall that parallelism comes in temporal and spatial forms. Pipelining is a case of temporal parallelism. Multiple execution units is a case of spatial parallelism. Superscalar processors exploit both forms of parallelism to squeeze out performance far exceeding that of our single-cycle and multicycle processors.

Commercial processors may be three-, four-, or even six-way superscalar. They must handle control hazards such as branches as well as data hazards. Unfortunately, real programs have many dependencies, so wide superscalar processors rarely fully utilize all of the execution units. Moreover, the large number of execution units and complex forwarding networks consume vast amounts of circuitry and power.

### 7.8.4 Out-of-Order Processor

To cope with the problem of dependencies, an *out-of-order processor* looks ahead across many instructions to *issue*, or begin executing, independent instructions as rapidly as possible. The instructions can be issued in a different order than that written by the programmer, as long as dependencies are honored so that the program produces the intended result.

Consider running the same program from Figure 7.69 on a two-way superscalar out-of-order processor. The processor can issue up to two instructions per cycle from anywhere in the program, as long as dependencies are observed. Figure 7.70 shows the data dependencies and the operation of the processor. The classifications of dependencies as RAW and WAR will be discussed shortly. The constraints on issuing instructions are described below.

- ▶ **Cycle 1**

- The `lw` instruction issues.
- The `add`, `sub`, and `and` instructions are dependent on `lw` by way of `$t0`, so they cannot issue yet. However, the `or` instruction is independent, so it also issues.

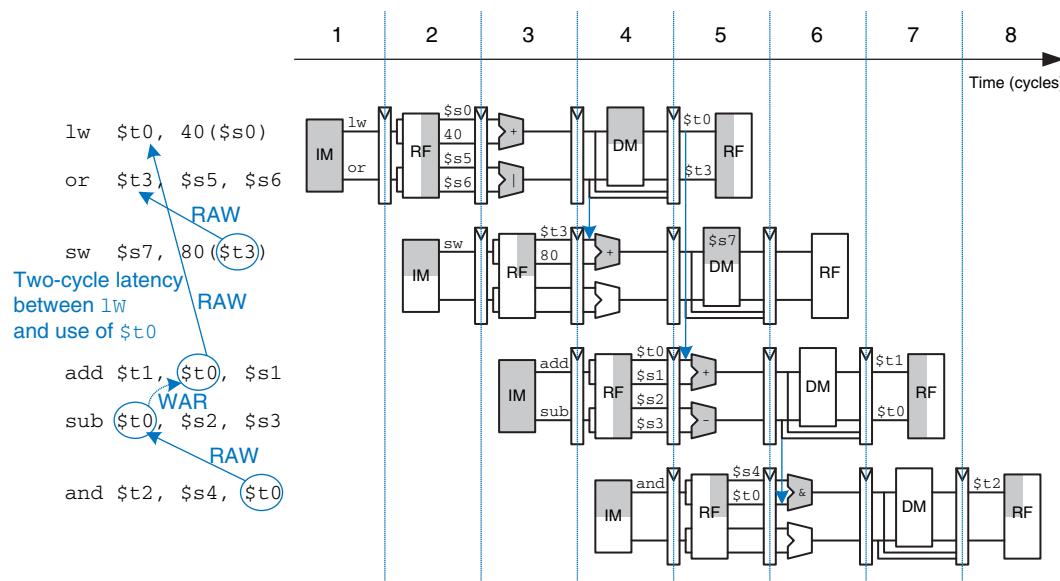


Figure 7.70 Out-of-order execution of a program with dependencies

- ▶ Cycle 2
  - Remember that there is a two-cycle latency between when a `lw` instruction issues and when a dependent instruction can use its result, so `add` cannot issue yet because of the `$t0` dependence. `sub` writes `$t0`, so it cannot issue before `add`, lest `add` receive the wrong value of `$t0`. and is dependent on `sub`.
  - Only the `sw` instruction issues.
- ▶ Cycle 3
  - On cycle 3, `$t0` is available, so `add` issues. `sub` issues simultaneously, because it will not write `$t0` until after `add` consumes `$t0`.
- ▶ Cycle 4
  - The `and` instruction issues. `$t0` is forwarded from `sub` to `and`.

The out-of-order processor issues the six instructions in four cycles, for an IPC of 1.5.

The dependence of `add` on `lw` by way of `$t0` is a read after write (RAW) hazard. `add` must not read `$t0` until after `lw` has written it. This is the type of dependency we are accustomed to handling in the pipelined processor. It inherently limits the speed at which the program can run, even if infinitely many execution units are available. Similarly, the dependence of `sw` on `or` by way of `$t3` and of `and` on `sub` by way of `$t0` are RAW dependencies.

The dependence between `sub` and `add` by way of `$t0` is called a *write after read* (WAR) hazard or an *antidependence*. `sub` must not write `$t0` before `add` reads `$t0`, so that `add` receives the correct value according to the original order of the program. WAR hazards could not occur in the simple MIPS pipeline, but they may happen in an out-of-order processor if the dependent instruction (in this case, `sub`) is moved too early.

A WAR hazard is not essential to the operation of the program. It is merely an artifact of the programmer's choice to use the same register for two unrelated instructions. If the `sub` instruction had written `$t4` instead of `$t0`, the dependency would disappear and `sub` could be issued before `add`. The MIPS architecture only has 32 registers, so sometimes the programmer is forced to reuse a register and introduce a hazard just because all the other registers are in use.

A third type of hazard, not shown in the program, is called *write after write* (WAW) or an *output dependence*. A WAW hazard occurs if an instruction attempts to write a register after a subsequent instruction has already written it. The hazard would result in the wrong value being

written to the register. For example, in the following program, add and sub both write \$t0. The final value in \$t0 should come from sub according to the order of the program. If an out-of-order processor attempted to execute sub first, a WAW hazard would occur.

```
add $t0, $s1, $s2
sub $t0, $s3, $s4
```

WAW hazards are not essential either; again, they are artifacts caused by the programmer's using the same register for two unrelated instructions. If the sub instruction were issued first, the program could eliminate the WAW hazard by discarding the result of the add instead of writing it to \$t0. This is called *squashing* the add.<sup>6</sup>

Out-of-order processors use a table to keep track of instructions waiting to issue. The table, sometimes called a *scoreboard*, contains information about the dependencies. The size of the table determines how many instructions can be considered for issue. On each cycle, the processor examines the table and issues as many instructions as it can, limited by the dependencies and by the number of execution units (e.g., ALUs, memory ports) that are available.

The *instruction level parallelism (ILP)* is the number of instructions that can be executed simultaneously for a particular program and micro-architecture. Theoretical studies have shown that the ILP can be quite large for out-of-order microarchitectures with perfect branch predictors and enormous numbers of execution units. However, practical processors seldom achieve an ILP greater than 2 or 3, even with six-way superscalar datapaths with out-of-order execution.

### 7.8.5 Register Renaming

Out-of-order processors use a technique called *register renaming* to eliminate WAR hazards. Register renaming adds some nonarchitectural *renaming registers* to the processor. For example, a MIPS processor might add 20 renaming registers, called \$r0-\$r19. The programmer cannot use these registers directly, because they are not part of the architecture. However, the processor is free to use them to eliminate hazards.

For example, in the previous section, a WAR hazard occurred between the sub and add instructions based on reusing \$t0. The out-of-order processor could *rename* \$t0 to \$r0 for the sub instruction. Then

---

<sup>6</sup> You might wonder why the add needs to be issued at all. The reason is that out-of-order processors must guarantee that all of the same exceptions occur that would have occurred if the program had been executed in its original order. The add potentially may produce an overflow exception, so it must be issued to check for the exception, even though the result can be discarded.

sub could be executed sooner, because \$r0 has no dependency on the add instruction. The processor keeps a table of which registers were renamed so that it can consistently rename registers in subsequent dependent instructions. In this example, \$t0 must also be renamed to \$r0 in the and instruction, because it refers to the result of sub.

Figure 7.71 shows the same program from Figure 7.70 executing on an out-of-order processor with register renaming. \$t0 is renamed to \$r0 in sub and to eliminate the WAR hazard. The constraints on issuing instructions are described below.

#### ► Cycle 1

- The lw instruction issues.
- The add instruction is dependent on lw by way of \$t0, so it cannot issue yet. However, the sub instruction is independent now that its destination has been renamed to \$r0, so sub also issues.

#### ► Cycle 2

- Remember that there is a two-cycle latency between when a lw issues and when a dependent instruction can use its result, so add cannot issue yet because of the \$t0 dependence.
- The and instruction is dependent on sub, so it can issue. \$r0 is forwarded from sub to and.
- The or instruction is independent, so it also issues.

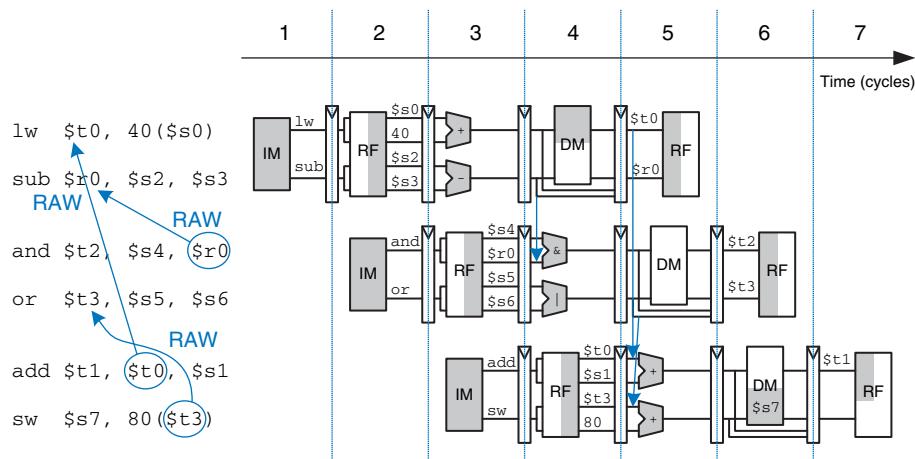


Figure 7.71 Out-of-order execution of a program using register renaming

### ► Cycle 3

- On cycle 3, \$t0 is available, so add issues. \$t3 is also available, so `sw` issues.

The out-of-order processor with register renaming issues the six instructions in three cycles, for an IPC of 2.

## 7.8.6 Single Instruction Multiple Data

The term *SIMD* (pronounced “sim-dee”) stands for *single instruction multiple data*, in which a single instruction acts on multiple pieces of data in parallel. A common application of SIMD is to perform many short arithmetic operations at once, especially for graphics processing. This is also called *packed* arithmetic.

For example, a 32-bit microprocessor might pack four 8-bit data elements into one 32-bit word. Packed add and subtract instructions operate on all four data elements within the word in parallel. Figure 7.72 shows a packed 8-bit addition summing four pairs of 8-bit numbers to produce four results. The word could also be divided into two 16-bit elements. Performing packed arithmetic requires modifying the ALU to eliminate carries between the smaller data elements. For example, a carry out of  $a_0 + b_0$  should not affect the result of  $a_1 + b_1$ .

Short data elements often appear in graphics processing. For example, a pixel in a digital photo may use 8 bits to store each of the red, green, and blue color components. Using an entire 32-bit word to process one of these components wastes the upper 24 bits. When the components from four adjacent pixels are packed into a 32-bit word, the processing can be performed four times faster.

SIMD instructions are even more helpful for 64-bit architectures, which can pack eight 8-bit elements, four 16-bit elements, or two 32-bit elements into a single 64-bit word. SIMD instructions are also used for floating-point computations; for example, four 32-bit single-precision floating-point values can be packed into a single 128-bit word.

### Figure 7.72 Packed arithmetic: four simultaneous 8-bit additions

padd8 \$s2, \$s0, \$s1

32      24 23      16 15      8 7      0      Bit position

$a_3 \quad a_2 \quad a_1 \quad a_0 \quad \$\$0$

10. **What is the primary purpose of the following statement?**

$$a_3 + b_3 \quad a_2 + b_2 \quad a_1 + b_1 \quad a_0 + b_0 \quad \$s2$$

### 7.8.7 Multithreading

Because the ILP of real programs tends to be fairly low, adding more execution units to a superscalar or out-of-order processor gives diminishing returns. Another problem, discussed in [Chapter 8](#), is that memory is much slower than the processor. Most loads and stores access a smaller and faster memory, called a *cache*. However, when the instructions or data are not available in the cache, the processor may stall for 100 or more cycles while retrieving the information from the main memory. Multithreading is a technique that helps keep a processor with many execution units busy even if the ILP of a program is low or the program is stalled waiting for memory.

To explain multithreading, we need to define a few new terms. A program running on a computer is called a *process*. Computers can run multiple processes simultaneously; for example, you can play music on a PC while surfing the web and running a virus checker. Each process consists of one or more *threads* that also run simultaneously. For example, a word processor may have one thread handling the user typing, a second thread spell-checking the document while the user works, and a third thread printing the document. In this way, the user does not have to wait, for example, for a document to finish printing before being able to type again. The degree to which a process can be split into multiple threads that can run simultaneously defines its level of *thread level parallelism* (TLP).

In a conventional processor, the threads only give the illusion of running simultaneously. The threads actually take turns being executed on the processor under control of the OS. When one thread's turn ends, the OS saves its architectural state, loads the architectural state of the next thread, and starts executing that next thread. This procedure is called *context switching*. As long as the processor switches through all the threads fast enough, the user perceives all of the threads as running at the same time.

A multithreaded processor contains more than one copy of its architectural state, so that more than one thread can be active at a time. For example, if we extended a MIPS processor to have four program counters and 128 registers, four threads could be available at one time. If one thread stalls while waiting for data from main memory, the processor could context switch to another thread without any delay, because the program counter and registers are already available. Moreover, if one thread lacks sufficient parallelism to keep all the execution units busy, another thread could issue instructions to the idle units.

Multithreading does not improve the performance of an individual thread, because it does not increase the ILP. However, it does improve the overall throughput of the processor, because multiple threads can use processor resources that would have been idle when executing a single thread. Multithreading is also relatively inexpensive to implement, because it replicates only the PC and register file, not the execution units and memories.

### 7.8.8 Homogeneous Multiprocessors

A *multiprocessor* system consists of multiple processors and a method for communication between the processors. A common form of multiprocessing in computer systems is *homogeneous multiprocessing*, also called *symmetric multiprocessing* (SMP), in which two or more identical processors share a single main memory.

The multiple processors may be separate chips or multiple *cores* on the same chip. Modern processors have enormous numbers of transistors available. Using them to increase the pipeline depth or to add more execution units to a superscalar processor gives little performance benefit and is wasteful of power. Around the year 2005, computer architects made a major shift to building multiple copies of the processor on the same chip; these copies are called cores.

Multiprocessors can be used to run more threads simultaneously or to run a particular thread faster. Running more threads simultaneously is easy; the threads are simply divided up among the processors. Unfortunately typical PC users need to run only a small number of threads at any given time. Running a particular thread faster is much more challenging. The programmer must divide the existing thread into multiple threads to execute on each processor. This becomes tricky when the processors need to communicate with each other. One of the major challenges for computer designers and programmers is to effectively use large numbers of processor cores.

Other forms of multiprocessing include *heterogeneous multiprocessing* and *clusters*. Heterogeneous multiprocessors, also called *asymmetric multiprocessors*, use separate specialized microprocessors for separate tasks and are discussed next. In *clustered multiprocessing*, each processor has its own local memory system. Clustering can also refer to a group of PCs connected together on the network running software to jointly solve a large problem.

Scientists searching for signs of extraterrestrial intelligence use the world's largest clustered multiprocessors to analyze radio telescope data for patterns that might be signs of life in other solar systems. The cluster consists of personal computers owned by more than 3.8 million volunteers around the world.

When a computer in the cluster is idle, it fetches a piece of the data from a centralized server, analyzes the data, and sends the results back to the server. You can volunteer your computer's idle time for the cluster by visiting [setiathome.berkeley.edu](http://setiathome.berkeley.edu).

### 7.8.9 Heterogeneous Multiprocessors

The homogeneous multiprocessors described in Section 7.8.8 have a number of advantages. They are relatively simple to design because the processor can be designed once and then replicated multiple times to increase performance. Programming for and executing code on a homogeneous multiprocessor is also relatively straightforward because any program can run on any processor in the system and achieve approximately the same performance.

Unfortunately, continuing to add more and more cores is not guaranteed to provide continued performance improvement. As of 2012, consumer applications employed only 2–3 threads on average at any given time,

and a typical consumer might be expected to have a couple of applications actually computing simultaneously. While this is enough to keep dual- and quad-core systems busy, unless programs start incorporating significantly more parallelism, continuing to add more cores beyond this point will provide diminishing benefits. As an added issue, because general purpose processors are designed to provide good average performance they are generally not the most power efficient option for performing a given operation. This energy inefficiency is especially important in highly power-constrained portable environments.

*Heterogeneous multiprocessors* aim to address these issues by incorporating different types of cores and/or specialized hardware in a single system. Each application uses those resources that provide the best performance, or power-performance ratio, for that application. Because transistors are fairly plentiful these days, the fact that not every application will make use of every piece of hardware is of minimal concern. Heterogeneous systems can take a number of forms. A heterogeneous system can incorporate cores with different microarchitectures that have different power, performance, and area tradeoffs. For example, a system could include both simple single-issue in-order cores and more complex superscalar out-of-order cores. Applications that can make efficient use of the higher performing, but more power hungry, out-of-order cores have that option available to them, while other applications that do not use the added computation effectively can use the more energy efficient in-order cores.

In such a system, the cores may all use the same ISA, which allows an application to run on any of the cores, or may employ different ISAs, which can allow further tailoring of a core to a given task. IBM's Cell Broadband Engine is an example of the latter. The Cell incorporates a single dual-issue in-order power processor element (PPE) with eight synergistic processor elements (SPEs). The SPEs use a new ISA, the *SPU ISA*, that is tailored to power efficiency for computationally intensive workloads. Although multiple programming paradigms are possible, the general idea is that the PPE handles most control and management decisions, such as dividing the workload among the SPEs, while the SPEs handle the majority of the computation. The heterogeneous nature of the Cell allows it to provide far higher computational performance for a given power and area than would be possible using traditional Power processors.

Other heterogeneous systems can include a mix of traditional cores and specialized hardware. Floating-point coprocessors are an early example of this. In early microprocessors, there was not space for floating-point hardware on the main chip. Users interested in floating-point performance could add a separate chip that provided dedicated floating-point support. Today's microprocessors include one or more floating-point

**Synergistic Processor Unit (SPU)**

**ISA.** The SPU ISA is designed to provide the same performance as general purpose processors at half the area and power for certain sets of workloads. Specifically, the SPU ISA targets graphics, stream processing, and other highly computational workloads, such as game physics and other system modeling. To achieve the desired performance, power, and area goals, the ISA incorporates a number of features, including 128-bit SIMD execution, software-managed memory, and a large register file. In software-managed memory the programmer is explicitly responsible for moving data into and out of local memory, as opposed to the caches of common processors, which bring data in automatically. If used correctly, this can both save power and improve performance because necessary data is brought in ahead of time and only when needed. The large register file helps avoid register starvation without the need for expensive register renaming.

units on chip and are now beginning to include other types of specialized hardware. AMD and Intel both have processors that incorporate a *graphics processing unit (GPU)* or FPGA and one or more traditional x86 cores on the same chip. AMD's Fusion line and Intel's Sandy Bridge are the first set of devices to incorporate a processor and GPU in the same die. Intel's E600 (Stellarton) series chips, released in early 2011, pair an Atom processor with an Altera FPGA, again on the same die. At a chip level, a cell phone contains both a conventional processor to handle user interaction, such as managing the phone book, processing websites and playing games, and a *digital signal processor (DSP)* with specialized instructions to decipher wireless data in real time. In power constrained environments, these types of integrated, specialized hardware provide better power-performance tradeoffs than performing the same operation on a standard core.

Heterogeneous systems are not without their drawbacks. They add complexity, both in terms of designing the different heterogeneous elements and in terms of the additional programming effort to decide when and how to make use of the varying resources. In the end, homogeneous and heterogeneous systems will both likely have their places. Homogeneous multiprocessors are good for situations, like large data centers, that have lots of thread level parallelism available. Heterogeneous systems are good for cases that have more varying workloads and limited parallelism.

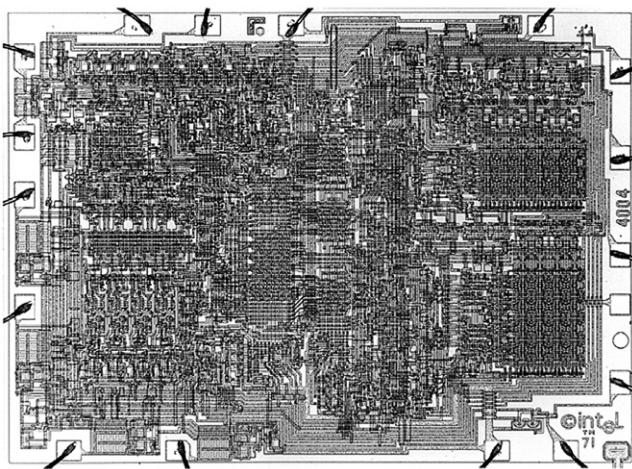
## 7.9 REAL-WORLD PERSPECTIVE: x86 MICROARCHITECTURE\*

Section 6.8 introduced the x86 architecture used in almost all PCs. This section tracks the evolution of x86 processors through progressively faster and more complicated microarchitectures. The same principles we have applied to the MIPS microarchitectures are used in x86.

Intel invented the first single-chip microprocessor, the 4-bit 4004, in 1971 as a flexible controller for a line of calculators. It contained 2300 transistors manufactured on a 12-mm<sup>2</sup> sliver of silicon in a process with a 10-μm feature size and operated at 750 kHz. A photograph of the chip taken under a microscope is shown in Figure 7.73.

In places, columns of four similar-looking structures are visible, as one would expect in a 4-bit microprocessor. Around the periphery are *bond wires*, which are used to connect the chip to its package and the circuit board.

The 4004 inspired the 8-bit 8008, then the 8080, which eventually evolved into the 16-bit 8086 in 1978 and the 80286 in 1982. In 1985, Intel introduced the 80386, which extended the 8086 architecture to 32 bits and defined the x86 architecture. Table 7.7 summarizes major



**Figure 7.73** 4004 microprocessor chip

Intel x86 microprocessors. In the 40 years since the 4004, transistor feature size has shrunk 160-fold, the number of transistors on a chip has increased by five orders of magnitude, and the operating frequency has increased by almost four orders of magnitude. No other field of engineering has made such astonishing progress in such a short time.

The 80386 is a multicycle processor. The major components are labeled on the chip photograph in Figure 7.74. The 32-bit datapath is

**Table 7.7** Evolution of Intel x86 microprocessors

Processor	Year	Feature Size ( $\mu\text{m}$ )	Transistors	Frequency (MHz)	Microarchitecture
80386	1985	1.5–1.0	275k	16–25	multicycle
80486	1989	1.0–0.6	1.2M	25–100	pipelined
Pentium	1993	0.8–0.35	3.2–4.5M	60–300	superscalar
Pentium II	1997	0.35–0.25	7.5M	233–450	out of order
Pentium III	1999	0.25–0.18	9.5M–28M	450–1400	out of order
Pentium 4	2001	0.18–0.09	42–178M	1400–3730	out of order
Pentium M	2003	0.13–0.09	77–140M	900–2130	out of order
Core Duo	2005	0.065	152M	1500–2160	dual core
Core 2 Duo	2006	0.065–0.045	167–410M	1800–3300	dual core
Core i-series	2009	0.045–0.032	382–731 <sup>+</sup> M	2530–3460	multi-core

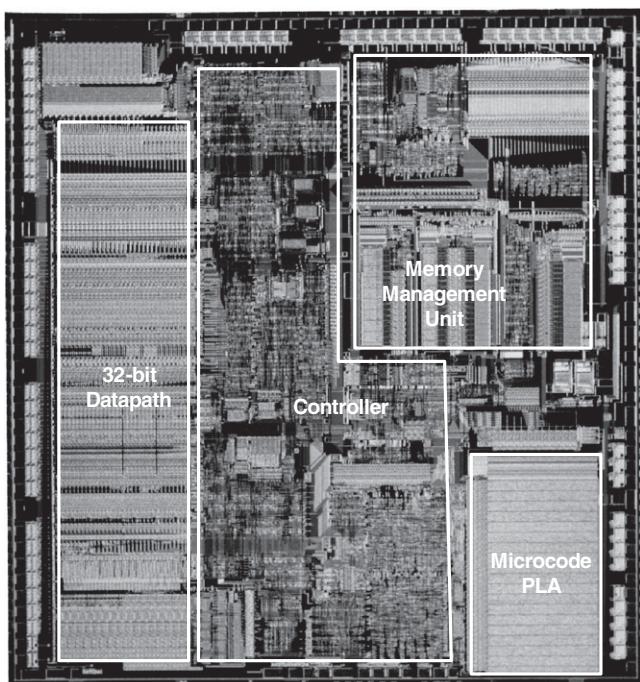
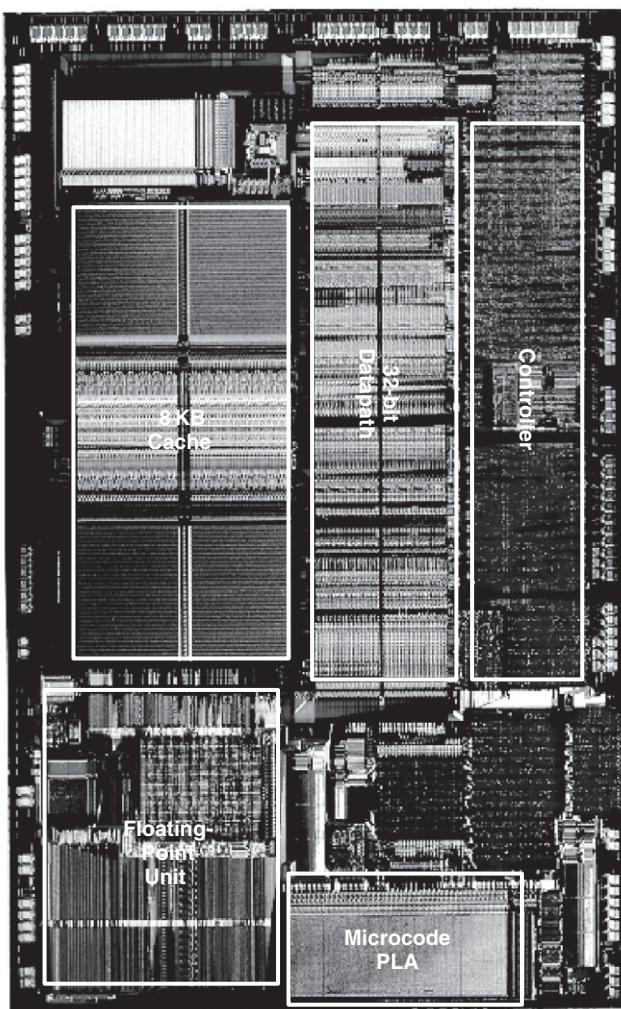


Figure 7.74 80386 microprocessor chip

clearly visible on the left. Each of the columns processes one bit of data. Some of the control signals are generated using a *microcode* PLA that steps through the various states of the control FSM. The memory management unit in the upper right controls access to the external memory.

The 80486, shown in Figure 7.75, dramatically improved performance using pipelining. The datapath is again clearly visible, along with the control logic and microcode PLA. The 80486 added an on-chip floating-point unit; previous Intel processors either sent floating-point instructions to a separate coprocessor or emulated them in software. The 80486 was too fast for external memory to keep up, so it incorporated an 8-KB cache onto the chip to hold the most commonly used instructions and data. Chapter 8 describes caches in more detail and revisits the cache systems on Intel x86 processors.

The Pentium processor, shown in Figure 7.76, is a superscalar processor capable of executing two instructions simultaneously. Intel switched to the name Pentium instead of 80586 because AMD was becoming a serious competitor selling interchangeable 80486 chips, and part numbers

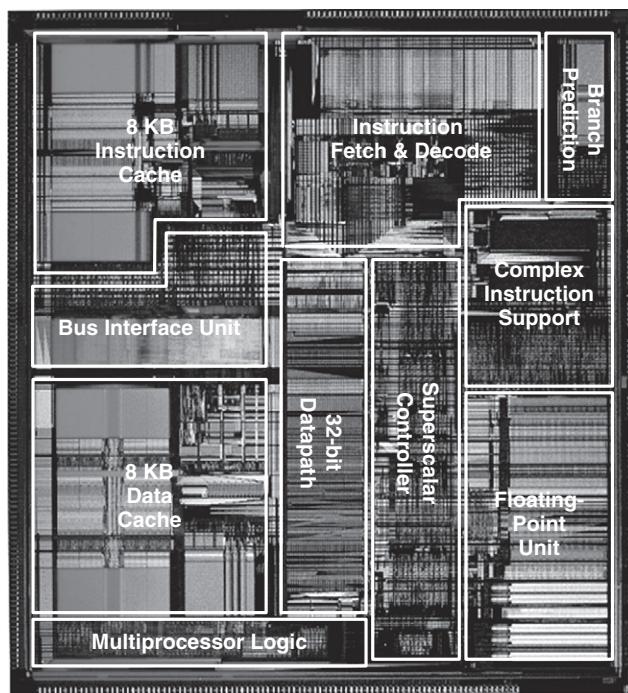


**Figure 7.75** 80486 microprocessor chip

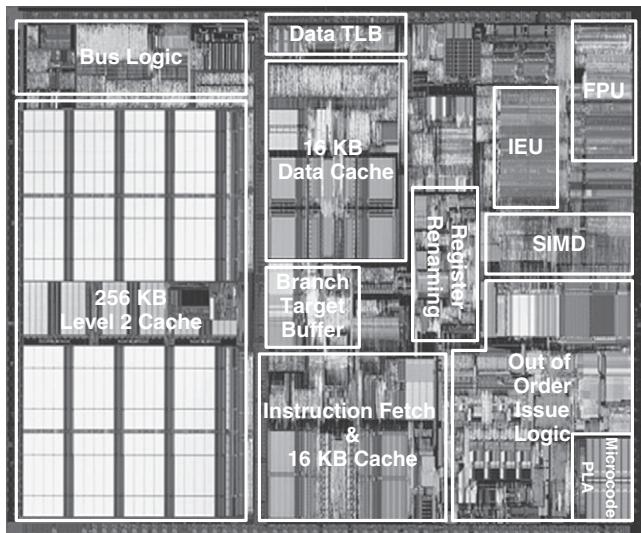
cannot be trademarked. The Pentium uses separate instruction and data caches. It also uses a branch predictor to reduce the performance penalty for branches.

The Pentium Pro, Pentium II, and Pentium III processors all share a common out-of-order microarchitecture, code-named P6. The complex x86 instructions are broken down into one or more micro-ops similar to MIPS instructions. The micro-ops are then executed on a fast out-of-order execution core with an 11-stage pipeline. Figure 7.77 shows the Pentium III. The 32-bit datapath is called the Integer Execution Unit (IEU).

**Figure 7.76** Pentium microprocessor chip



**Figure 7.77** Pentium III microprocessor chip



The floating-point datapath is called the Floating Point Unit (FPU). The processor also has a SIMD unit to perform packed operations on short integer and floating-point data. A larger portion of the chip is dedicated to issuing instructions out-of-order than to actually executing the instructions. The instruction and data caches have grown to 16 KB each. The Pentium III also has a larger but slower 256-KB second-level cache on the same chip.

By the late 1990s, processors were marketed largely on clock speed. The Pentium 4 is another out-of-order processor with a very deep pipeline to achieve extremely high clock frequencies. It started with 20 stages, and later versions adopted 31 stages to achieve frequencies greater than 3 GHz. The chip, shown in Figure 7.78, packs in 42 to 178 million transistors (depending on the cache size), so even the major execution units are difficult to see on the photograph. Decoding three x86 instructions per cycle is impossible at such high clock frequencies because the instruction encodings are so complex and irregular. Instead, the processor predecodes the instructions into simpler micro-ops, then stores the micro-ops in a memory called a *trace cache*. Later versions of the Pentium 4 also perform multithreading to increase the throughput of multiple threads.

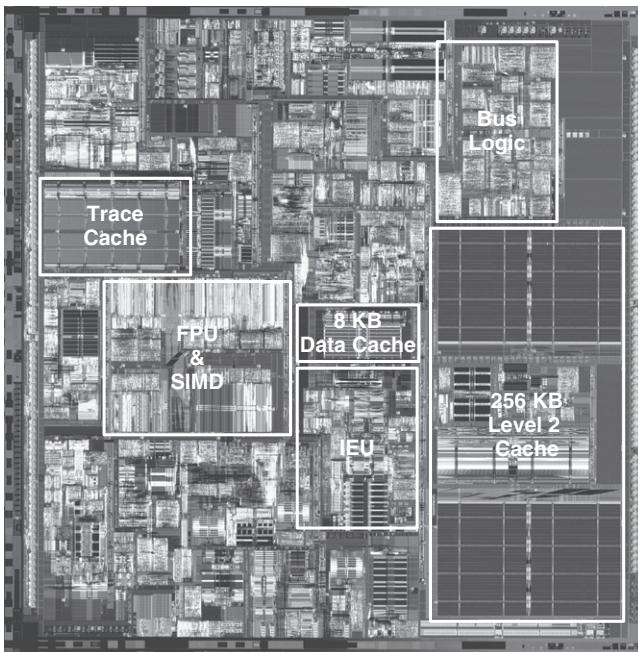
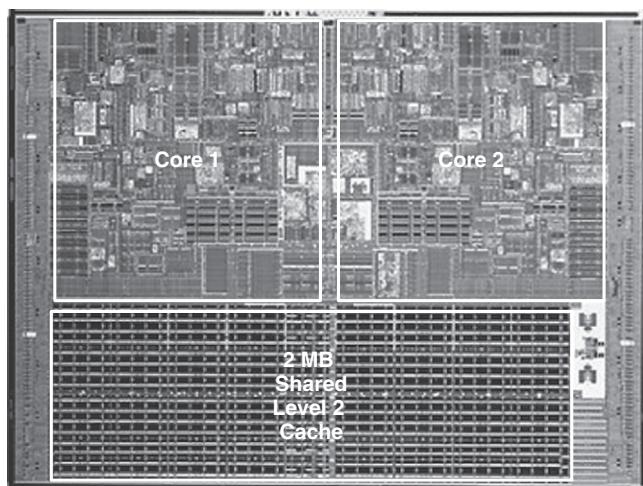


Figure 7.78 Pentium 4 microprocessor chip

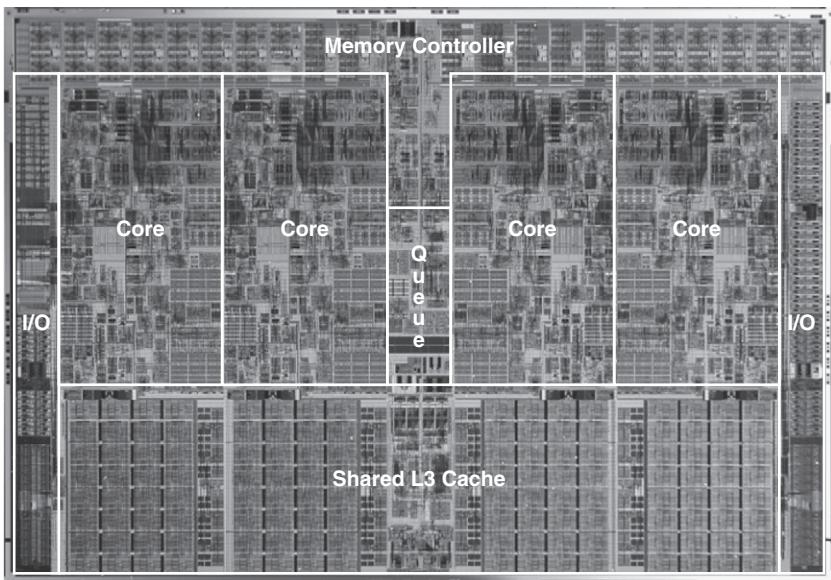


**Figure 7.79** Core Duo microprocessor chip

The Pentium 4's reliance on deep pipelines and high clock speed led to extremely high power consumption, sometimes more than 100 W. This is unacceptable in laptops and makes cooling of desktops expensive.

Intel discovered that the older P6 architecture could achieve comparable performance at much lower clock speed and power. The Pentium M uses an enhanced version of the P6 out-of-order microarchitecture with 32-KB instruction and data caches and a 1- to 2-MB second-level cache. The Core Duo is a multicore processor based on two Pentium M cores connected to a shared 2-MB second-level cache. The individual functional units in Figure 7.79 are difficult to see, but the two cores and the large cache are clearly visible.

In 2009, Intel introduced a new microarchitecture code-named Nehalem that streamlines the initial Core microarchitecture. These processors, including the Core i3, i5, and i7 series, extend the instruction set to 64 bits. They offer from 2 to 6 cores, 3–15 MB of third-level cache, and a built-in memory controller. Some models include built-in graphics processors, also called *graphics accelerators*. Some support “Turbo-Boost” to improve the performance of single-threaded code by turning off the unused cores and raising the voltage and clock frequency of the boosted core. Some offer “hyperthreading,” Intel’s term for 2-way multithreading that doubles the number of cores from the user’s perspective. Figure 7.80 shows a Core i7 die with four cores and 8 MB of shared L3 cache.



**Figure 7.80** Core i7 microprocessor chip

(Source: [http://www.intel.com/pressroom/archive/releases/2008/20081117comp\\_sm.htm](http://www.intel.com/pressroom/archive/releases/2008/20081117comp_sm.htm).

Courtesy Intel)

## 7.10 SUMMARY

This chapter has described three ways to build MIPS processors, each with different performance and cost trade-offs. We find this topic almost magical: how can such a seemingly complicated device as a microprocessor actually be simple enough to fit in a half-page schematic? Moreover, the inner workings, so mysterious to the uninitiated, are actually reasonably straightforward.

The MIPS microarchitectures have drawn together almost every topic covered in the text so far. Piecing together the microarchitecture puzzle illustrates the principles introduced in previous chapters, including the design of combinational and sequential circuits, covered in [Chapters 2 and 3](#); the application of many of the building blocks described in [Chapter 5](#); and the implementation of the MIPS architecture, introduced in [Chapter 6](#). The MIPS microarchitectures can be described in a few pages of HDL, using the techniques from [Chapter 4](#).

Building the microarchitectures has also heavily used our techniques for managing complexity. The microarchitectural abstraction forms the link between the logic and architecture abstractions, forming the crux of this book on digital design and computer architecture. We also use the abstractions of block diagrams and HDL to succinctly describe the

arrangement of components. The microarchitectures exploit regularity and modularity, reusing a library of common building blocks such as ALUs, memories, multiplexers, and registers. Hierarchy is used in numerous ways. The microarchitectures are partitioned into the datapath and control units. Each of these units is built from logic blocks, which can be built from gates, which in turn can be built from transistors using the techniques developed in the first five chapters.

This chapter has compared single-cycle, multicycle, and pipelined microarchitectures for the MIPS processor. All three microarchitectures implement the same subset of the MIPS instruction set and have the same architectural state. The single-cycle processor is the most straightforward and has a CPI of 1.

The multicycle processor uses a variable number of shorter steps to execute instructions. It thus can reuse the ALU, rather than requiring several adders. However, it does require several nonarchitectural registers to store results between steps. The multicycle design in principle could be faster, because not all instructions must be equally long. In practice, it is generally slower, because it is limited by the slowest steps and by the sequencing overhead in each step.

The pipelined processor divides the single-cycle processor into five relatively fast pipeline stages. It adds pipeline registers between the stages to separate the five instructions that are simultaneously executing. It nominally has a CPI of 1, but hazards force stalls or flushes that increase the CPI slightly. Hazard resolution also costs some extra hardware and design complexity. The clock period ideally could be five times shorter than that of the single-cycle processor. In practice, it is not that short, because it is limited by the slowest stage and by the sequencing overhead in each stage. Nevertheless, pipelining provides substantial performance benefits. All modern high-performance microprocessors use pipelining today.

Although the microarchitectures in this chapter implement only a subset of the MIPS architecture, we have seen that supporting more instructions involves straightforward enhancements of the datapath and controller. Supporting exceptions also requires simple modifications.

A major limitation of this chapter is that we have assumed an ideal memory system that is fast and large enough to store the entire program and data. In reality, large fast memories are prohibitively expensive. The next chapter shows how to get most of the benefits of a large fast memory with a small fast memory that holds the most commonly used information and one or more larger but slower memories that hold the rest of the information.

## Exercises

---

**Exercise 7.1** Suppose that one of the following control signals in the single-cycle MIPS processor has a *stuck-at-0 fault*, meaning that the signal is always 0, regardless of its intended value. What instructions would malfunction? Why?

- (a) *RegWrite*
- (b) *ALUOp<sub>1</sub>*
- (c) *MemWrite*

**Exercise 7.2** Repeat Exercise 7.1, assuming that the signal has a stuck-at-1 fault.

**Exercise 7.3** Modify the single-cycle MIPS processor to implement one of the following instructions. See Appendix B for a definition of the instructions. Mark up a copy of Figure 7.11 to indicate the changes to the datapath. Name any new control signals. Mark up a copy of Table 7.8 to show the changes to the main decoder. Describe any other changes that are required.

- (a) *sll*
- (b) *lui*
- (c) *slti*
- (d) *blez*

**Table 7.8 Main decoder truth table to mark up with changes**

Instruction	Opcode	RegWrite	RegDst	ALUSrc	Branch	MemWrite	MemtoReg	ALUOp
R-type	000000	1	1	0	0	0	0	10
lw	100011	1	0	1	0	0	1	00
sw	101011	0	X	1	0	1	X	00
beq	000100	0	X	0	1	0	X	01

**Exercise 7.4** Repeat Exercise 7.3 for the following MIPS instructions.

- (a) *jal*
- (b) *lh*
- (c) *jr*
- (d) *sr*

**Exercise 7.5** Many processor architectures have a *load with postincrement* instruction, which updates the index register to point to the next memory word after completing the load. `lwinc $rt, imm($rs)` is equivalent to the following two instructions:

```
lw $rt, imm($rs)  
addi $rs, $rs, 4
```

Repeat Exercise 7.3 for the `lwinc` instruction. Is it possible to add the instruction without modifying the register file?

**Exercise 7.6** Add a single-precision floating-point unit to the single-cycle MIPS processor to handle `add.s`, `sub.s`, and `mul.s`. Assume that you have single-precision floating-point adder and multiplier units available. Explain what changes must be made to the datapath and the controller.

**Exercise 7.7** Your friend is a crack circuit designer. She has offered to redesign one of the units in the single-cycle MIPS processor to have half the delay. Using the delays from Table 7.6, which unit should she work on to obtain the greatest speedup of the overall processor, and what would the cycle time of the improved machine be?

**Exercise 7.8** Consider the delays given in Table 7.6. Ben Bitdiddle builds a prefix adder that reduces the ALU delay by 20 ps. If the other element delays stay the same, find the new cycle time of the single-cycle MIPS processor and determine how long it takes to execute a benchmark with 100 billion instructions.

**Exercise 7.9** Suppose one of the following control signals in the multicycle MIPS processor has a stuck-at-0 fault, meaning that the signal is always 0, regardless of its intended value. What instructions would malfunction? Why?

- (a) *MemtoReg*
- (b) *ALUOp<sub>0</sub>*
- (c) *PCSrc*

**Exercise 7.10** Repeat Exercise 7.9, assuming that the signal has a stuck-at-1 fault.

**Exercise 7.11** Modify the HDL code for the single-cycle MIPS processor, given in Section 7.6.1, to handle one of the new instructions from Exercise 7.3. Enhance the testbench, given in Section 7.6.3, to test the new instruction.

**Exercise 7.12** Repeat Exercise 7.11 for the new instructions from Exercise 7.4.

**Exercise 7.13** Modify the multicycle MIPS processor to implement one of the following instructions. See Appendix B for a definition of the instructions. Mark up a copy of Figure 7.27 to indicate the changes to the datapath. Name any new

control signals. Mark up a copy of [Figure 7.39](#) to show the changes to the controller FSM. Describe any other changes that are required.

- (a) srlv
- (b) ori
- (c) xori
- (d) jr

**Exercise 7.14** Repeat [Exercise 7.13](#) for the following MIPS instructions.

- (a) bne
- (b) lb
- (c) lbu
- (d) andi

**Exercise 7.15** Repeat [Exercise 7.5](#) for the multicycle MIPS processor. Show the changes to the multicycle datapath and control FSM. Is it possible to add the instruction without modifying the register file?

**Exercise 7.16** Repeat [Exercise 7.6](#) for the multicycle MIPS processor.

**Exercise 7.17** Suppose that the floating-point adder and multiplier from [Exercise 7.16](#) each take two cycles to operate. In other words, the inputs are applied at the beginning of one cycle, and the output is available in the second cycle. How does your answer to [Exercise 7.16](#) change?

**Exercise 7.18** Your friend, the crack circuit designer, has offered to redesign one of the units in the multicycle MIPS processor to be much faster. Using the delays from [Table 7.6](#), which unit should she work on to obtain the greatest speedup of the overall processor? How fast should it be? (Making it faster than necessary is a waste of your friend's effort.) What is the cycle time of the improved processor?

**Exercise 7.19** Repeat [Exercise 7.8](#) for the multicycle processor. Assume the instruction mix of [Example 7.7](#).

**Exercise 7.20** Suppose the multicycle MIPS processor has the component delays given in [Table 7.6](#). Alyssa P. Hacker designs a new register file that has 40% less power but twice as much delay. Should she switch to the slower but lower power register file for her multicycle processor design?

**Exercise 7.21** Goliath Corp claims to have a patent on a three-ported register file. Rather than fighting Goliath in court, Ben Bitdiddle designs a new register file that has only a single read/write port (like the combined instruction and data memory). Redesign the MIPS multicycle datapath and controller to use his new register file.

**Exercise 7.22** What is the CPI of the redesigned multicycle MIPS processor from Exercise 7.21? Use the instruction mix from Example 7.7.

**Exercise 7.23** How many cycles are required to run the following program on the multicycle MIPS processor? What is the CPI of this program?

```

addi $s0, $0, done # result = 5

while:
    beq $s0, $0, done # if result > 0, execute while block
    addi $s0, $s0, -1 # while block: result = result - 1
    j     while

done:

```

**Exercise 7.24** Repeat Exercise 7.23 for the following program.

```

add  $s0, $0, $0      # i = 0
add  $s1, $0, $0      # sum = 0
addi $t0, $0, 10      # $t0 = 10

loop:
    slt  $t1, $s0, $t0  # if (i < 10), $t1 = 1, else $t1 = 0
    beq  $t1, $0, done   # if $t1 == 0 (i >= 10), branch to done
    add  $s1, $s1, $s0    # sum = sum + i
    addi $s0, $s0, 1      # increment i
    j     loop
done:

```

**Exercise 7.25** Write HDL code for the multicycle MIPS processor. The processor should be compatible with the following top-level module. The `mem` module is used to hold both instructions and data. Test your processor using the testbench from Section 7.6.3.

```

module top(input logic      clk, reset,
            output logic [31:0] writedata, adr,
            output logic         memwrite);

    logic [31:0] readdata;

    // instantiate processor and memories
    mips mips(clk, reset, adr, writedata, memwrite, readdata);
    mem mem(clk, memwrite, adr, writedata, readdata);

endmodule

module mem(input logic      clk, we,
            input logic [31:0] a, wd,
            output logic [31:0] rd);

    logic [31:0] RAM[63:0];

initial
begin
    $readmemh("memfile.dat", RAM);
end

```

```
assign rd=RAM[a[31:2]]; // word aligned
always @(posedge clk)
  if (we)
    RAM[a[31:2]] <= wd;
endmodule
```

**Exercise 7.26** Extend your HDL code for the multicycle MIPS processor from [Exercise 7.25](#) to handle one of the new instructions from [Exercise 7.13](#). Enhance the testbench to test the new instruction.

**Exercise 7.27** Repeat [Exercise 7.26](#) for one of the new instructions from [Exercise 7.14](#).

**Exercise 7.28** The pipelined MIPS processor is running the following program. Which registers are being written, and which are being read on the fifth cycle?

```
addi $s1, $s2, 5
sub $t0, $t1, $t2
lw   $t3, 15($s1)
sw   $t5, 72($t0)
or   $t2, $s4, $s5
```

**Exercise 7.29** Repeat [Exercise 7.28](#) for the following MIPS program. Recall that the pipelined MIPS processor has a hazard unit.

```
add $s0, $t0, $t1
sub $s1, $t2, $t3
and $s2, $s0, $s1
or  $s3, $t4, $t5
slt $s4, $s2, $s3
```

**Exercise 7.30** Using a diagram similar to [Figure 7.52](#), show the forwarding and stalls needed to execute the following instructions on the pipelined MIPS processor.

```
add $t0, $s0, $s1
sub $t0, $t0, $s2
lw   $t1, 60($t0)
and $t2, $t1, $t0
```

**Exercise 7.31** Repeat [Exercise 7.30](#) for the following instructions.

```
add $t0, $s0, $s1
lw   $t1, 60($s2)
sub $t2, $t0, $s3
and $t3, $t1, $t0
```

**Exercise 7.32** How many cycles are required for the pipelined MIPS processor to issue all of the instructions for the program in [Exercise 7.23](#)? What is the CPI of the processor on this program?

**Exercise 7.33** Repeat [Exercise 7.32](#) for the instructions of the program in [Exercise 7.24](#).

**Exercise 7.34** Explain how to extend the pipelined MIPS processor to handle the addi instruction.

**Exercise 7.35** Explain how to extend the pipelined processor to handle the j instruction. Give particular attention to how the pipeline is flushed when a jump takes place.

**Exercise 7.36** Examples 7.9 and 7.10 point out that the pipelined MIPS processor performance might be better if branches take place during the Execute stage rather than the Decode stage. Show how to modify the pipelined processor from Figure 7.58 to branch in the Execute stage. How do the stall and flush signals change? Redo Examples 7.9 and 7.10 to find the new CPI, cycle time, and overall time to execute the program.

**Exercise 7.37** Your friend, the crack circuit designer, has offered to redesign one of the units in the pipelined MIPS processor to be much faster. Using the delays from Table 7.6 and Example 7.10, which unit should she work on to obtain the greatest speedup of the overall processor? How fast should it be? (Making it faster than necessary is a waste of your friend's effort.) What is the cycle time of the improved processor?

**Exercise 7.38** Consider the delays from Table 7.6 and Example 7.10. Now suppose that the ALU were 20% faster. Would the cycle time of the pipelined MIPS processor change? What if the ALU were 20% slower?

**Exercise 7.39** Suppose the MIPS pipelined processor is divided into 10 stages of 400 ps each, including sequencing overhead. Assume the instruction mix of Example 7.7. Also assume that 50% of the loads are immediately followed by an instruction that uses the result, requiring six stalls, and that 30% of the branches are mispredicted. The target address of a branch or jump instruction is not computed until the end of the second stage. Calculate the average CPI and execution time of computing 100 billion instructions from the SPECINT2000 benchmark for this 10-stage pipelined processor.

**Exercise 7.40** Write HDL code for the pipelined MIPS processor. The processor should be compatible with the top-level module from HDL Example 7.13. It should support all of the instructions described in this chapter, including addi and j (see Exercises 7.34 and 7.35). Test your design using the testbench from HDL Example 7.12.

**Exercise 7.41** Design the hazard unit shown in Figure 7.58 for the pipelined MIPS processor. Use an HDL to implement your design. Sketch the hardware that a synthesis tool might generate from your HDL.

**Exercise 7.42** A *nonmaskable interrupt* (NMI) is triggered by an input pin to the processor. When the pin is asserted, the current instruction should finish, then the processor should set the Cause register to 0 and take an exception. Show how to modify the multicycle processor in Figures 7.63 and 7.64 to handle nonmaskable interrupts.

## Interview Questions

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The following exercises present questions that have been asked at interviews for digital design jobs.

**Question 7.1** Explain the advantages of pipelined microprocessors.

**Question 7.2** If additional pipeline stages allow a processor to go faster, why don't processors have 100 pipeline stages?

**Question 7.3** Describe what a hazard is in a microprocessor and explain ways in which it can be resolved. What are the pros and cons of each way?

**Question 7.4** Describe the concept of a superscalar processor and its pros and cons.