

# nnass5f\_karnati

November 5, 2019

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In [100]: #importing the dataset
          from sklearn.datasets import load_digits, fetch_openml
          from sklearn.model_selection import train_test_split
          import numpy as np
          import matplotlib.pyplot as plt
          from tqdm import tqdm

          #fetching training data of 60000 and testing data of 10000
          #splitting into train,test
          x,y = fetch_openml('mnist_784', version=1, return_X_y=True)
          xtrain, xtest, ytrain, ytest = train_test_split(x,y, train_size=60000, test_size=10000)

          xtrain = xtrain.astype(np.float)
          xtest = xtest.astype(np.float)
          xtrain = xtrain/255
          xtest = xtest/255

          #converting output to int
          ytrain = ytrain.astype(np.int)
          ytest = ytest.astype(np.int)

          #we are using one hot encodign for classification
          ytrain = one_hot_encoding(ytrain)
          yt = one_hot_encoding(ytest)

          def one_hot_encoding(output, num_labels=10):
              one_h = np.zeros((output.shape[0], num_labels))
              for x, y in enumerate(output):
                  one_h[x,y] = 1.0
              return one_h

In [112]: #Activation fn chosen = Sigmoid
          def sigmoid(z):
              s = 1 / (1 + np.exp(-z))
              return s

In [113]: class mnistq(object):
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def __init__(self, num_hidden, epoch=40, alpha=0.01):
    self.epoch = epoch
    self.alpha = alpha #learning rate
    self.input_size = 784
    self.output_size = 10
    self.hidden = num_hidden #neurons in the hidden layer - given below

    print('Initialized with random W')
    print('*****')
    self.weight1 = np.random.normal(0, 0.2, [self.input_size, self.hidden]) #wei
    self.bias1 = np.zeros((1, self.hidden)) # bias for weight 1
    self.weight2 = np.random.normal(0, 0.2, [self.hidden, self.output_size]) #we
    self.bias2 = np.zeros((1, self.output_size)) # bias for weight 2

#Used to train the network - takes the training input and output, and batch value
def train(self, training_inputs, training_outputs, xtest, yt, batch):

    print('Training with a '+str(batch)+' batch size')
    print('*****')
    #momentum value
    beta = 0.3
    #intializing previous gradients
    prev_grad_w2 = 0
    prev_grad_w1 = 0

    #for the number of epochs specified
    pbar = tqdm(range(self.epoch))
    for k in pbar:
        it = 0
        avg_error = 0
        while it < training_inputs.shape[0]:

            #take the batch size of inputs and outputs
            tx = training_inputs[it:it+batch]
            ty = training_outputs[it:it+batch]

            # Forward propogation
            z1 = np.dot(tx, self.weight1) + self.bias1
            a1 = sigmoid(z1)
            z2 = np.dot(a1, self.weight2) + self.bias2
            y = sigmoid(z2)

            #Backpropogation and error calculation
            dy2 = y*(1-y) #derivative of final output
            dy1 = a1*(1-a1) #derivative of hidden layer output
            output_error = np.subtract(ty,y) #error in output layer
            avg_error += np.mean(output_error)
            output_delta = output_error * dy2 #element wise mulitplication

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hidden_error = np.dot(output_delta, self.weight2.T)
hidden_layer_delta = hidden_error * dy1 #element wise multiplication

# using momentum, beta set to 0.3
momentum_factor_w1 = beta * prev_grad_w1
momentum_factor_w2 = beta * prev_grad_w2

#Backpropogation calculation of each weight and bias
dW2 = np.dot(a1.T, output_delta) # forward * backward
db2 = np.sum(output_delta, axis = 0, keepdims = True)
dW1 = np.dot(tx.T, hidden_layer_delta)
db1 = np.sum(hidden_layer_delta, axis = 0, keepdims = True)

#update weights and bias
self.weight2 += (1./batch * self.alpha * dW2) + momentum_factor_w2
self.bias2 += 1./batch * self.alpha * db2
self.weight1 += (1./batch * self.alpha * dW1) + momentum_factor_w1
self.bias1 += 1./batch * self.alpha * db1

#save the graident to use in next batch iteration
prev_grad_w1 = 1./batch * self.alpha * dW1
prev_grad_w2 = 1./batch * self.alpha * dW2

#input("Wait")

#increment to access next set of inputs
it = it + batch

avg_error /= float(training_inputs.shape[0])
pbar.set_description("Error: %.4f" %(avg_error))
print("Training acc at epoch:",k)
trainacc = self.test(training_inputs, training_outputs)
print("Pred acc at epoch:",k)
predicacc = self.test(xtest, yt)
prederr.append((1-(predicacc/100)))
trainerr.append(1-(trainacc/100))

# accuracy testing - for training and testing
def test(self, test_input, test_output):

    #forward feed
    z1 = np.dot(test_input, self.weight1) + self.bias1
    a1 = sigmoid(z1)
    z2 = np.dot(a1, self.weight2) + self.bias2
    y = sigmoid(z2)

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a = np.zeros((10000, 1))

# To see how accurate the neural network is compared to the correct values
acc = 0.0
for i in range(10000):
    if np.argmax(y[i]) == np.argmax(test_output[i]):
        acc += 1
    a[i] = np.argmax(y[i])
accper = acc / 10000 * 100
print( accper, "%")
return accper

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In [114]: #driver func
          trainerr = []
          prederr = []
          mnt = mnistq(128)
          #Training
          mnt.train(xtrain,ytrain,xtest, yt,4)
          print("Final accuracy of test data")
          prediction = mnt.test(xtest, yt)

```

Initialized with random W

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Training with a 4 batch size

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0%|

Error: -0.0066: 0%|

Training acc at epoch: 0

84.78999999999999 %

Pred acc at epoch: 0

85.77 %

Error: -0.0066: 2%|

| 1/40 [

Error: -0.0038: 2%|

| 1/40 [

Training acc at epoch: 1  
87.82 %  
Pred acc at epoch: 1  
88.5 %

Error: -0.0038: 5%|

| 2/40 [00:

Error: -0.0025: 5%|

| 2/40 [00:

Training acc at epoch: 2  
89.34 %  
Pred acc at epoch: 2  
89.69 %

Error: -0.0025: 8%|

| 3/40 [00:

Error: -0.0019: 8%|

| 3/40 [00:

Training acc at epoch: 3  
90.10000000000001 %  
Pred acc at epoch: 3  
90.38000000000001 %

Error: -0.0019: 10%|

| 4/40 [00:40:

Error: -0.0016: 10%|

| 4/40 [00:50:

Training acc at epoch: 4  
90.68 %  
Pred acc at epoch: 4  
91.0 %

Error: -0.0016: 12%| | 5/40 [00:51<00:00]

Error: -0.0013: 12%| | 5/40 [01:02<00:00]

Training acc at epoch: 5  
91.16 %  
Pred acc at epoch: 5  
91.23 %

Error: -0.0013: 15%| | 6/40 [01:03<00:00]

Error: -0.0012: 15%| | 6/40 [01:18<00:00]

Training acc at epoch: 6  
91.38 %  
Pred acc at epoch: 6  
91.66 %

Error: -0.0012: 18%| | 7/40 [01:19<00:00]

Error: -0.0010: 18%| | 7/40 [01:33<00:00]

Training acc at epoch: 7  
91.78 %  
Pred acc at epoch: 7  
92.0 %

Error: -0.0010: 20%| | 8/40 [01:34<00:00]

Error: -0.0010: 20%| | 8/40 [01:47<00:00]

Training acc at epoch: 8  
92.03 %

Pred acc at epoch: 8  
92.22 %

Error: -0.0010: 22%|

| 9/40 [01:48<06:54, 1

Error: -0.0009: 22%|

| 9/40 [01:57<06:54, 1

Training acc at epoch: 9  
92.17999999999999 %  
Pred acc at epoch: 9  
92.53 %

Error: -0.0009: 25%|

| 10/40 [01:58<06:14, 12

Error: -0.0008: 25%|

| 10/40 [02:10<06:14, 12

Training acc at epoch: 10  
92.35 %  
Pred acc at epoch: 10  
92.78 %

Error: -0.0008: 28%|

| 11/40 [02:11<06:03, 12.5

Error: -0.0008: 28%|

| 11/40 [02:31<06:03, 12.5

Training acc at epoch: 11  
92.64 %  
Pred acc at epoch: 11  
93.0 %

Error: -0.0008: 30%| | 12/40 [02:32<07:06, 15.25s/it]

Error: -0.0007: 30%| | 12/40 [02:51<07:06, 15.25s/it]

Training acc at epoch: 12  
92.9 %  
Pred acc at epoch: 12  
93.24 %

Error: -0.0007: 32%| | 13/40 [02:52<07:29, 16.63s/it]

Error: -0.0007: 32%| | 13/40 [03:07<07:29, 16.63s/it]

Training acc at epoch: 13  
93.06 %  
Pred acc at epoch: 13  
93.35 %

Error: -0.0007: 35%| | 14/40 [03:08<07:05, 16.35s/it]

Error: -0.0007: 35%| | 14/40 [03:20<07:05, 16.35s/it]

Training acc at epoch: 14  
93.26 %  
Pred acc at epoch: 14  
93.5 %

Error: -0.0007: 38%| | 15/40 [03:21<06:22, 15.31s/it]

Error: -0.0007: 38%| | 15/40 [03:35<06:22, 15.31s/it]

Training acc at epoch: 15  
93.41000000000001 %



Pred acc at epoch: 15  
93.67 %

Error: -0.0007: 40%| | 16/40 [03:36<06:05, 15.21s/it]

Error: -0.0006: 40%| | 16/40 [03:51<06:05, 15.21s/it]

Training acc at epoch: 16  
93.63 %  
Pred acc at epoch: 16  
93.84 %

Error: -0.0006: 42%| | 17/40 [03:52<05:55, 15.47s/it]

Error: -0.0006: 42%| | 17/40 [04:05<05:55, 15.47s/it]

Training acc at epoch: 17  
93.78 %  
Pred acc at epoch: 17  
93.92 %

Error: -0.0006: 45%| | 18/40 [04:06<05:30, 15.04s/it]

Error: -0.0006: 45%| | 18/40 [04:18<05:30, 15.04s/it]

Training acc at epoch: 18  
93.89 %  
Pred acc at epoch: 18  
94.01 %

Error: -0.0006: 48%| | 19/40 [04:18<04:58, 14.21s/it]

Error: -0.0006: 48%| | 19/40 [04:32<04:58, 14.21s/it]

Training acc at epoch: 19  
94.02000000000001 %  
Pred acc at epoch: 19  
94.08999999999999 %

Error: -0.0006: 50%| | 20/40 [04:33<04:48, 14.44s/it]

Error: -0.0006: 50%| | 20/40 [04:51<04:48, 14.44s/it]

Training acc at epoch: 20  
94.17 %  
Pred acc at epoch: 20  
94.23 %

Error: -0.0006: 52%| | 21/40 [04:52<04:57, 15.64s/it]

Error: -0.0006: 52%| | 21/40 [05:04<04:57, 15.64s/it]

Training acc at epoch: 21  
94.27 %  
Pred acc at epoch: 21  
94.31 %

Error: -0.0006: 55%| | 22/40 [05:04<04:25, 14.75s/it]

Error: -0.0006: 55%| | 22/40 [05:20<04:25, 14.75s/it]

Training acc at epoch: 22  
94.48 %

Pred acc at epoch: 22  
94.39 %

Error: -0.0006: 57%| | 23/40 [05:21<04:19, 15.28s/it]

Error: -0.0006: 57%| | 23/40 [05:31<04:19, 15.28s/it]

Training acc at epoch: 23  
94.57 %  
Pred acc at epoch: 23  
94.5 %

Error: -0.0006: 60%| | 24/40 [05:32<03:45, 14.09s/it]

Error: -0.0005: 60%| | 24/40 [05:45<03:45, 14.09s/it]

Training acc at epoch: 24  
94.64 %  
Pred acc at epoch: 24  
94.57 %

Error: -0.0005: 62%| | 25/40 [05:47<03:34, 14.30s/it]

Error: -0.0005: 62%| | 25/40 [06:00<03:34, 14.30s/it]

Training acc at epoch: 25  
94.77 %  
Pred acc at epoch: 25  
94.64 %

Error: -0.0005: 65%| | 26/40 [06:00<03:16, 14.03s/it]

Error: -0.0005: 65%| | 26/40 [06:14<03:16, 14.03s/it]

Training acc at epoch: 26  
94.84 %  
Pred acc at epoch: 26  
94.72 %

Error: -0.0005: 68%| | 27/40 [06:15<03:03, 14.14s/it]

Error: -0.0005: 68%| | 27/40 [06:27<03:03, 14.14s/it]

Training acc at epoch: 27  
95.0 %  
Pred acc at epoch: 27  
94.74000000000001 %

Error: -0.0005: 70%| | 28/40 [06:27<02:44, 13.73s/it]

Error: -0.0005: 70%| | 28/40 [06:37<02:44, 13.73s/it]

Training acc at epoch: 28  
95.14 %  
Pred acc at epoch: 28  
94.8 %

Error: -0.0005: 72%| | 29/40 [06:38<02:20, 12.80s/it]

Error: -0.0005: 72%| | 29/40 [06:49<02:20, 12.80s/it]

Training acc at epoch: 29  
95.21 %

Pred acc at epoch: 29  
94.85 %

Error: -0.0005: 75%| | 30/40 [06:49<02:03, 12.33s/it]

Error: -0.0005: 75%| | 30/40 [07:01<02:03, 12.33s/it]

Training acc at epoch: 30  
95.26 %  
Pred acc at epoch: 30  
94.98 %

Error: -0.0005: 78%| | 31/40 [07:02<01:51, 12.34s/it]

Error: -0.0005: 78%| | 31/40 [07:11<01:51, 12.34s/it]

Training acc at epoch: 31  
95.33 %  
Pred acc at epoch: 31  
95.03 %

Error: -0.0005: 80%| | 32/40 [07:12<01:33, 11.69s/it]

Error: -0.0005: 80%| | 32/40 [07:24<01:33, 11.69s/it]

Training acc at epoch: 32  
95.39999999999999 %  
Pred acc at epoch: 32  
95.1 %

Error: -0.0005: 82%| | 33/40 [07:25<01:24, 12.05s/it]

Error: -0.0005: 82%| | 33/40 [07:35<01:24, 12.05s/it]

Training acc at epoch: 33  
95.44 %  
Pred acc at epoch: 33  
95.16 %

Error: -0.0005: 85%| | 34/40 [07:36<01:10, 11.71s/it]

Error: -0.0005: 85%| | 34/40 [07:47<01:10, 11.71s/it]

Training acc at epoch: 34  
95.52000000000001 %  
Pred acc at epoch: 34  
95.19999999999999 %

Error: -0.0005: 88%| | 35/40 [07:47<00:58, 11.67s/it]

Error: -0.0005: 88%| | 35/40 [07:59<00:58, 11.67s/it]

Training acc at epoch: 35  
95.63000000000001 %  
Pred acc at epoch: 35  
95.27 %

Error: -0.0005: 90%| | 36/40 [08:00<00:47, 11.95s/it]

Error: -0.0005: 90%| | 36/40 [08:12<00:47, 11.95s/it]

Training acc at epoch: 36  
95.7 %

Pred acc at epoch: 36  
95.28999999999999 %

Error: -0.0005: 92%| | 37/40 [08:12<00:36, 12.10s/it]

Error: -0.0005: 92%| | 37/40 [08:26<00:36, 12.10s/it]

Training acc at epoch: 37  
95.75 %  
Pred acc at epoch: 37  
95.33 %

Error: -0.0005: 95%| | 38/40 [08:26<00:25, 12.72s/it]

Error: -0.0005: 95%| | 38/40 [08:38<00:25, 12.72s/it]

Training acc at epoch: 38  
95.78999999999999 %  
Pred acc at epoch: 38  
95.36 %

Error: -0.0005: 98%| | 39/40 [08:39<00:12, 12.75s/it]

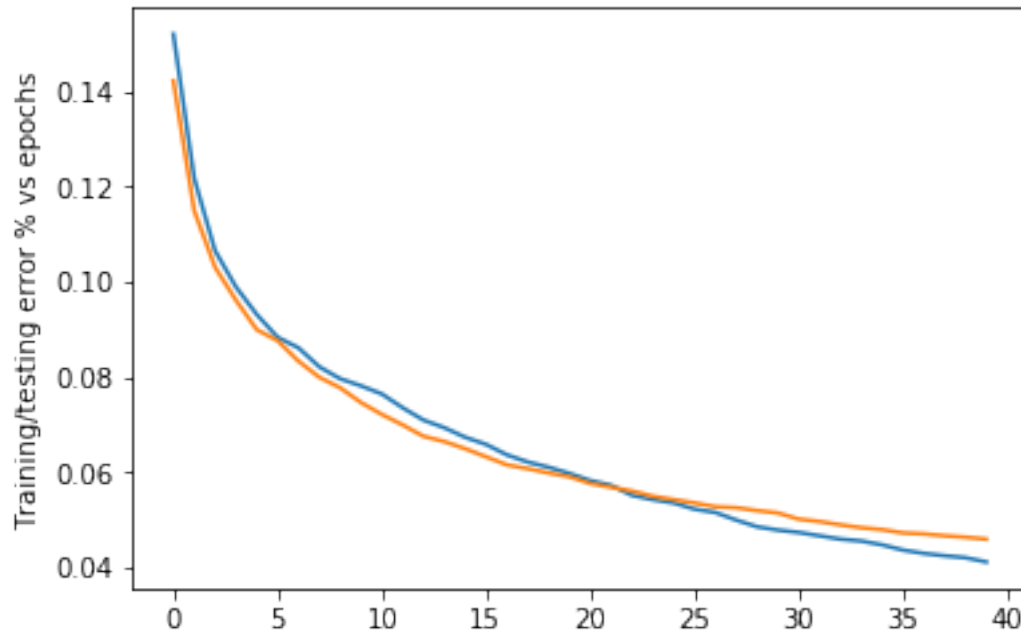
Error: -0.0005: 98%| | 39/40 [08:50<00:12, 12.75s/it]

Training acc at epoch: 39  
95.88 %  
Pred acc at epoch: 39  
95.39999999999999 %

Error: -0.0005: 100%|| 40/40 [08:51<00:00, 12.46s/it]

Final accuracy of test data  
95.39999999999999 %

```
In [115]: plt.plot(trainerr)
plt.plot(prederr)
plt.ylabel('Training/testing error % vs epochs')
plt.show()
#Training = Blue line, Testing = brown line
```



Learning alpha = 0.01, beta-momentum = 0.3, hidden units = 128, batch size = 4 , epochs =40