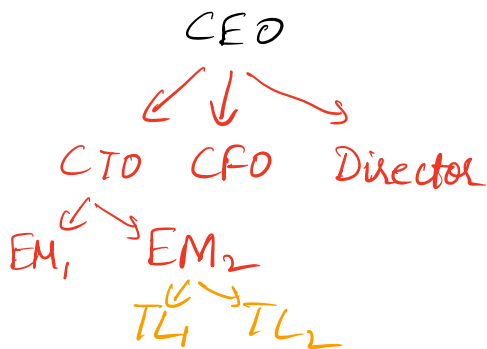
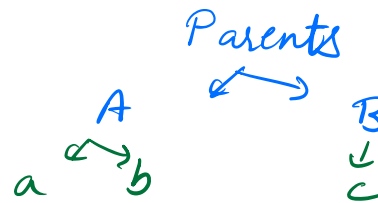


Hierarchy Org structure

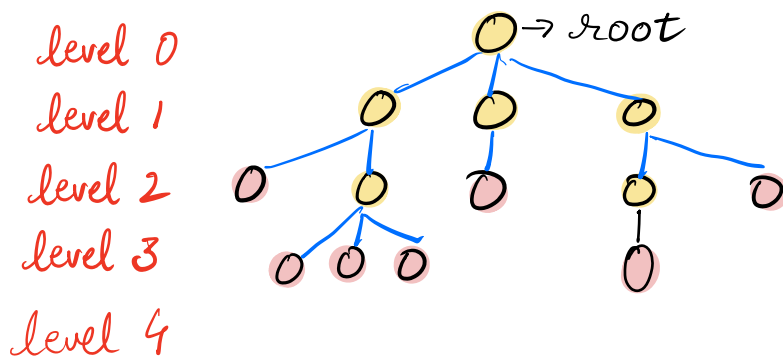


Family Structure



Vishal
Abhay

○



- Non Leaf Node
- Leaf Node
no children

○ → Node

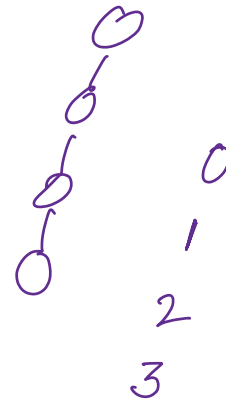
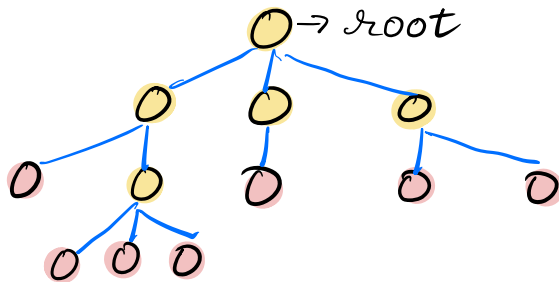
/ → Edge

Relationships

- Parent
- Child
- Siblings
 - ↳ originating from same parent
- Cousins
 - ↳ originating from same grand parent.
 - (same level is needed)

Depth

level 0
level 1
level 2
level 3



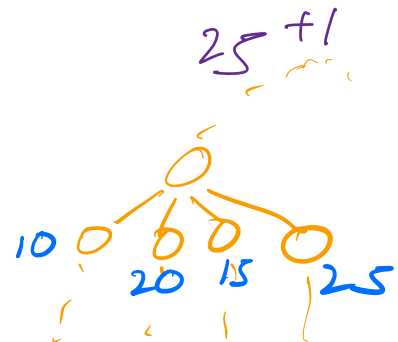
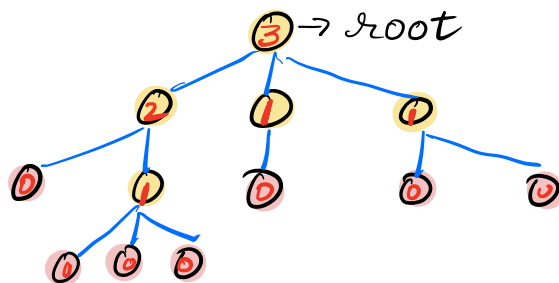
level = depth [Level is 0 index]

Depth(node) : Length of path from root to node

$$\text{Depth}(\text{node}) = \text{depth}(\text{par}) + 1$$

HEIGHT

level 0
level 1
level 2
level 3



Height(node) : Length of **longest** path from node to the deepest descendant leaf node.

$$\text{Height}(\text{node}) = \max(\text{height}(\text{child})) + 1$$

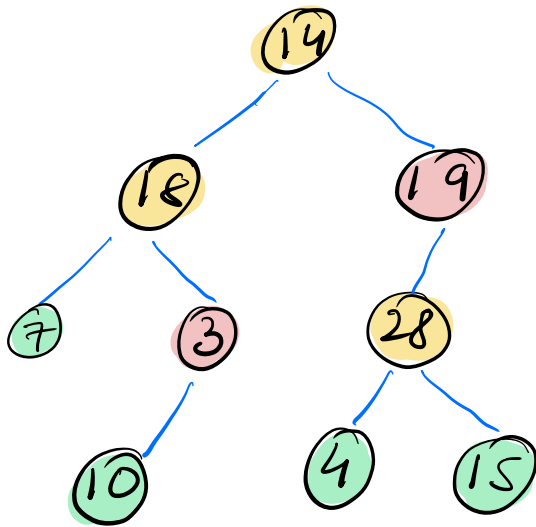
$$\text{Height}(\text{leaf}) = 0$$

Naming of trees

At max 2 children : **BINARY TREE**

At max 3 children : **TERNARY TREE**

At max N children : **N-ary TREE**



- 0 children
- 1 children
- 2 children

BINARY TREES

```
class Node {
```

```
    int data
```

```
    Node left
```

```
    Node right
```

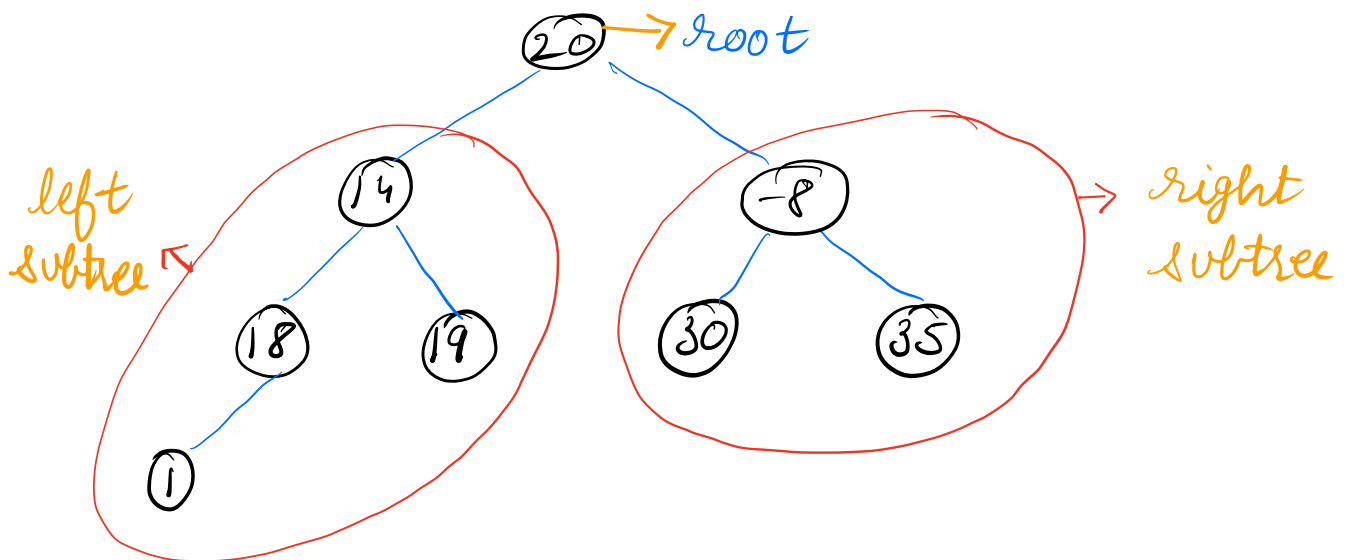
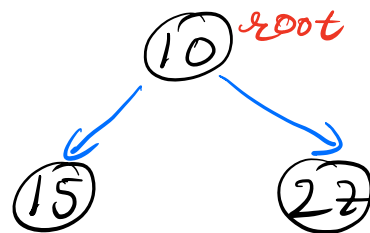
```
Node (int x) {
```

```
    data = x
```

```
    left = null
```

```
    right = null
```

```
Node root = new Node(10)  
root.left = new Node(15)  
root.right = new Node(22)
```



left subtree → Family of the left child.

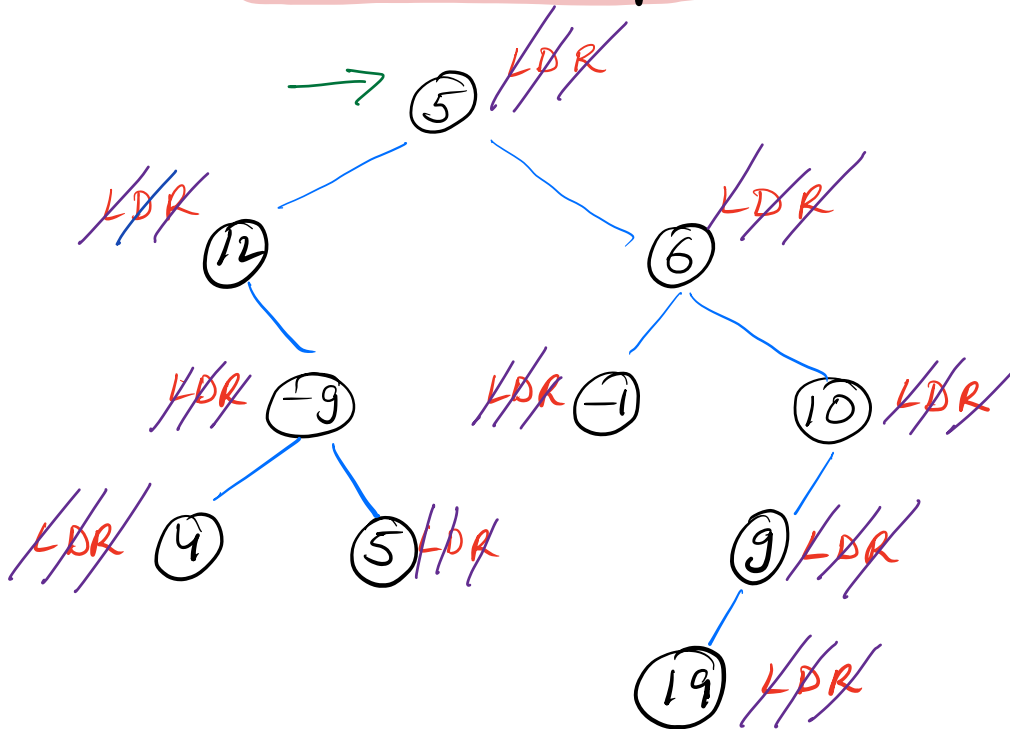
Recursion

- 1) **Assumption**: Decide what your function does, and assume it does exactly that
- 2) **Main Logic**: Solving Assumption with subproblem
- 3) **Base Condition**: When should code stop.

Tree Traversals

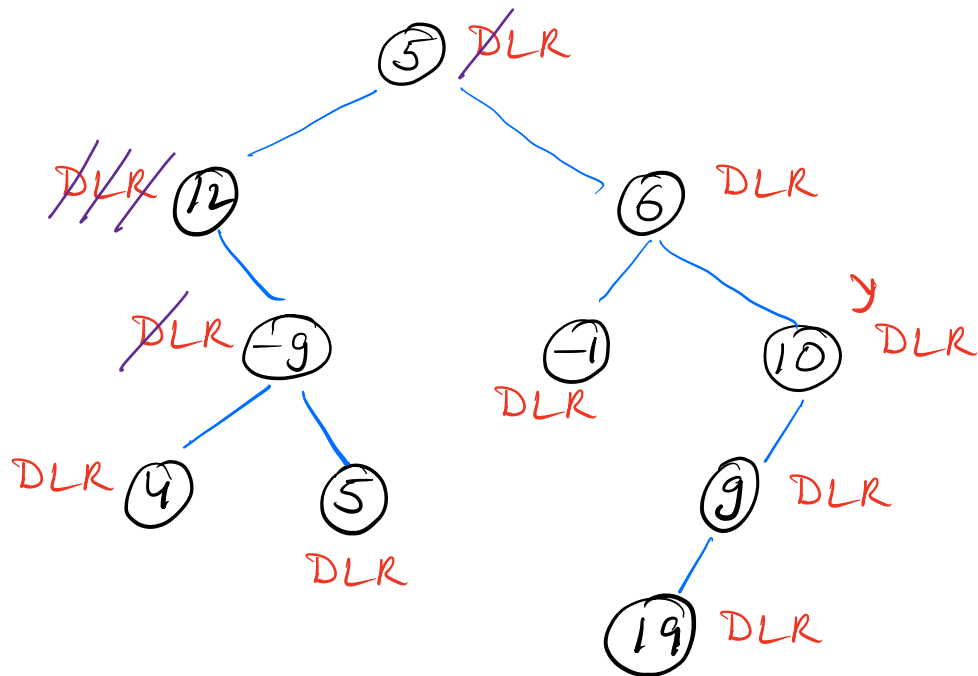
- 1) Preorder [data Left Right] DLR
- 2) Inorder [Left data Right] LDR
- 3) Postorder [Left Right data] LRD

Inorder example



Ans: 12 4 -9 5 5 -1 6
19 9 10

Pre order example



Ans: 5 12 -9 4 5 6 -1 10 9 19

Postorder LRD

4 5 -9 12 -1 19 9 10 6 5

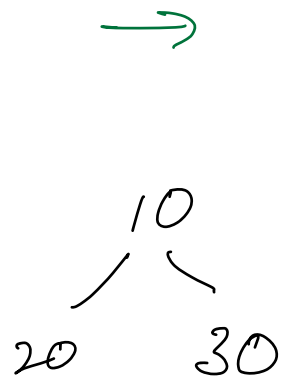
Q1 INORDER TRAVERSAL Code

Assumption: Print all node values
in inorder fashion

Base Case: if $root == null$ return

Logic: LDR
left subtree → right subtree

```
void inorder (Node root) {  
    if (root == null)  
        return  
    inorder (root.left)  
    print (root.data)  
    inorder (root.right)  
}
```



20 10 30

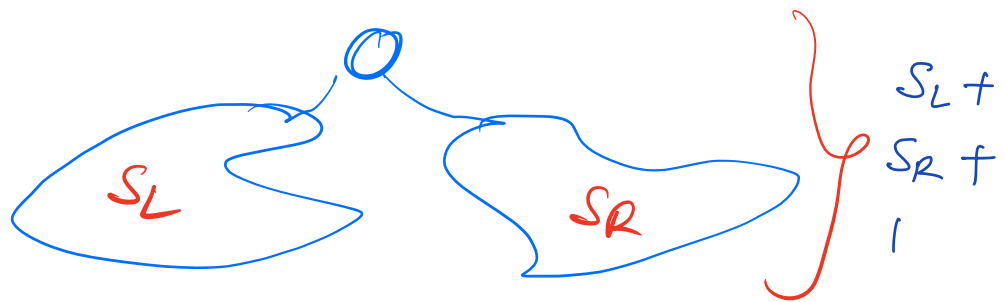
Going to parent \Rightarrow return statement
in recursive function

Q2 Given Binary Tree, calc size of tree

Assumption: Returns no of nodes in tree

Base Case: if root is NULL, ans = 0

Logic:



```
int size(Node root) {
```

```
    if (root == NULL)
        return 0
```

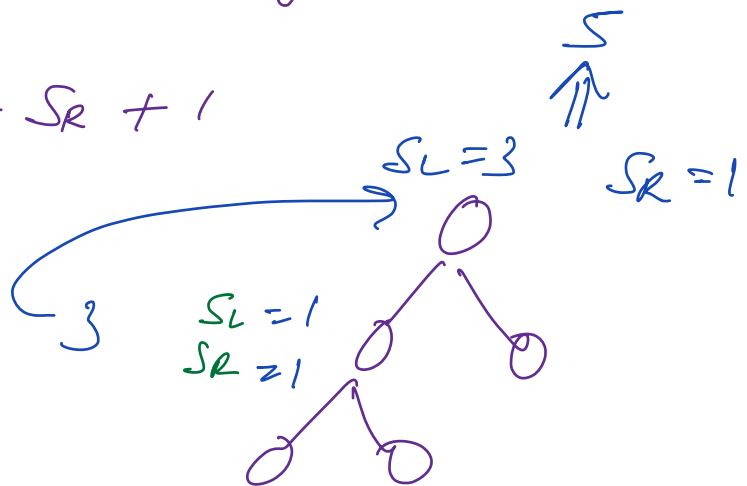
```
    S_L = size(root.left)
```

```
    S_R = size(root.right)
```

```
    return S_L + S_R + 1
```

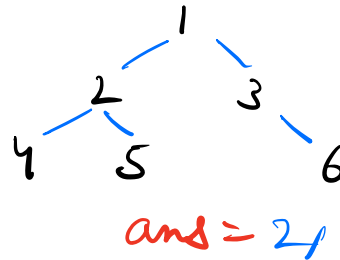
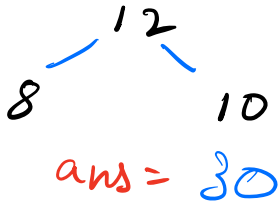
```
}
```

TC: $O(N)$
SC: $O(N)$



Q3 Given Binary Tree, find sum of node values of all nodes.

Eg:



Assumption: return sum of all nodes

Base Case: if root is NULL, ans = 0

Logic:

```
int sum(Node root) {
```

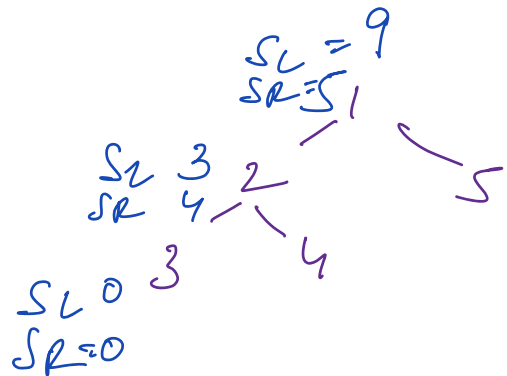
```
    if (root == NULL)
        return 0
```

```
    sum-l = sum(root.left)
```

```
    sum-r = sum(root.right)
```

```
    return sum-l + sum-r + root.data
```

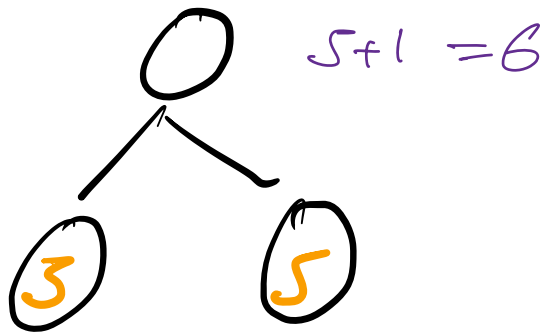
```
}
```



TC: $O(N)$

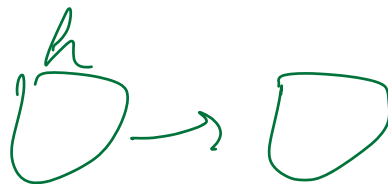
SC: $O(N)$

Q4) Height of a tree



```
int height (root) {  
    if (root == null)  
        return 0  
    hl = height (root.left)  
    hr = height (root.right)  
    return max(hl, hr) + 1  
}
```

{done}



—

1

2

3

