

Soumya Sambit Mangaraj

Senior Software Engineer @Goldman Sachs

Ex : SDE 2 @PayPal | GATE AIR 485

5+ years of Industry Experience

2+ years of Teaching Experience

Today's Contest :

1. Print Zig-Zag
2. Numbers smaller than current number
3. Longest subarray with sum K

Print Zig Zag

Problem Description

Given a positive integer N , print a pattern of numbers based on observation of following examples:

$N \rightarrow 1$

O/P $1 \rightarrow 1\ 1\ 1$

$N \rightarrow 2$ " "

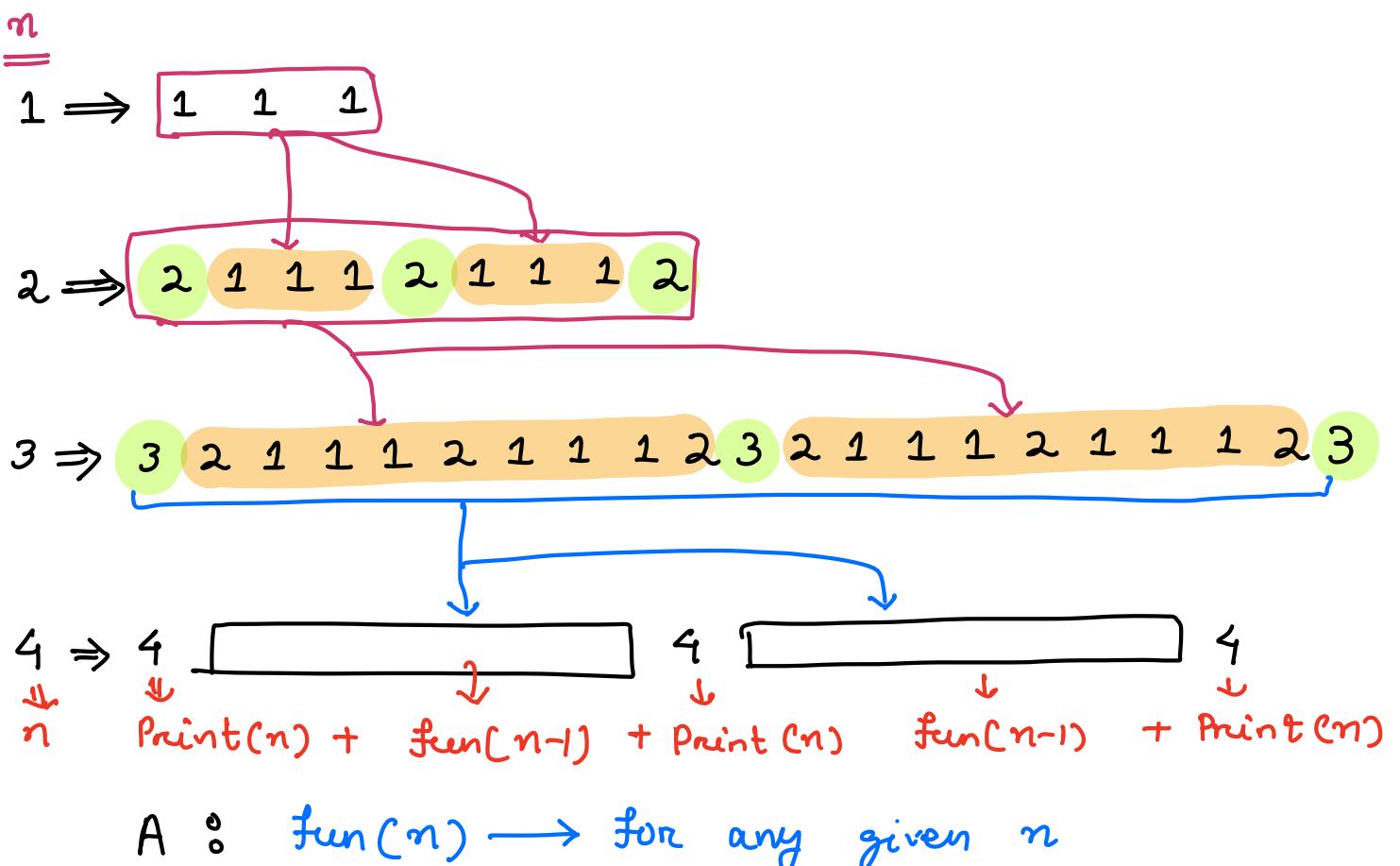
O/P $2 \rightarrow 2\ 1\ 1\ 1\ 2\ 1\ 1\ 1\ 2$

$N \rightarrow 3$

O/P $3 \rightarrow 3\ 2\ 1\ 1\ 1\ 2\ 1\ 1\ 1\ 2\ 3\ 2\ 1\ 1\ 1\ 2\ 1\ 1\ 1\ 2\ 3$

Problem Constraints

$1 \leq N \leq 10$



$$F : \text{Print}(n) + \text{fun}(n-1) + \text{Print}(n) + \text{fun}(n-1) + \text{Print}(n)$$

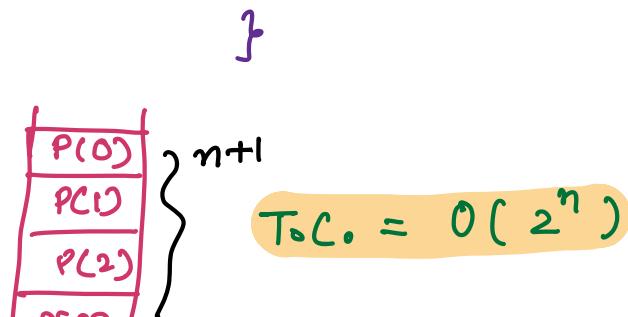
Print zigzag

B : $n=0 \Rightarrow \text{return};$

```

void PrintZigZag (int n) {
    if (n == 0) { return; } // Base Case
    System.out.print(n + " ");
    2 ← printZigZag (n-1); // 1st Recursion Call
    System.out.print(n + " ");
    2 ← printZigZag (n-1); // 2nd Recursion Call
    System.out.print(n + " ");
}

```



$$T.C. = O(2^n)$$

$$T(n) = T(n-1) + T(n-2)$$

$$\downarrow$$

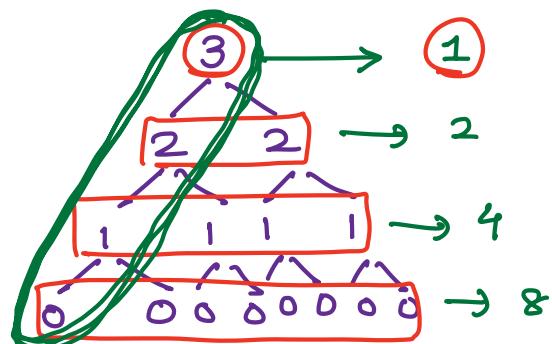
$$T.C. = O(2^n)$$

$$S.C. = O(n)$$

T.C.

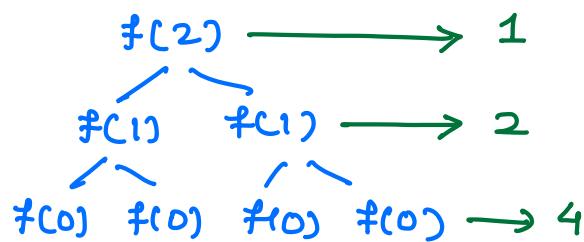
$$1+2+4 = 7 = 2^3 - 1$$

$$n \rightarrow 2^{n+1} - 1 = O(2^n)$$



$$\begin{aligned}
& 1+2+4+8+\dots = \\
& \underbrace{1+2+4+8}_{\text{Sum of G.P.}} = 2^n
\end{aligned}$$

of function calls



$$n \rightarrow 2^{n+1} - 1 = O(2^n)$$

Ques/ Given the integer array A of size N, find out how many no. in the array are smaller than it. That is for each $A[i]$ you have to count the no. of valid j such that $A[j] < A[i]$

Constraints

$$1 \leq N \leq 10^5$$

$$0 \leq A[i] \leq 10^3$$

In simple words, they are asking you to calculate no. of ele smaller than the current ele

Ex 1: $arr[5] = \{8, 1, 2, 2, 3, 4\}$
 $ans[5] = \{4, 0, 1, 1, 3\}$

Ex 2: $arr[8] = [5, 1, 6, 2, 8, 9, 6, 11]$

$ans[8] = [2, 0, 3, 1, 5, 6, 3, 7]$

Ex 3: $arr[4] = [5, 5, 5, 5]$

$ans[4] = [0, 0, 0, 0]$

Idea 1 (Brute force): For every element; Get count of no of elements lesser than current elements.

$$T.C = O(n \cdot n) = O(n^2)$$

$$S.C = O(1)$$

Optimised Idea -

	0	1	2	3	4	5	6	7	8	9
arr[10] =	3	4	2	4	2	7	1	7	2	7

Step 1 : Iterate on this Arr; find $\max = 7$

1. All elements $\Rightarrow [0 \dots 7]$

2. Need frequency.

Step 2 : Iterate on Arr; Store frequency ($\text{cnt}[\max+1]$)

	0	1	2	3	4	5	6	7	8	9
arr[10] =	3	4	2	4	2	7	1	7	2	7

→

0	1	2	3	4	5	6	7
0	1	2	1	1	1	0	0

$\max = 7$

$\text{cnt}[8] =$

0	1	2	3	4	5	6	7
2	3	2	1	2	0	0	3

$\text{cnt}[8] =$

0	1	2	3	4	5	6	7
0	1	3	1	2	0	0	3

How many elements are smaller than 4 ?

↪ $\text{cnt}[0] + \text{cnt}[1] + \text{cnt}[2] + \text{cnt}[3]$

$$= \underline{\text{cnt}[0 \dots 3]} = 0 + 1 + 3 + 1 = 5$$

→ Prefix Sum

of elements smaller than 5 = $\text{cnt}[0 \dots 4]$

$$3 = \text{cnt}[0 \dots 2]$$

$$7 = \text{cnt}[0 \dots 6]$$

} Prefix Sum

Eg: $arr[10] = [3 \ 4 \ 2 \ 4 \ 2 \ 7 \ 1 \ 7 \ 2 \ 7]$

$$\max = 7$$

\downarrow

$[0 \dots 7]$

$int[m+1] freq:$

0	1	2	3	4	5	6	7
0	1	3	1	2	0	0	3

value

count

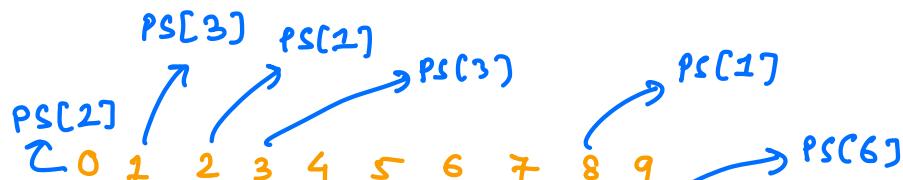
$int[m+1] PSum:$

0	1	2	3	4	5	6	7
0	1	4	5	7	7	7	10

count of # of elements ≤ 2

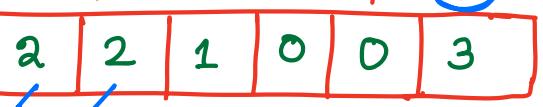
count of # of elements < 3

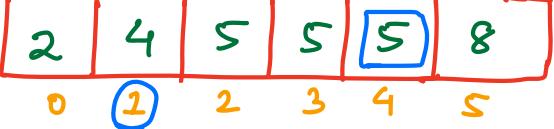
count of # of elements $\leq 3 < 4$



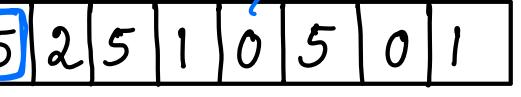
$ans[10] = [4 \ 5 \ 1 \ 5 \ 1 \ 7 \ 0 \ 7 \ 1 \ 7]$

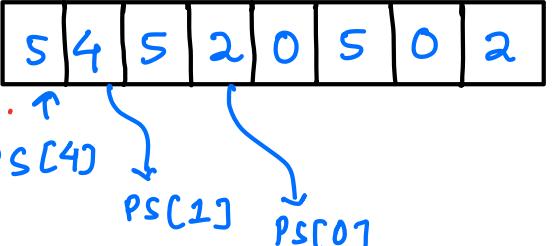
Eg: arr[7] =  max = 5

$s+1 = 6$
 $[max+1]$ FreqArr = 

$[max+1]$ PSum = 

$0 \leq A[i] \leq 1000$

$A[7] = $

$ans[7] = $

Edge case
 $A[i] == 0 \Rightarrow ans[i] = 0$

```

int[] lesser(int[] A) {
    int max = getMax(A); // Todo
    // Create frequency Array
    int[] freq = new int[max+1];
    for (i=0; i<n; i++) {
        int val = A[i];
        freq[val]++;
    }

    int[] psum = new int[max+1]; // Todo
    int[] ans = new int[n];
    for (i=0; i<n; i++) {
        int val = A[i];
        if (val == 0) {
            ans[i] = 0;
        } else {
            ans[i] = psum[val-1];
        }
    }
    return ans;
}

```

Longest Subarray with Sum = k

→ Given an array of N integers, find the length of longest subarray such that sum of subarray = k

arr[10]:

0	1	2	3	4	5	6	7	8	9
8	2	1	-3	4	3	1	-2	-3	2

$1 \leq N \leq 10^5$

$$[a-b] = b-a+1 \quad k=6$$

$$\text{subArr}[2-6] = 6 ; \text{len} = 6-2+1 = 5$$

$$\text{subArr}[4-7] = 6 ; \text{len} = 7-4+1 = 4$$

$$\text{subArr}[1-7] = 6 ; \text{len} = 7-1+1 = 7 \rightarrow \text{MaxLen.}$$

Idea For all the subarrays

Get sum = k ;

Find the maximum length among them.

$$\text{T.C.} = O(n^2 * n) = O(n^3)$$

↓

$O(n^2 * 1)$ with Prefix sum

$O(n^2)$

$n = 10^5$

$O(10^{10}) \Rightarrow$ Higher

↓
Reduce T.C.

sum of subarray = k

↳ Continuous Sum

↳ Prefix Sum

$$\begin{array}{c} y \\ \hline x \\ z \end{array}$$

i $i+1$ j

$$z = x - y = PS[j] - PS[i]$$

↳ $\text{Sum}[i+1 \dots j]$

$K = 6$

$a[11] :$

3	5	2	1	-3	4	3	1	-2	-3	2
0	1	2	3	4	5	6	7	8	9	10
0	1	2	3	4	5	6	7	8	9	10

$\text{Psum}[11] :$

3	8	10	11	8	12	15	16	14	11	13
3	8	6	9	8	12	15	16	14	11	13
3	8	6	9	8	12	15	16	14	11	13

$$\text{Sum}[i+1 \dots j] = K = PS[j] - PS[i]$$

$$\text{len} = 7 - 2 = 5 ; \quad \text{Sum}[3 \dots 7] = PS[7] - PS[2] = 16 - 10 = 6$$

$$\text{len} = 8 - 1 = 7 ; \quad \text{Sum}[2 \dots 8] = PS[8] - PS[1] = 14 - 8 = 6$$

$$\text{len} = j - (i+1) + 1 = j - i - 1 + 1 = j - i \rightarrow \text{len}$$

$$\text{Sum}[i+1 \dots j] = PS[j] - PS[i] = K$$

$$\{ j > i \} \Rightarrow PS[j] - K = PS[i]$$

By finding j , $PS[j]$; we need to look for $PS[i]$

$$PS[j] - K$$

$arr[11]$:	<table border="1"> <tr> <td>3</td><td>5</td><td>12</td><td>1</td><td>-3</td><td>4</td><td>3</td><td>1</td><td>-2</td><td>-3</td><td>2</td></tr> <tr> <td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> </table>	3	5	12	1	-3	4	3	1	-2	-3	2	0	1	2	3	4	5	6	7	8	9	10
3	5	12	1	-3	4	3	1	-2	-3	2													
0	1	2	3	4	5	6	7	8	9	10													

$K=6$

$psum[11]$:	<table border="1"> <tr> <td>3</td><td>8</td><td>10</td><td>11</td><td>8</td><td>12</td><td>15</td><td>16</td><td>19</td><td>11</td><td>13</td></tr> <tr> <td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> </table>	3	8	10	11	8	12	15	16	19	11	13	0	1	2	3	4	5	6	7	8	9	10
3	8	10	11	8	12	15	16	19	11	13													
0	1	2	3	4	5	6	7	8	9	10													

$$15 - \underline{9} = 6 \quad \downarrow \quad \text{len} = 7 - 2 = 5$$

$$16 - \underline{10} = 6$$

$$14 - \underline{8} = 6$$

$$PS[j] - PS[i] = 6$$

$$3 - \underline{x} = 6$$

$$3 - x = 6 \Rightarrow x = -3$$

$$8 - \underline{2} = 6$$

$$10 - \underline{4} = 6$$

$$11 - \underline{5} = 6$$

Obs : Don't update the value if $psum[i]$ is in hashmap ; if it is present .

Since ; we have to find out longest

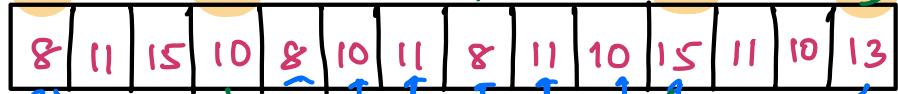
$A[14]$:

8	3	4	-5	-2	2	1	-3	3	-1	5	-4	-1	3
---	---	---	----	----	---	---	----	---	----	---	----	----	---



$K=5$

$PS[14]$:



Hash Map

$K : V$

$\langle 8, 0 \rangle$

$\langle 11, 1 \rangle$

$\langle 15, 2 \rangle$

$\langle 10, 3 \rangle$

$$15 - 5 = 10$$

$$13 - 5 = 8$$

$$\rightarrow len = 10 - 3 = 7$$

$$len = 13 - 0 = 13$$

Edge case \Rightarrow `hmap.put(0, -1);`

$A :$

2	3	1
---	---	---

 $K=5$

$PS :$

2	5	6
---	---	---

Hash Map

$\langle 0, -1 \rangle$

$\langle 2, 0 \rangle$

$\langle 5, 1 \rangle$

$\langle 6, 2 \rangle$

$$2 - 5 = -3$$

$$5 - 5 = 0$$

$$6 - 5 = 1$$

$$\begin{aligned} len &= 1 - (-1) \\ &= 2 \end{aligned}$$

```

int longest (int[] A) {
    int psum[n]; // Todo
    HashMap<Integer, Integer> hmap = new HashMap<>();
    int ans=0;
    hmap.put(0,-1); // Edge Case
    for (i=0; i < n; i++) {
        int ele = psum[i];
        int target = ele - k;
        if (hmap.containsKey(target)) {
            ans = max(ans, i - hmap.get(target));
        }
        else {
            if (hmap.containsKey(ele) == false) {
                hmap.put(ele, i);
            }
        }
    }
    return ans;
}

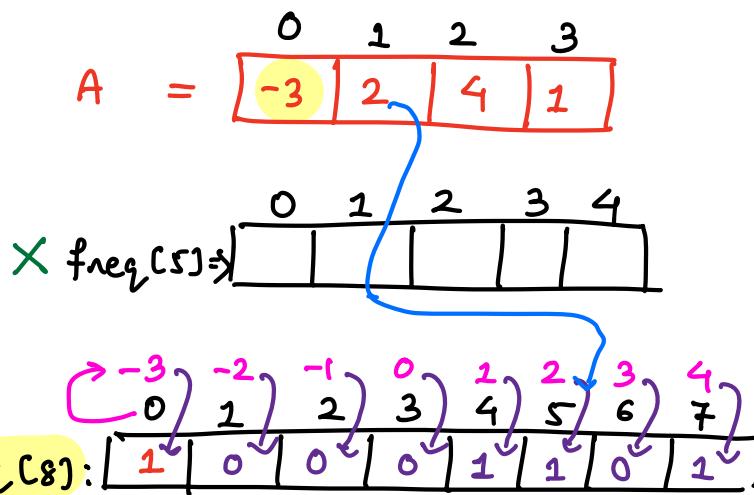
```

In Order to find longest sub Array.

$T.C = O(n)$

$S.C = O(n)$

Doubt session



$$\max = 4 \quad \checkmark$$

$$\min = -3 \quad \checkmark$$

$$[\max - \min + 1]$$

$$\text{size freq} = 4 - (-3) + 1$$

$$= 4 + 3 + 1 = 8$$

$$-3 + |\min| = -3 + |-3| = -3 + 3 = 0$$

$$2 + |\min| = 2 + |-3| = 2 + 3 = 5$$

$$4 + |\min| = 4 + |-3| = 4 + 3 = 7$$

$$1 + |\min| = 1 + |-3| = 1 + 3 = 4$$