

Today's Content

- a) Intro
- b) All subsets
- c) All combinations
- d) All solutions

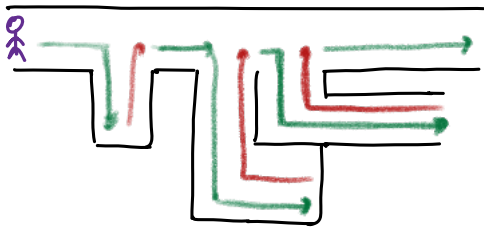
Back Tracking: Generating all solutions using recursion \rightarrow Backtracking

↳ a. all subsets

Maze:

b. all combinations

c. all ways



Idea: While generating all solutions, choose path but we cannot go any further, backtrack & take another path.

18) Given N , print all N digit numbers formed only by 1, 2
in increasing order

$N=2$:

dec

1	1	→	0	0	0
1	2		0	1	1
2	1		1	0	2
2	2		1	1	3

$N=3$:

1	1	1
1	1	2
1	2	1
1	2	2
2	1	1
2	1	2
2	2	1
2	2	2

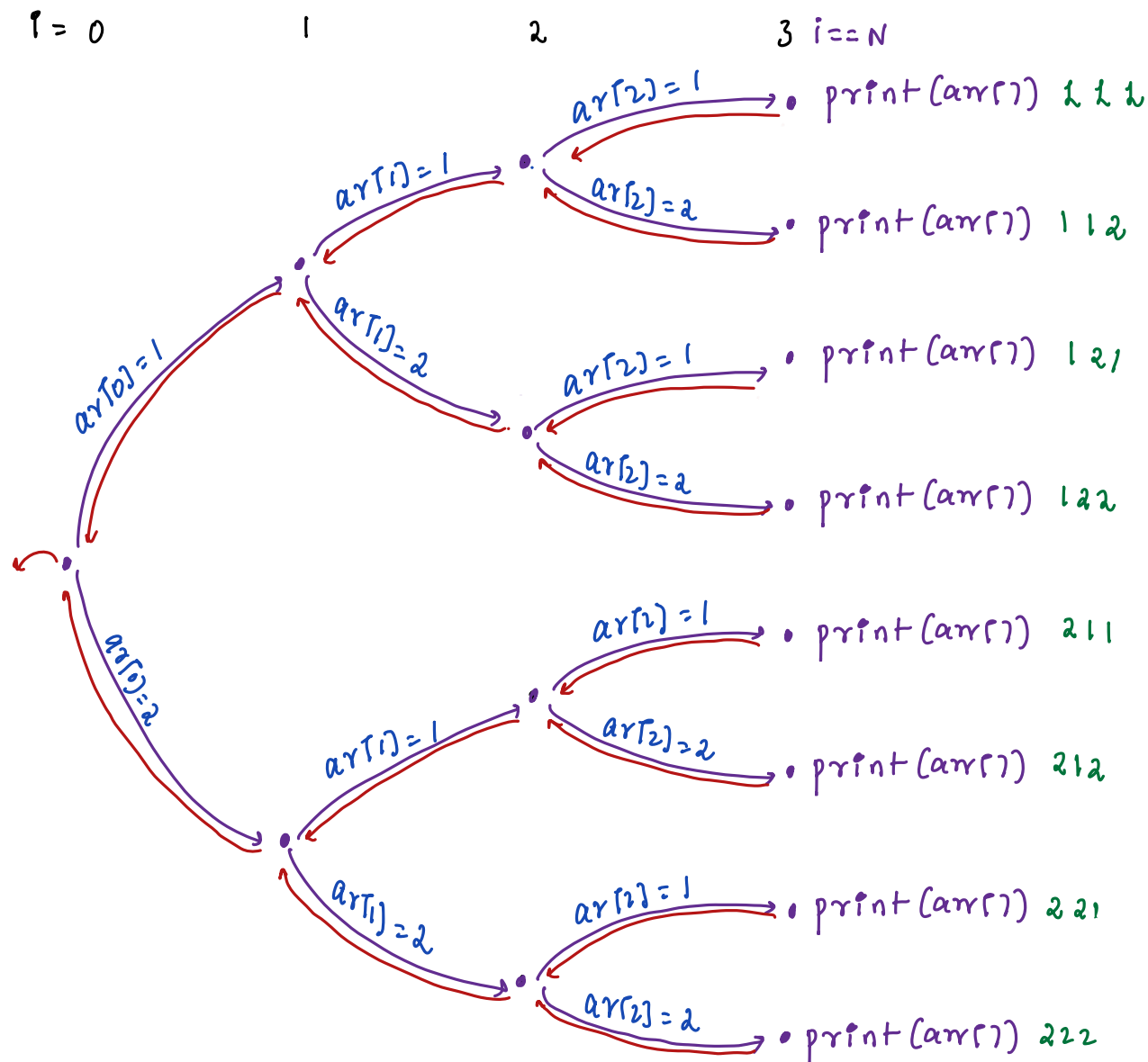
Idea:

1. Using bit manipulation: $1 \neq 0$ $2 \neq 1$

2. Using queues:

3. Using backtracking:

Tracing $N=3$: $arr[3] = \{ 2 \quad 2 \quad 2 \}$ To store 3 digit number



func():

parameters: What all parameters we need to pass
ar[N], i: {curr index}, N: {size of arr}

Subproblems: How many choices
2 choices

Return type: void

```
void printAll(int ar[], int i, int N) {
```

```
    if (i == N) { // Stop:
        print entire ar[]
    }
    return;
```

```
    // At ith index choices
```

```
    ar[i] = 1;
```

```
    printAll(ar, i+1, N)
```

```
    ar[i] = 2;
```

```
    printAll(ar, i+1, N)
```

```
    return;
```

```
}
```

rough code

```
if (no choice) {
```

```
    do something
```

```
}
```

```
Choices call
```

```
return
```

```
}
```

```
main() {
```

```
    int ar[N]
```

```
    printAll(ar, 0, N);
```

```
}
```

0 1
ar[2] = { 2 2 }

main() {

int ar[2]

printAll(ar, 0, N);

}

void printAll(int ar[], int i=0, int N=2){

1. if(i == N) { print(ar[i]) return }
2. ar[i] = 1;
3. printAll(ar, i+1, N)
4. ar[i] = 2;
5. printAll(ar, i+1, N)
6. return

}

void printAll(int ar[], int i=1, int N=2){

1. if(i == N) { print(ar[i]) return }
2. ar[i] = 1;
3. printAll(ar, i+1, N)
4. ar[i] = 2;
5. printAll(ar, i+1, N)
6. return

}

void printAll(int ar[], int i=2, int N=2){

1. if(i == N) { print(ar[i]) return }
2. ar[i] = 1;
3. printAll(ar, i+1, N)
4. ar[i] = 2;
5. printAll(ar, i+1, N)
6. return

}

void printAll(int ar[], int i=2, int N=2){

1. if(i == N) { print(ar[i]) return }
2. ar[i] = 1;
3. printAll(ar, i+1, N)
4. ar[i] = 2;
5. printAll(ar, i+1, N)
6. return

}

void printAll(int ar[], int i=2, int N=2){

1. if(i == N) { print(ar[i]) return }
2. ar[i] = 1;
3. printAll(ar, i+1, N)
4. ar[i] = 2;
5. printAll(ar, i+1, N)
6. return

}

void printAll(int ar[], int i=2 int N=2){

1. if(i == N) { print(ar[i]) return }
2. ar[i] = 1;
3. printAll(ar, i+1, N)
4. ar[i] = 2;
5. printAll(ar, i+1, N)
6. return

}

void printAll(int ar[], int i=2, int N=2){

1. if(i == N) { print(ar[i]) return }
2. ar[i] = 1;
3. printAll(ar, i+1, N)
4. ar[i] = 2;
5. printAll(ar, i+1, N)
6. return

}

Output:

1 1

1 2

2 1

2 2

Q) Given $arr[N]$ elements, count of subsequence with $sum = k$

Ex1:

$arr[3] = \begin{matrix} 0 & 1 & 2 \\ 5 & 7 & 2 \end{matrix}$

$k=7$, Subsequences = $\{5, 2\} \{7\}$: return 2

Need not be continuous
Order of index maintained

Idea1: Generate all subsequence sums & compare $== k$

TC: $O(2^N * N)$ SC: $O(1)$

Idea2: 1. Hashmap $arr[k]$:

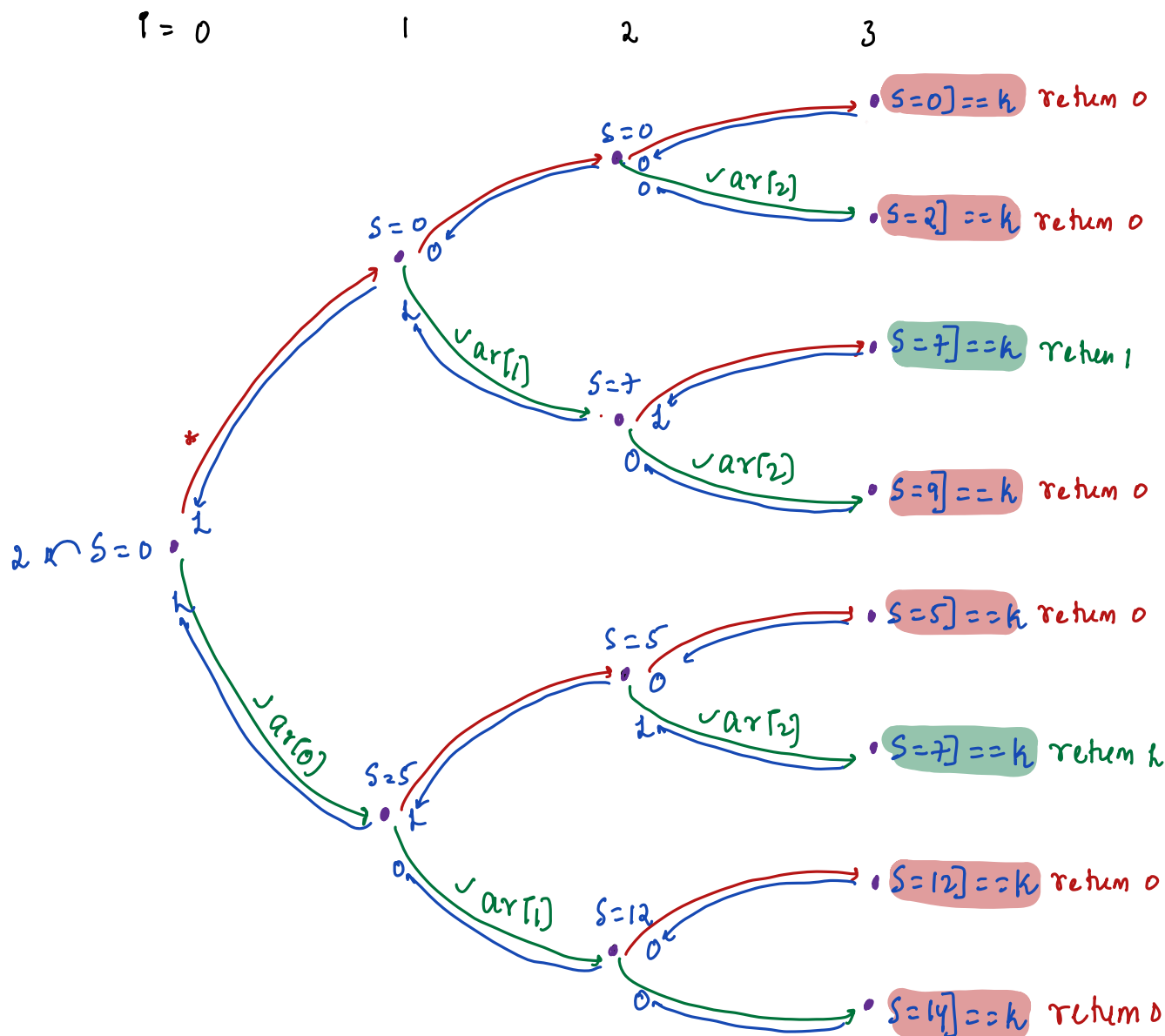
{Subsequence can contain > 2 elem}

2. Using $sum[]$: Range:

{Elements need not be continuous}

Idea3: Using backtracking

$arr[3] = \begin{matrix} 0 & 1 & 2 \\ 5 & 7 & 2 \end{matrix}$ $k=7$



func():

parameters: arr , i , N , sum , k

Subproblems: 2 choices, pick it, leave it

Return type: int

int CountSubSum(int arr , int i , int N , int sum , int k) { $Tc: O(2^N)$

$Sc: O(N)$

if ($i == N$) {

 if ($sum == k$) { return 1 }

 else return 0

// At i^{th} index choices

 // We don't pick i^{th} sum:

int $l =$ CountSubSum(arr , $i+1$, N , sum , k)

 // We pick i^{th} ele: $sum + arr[i]$

int $r =$ CountSubSum(arr , $i+1$, N , $sum + arr[i]$, k)

 return $l + r$;

rough code

if (no choice) {

 do something

 return

choices can

return

3Q) Given $N \times N$ mat[], print all valid placement of N Queens such that no queen can, kill other queen :

Note: If 2 queen belong to same row/column/diagonal they will kill

Ex:

$N=4$

	0	1	2	3
0	Q			
1			Q	
2				Q
3		Q		

Not valid

	0	1	2	3
0		Q		
1				Q
2	Q			
3			Q	

Valid

	0	1	2	3
0			Q	
1	Q			
2				Q
3		Q		

Valid

func():

parameters: mat[N][N], i, N

Subproblems: All Columns in i^{th} row

are my choices =

	0	1	2	.	.	$N-1$
i^{th}	Q	Q	.	.	.	Q

Return type: void

→ // Queens to place

void NQueens(int mat[][N], int i, int N) {

if (i == N) {

print entire mat[]

return;

// At i^{th} row:

for (int j = 0; j < N; j++) {

// Try place at [i, j] = Q;

if (valid(mat, i, j) == True) {

mat[i][j] = 1;

NQueens(mat, i+1, N)

mat[i][j] = 0;

}

return;

	0	1	2	3	4	5
0					Q	
1		Q				
2						Q
3			Q			
4						
5						

valid: mat[i, j]: check at mat(3, 2)

row: No need, we only place 1 Queen

col: (3, 2) → (2, 2) → (1, 2) → (0, 2) → (-1, 2)

left: (3, 2) → (2, 1) → (1, 0) → (0, -1)

[n, y] → [n-1, y-1]

right: (3, 2) → (3, 3) → (1, 4) → (0, 5) → (-1, 6)

[n, y] → [n-1, y+1]

Note: Start placing queen from 0th row & in each row only 1 Queen

Note: 1 → Queen 0 → Empty

	0	1	2	3
→ 0	Q	Q	Q	
1				
2				
3				

	0	1	2	3
0	Q			
→ 1	X	X	Q	Q
2				
3				

	0	1	2	3
0		Q		
→ 1	X	X	X	Q
2				
3				

	0	1	2	3
0			Q	
→ 1				
2				
3				

	0	1	2	3
0				
1				
2				
3				

	0	1	2	3
0	Q			
1			Q	
→ 2	X	X	X	X
3				

	0	1	2	3
0	Q			
1				Q
→ 2	X	Q	X	X
3				

	0	1	2	3
0		Q		
1				Q
→ 2	Q	X	X	X
3				

	0	1	2	3
0				
1				
2				
3				

	0	1	2	3
0	Q			
1				Q
2		Q		
→ 3	X	X	X	X

	0	1	2	3
0		Q		
1				Q
2	Q			
→ 3	X	X	Q	X

	0	1	2	3
0				
1				
2				
3				

Doubt:

mat[i][j] = Q

Make a function call

mat[i][j] = 0

	0	1	2	3
0		Q		
1				Q
2	Q			
3			Q	

→ 4 : valid place:
print mat return

	0	1	2	3
0				
1				
2				
3				