

2 questions :

1. Sum the difference
2. Sum of all subarrays

Q. given an integer array of size N

↓  
subsequences =  $2^N$

Sum { For every subsequence, difference of largest no - smallest no }

Example :

	l	s	diff
3 5 10	0	0	0
3	3	3	0
5	5	5	0
10	10	10	0
3 5	5	3	2
3 10	10	3	7
5 10	10	5	5
3 5 10	10	3	7
			<u>Σ 21</u>

( Sum of all max of each sub-sequence ) - ( Sum of all min of each sub-seq )

$$\begin{aligned}
 & \left( 0 + 3 + 5 + 10 + 5 + 10 + 10 + 10 \right) - \left( 0 + 3 + 5 + 10 + 3 + 3 + 5 + 3 \right) \\
 & = 53 - 32 = 21
 \end{aligned}$$

Overview: How to solve this q

Example:

3 5 10

3  
5  
10  
3 5  
3 10  
5 10  
3 5 10

1  
3  
5  
10  
5  
10  
10  
10

1  
3  
5  
10  
3  
3  
5  
3

diff  
0  
0  
0  
2  
7  
5  
7

$\Sigma 21$

$$\left( \underline{3+5+10+5+10+10+10} \right) - \left( \underline{3+5+10+3+3+5+3} \right)$$

$\Sigma \text{ large}$                        $\Sigma \text{ small}$

(53)

(32)

= 21

answer of this question =

$$\text{Sum} \left[ \text{For every subsequence, } \underline{\text{largest no}} \right] \rightarrow \text{Sum} \left[ \text{For every subsequence, } \underline{\text{smallest no}} \right]$$

Code:

```
int Sum-max-sub (int [] ar) {  
    int N = ar.length  
    int sum = 0  
    Arrays.sort(ar)  
    for (i = 0; i < N; i++) {  
        sum = sum + ar[i] * 2i  
    }  
    return sum  
}
```

Sum of min of subsequences

Code:

```
int Sum-min-sub (int [] ar) {  
    int N = ar.length  
    int sum = 0  
    Arrays.sort(ar)  
    for (i = 0; i < N; i++) {  
        sum = sum + ar[i] * 2N-i-1  
    }  
    return sum  
}
```

Obs:

0	1	2
2	4	5

$i$   
↓  
3  
7  
↓

4	5
8	10

---

7

7

	2	
7	<hr/>	
7	8	
7		10

7	8	10
---	---	----

8	10
---	----

---

$N = 6$

$i = 3$

$6 - 3 - 1$

$= 2$

$2^2 = 4$

min

1.

$i+1 \quad i+2 \quad \dots \quad N-1$   
 {  
 elements

---

$(N-1) - (i+1) + 1$

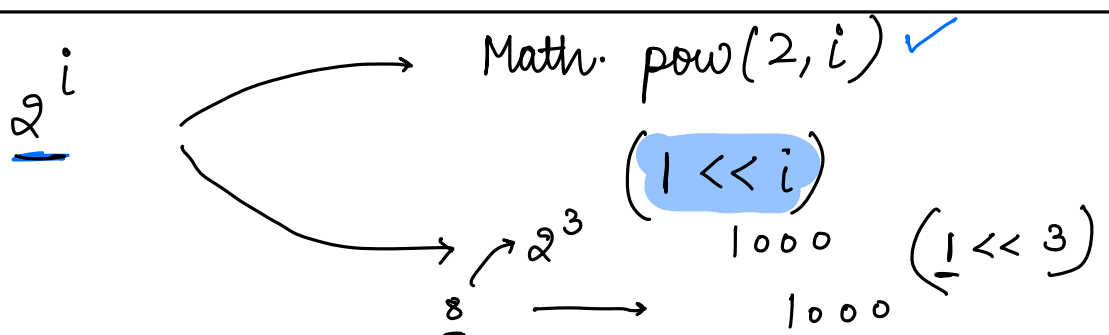
←  $\begin{matrix} N-1 & - & i & \cancel{+1} & \cancel{+1} \\ N- & i & - & 1 \end{matrix}$

$2^{N-i-1}$  } arr[i]  
min

## Final Code :

```
int Sum — sub (int [] ar ) {  
    int N = ar.length  
    max_sum = 0  
    Arrays.sort (ar)  
    int MOD = 1000000007  
    for (i = 0 ; i < N ; i++) {  
        max_sum = (max_sum + (ar[i] × 2i) % MOD) % MOD  
        min_sum = (min_sum + (ar[i] × 2N-i-1) % MOD) % MOD  
    }  
    return max_sum — min_sum  
}
```

Doubt :



Q. Sum of all subarrays

(long)

Subsums (int[] arr) {  
int N = arr.length

long total = 0

for ( i = 0 ; i < N ; i++ ) {

long occ = (i+1) \* (N-i)

long contri = arr[i] \* occ

long total = total + contri

}  
return total

}

TC:  $O(N)$

SC:  $O(1)$

Constraints:  $1 \leq N \leq 10^5$

$1 \leq arr[i] \leq 10^4$

$(i+1) \times (N-i)$   
100

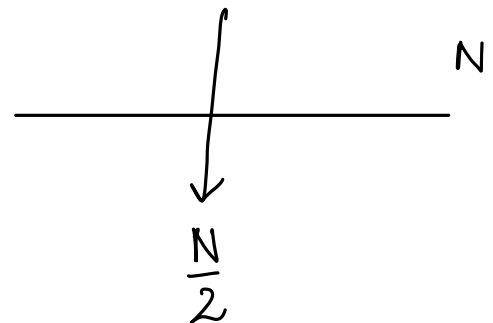
N = 100

$(i+1) \times (N-i)$

i = 70      (71) x (30)  $\approx$  2100

i = 50      (51 x 50)  $\approx$  2500

i  $\rightarrow$  mid value



$$\left(\frac{N}{2} + 1\right) \left(\underbrace{\frac{N}{2} - \frac{N}{2}}_{\frac{N}{2}}\right)$$

$$\left(\frac{N}{2} + 1\right) \left(\frac{N}{2}\right) \approx \frac{N^2}{2}$$

$$N \rightarrow 10^5$$

$$\frac{10^{10}}{10} \rightarrow \text{long}$$