

Directions: show all work and simplify your answers

1. Find the derivatives of the following functions:

a) $y = \cos(\sec(4x))$

b) $f(x) = [(x^4 - 3)^8 - 4x^3]^5$

c) $y = \cos^5(\sin^3(x))$

2. Find an equation of the tangent line to the curve at the given point:

a) $f(x) = \sqrt{1 + x^6}$ at the point (2,3)

b) $f(x) = x^3 + 2x^4 - 6$ at the point (3,2)

c) $f(x) = \sin(x) + 3x^4$ at a point where $x = \frac{\pi}{4}$

3. Find the $\frac{dy}{dx}$ by using implicit differentiation

a) $2x^3 - xy^2 + x^3 + y^4$

b) $x^2y^{10} = 9$

c) $\sin(x) + 4\cos(y) - 3y^2 = 9x$

d) $x^3 = (4y^2x^4 + 3x^2)$