

1b You won't go skiing, or you will and there won't be any snow.

Let sk represent, "You will go skiing."

Let sn represent, "There will be snow."

Answer: $\neg sk \vee (sk \wedge \neg sn)$

2b I'll have either fish or chicken, but I won't have both fish and mashed potatoes.

Let c represent the phrase, "I will have chicken"

Let p represent the phrase, "I will have mashed potatoes".

Let f represent the phrase "I will have fish".

Answer $(f \vee c) \wedge \neg(f \wedge p)$

3 a) Alice and Bob are not both in the room.

Let A represent the phrase, "Alice is in the room."

Let B represent the phrase, "Bob is in the room."

Answer: $\neg(A \wedge B)$

b) Alice and Bob are both not in the room.

If Alice is in the room Bob is not and so vice versa.

Let A represent the phrase, "Alice is in the room."

Let B represent the phrase, "Bob is in the room."

$\neg A \wedge \neg B$

c) Either Alice or Bob are not in the room.

Let A represent the phrase, "Alice is in the room."

Let B represent the phrase, "Bob is in the room."

Answer: $(\neg A) \vee (\neg B)$

d) Neither Alice or Bob are not in the room.

Let A represent the phrase, "Alice is in the room."

Let B represent the phrase, "Bob is in the room."

Answer: $\neg(A \vee B)$

4 a) $\neg(\neg P \vee \neg\neg R)$

$\neg\neg R$ has the same meaning of R by double negation

$\neg P$ by negation rule means not P

$\neg(\neg P \vee \neg\neg R) \equiv \neg(\neg P \vee R)$

This formula is well formed as the meaning still upholds even when the different rules are applied.

b) $\neg(P, Q, \wedge R)$

Based on what we are given, a (,) symbols is not a valid connectives, so therefore, this is not a well formed formula.

c) $P \wedge \neg P$

This is a well formed formula as it has a comparison of a negation and itself.

d) $(P \vee Q)(P \vee R)$

Since there is no valid connectives between two statements this is not a valid one as you

cannot multiply statements together.

6a $(S \vee G) \wedge (\neg S \vee \neg G)$

$S \rightarrow$ Steve is happy.

$G \rightarrow$ George is happy.

Since there is an and sign between two reasoning, that means one has to be happy and the other is not happy.

Therefore in the English language: Either Steve or George is happy, and either Steve or George is not happy.