

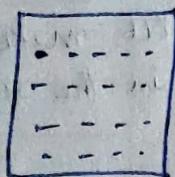
## Hash Map:

Why data structure?

→ To store input for algorithms and to provide output from algorithms.

## Operations:

- a) Insertion
- b) Deletion
- c) Search

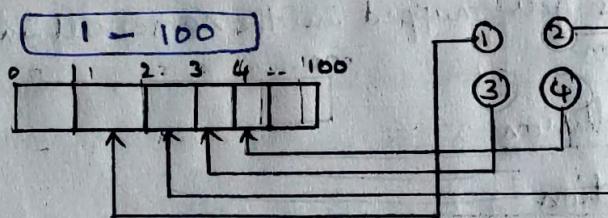


Insertion and Deletion rarely happen as widely.

→ Search is widely used.

- |                  |               |                  |             |
|------------------|---------------|------------------|-------------|
| → Unsorted Array | $O(n)$        | → Binary Tree    | $O(n)$      |
| → Sorted Array   | $O(n \log n)$ | → B.S.T          | $O(n)$      |
| → Linked List    | $O(n)$        | → Balanced B.S.T | $O(\log n)$ |
|                  |               | → Priority Queue | $O(n)$      |
- The best search complexity till now is  $O(\log n)$ .

## D.A.T → Direct Access Table.



a) Insert 6  
Go to 6<sup>th</sup> index  
and add  
 $O(1)$

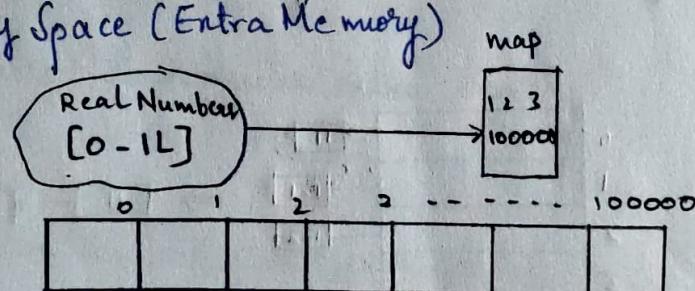
b) Deletion → 6.  
 $O(1)$

## Advantage:

→ Every operation can be accomplished in  $O(1)$ .

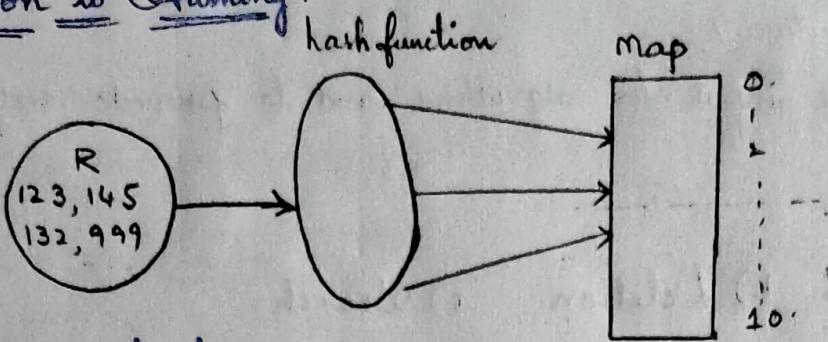
## Disadvantage:

Memory Space (Extra Memory)



- You want to insert 100000 value then [1, 2, 3, 100000]  
it is not the best approach, because memory is getting wasted. As we want to insert only 4 values out of 1L size.  
→ For small values, D.A.T is good

## Introduction to Hashing



→ We have a pool of numbers, we will make the numbers pass through a function such that the numbers in the real number pool map to some value inside the machine.

hash function  $\rightarrow \% 10$

$$121 \% 10 \Rightarrow 1 \quad 132 \% 10 \Rightarrow 2$$

$$145 \% 10 \Rightarrow 5 \quad 999 \% 10 \Rightarrow 9$$

0	1	2	3	4	5	6	7	8	9
121	132			145				999	

Insertion  $\rightarrow O(1)$ , Search  $\rightarrow O(1)$ , Deletion  $\rightarrow O(1)$

$21 \% 10 \rightarrow 1$ , we get collision.

### Collision:

When 2 elements gets mapped in the same cell in two situations is known as collision.

### Ways to Handle Collision:

#### 1. Better Hash function

$\% 10$ , Prime number

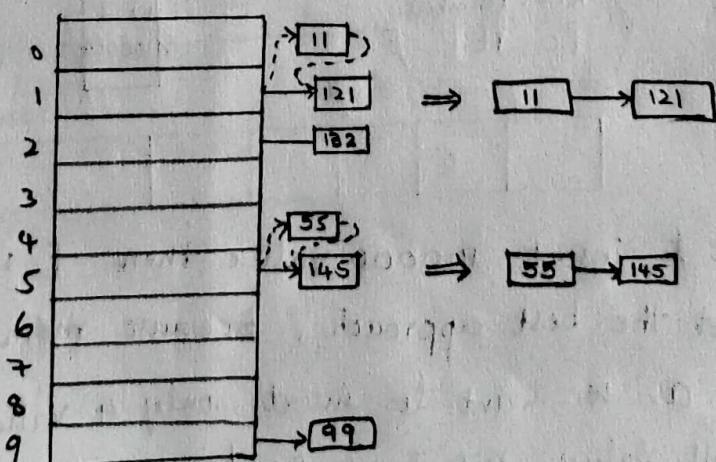
→ We can decrease the collision but not zero.

#### 2. Chaining

#### 3. Open Addressing

- a) Linear Probing
- b) Quadratic Probing
- c) Double Hashing

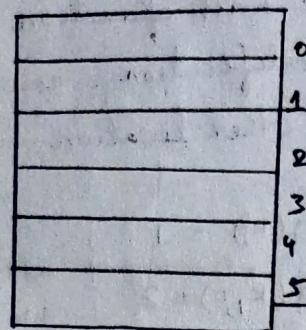
### Chaining:



Note: In case of collision, go to that particular index, and make the first node of linked list as the element.

→ Insertion takes  $O(1)$

Search:



5, 15, 25, 35, 45

$$T(n) = O(n)$$

Load factor:

$\frac{n}{m} \rightarrow$  elements in the list

$\frac{n}{m} \rightarrow$  size of the hashtable.

Average Search Time:

$$\Theta\left(1 + \frac{n}{m}\right) \rightarrow \text{load factor}$$

$$m = 6, n = 10 \Rightarrow \frac{n}{m} = \frac{10}{6} = 1.6$$

L.F.: The value after that, the size of the hashmap doubles.

usually the load factor is 75%.

i.e. once the size reaches 75%, the hashmap doubles.

$$6 \times \frac{75}{100} = 4.5, \text{ once it reaches } 5, \text{ it doubles}$$

Advantage: most operations in  $O(1)$ , collision is taken care of

(insertion)

Disadvantage:

need to consider extra space.

Open Addressing:

→ It handles the collision without using extra space.

$$\text{l.f.} \rightarrow 0 \leq \text{l.f.} \leq 1 \quad \alpha = \frac{n}{m} = \frac{n}{n} = 1$$

0	
1	s
2	
3	
4	15
5	

As it's already available at that location,  
15 cannot be inserted, we will apply  
the hash function with certain  
modification, never 15 will be inserted  
at other location.

ex. ①

0	
1	k
2	r <sub>1</sub>
3	k <sub>2</sub>
4	z

$$h(k) = 1$$

$h(k_1, 0) = 2$  → after applying hash function  
we are getting index '2'

$h(k_2, 0) = 4$  → collision as 'z' is already  
present

$$h(k_2, 1) = 3$$

→ collision Number

$h(k_1, 0) \rightarrow 2$  → but it is already  
occupied by 'A'

$h(k_1, 1) \rightarrow 6$  → This is also occupied

$h(k_1, 2) \rightarrow 7 \rightarrow$  "

$h(k_1, 3) \rightarrow 4 \rightarrow$  "

$h(k_1, 4) \rightarrow 5$

0	
1	A
2	D
3	Del
4	x <sub>1</sub>
5	B
6	C
7	

## Search:

→ we need to search for k<sub>1</sub>, again follow the same hashing  
function steps and check in that index if the value is equal  
to k<sub>1</sub>, else recompute the hash function.

→ Let's say some one deleted 'D' at 4<sup>th</sup> index and empty value  
is present. It is understood that it is not gone to that location  
so, its better to write "Del" after deleting the element and it  
will move further to find k<sub>1</sub>.

$$\rightarrow TC = O(n)$$

→ The hash function should be written in such a way that  
elements occupy uniform slots.

→ So that collision problem decreases and the search operation  
comes out to O(1).

### Linear Probing:

$$\rightarrow h'(k, i) \rightarrow (h(k) + i) \% m$$

$$h(k, i) \rightarrow (h(k) + i) \% m$$

$$h(k, 0) = 1$$

$$h(k, 1) = 1 + 1 \rightarrow 2$$

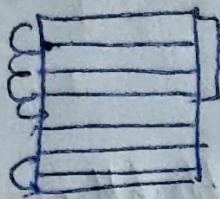
	0
A	1
B	2
C	3
D	4
K	5

collision number

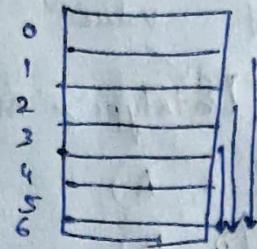
Probing  $\rightarrow$  finding the next location.

$\rightarrow$  here it is probing in a linear manner.

### Primary Clustering:



$\Rightarrow$  Blocks will get created



It will form blocks  
the probability of new  
collision might increase.

### Secondary Clustering:

$$h(k_1) \Rightarrow 1$$

$$h(k_1, 1) \Rightarrow 2$$

$$h(k_1, 2) \Rightarrow 3$$

$$\rightarrow h(k_1, 3) \Rightarrow 4$$

$$h(k_2) \Rightarrow 1$$

$$h(k_2, 1) \Rightarrow 2$$

$$h(k_2, 2) \Rightarrow 3$$

$$\rightarrow h(k_2, 3) \Rightarrow 4$$

$\rightarrow$  If 2 numbers map to the same number initially then both the numbers follows the same prob sequence.

### Quadratic Probing:

$$h(k, i) = ((h(k) + (i^2 k + i)) \% m)$$

	0
	2
	4
	5
	7
	9

$$h(k, 0) \Rightarrow 0$$

$$h(k, 1) \Rightarrow 4$$

$$h(k, 2) \Rightarrow 6$$

$$h(k, 3) \Rightarrow 8$$

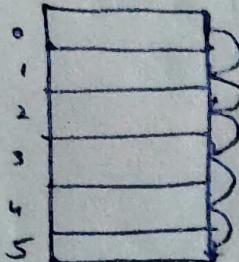
Probed Index is calculated in a  
Quadratic manner

→ It suffers from Secondary clustering, but not from Primary clustering.

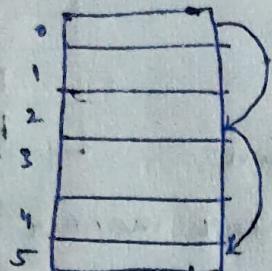
## Double Hashing:

$$h(k) = [h_1(k) + i h_2(k)] \% n$$

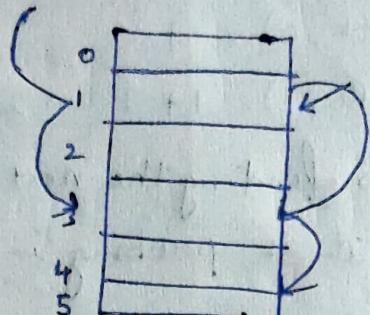
$$y = y(m_1) + y(m_2)$$



LP



QP



DH  
no. Secondary clustering

## Syntax & Methods:

- \*  $\text{HashMap} < \text{Datatype}, \text{Datatype} \rangle$  map = new  $\text{HashMap} < \rangle$ ;
- map.put(1, A);  
map.put(2, B);  
map.put(3, C);
- It is an unordered map.

- \*  $\text{LinkedHashMap} < \text{Integer}, \text{String} \rangle$  map = new  $\text{LinkedHashMap} < \rangle$ ;
- (for maintaining the order)
- map.put(1, A);  
map.put(2, B);  
map.put(3, C);
- 1 A  
3 C  
2 B
- Same order of insertion

- \* For MultiThreaded Env, where update & Read operations happens simultaneously. Then ConcurrentHashMap should be used.
- To iterate over a hash Map.

```
for (Map.Entry<Integer, String> entry: map.entrySet()) {  
    S.O..println(entry.getKey() + " " + entry.getValue());  
}
```

## Two Sum

[2, 7, 11, 15] Target = 9 , o/p: [0, 1]

[3, 2, 4] Target = 6 , o/p: [1, 2]

→ Algo:

1. check if  $\text{target} - \text{arr}[i]$  is available in the map , If yes  
return the indices of numbers index, ~~i+1~~
2. If not, add the number  $\text{arr}[i]$  and its index to the map.

Map<Integer, Integer> map = new HashMap<>();

for(int i=0; i<arr.length; i++){

int num = target - arr[i];

if (map. containsKey (num)) {

return new int []{ map.get (num), i};

}

else {

map. put (num[i], i);

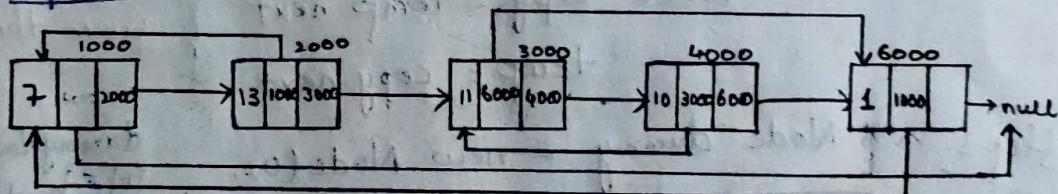
if (num != target) {

}

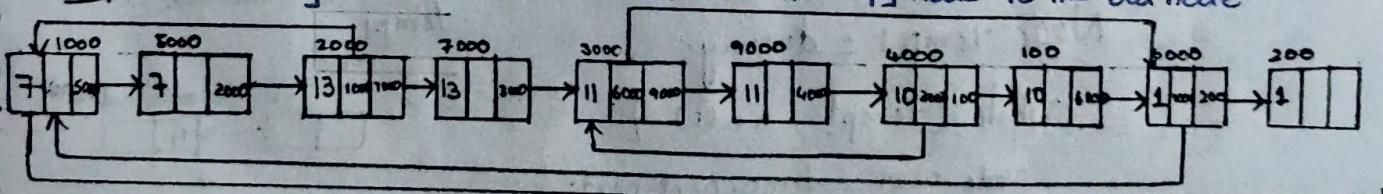
return new int []{};

## Copy list with Random Pointer:

Without Extra Space:

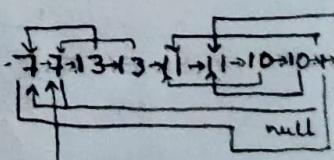
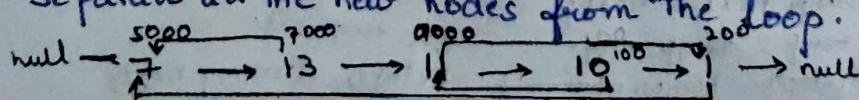


Step 1: Creating new nodes and point the copy node to the old node.



Step 2: For the new nodes, point to the random nodes.

Step 3: Separate all the new nodes from the loop.



Node copyList(Node head){

if(head == null){

return null;

}

Node temp = head;

while(temp != null){

Step:

temp  
↓  
7 → 13 → 11

newNode  
7

next = 13

Node newNode = new Node(temp.data);

Node next = temp.next;

temp.next = newNode;

newNode.next = next;

temp = next;

}

temp  
↓  
7 → 7 → 13  
newNode  
↓  
7 → 7 → 13  
next  
↓  
13  
next  
↓  
temp

// Pointing the random pointer

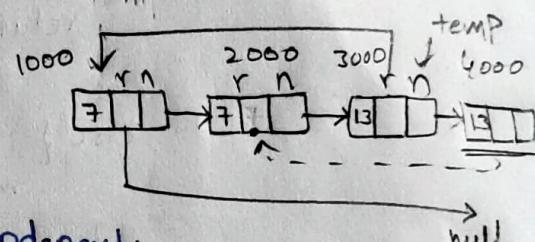
temp = head;

while(temp != head){

if(temp.rand != null){

temp.next.rand = temp.rand.next;

(13).      = 13    .next



= 1000.next

= 2000

Node copy = temp.next

temp = copy.next

} move the temp to copy's next

Step 3:

Node dummy = new Node(0);

temp = head;

Node templ = dummy;

while(temp != null){

Node next = temp.next.next; ⑬

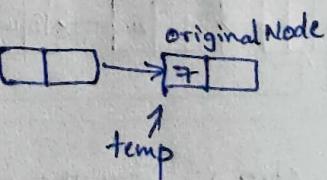
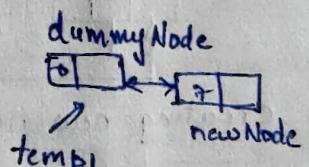
Node copy = temp.next; ⑭

templ.next = copy; ⑮

temp.next = next; ⑯ So temp = 13

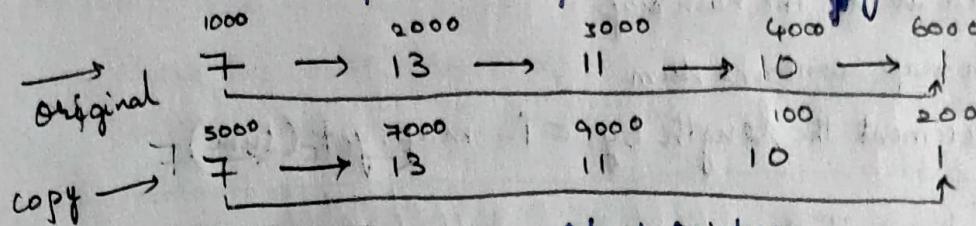
temp = temp.next; ⑰ So templ = ⑭

templ = templ.next; } return dummy.next;



## With Extra Space:

- 1) Create a copy of each node.
- 2) Store the original node as key and copy node as value.
- 3) Create next & random pointers for copy nodes.



Key	Value
1000	5000
2000	7000
3000	9000
4000	100
6000	200

### Next Pointers:

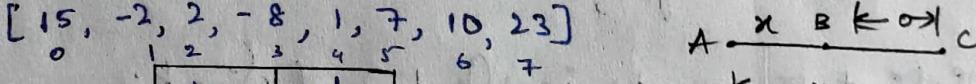
$$\begin{aligned} \text{map.get(temp).next} &= \text{map.get(temp.next)} \\ \underline{\text{map.get(1000).next}} &= \underline{\text{map.get(1000.next)}} \\ 5000.\text{next} &= \text{map.get(2000)} \\ &\quad \vdots \\ &= 7000 \end{aligned}$$

### Random Pointers:

$$\begin{aligned} \text{map.get(temp).rand} &= \text{map.get(temp.rand)} \\ \text{map.get(1000).rand} &= \text{map.get(1000.rand)} \\ 5000.\text{rand} &= \text{map.get(6000)} \\ &= \underline{200} \end{aligned}$$

## \* Longest SubArray With SumZero:

[15, -2, 2, -8, 1, 7, 10, 23]



Key	Value
0	-1
15	0
13	1
7	3
8	4
25	5
48	7

At index 3  $\xrightarrow{(15-8)}$

At index 6  $\xrightarrow{(15+10)}$

$\leftarrow$  at start

At index 2  $\Rightarrow$  Sum  $\Rightarrow 13 + 2 = 15$

$$\begin{aligned} \text{length} &= i - \text{map.get(sum)} \\ &= 2 - \text{map.get}(15) \\ &= 2 - 0 = 2 \end{aligned}$$

At index 5  $\Rightarrow$  Sum  $\underline{= 15}$

$$\begin{aligned} \text{length} &= i - \text{map.get(sum)} \\ &= 5 - 0 \\ &= 5 \checkmark \end{aligned}$$

So longest SubArray = 5

### Algo:

- Create a hashmap to hold  $\rightarrow$  Sum Up Till Now  $\rightarrow$  (occurrence of that sum)
- Iterate over the array,
- If hash map does not contain the sum  
Add it to the hash map.
- If hash map contains sum.  
Increment the length by  $= i - \text{map.get(sum)}$

Map<Integer, Integer> map = new HashMap<>();

int length = 0, sum = 0;

map.put(0, -1);

for (int i = 0; i < arr.length; i++) {

sum += arr[i];

if (map.contains(sum)) {

length = i - map.get(sum);

}  
else {

map.put(sum, i);

}  
return length;

### \*\* Distinct Elements in Window of Size k:

[ 2 5 5 6 3 2 3 ], k=4

O/P: [3, 3, 4, 3]

→ Sliding Window

→ Hash Map (Element  $\Rightarrow$  Count)

- At first window

2  $\rightarrow$  1 count

5  $\rightarrow$  2 count

6  $\rightarrow$  1 count

3  $\rightarrow$  2 count

2  $\rightarrow$  3 count

3  $\rightarrow$  4 count

At first Window       $\text{arr}[i] = 2$

$2 \rightarrow 1$

$5 \rightarrow 2$

$6 \rightarrow 1$

$\}$

At 2<sup>nd</sup> window

5 5 6 3

5  $\rightarrow$  2 (no update in value)

6  $\rightarrow$  1 (no update in value)

3  $\rightarrow$  1 (no update in value)

→ hashmap size  $\rightarrow (3)$

→ check the count of  $\text{arr}[i]$ .

in the map, because we will be

discarding this element and moving to  
the next window, so we should decrement  
the count.

a) If  $\text{arr}[i]$  count  $= 1$  then remove the entry

b) If  $\text{arr}[i]$  count  $> 1$ , then decrement.

a)  $\text{arr}[i] = 5$

$\text{arr}[i]$  count  $> 1$

so decrement  
count.

so map will be

5  $\rightarrow$  1

6  $\rightarrow$  1

3  $\rightarrow$  1

At 3<sup>rd</sup> window:

5, 6, 3, 2

5  $\rightarrow$  1

6  $\rightarrow$  1

3  $\rightarrow$  2

2  $\rightarrow$  1

map.size  $\rightarrow 4$

At 4<sup>th</sup> window

6, 3, 2, 3

6  $\rightarrow$  1

3  $\rightarrow$  2

2  $\rightarrow$  1

map.size  $\rightarrow (3)$

After decrementing  $\text{arr}[i]$ 's

count, map will be

6  $\rightarrow$  1

3  $\rightarrow$  1

2  $\rightarrow$  1

Algo:

- 1) Initialize 2 pointers  $i, j = 0$
- 2) Iterate the array until  $j < \text{arr.length}$
- 3) Add the elements  $\in$  its count in the map
- 4) If the window size is Reached  
get the hash map size.
- 5) Remove the entry of index start if count is 1
- 6) decrement the Value of entry if count is  $> 1$ .

```

Map<Integer, Integer> map = new HashMap<>();
ArrayList<Integer> list = new ArrayList<>();
int i=0; int j=0;
while(j < n) {
    if(!map.contains(A[j])) {
        map.put(A[j], 1);
    }
    else {
        map.put(A[j], map.get(A[j])+1);
    }
    if(j-i+1 == k) {
        list.add(map.size());
        if(map.get(A[i]) == 1) {
            map.remove(A[i]);
        }
        else {
            map.put(A[i], map.get(A[i])-1);
        }
        i++;
    }
    j++;
}

```

# Group Anagrams :- [ "eat", "tea", "tan", "ate", "nat", "bat" ]

→ Based on key, we need to group the strings.

→ Before grouping we need to check if the key is available in the map.

→ Key in the Map is a "map" < character, Integer >

1. eat	→ frequencyMap	e → 1 a → 1 t → 1	4. ate	a → 1 t → 1 e → 1
2. tea	→ frequency map	t → 1 e → 1	5. bat	b → 1 a → 1 t → 1
[eat, tea, ate]	[bat]	a → 1		This map is already available add it to the list
3. tan	[tan, nat]	t → 1 a → 1 n → 1		not available in map, so create a new list

```

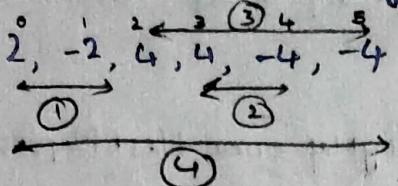
Map< Map<character, Integer>, List<String>> map = new HashMap<>();
for (String str: strs) {
    Map<Character, Integer> frequencyMap = new HashMap<>();
    for (int i=0; i < str.length(); i++) {
        char ch = str.charAt(i);
        if (!frequencyMap.containsKey(ch)) {
            frequencyMap.put(ch, 1);
        } else {
            frequencyMap.put(ch, frequencyMap.get(ch)+1);
        }
    }
    if (!map.containsKey(frequencyMap)) {
        List<String> list = new ArrayList<>();
        list.add(str);
        map.put(frequencyMap, str);
    } else {
        List<String> list = map.get(frequencyMap);
        list.add(str);
    }
}
List<List<String>> result = new ArrayList<>();
for (List<String> values: map.values()) {
    result.add(values);
}
return result;

```

$\begin{array}{l} 1) \begin{matrix} e-1 \\ a-1 \\ t-1 \end{matrix} [eat, tea, ate] \\ 2) \begin{matrix} t-1 \\ a-1 \end{matrix} [tan, nat] \\ 3) \begin{matrix} b-1 \\ a-1 \\ t-1 \end{matrix} [bat] \end{array}$

$\boxed{[eat, tea, ate], [tan, nat], [bat]}$

## Count of Zero Sum Subarray:



$$\text{ans} = 0$$

At index ①:- sum = 2

2 is not available in map.

$$\text{ans} = 0$$

At index ①:- sum = 2 + arr[i]

= 2 - 2 = 0  
0 is available in map.

$$\text{ans} += \text{map.get}(0) \Rightarrow \text{ans} += 1$$

ans = 1, increment the value of 'i' as we found '0' again

At index ②:- sum = 0 + 4 = 4, 4 is not available in map.

add (4, 1) in map.

At index ③:- sum = 4 + 4 = 8, 8 is not available in map

add (8, 1) in map.

At index ④:- sum = 8 - 4 = 4, 4 is available in map.

$$\text{ans} += \text{map.get}(4)$$

$$\text{ans} = 1 + 1 = 2$$

At index ⑤:- sum = 4 - 4 = 0 is available in map.

$$\text{ans} += \text{map.get}(0)$$

$$\text{ans} = 2 + 2 = 4$$

int ans = 0;

Map<Integer, Integer> map = new HashMap<>();

int sum = 0;

map.put(0, 1); for (int i = 0; i < arr.length; i++) { sum += arr[i]; }

if (!map.containsKey(sum)) {

[ [true] ] map.put(sum, i); [ [true, not true] ]

}

ans += map.get(sum);

map.put(sum, map.get(sum) + 1);

}

return ans;

map	
0	→ 1
2	→ 1
4	→ 1
8	→ 1