

Physical Layer Design for a Narrow Band Communication System

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Abstract—This a simple document explaining a question about the concept of similar triangles.

Download all python codes from

svn co <https://github.com/SiddharthPh/Summer2020/trunk/geometry/codes>

and latex-tikz codes from

svn co <https://github.com/gadepall/school/trunk/ncert/geometry/figs>

1 SPECIFICATIONS

1.0.1. Constellation diagram of BPSK

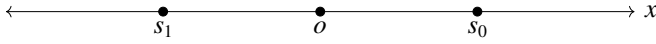


Fig. 1.0.1.1: Constellation diagram

1.0.2. Encoding

We will encode bits as symbols s_0 and s_1 . Here, we will transmit s_0 if bit is 0 and we transmit s_1 if bit is 1.

$$s = \begin{cases} s_0, & \text{bit} = 0 \\ s_1, & \text{bit} = 1 \end{cases}$$

1.0.3. Decision rule for BPSK.

Given symbols s_0 and s_1 are equiprobable and assume symbol carries $\sqrt{E_b}$ per bit and consider a additive white gaussian noise(AWGN) with mean 0 and variance $\frac{N_0}{2}$ and take symbols as equiprobable. The received symbols can be:

$$y|s_0 = \sqrt{E_b} + n \quad (1.0.3.1)$$

$$y|s_1 = -\sqrt{E_b} + n \quad (1.0.3.2)$$

According to MAP detection rule, we will decode the received signal as symbol s for which $p(s|y)$ is more.

$$\hat{s} = \max_{s \in \{s_0, s_1\}} p(s|y) \quad (1.0.3.3)$$

$$\Rightarrow p(s_0|y) \underset{s_1}{\overset{s_0}{\geq}} p(s_1|y) \quad (1.0.3.4)$$

Using Bayes rule,

$$p(s_0|y) = \frac{p(y|s_0) p(s_0)}{p(y)} \quad (1.0.3.5)$$

$$p(s_1|y) = \frac{p(y|s_1) p(s_1)}{p(y)} \quad (1.0.3.6)$$

Since symbols are equi probable. $p(s_0)$ & $p(s_1)$ are equal.

$$\frac{p(y|s_0) p(s_0)}{p(y)} \underset{s_1}{\overset{s_0}{\geq}} \frac{p(y|s_1) p(s_1)}{p(y)} \quad (1.0.3.7)$$

$$\Rightarrow p(y|s_0) \underset{s_1}{\overset{s_0}{\geq}} p(y|s_1) \quad (1.0.3.8)$$

$$\Rightarrow \frac{1}{\sqrt{2\pi}} \exp -\frac{(y - \sqrt{E_b})^2}{\frac{N_0}{2}} \underset{s_1}{\overset{s_0}{\geq}} \quad (1.0.3.9)$$

$$\frac{1}{\sqrt{2\pi}} \exp -\frac{(y + \sqrt{E_b})^2}{\frac{N_0}{2}} \quad (1.0.3.10)$$

$$\Rightarrow (y + \sqrt{E_b})^2 \underset{s_1}{\overset{s_0}{\geq}} (y - \sqrt{E_b})^2 \quad (1.0.3.11)$$

$$\Rightarrow y \underset{s_1}{\overset{s_0}{\geq}} 0 \quad (1.0.3.12)$$

The decision region of BPSK is:

$$y \underset{s_1}{\overset{s_0}{\geq}} 0 \quad (1.0.3.13)$$

1.0.4. Decoding

Consider, y is the received symbol. Then, we need to decode this symbol into bits. Here, we will use decision region to decode into bits.

$$\text{bit} = \begin{cases} y > 0, & \text{bit} = 0 \\ y < 0, & \text{bit} = 1 \end{cases}$$

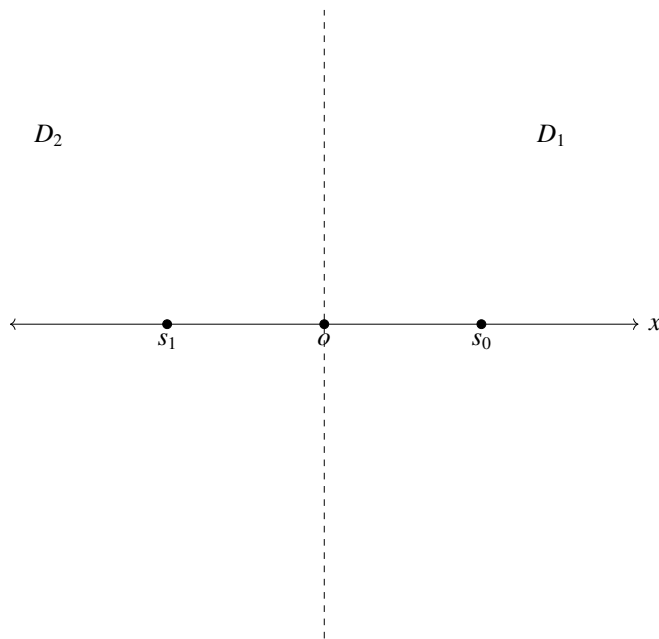


Fig. 1.0.3.1: Decision region for BPSK

So, if received symbol $y > 0$, we decode that symbol into 0 and if $y < 0$ we decode it as 1.

1.0.5. The following code has simulation of ber of BPSK.

codes/psk_ber.py

1.0.6. Fixed point code

- Fixed point code is used to decrease execution time and to decrease no. of bytes used to store data.
- Like, it's easier to store an integer like 1000 than to store a floating number 13.356.
- In computational part of code, decimals take more time to execute compared to integers.

codes/psk_ber.m

In the above code, the computational part of code is,

a signal is received so we need to find no. of -ve values are in that signal. Since, stored values are in decimal. We are converting into integers.

- So, first we are converting noise stored values into integer.

$$n1 = n * 100000 \quad (1.0.6.1)$$

- then, converting signal energy (E_b) into integer.

$$sig = E_b * 100000 \quad (1.0.6.2)$$

- We are doing this because decimal addition are difficult than integer.