

Final Report - Group 01

HDI and Broadband - Data Analysis

Amie Leung, Ivan Nguyen, Janna Cameron, Kaye Ann Caroningan, and Syed Hassan

Nov 29, 2025

Abstract

This report analyzes the relationship between Human Development Index (HDI) and broadband access across various countries, highlighting trends and insights from the data. Lorem ipsum dolor sit amet, consectetur adipiscing elit. In egestas lobortis porta. Phasellus tincidunt metus sed mollis imperdiet. Aliquam blandit nibh in fermentum consequat. Fusce blandit magna quis nulla ornare, non mattis enim tempor. Nulla et odio dui. Nunc ut elit venenatis, porttitor dui et, placerat tortor. Sed aliquet sodales magna, sit amet porta odio tempor in. CHANGE THIS AT THE END

Contents

1. Motivation	2
2. Review of Similar Research	3
3. Research Questions	3
3.1. Question 1	3
3.2. Question 2	3
3.3. Question 3	3
4.1 Loading the files	3
4.2. Data Structure	4
4.3. Selecting the required columns	5
4.4. Standardizing country names - rows	6
4.5. Handling duplicates (if any):	7
4.6. Handling missing values - rows	7
5. Methodology	7
5.2. Data Distribution	8
5.2.1. Distribution of HDI	8
5.2.2. Distribution of Broadband	9
5.2.3. Distribution of GDP	11
5.2.4. Reshape the data	12

Merge the data	12
Skewness	12
Distribution of GDP (2011)	23
Standardization	26
Question 1	26
Descriptives and EDA	26
Correlation matrix	26
Plots	27
Question 2	28
Question 3	28
Descriptives and EDA	29
Plots	29
T-test	29
Wilcoxon-test	30
Question ??	32
Create a multi regression with gdp as the control variable	32
Checking assumptions	33
Lack of Multicollinearity	33
Independence	33
Normality of residuals	33
6. Results and Interpretation	35
7. Discussions	35
Appendix	36
Code	36
References	37

1. Motivation

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condimentum nisi. Sed at pellentesque mi. Vivamus id justo non elit lacinia efficitur. Sed commodo vehicula nisi, a tristique lectus cursus at. Nullam finibus elementum justo, a molestie augue iaculis sit amet. Praesent quis ante sit amet arcu condimentum commodo quis eu lectus. Curabitur pellentesque mattis enim, eu elementum lectus sollicitudin pellentesque. CHANGE THIS OF COURSE

2. Review of Similar Research

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3. Research Questions

3.1. Question 1

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3.2. Question 2

Lorem ipsum dolor sit amet, consectetur adipiscing elit. In egestas lobortis porta. Phasellus tincidunt metus sed mollis imperdiet. Aliquam blandit nibh in fermentum consequat. Fusce blandit magna quis nulla ornare, non mattis enim tempor. Nulla et odio dui. Nunc ut elit venenatis, porttitor dui et, placerat tortor. Sed aliquet sodales magna, sit amet porta odio tempor in. CHANGE THIS OF COURSE

3.3. Question 3

CHANGE THIS OF COURSE # 4. Data {#sec-data}

Lorem ipsum dolor sit amet, consectetur adipiscing elit. In egestas lobortis porta. Phasellus tincidunt metus sed mollis imperdiet. Aliquam blandit nibh in fermentum consequat. Fusce blandit magna quis nulla ornare, non mattis enim tempor. Nulla et odio dui. Nunc ut elit venenatis, porttitor dui et, placerat tortor. Sed aliquet sodales magna, sit amet porta odio tempor in. CHANGE THIS OF COURSE # 4. Data {#sec-data}

We are using three files from the Gapminder dataset:
HDI, Broadband, and GDP. (*Gapminder Datasets 2023*)

4.1 Loading the files

```
hdi <- read.csv("data/hdi_human_development_index.csv")
broadband <- read.csv("data/broadband_subscribers_per_100_people.csv")
gdp <- read.csv("data/gdp_pcav.csv")
```

4.2. Data Structure

In this section we will clean the header names of each dataset and explore and describe the datasets one by one.

1. Human Development Index (HDI): Based on data from the United Nations Development Programme website, this dataset contains the HDI scores for each country between the years 1990 and 2023. There are 193 rows and 35 columns. The data contains some missing values for certain periods.

Let's explore the shape of the dataset.

Rows x Columns

```
## [1] 193 35
```

Since there are 35 columns, let's only see the first and last five columns to see more detail of column names (after cleaning).

```
## [1] "country" "x1990"   "x1991"   "x1992"   "x1993"
## [1] "x2019"   "x2020"   "x2021"   "x2022"   "x2023"
```

The year range of this dataset is 1990 - 2023. We can also see that the column names have “x” characters that need to be cleaned further.

2. Broadband subscribers (per 100 people): This dataset contains the number of fixed broadband subscriptions per 100 people between the years 1998 and 2023. Included in this measurement are all wired connections that provide high-speed internet access (≥ 256 kbits/s), covering both residential and organizational subscriptions but excluding mobile-cellular networks. There are 193 rows and 28 columns. The data contains some missing values, mainly concentrated in the earlier years.

Rows x Columns

```
## [1] 206 27
```

And the first and last five column names:

```
## [1] "country" "x1998"   "x1999"   "x2000"   "x2001"
## [1] "x2019"   "x2020"   "x2021"   "x2022"   "x2023"
```

The year range of this dataset is 1998 - 2023. Again, the column names have “x”s that aren't helpful. Several columns have chr data type, which we will need to clean up.

3. Gross Domestic Product (GDP): Adjusted for inflation and cost-of-living differences, this dataset measures the value of goods and services produced per person for each country, compiling data from the early 19th century to the present year. There are 194 rows and 303 columns.

Rows x Columns

```
## [1] 193 303
```

And the first and last five column names:

```
## [1] "geo"    "name"   "x1800"  "x1801"  "x1802"
```

```
## [1] "x2096" "x2097" "x2098" "x2099" "x2100"
```

This dataset has the most number of years ranging from 1800 - 2100. The future year values might be predicted or empty which we can analyze further when standardizing and cleaning rows. The *geo* column is also interesting as after standardizing the country names, and merging the datasets, we can also map the data if needed.

Please note: all datasets were sourced from the Gapminder repository. Data from the year 2022 coincides with the tail end of the COVID-19 pandemic; however, for the purposes of this report, we will not account for its potential impacts on GDP and HDI, particularly with regard to health.

4.3. Selecting the required columns

Since the dataset has values from 100+ years, we will narrow them down to the most recent decade starting from 2010 to 2023. Will also clean the years by removing the ‘x’ character before we select the columns of interest (“X2010” -> 2010).

HDI

```
##      country 2011 2012 2013 2014 2015 2016 2017 2018 2019 2020 2021
## 1 Afghanistan 0.474 0.484 0.492 0.497 0.496 0.495 0.496 0.498 0.507 0.501 0.486
## 2      Angola 0.545 0.557 0.567 0.577 0.603 0.609 0.610 0.611 0.611 0.610 0.609
## 3     Albania 0.781 0.790 0.793 0.797 0.797 0.797 0.798 0.801 0.805 0.794 0.794
##   2022 2023
## 1 0.495 0.496
## 2 0.615 0.616
## 3 0.806 0.810
```

Need to talk about the values. WHAT DO THE VALUES MEAN

Broadband

```
##      country 2011     2012     2013     2014     2015     2016     2017     2018
## 1       Aruba     NA      NA 18.70000 18.60000 18.2000     NA      NA      NA
## 2 Afghanistan     NA 0.00491 0.00474 0.00457 0.0209 0.0254 0.0257 0.0435
## 3      Angola 0.0653 0.08150 0.08520 0.32300 0.5450 0.2900 0.3210 0.3500
##   2019 2020 2021 2022 2023
## 1 17.700 17.700 17.7000 17.5000      NA
## 2 0.052 0.068 0.0664 0.0796 0.0801
## 3 0.368 0.363 0.3910 0.3870 0.3740
```

Need to talk about the values. WHAT DO THE VALUES MEAN

GDP

```

##      country    2011    2012    2013    2014    2015    2016
## 1 Afghanistan 1962.057 2123.871 2166.402 2145.500 2109.747 2102.452
## 2 Angola     7663.286 8011.050 8099.679 8183.165 7966.886 7487.925
## 3 Albania    11052.778 11227.950 11361.252 11586.817 11878.438 12291.842
##      2017    2018    2019    2020    2021    2022    2023
## 1 2097.120 2061.709 2080.941 1969.306 1517.016 1386.755 1359.020
## 2 7216.061 6878.590 6602.269 6029.692 5911.836 5906.116 5778.834
## 3 12770.992 13317.119 13653.182 13278.370 14595.944 15491.992 16209.877

```

Need to talk about the values. WHAT DO THE VALUES MEAN

4.4. Standardizing country names - rows

Since the datasets might have countries that are not listed in the others, we need to make sure that we standardize all the country names to match one of the datasets as our source. We will take the HDI dataset as our source, and compare the names, and check for the difference in rows/country names. If we find any difference, we will make sure to either match those rows to the source dataset country names, and also remove territories and records that are not common amongst all.

```

## [1] "Number of rows in HDI, Broadband, and GDP datasets:"

## HDI: 193 , Broadband: 206 , GDP: 193

## [1] "Countries in Broadband but NOT in HDI:"

## [1] "Aruba"                  "Bermuda"                "Cayman Islands"
## [4] "Faeroe Islands"          "Gibraltar"              "Greenland"
## [7] "Guam"                   "Macao, China"            "Monaco"
## [10] "New Caledonia"           "Curaçao"                "French Polynesia"
## [13] "British Virgin Islands"

## [1] "Countries in GDP but NOT in HDI:"

## [1] "Monaco"      "North Korea"

```

We can see some differences in countries within each dataset. We will now standardize and filter the data to only focus on countries that are common amongst all three datasets.

After standardizing:

```

## Number of rows in HDI dataset: 191

## Number of rows in Broadband dataset: 191

## Number of rows in GDP dataset: 191

```

Now let's check for duplicates.

4.5. Handling duplicates (if any):

```
## 0 rows removed.
```

```
## 0 rows removed.
```

```
## 0 rows removed.
```

Now that we have standardized names, and checked for duplicates, let's explore the missing values.

4.6. Handling missing values - rows

```
## [1] "Empty values in HDI"
```

```
## [[1]]  
## country 2011 2012 2013 2014 2015 2016 2017 2018 2019  
## 0 1 1 1 1 1 1 1 1 1  
## 2020 2021 2022 2023  
## 1 1 1 0
```

```
## [1] "Empty values in Broadband"
```

```
## [[1]]  
## country 2011 2012 2013 2014 2015 2016 2017 2018 2019  
## 0 14 7 6 7 5 7 7 20 4  
## 2020 2021 2022 2023  
## 6 3 2 40
```

```
## [1] "Empty values in GDP"
```

```
## [[1]]  
## country 2011 2012 2013 2014 2015 2016 2017 2018 2019  
## 0 0 0 0 0 0 0 0 0 0  
## 2020 2021 2022 2023  
## 0 0 0 0
```

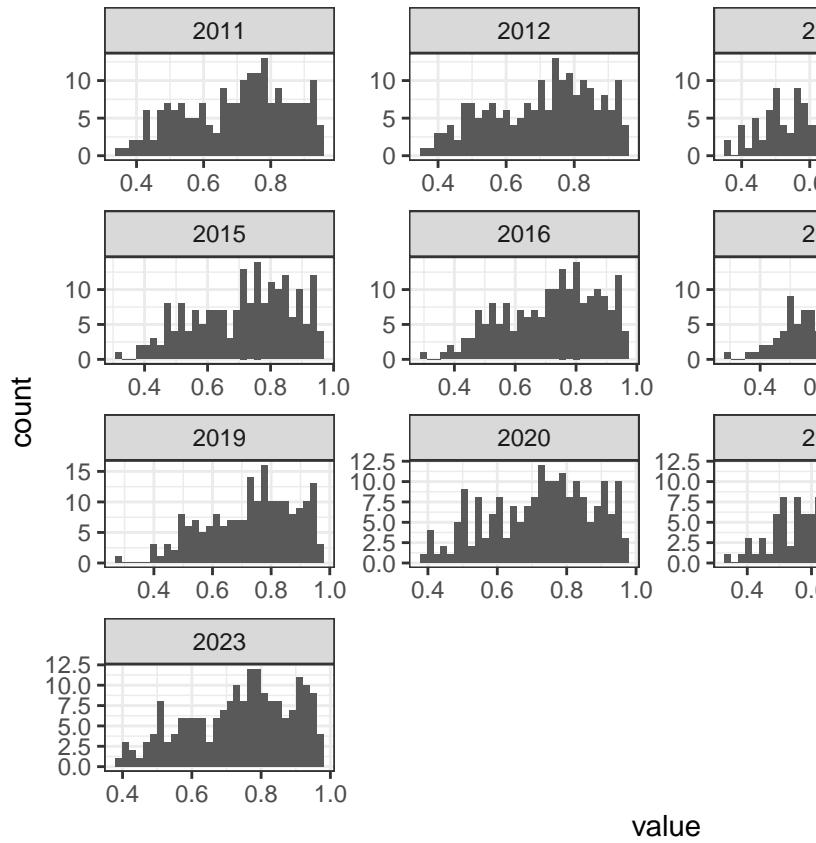
Not dropping any at this point

5. Methodology

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5.2. Data Distribution

5.2.1. Distribution of HDI



#SYED: Can we show the 2011 and 2022 values only?

Table: Data summary

Name	hdi_clean
Number of rows	191
Number of columns	14
<hr/>	
Column type frequency:	
character	1
numeric	13
<hr/>	
Group variables	None

Variable type: character

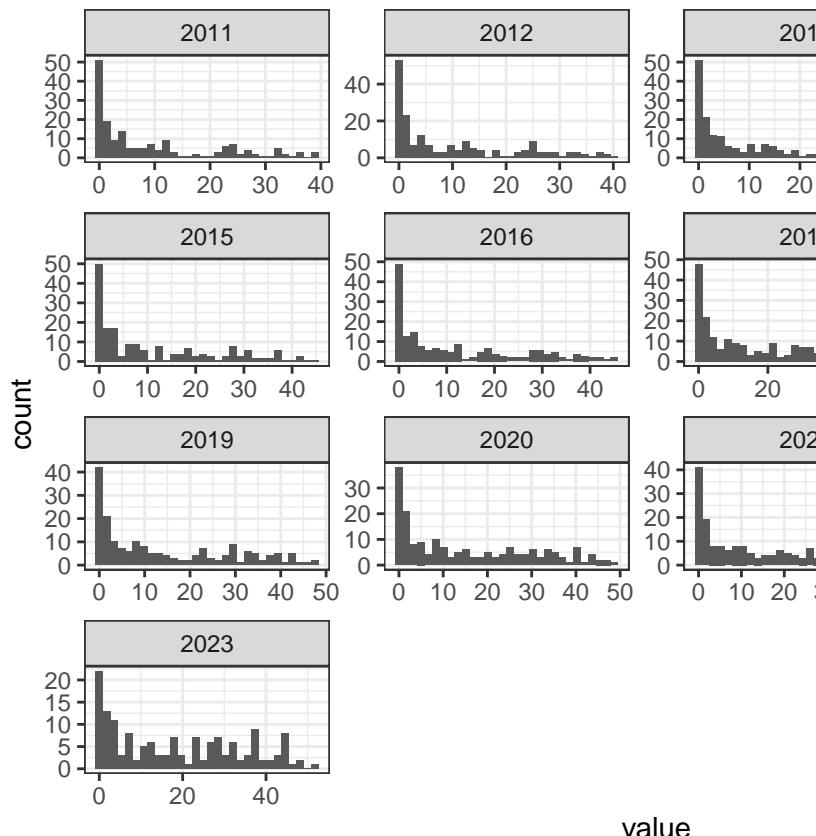
skim_variable	n_missing	complete_rate	min	max	empty	n_unique	whitespace
country	0	1	2	30	0	191	0

Variable type: numeric

skim_variable	n_missing	complete_rate	mean	sd	p0	p25	p50	p75	p100	hist
2011	1	0.99	0.70	0.15	0.35	0.57	0.72	0.82	0.95	
2012	1	0.99	0.71	0.15	0.36	0.58	0.73	0.82	0.95	
2013	1	0.99	0.71	0.15	0.36	0.58	0.74	0.83	0.95	
2014	1	0.99	0.71	0.15	0.32	0.59	0.74	0.83	0.96	
2015	1	0.99	0.72	0.15	0.32	0.60	0.74	0.84	0.96	
2016	1	0.99	0.72	0.15	0.30	0.61	0.75	0.84	0.96	
2017	1	0.99	0.72	0.15	0.29	0.61	0.75	0.84	0.96	
2018	1	0.99	0.73	0.15	0.37	0.61	0.75	0.85	0.97	
2019	1	0.99	0.73	0.15	0.28	0.61	0.75	0.85	0.97	
2020	1	0.99	0.73	0.15	0.39	0.61	0.74	0.84	0.97	
2021	1	0.99	0.73	0.15	0.34	0.61	0.74	0.84	0.97	
2022	1	0.99	0.74	0.15	0.38	0.62	0.76	0.85	0.97	
2023	0	1.00	0.74	0.15	0.39	0.62	0.76	0.86	0.97	

Comment on the distribution

5.2.2. Distribution of Broadband



#SYED: Can we show the 2011 and 2022 values only?

Table: Data summary

Name	broadband_clean
Number of rows	191
Number of columns	14

Column type frequency:	
character	1
numeric	13
Group variables	None

Variable type: character

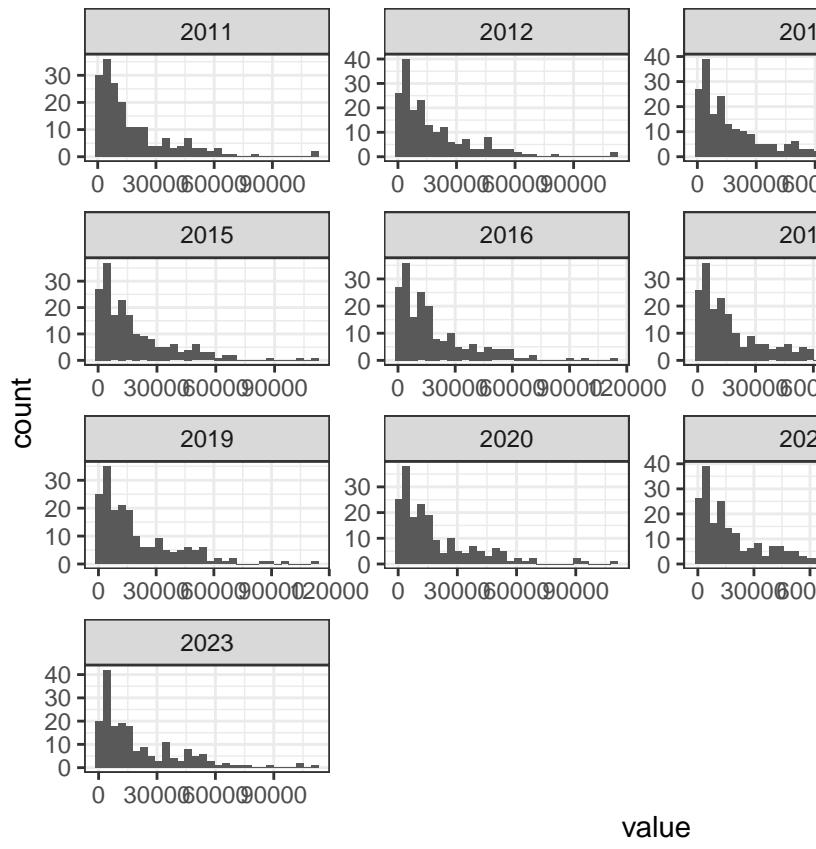
skim_variable	n_missing	complete_rate	min	max	empty	n_unique	whitespace
country	0	1	2	30	0	191	0

Variable type: numeric

skim_variable	n_missing	complete_rate	mean	sd	p0	p25	p50	p75	p100	hist
2011	14	0.93	9.61	11.31	0	0.40	4.26	16.20	38.9	
2012	7	0.96	10.06	11.66	0	0.38	4.73	17.45	40.2	
2013	6	0.97	10.63	12.08	0	0.47	4.94	18.40	42.5	
2014	7	0.96	11.24	12.47	0	0.54	5.62	19.80	43.2	
2015	5	0.97	11.78	12.90	0	0.61	6.31	20.70	44.7	
2016	7	0.96	12.40	13.25	0	0.69	7.11	21.97	45.1	
2017	7	0.96	13.23	13.99	0	0.83	8.14	22.98	62.2	
2018	20	0.90	14.43	14.03	0	1.33	10.00	27.20	47.4	
2019	4	0.98	14.00	14.28	0	1.06	8.85	26.55	47.5	
2020	6	0.97	15.07	14.70	0	1.30	9.40	27.10	48.7	
2021	3	0.98	15.48	14.98	0	1.37	10.60	27.20	50.3	
2022	2	0.99	16.08	15.25	0	1.48	11.00	29.00	51.2	
2023	40	0.79	18.41	15.52	0	2.78	16.10	31.55	51.7	

Comment on the distribution

5.2.3. Distribution of GDP



#SYED: Can we show the 2011 and 2022 values only?

Table: Data summary

Name	gdp_clean
Number of rows	191
Number of columns	14
<hr/>	
Column type frequency:	
character	1
numeric	13
<hr/>	
Group variables	None

Variable type: character

skim_variable	n_missing	complete_rate	min	max	empty	n_unique	whitespace
country	0	1	2	30	0	191	0

Variable type: numeric

skim_variable	n_missing	complete_rate	mean	sd	p0	p25	p50	p75	p100	hist
2011	0	1	18175.43	19634.09	807.66	3705.53	10933.21	24937.33	111840.3	

skim_variable	missing	complete	rate	mean	sd	p0	p25	p50	p75	p100	hist
2012	0	1	18359.22	19518.19	506.72	3770.56	11098.89	25689.84	110892.4		
2013	0	1	18472.83	19488.91	624.18	3968.33	11361.25	25872.48	110354.4		
2014	0	1	18700.32	19561.46	614.46	4033.83	11767.16	26482.08	110611.0		
2015	0	1	18979.66	19815.30	594.92	4172.21	12030.38	27189.90	110483.3		
2016	0	1	19226.13	19995.38	501.11	4321.96	12336.90	27857.71	113510.3		
2017	0	1	19559.76	20168.35	458.77	4518.15	12497.82	28710.15	112243.4		
2018	0	1	19916.38	20450.98	435.41	4530.59	13218.92	29622.61	111441.6		
2019	0	1	20184.39	20670.50	425.94	4803.56	13215.57	30351.18	112461.8		
2020	0	1	19053.94	19977.86	386.68	4691.03	12407.79	26943.40	109597.0		
2021	0	1	20164.82	21367.89	395.80	4829.15	13045.93	30234.91	115683.5		
2022	0	1	20922.87	22044.01	364.70	4736.43	13148.07	33000.12	114938.7		
2023	0	1	21088.15	21712.32	354.18	4859.07	13416.93	33417.31	111043.4		

Comment on the distribution

5.2.4. Reshape the data

Merge the data

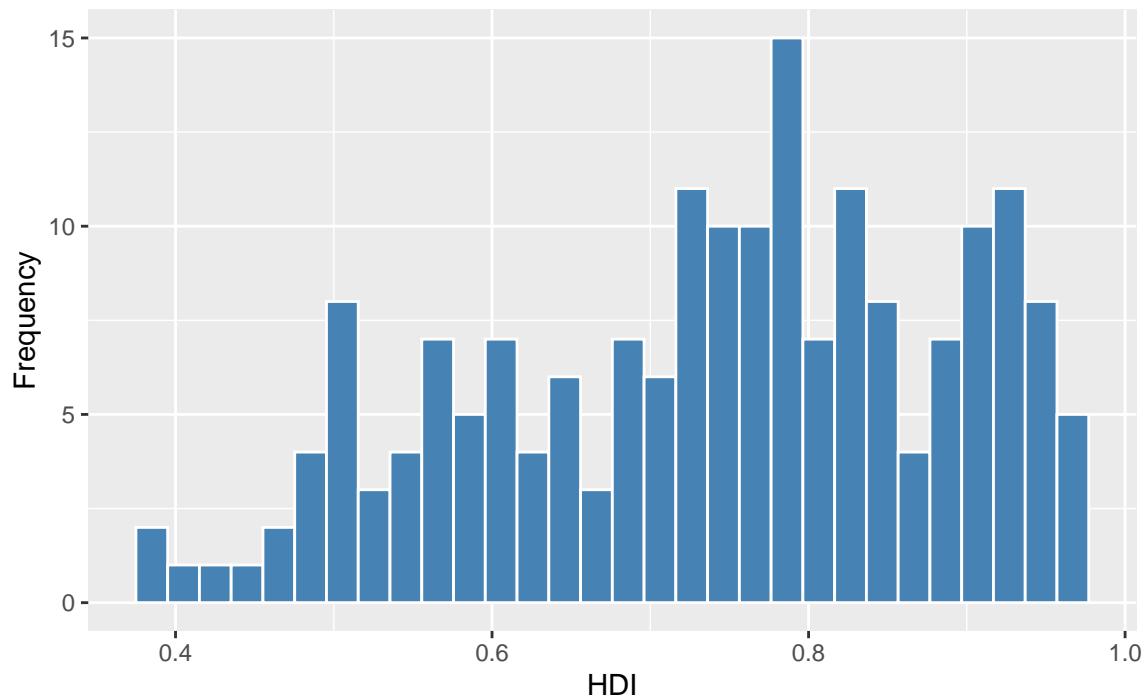
Skewness

Although the original data spanned multiple years, this analysis focuses only on 2011 and 2022. We chose the former column as this coincides with the year that the UN declared internet access a basic human right (United Nations Human Rights Council, 2011). Although 2023 is the most recent year in our dataset, we decided to use 2022 because this year had the fewest missing values. More than 10% of the values for broadband subscriptions in 2023 (49/193) were missing.

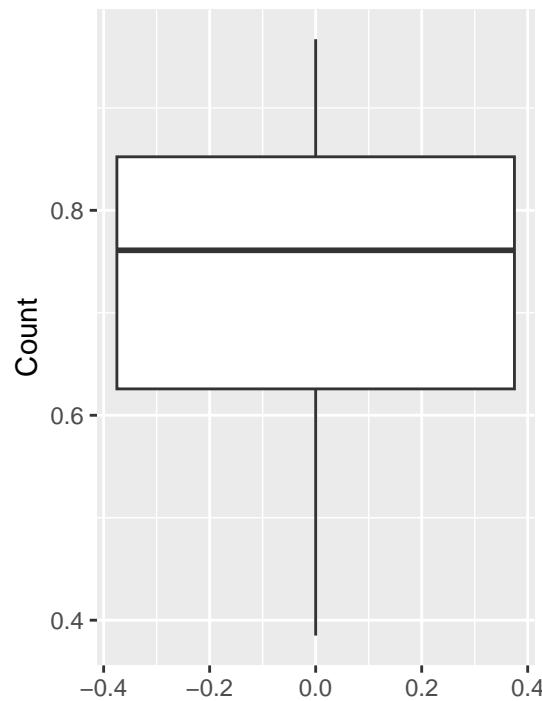
Before modelling, we conducted an exploratory data analysis on the 2011 and 2022 distributions of HDI, broadband subscriptions, and GDP using histograms and boxplots to assess skewness and normality.

Distribution of Human Development Index (2022) The 2022 HDI histogram and boxplot below indicate a mild left skew. However, because the skewness is not substantial, we chose not to transform the data.

Human Development Indices (HDI) in 2022

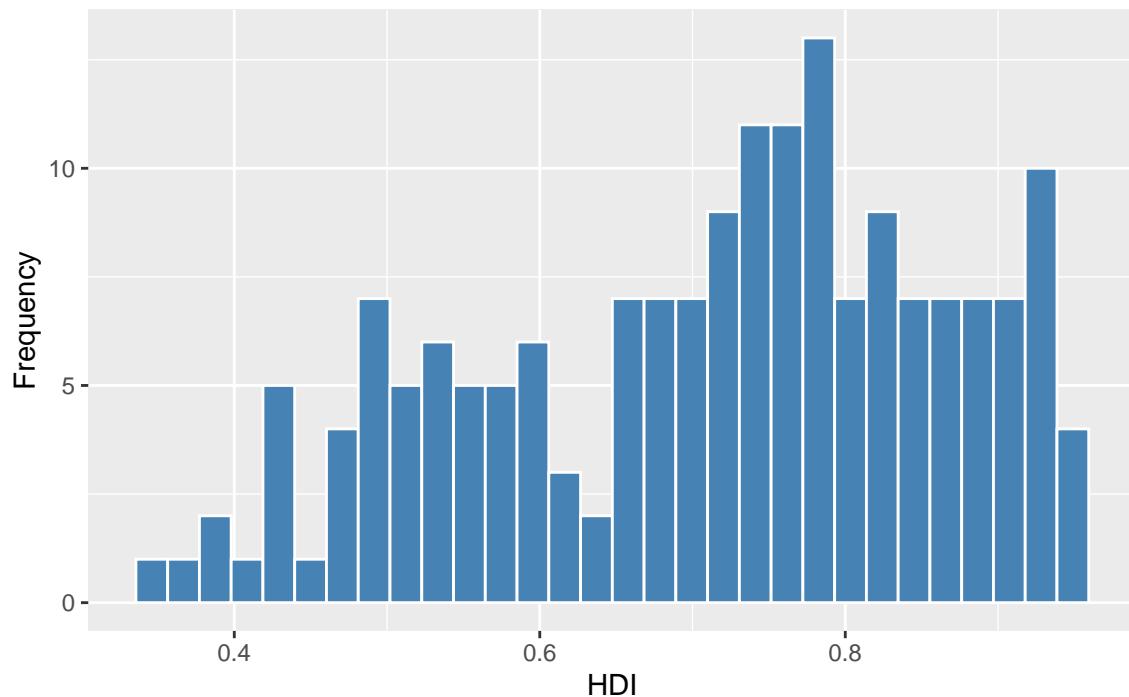


Human Development Indices (HDI) in 2022

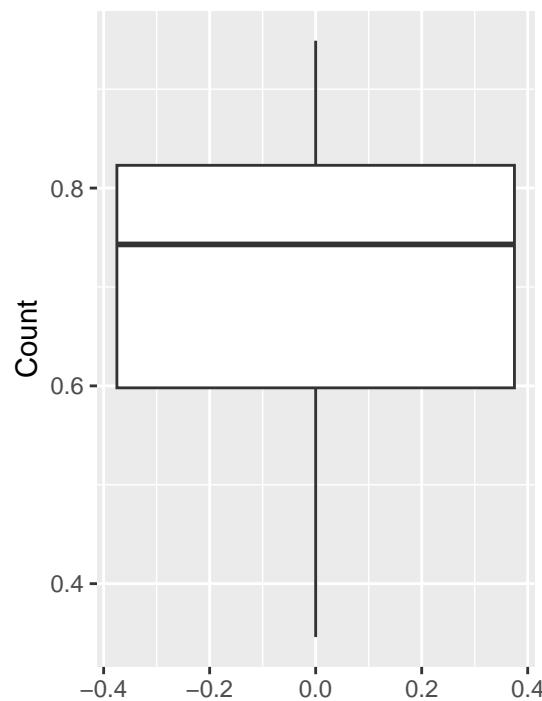


Distribution of Human Development Index (2011) The 2011 HDI histogram and boxplot also show a mild left skew. Similar to the 2022 HDI data, the skewness is not substantial, therefore we chose not to transform the data.

Human Development Indices (HDI) in 2011

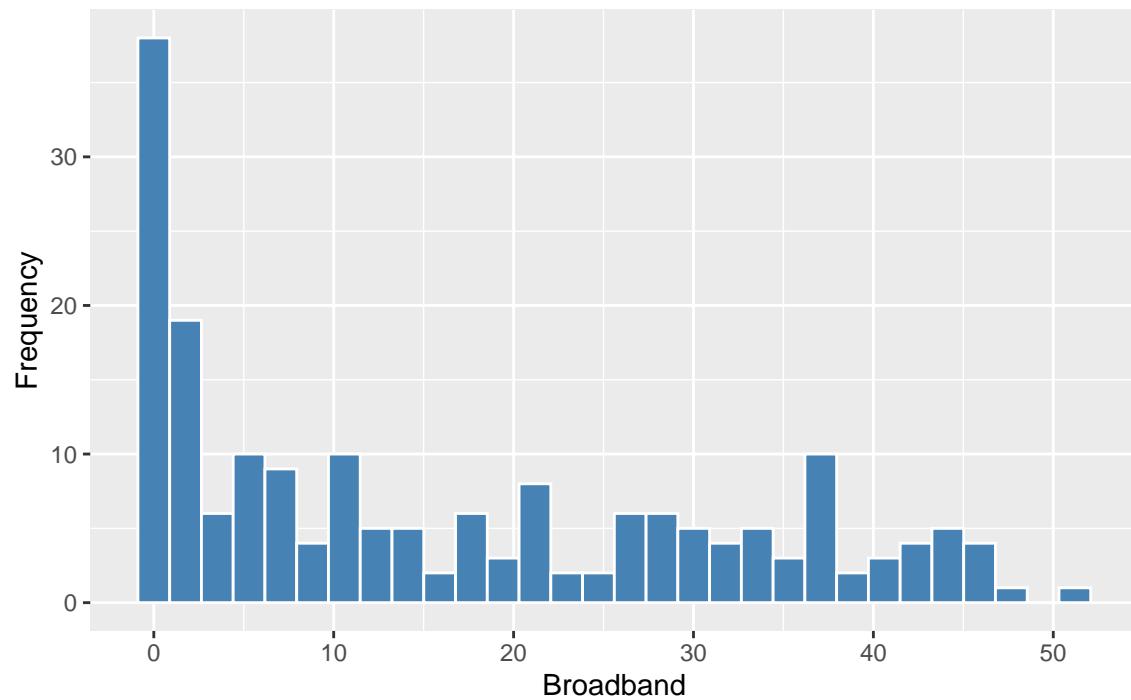


Human Development Indices (HDI) in 2011

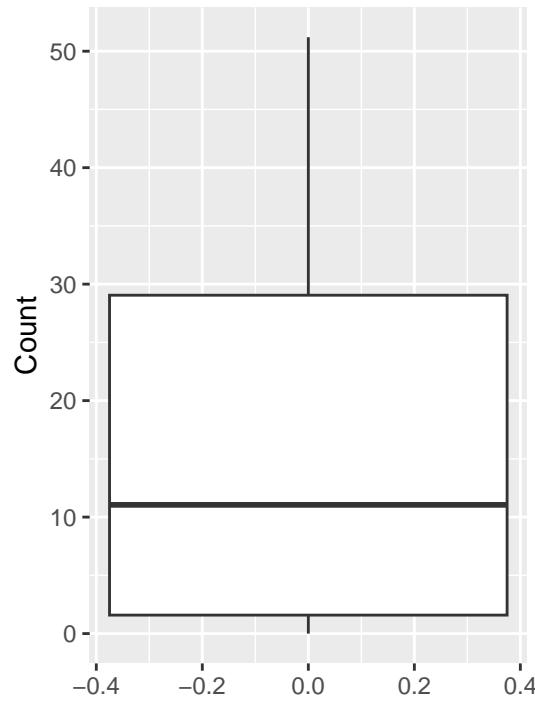


Distribution of Broadband (2022) The 2022 broadband subscription histogram and boxplot show a strong right skew, indicating the need to transform this variable before running the linear regression model.

Distribution of Broadband in 2022

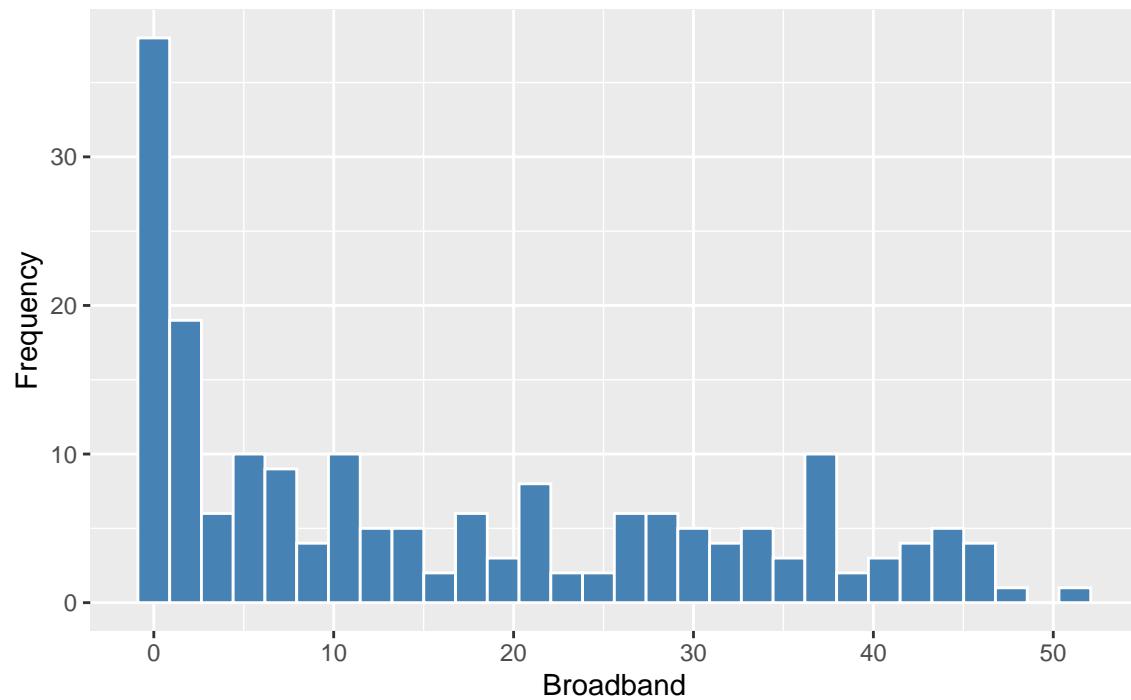


Box plot of Broadband in 2022

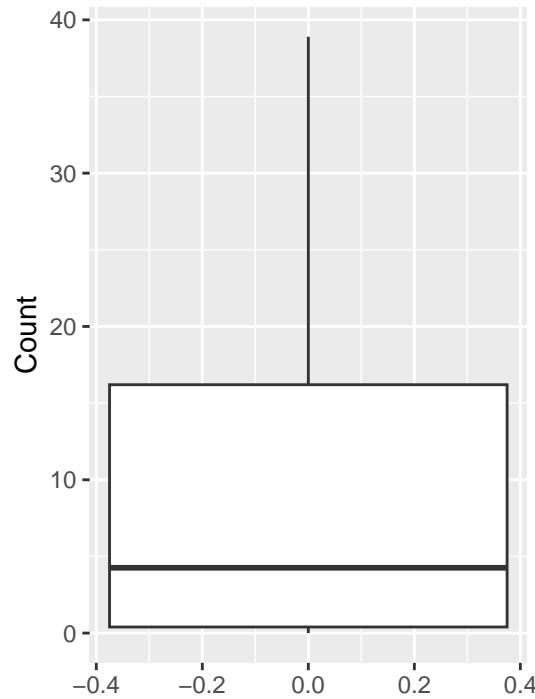


Distribution of Broadband (2011) The 2011 broadband subscription data is also strongly right skewed based on the histogram and boxplot below. Therefore, we also need to transform this variable before including them in our model.

Distribution of Broadband in 2011



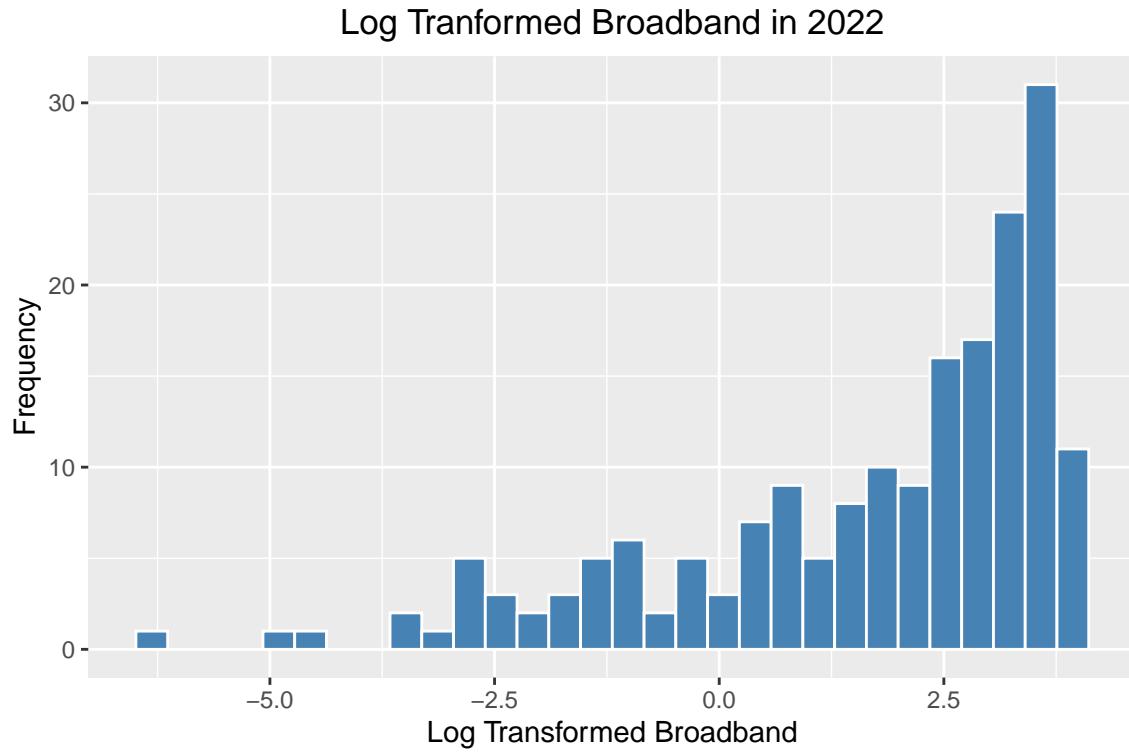
Box plot of Broadband in 2011



Option 1: Log Transform To address the severe right skew in the 2022 broadband subscription values, we applied a log transformation. First, all countries with a broadband value of zero were removed, as the

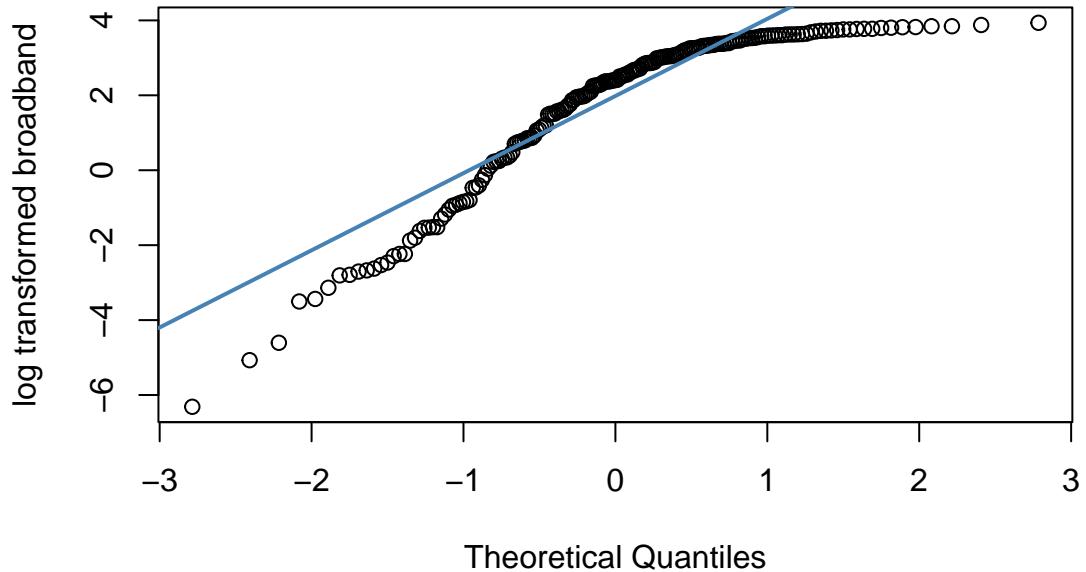
logarithm of zero is undefined. We then created a new column, log_broadband, by taking the natural log of the broadband subscription values in the data set.

After the transformation, we visualized the distribution of log_broadband using a histogram and Quantile - Quantile (Q-Q) plot to assess whether the skewness had improved. However, the histogram and Q-Q plot indicate that the log transformation did not adequately normalize the data.



```
##  
## Shapiro-Wilk normality test  
##  
## data: data_2022$log_broadband  
## W = 0.85633, p-value = 2.711e-12
```

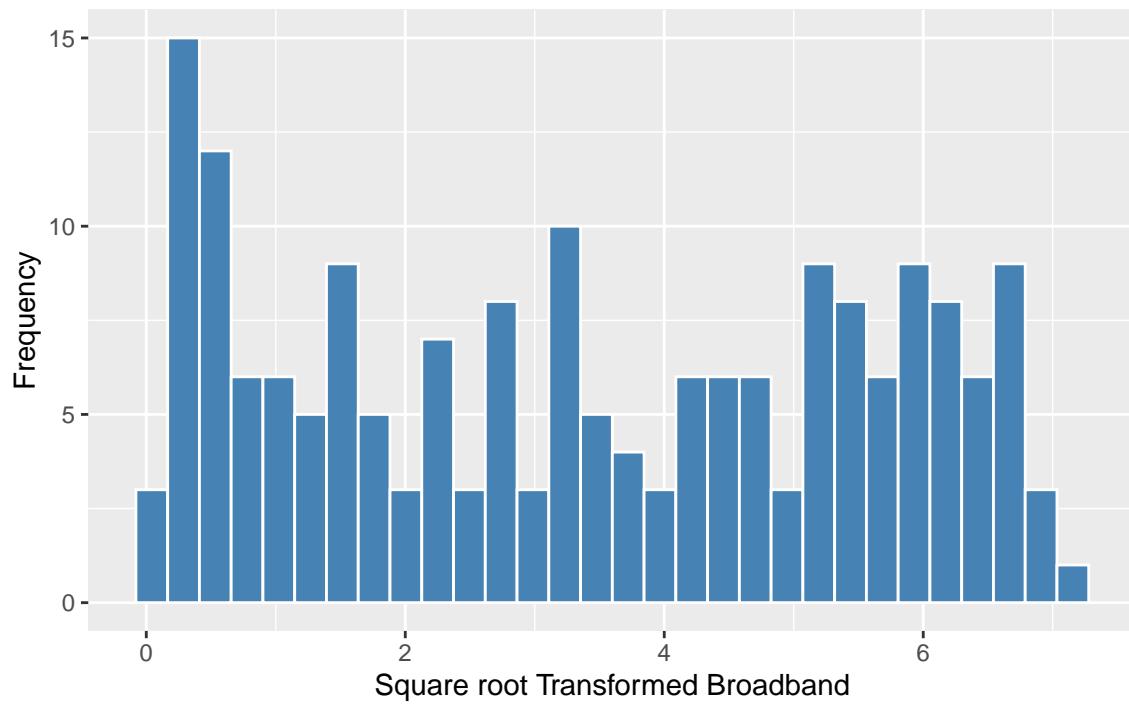
Q-Q Plot for log transformed broadband



The histogram shows that the log-transformed broadband values in 2022 is left-skewed. Furthermore, the S-shaped curve on the Q-Q plot provides further evidence that the log transformed data do not appear to have a normal distribution.

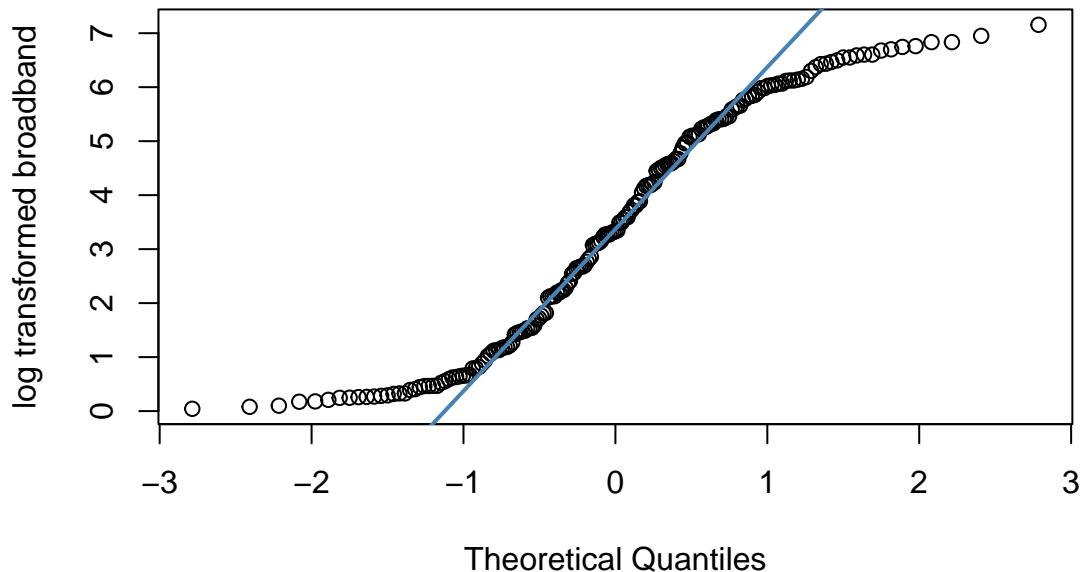
Option 2: Square root Transform Because the log transformation did not sufficiently improve normality, we then consider a square root transformation instead. We created another column, `sqrt_broadband`, by taking the square root of the broadband subscription values in the 2022 dataset. After that, we created the histogram and Q-Q plot to visualize the distribution, which show a noticeable improvement in symmetry compared to both the original and log-transformed values

Square root Tranformed Broadband in 2022



```
##  
## Shapiro-Wilk normality test  
##  
## data: data_2022$sqrt_broadband  
## W = 0.9293, p-value = 6.888e-08
```

Q-Q Plot for Square root transformed broadband



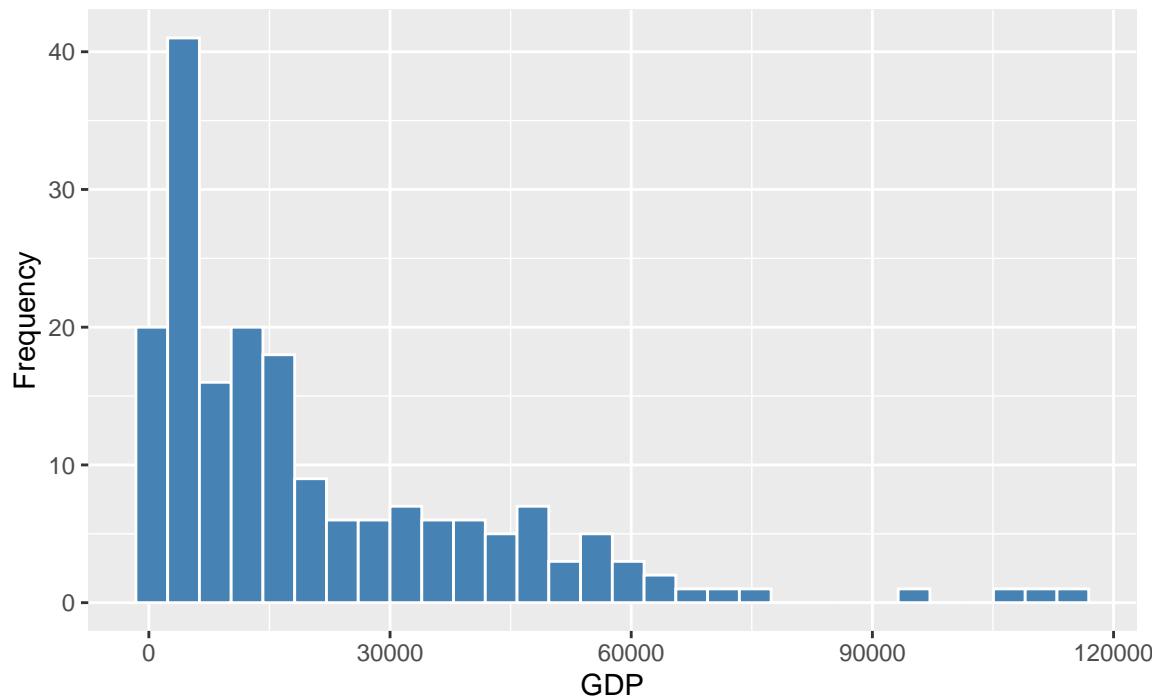
The histogram of the square root-transformed broadband values appears more evenly distributed across the range. Besides that, the Q-Q plot also confirms that the square root transformation brings the data closer to normality, where the points closely follow the theoretical normal line, indicating good alignment with a normal distribution.

Overall, these results make square root transformation a more appropriate approach for the 2022 broadband subscription variable.

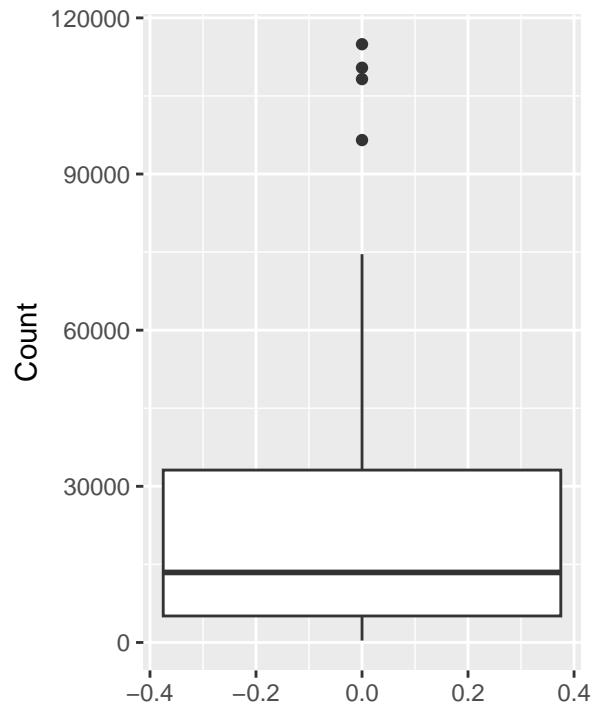
Square root Transform for 2011 broadband Because we applied a square-root transformation to the 2022 broadband subscription data, we can apply the same transformation to the 2011 broadband values for consistency. The histogram and Q-Q plot show that the square-root transformation effectively reduces skewness and moves the 2011 broadband subscription data closer to a normal distribution.

Distribution of Gross Domestic Product (2022) GDP values in 2022 shows a highly skewed distribution as shown in the histogram and boxplot below. The box plot also shows numerous statistical outliers. This suggests that GDP values in 2022 will need to be transformed before including in the regression model.

Gross Domestic Product (GDP) in 2022

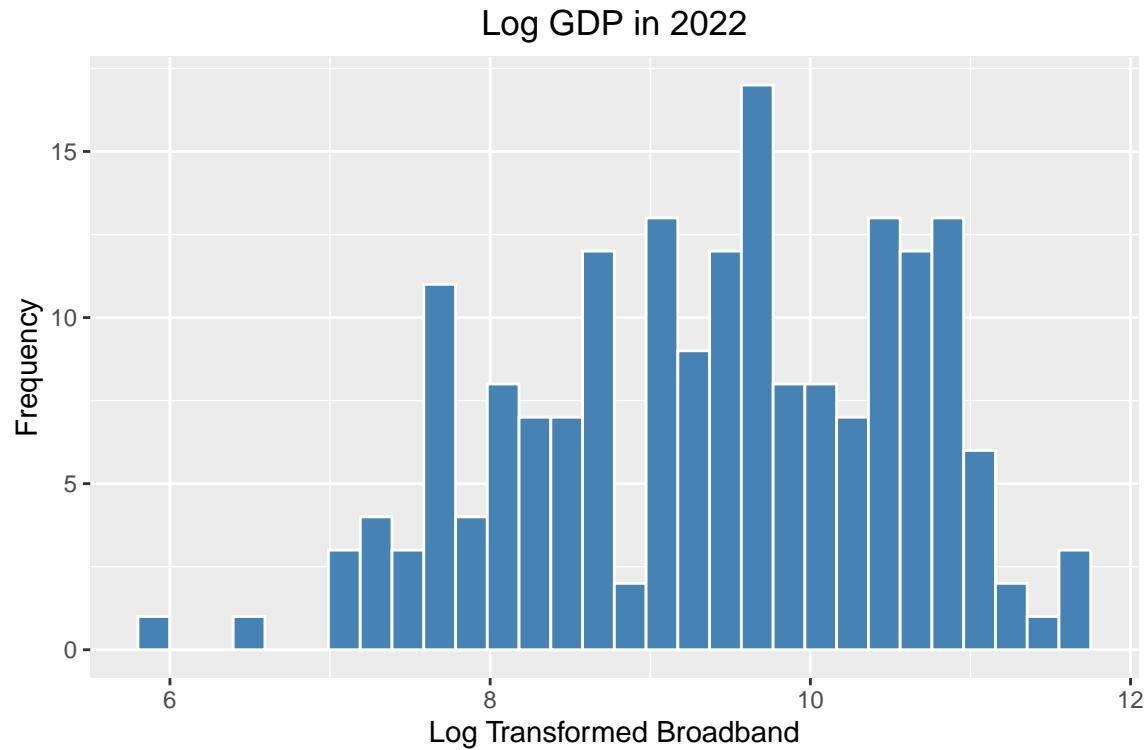


Box plot of GDP in 2022



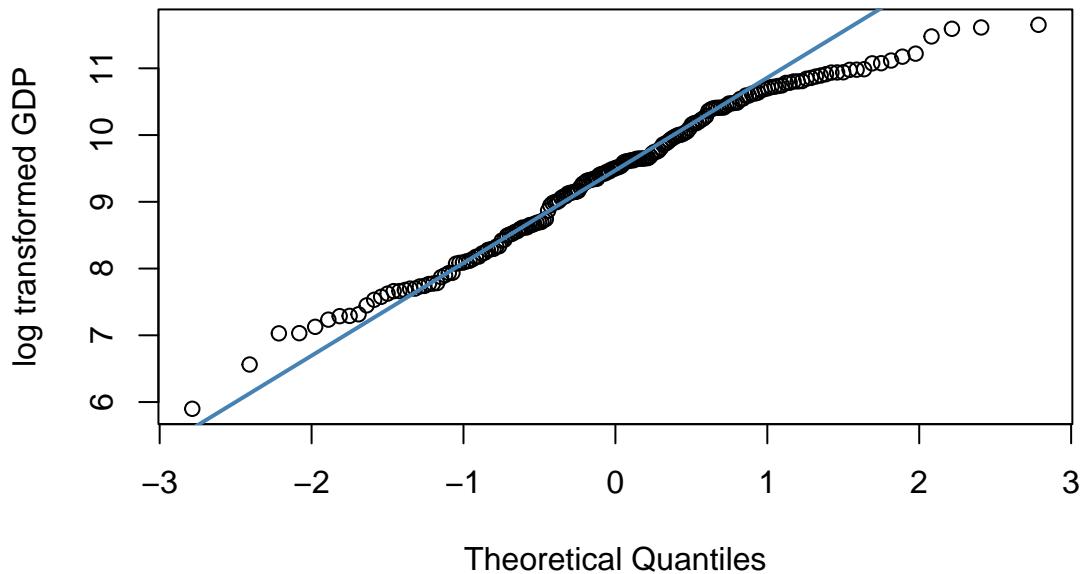
Log Transform for 2022 GDP After applying a log transformation to 2022 GDP values, the distribution becomes more symmetric and approximately normal. The histogram indicates reduced skewness compared to the original data. The Q-Q plot confirms this with most points falling closely along the theoretical normal

line. Overall, the log transformation is effective in improving the suitability of GDP for the regression modelling.



```
##  
## Shapiro-Wilk normality test  
##  
## data: data_2022$log_gdp  
## W = 0.97764, p-value = 0.004284
```

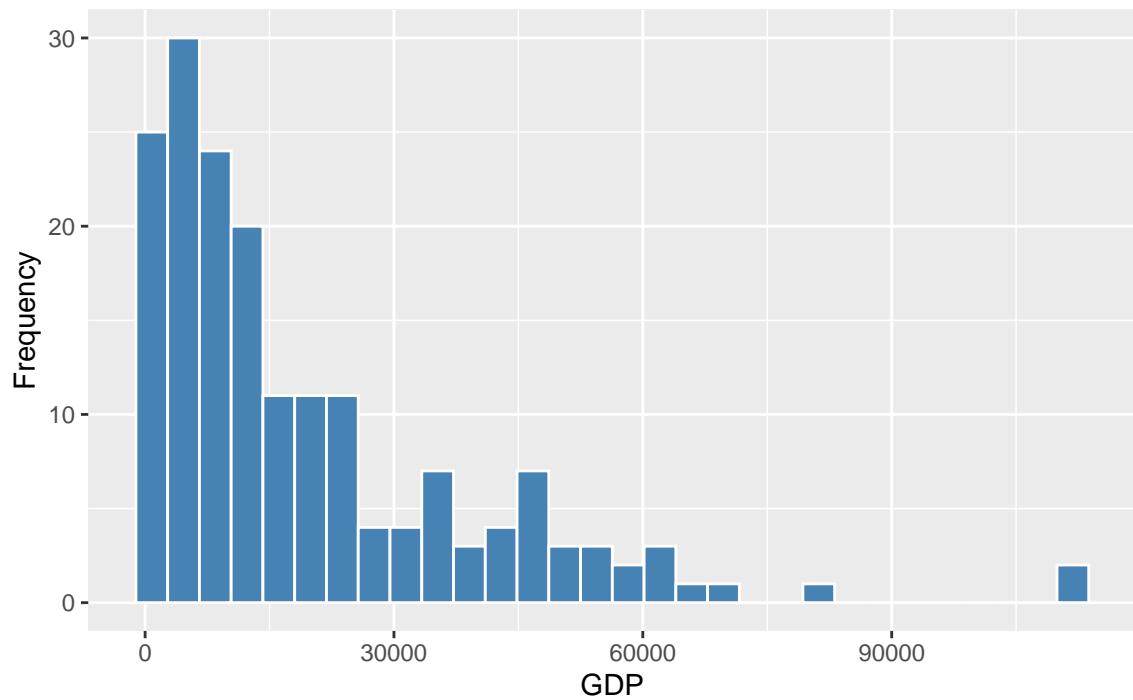
Q-Q Plot for log transformed GDP in 2022



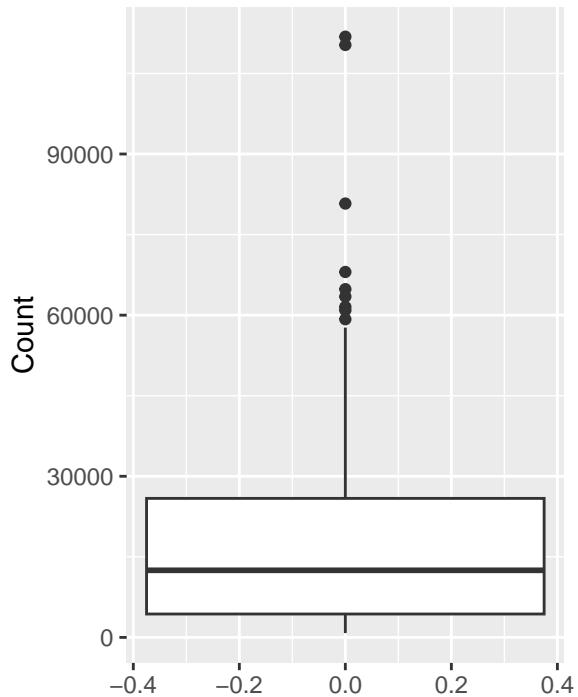
Distribution of GDP (2011)

The distribution of GDP in 2011 is highly right-skewed, as shown by both the histogram and the box plot. There are several extreme values appear as outliers well above the upper whisker. We will need to transform the data before including it in the model.

Gross Domestic Product (GDP) in 2011

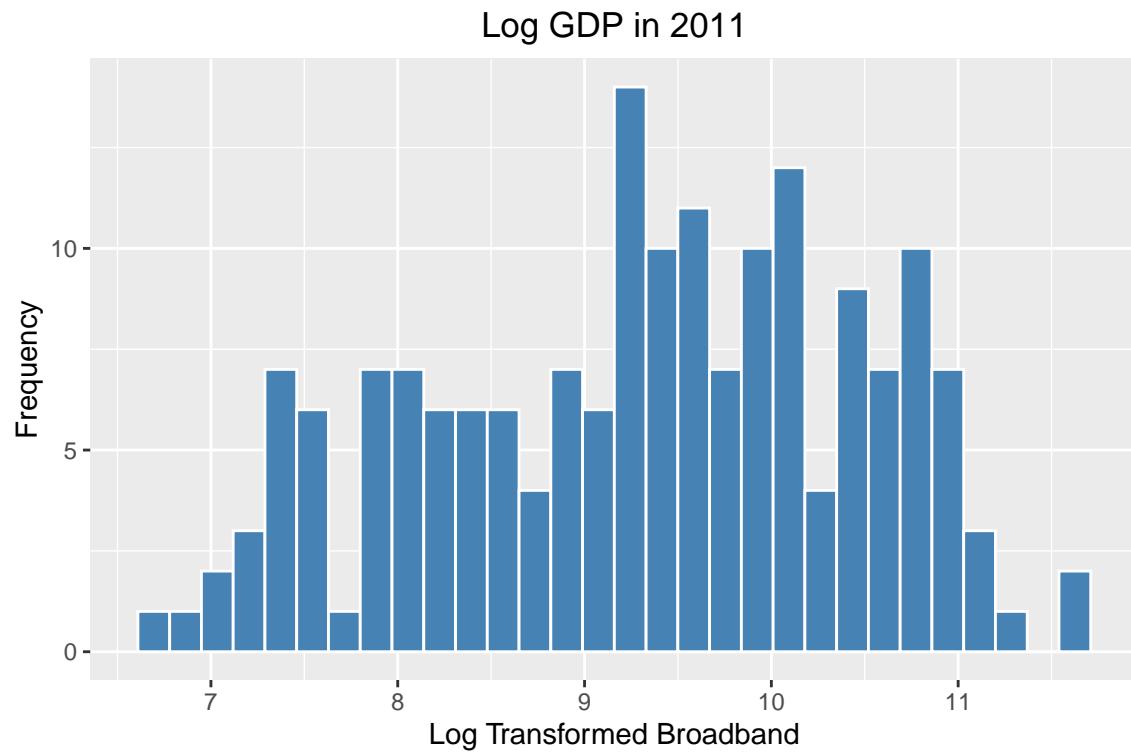


Box plot of GDP in 2011



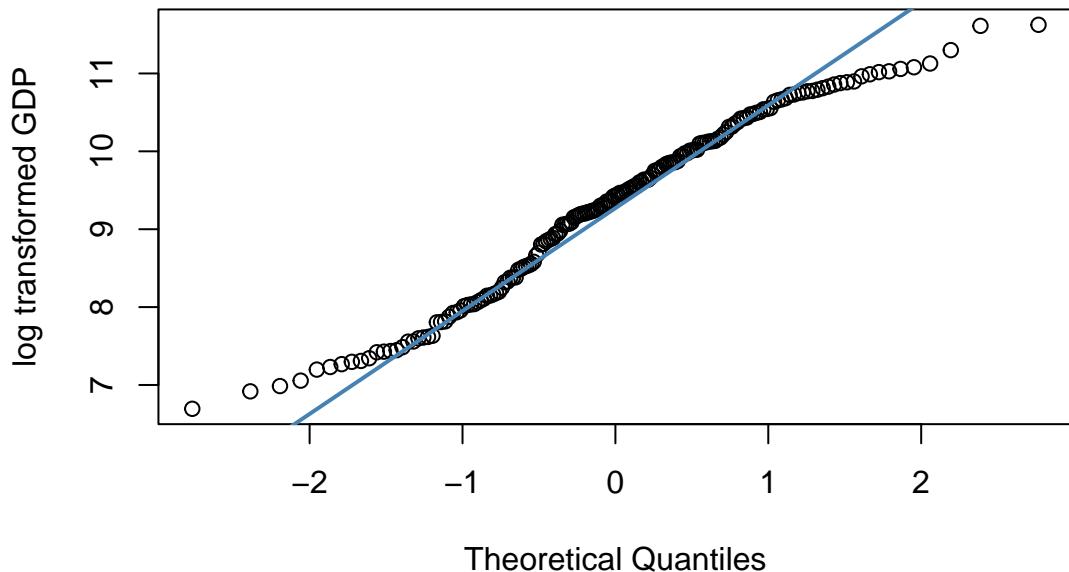
Since a log transformation was successfully applied to the 2022 GDP values, the same approach will be used for the 2011 data. After applying a log transformation, the distribution of GDP in 2011 becomes much more symmetric and closer to a normal shape. The Q-Q plot also shows most points fall closely

along the theoretical normal line, indicating that the transformed data approximates normality. Overall log transformation effectively reduces skewness and makes the data more suitable for modelling.



```
##  
## Shapiro-Wilk normality test  
##  
## data: data_2011$log_gdp  
## W = 0.97339, p-value = 0.001804
```

Q-Q Plot for log transformed GDP in 2011



Standardization

We standardized our data using z-scores to ensure that all variables were equally weighted in our analysis. Standardization is the process of transforming raw values into z-scores, which express each observation relative to the mean and standard deviation of its variable.

For each year (2011 and 2022), we calculated the mean and standard deviation of each variable. Z-scores were computed using the formula $z = (x - \mu) / \sigma$, where x is the observation value, μ is the mean, and σ is the standard deviation of the variable.

This transformation produced standardized variables with a mean of 0 and standard deviation of 1, allowing for comparisons across our three variables HDI, Broadband access, and GDP.

Question 1

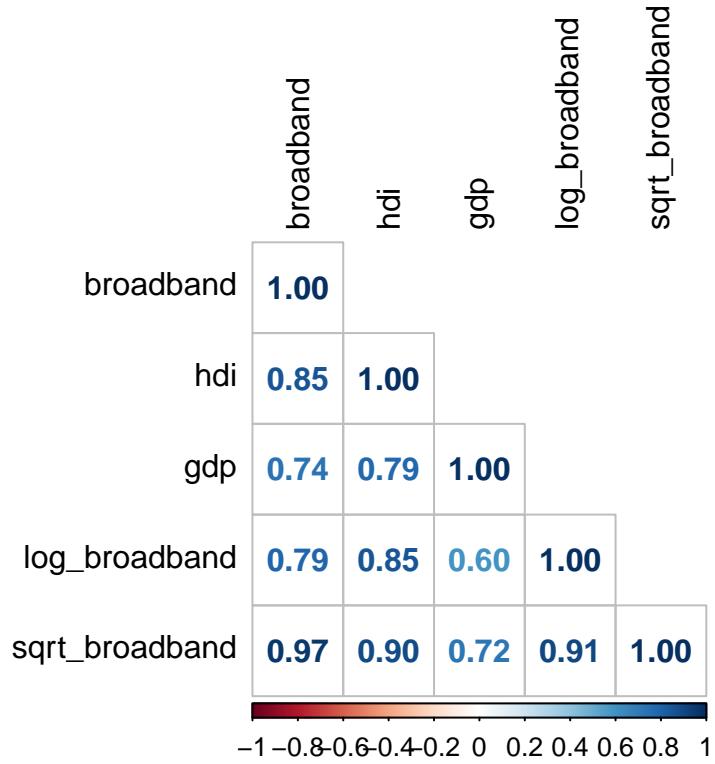
What is the relationship between HDI and broadband subscriptions, based on the latest available data, which is 2022.

Descriptives and EDA

Let's peek at means and standard deviations.

Correlation matrix

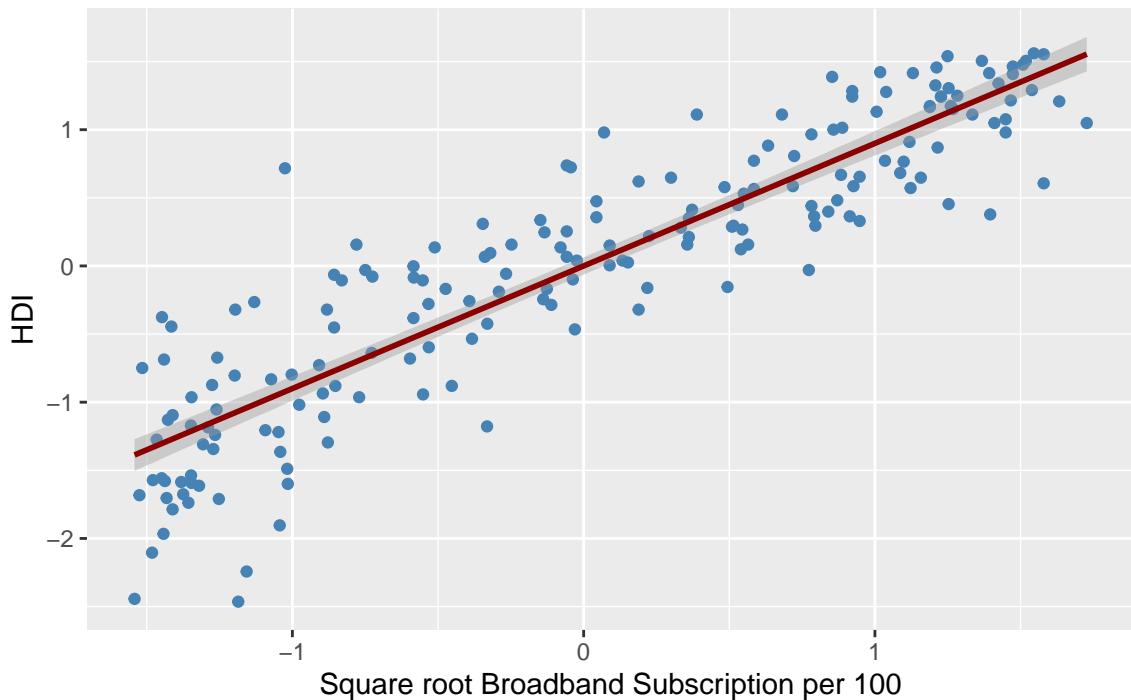
Let's look at the correlations between the independent variables. We want there to be low correlations for no multicollinearity.



Plots

Scatterplot

Scatter Plot with Best Fitted Line of Square root Broadband vs HDI in 2015



```

## 
## Call:
## lm(formula = hdi ~ sqrt_broadband + log_gdp, data = data_2022_standardized)
## 
## Residuals:
##      Min       1Q   Median       3Q      Max 
## -0.87118 -0.14524  0.02077  0.13574  0.79086 
## 
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)    
## (Intercept) -6.138e-16 1.926e-02   0.00     1    
## sqrt_broadband 2.940e-01 3.869e-02    7.60 1.46e-12 ***
## log_gdp       6.991e-01 3.869e-02   18.07 < 2e-16 ***
## --- 
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1 
## 
## Residual standard error: 0.2633 on 184 degrees of freedom
## Multiple R-squared:  0.9314, Adjusted R-squared:  0.9307 
## F-statistic:  1249 on 2 and 184 DF,  p-value: < 2.2e-16

```

Question 2

Are there countries that significantly deviate from this relationship between HDI and broadband subscription rate?

```

## # A tibble: 2 x 10
##   country broadband hdi   gdp log_broadband sqrt_broadband log_gdp
##   <chr>      <dbl> <dbl> <dbl>        <dbl>        <dbl> <dbl>
## 1 Kiribati    -1.06 -0.687 -0.874      -2.03      -1.44  -1.51
## 2 Mali         -1.02 -2.24  -0.870      -0.903      -1.16  -1.48
## # i 3 more variables: fitted_hdi <dbl>, residuals <dbl>, std_resid <dbl>

```

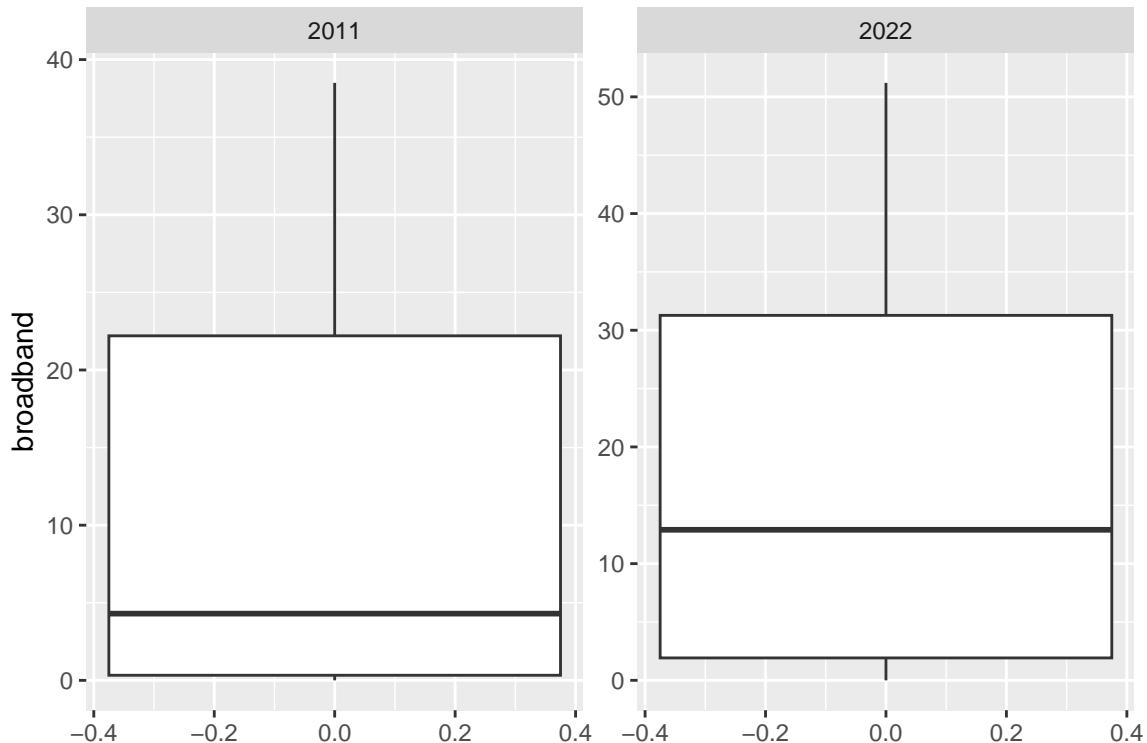
Our outliers in 2022 are Kiribati and Mali

Question 3

How has broadband access by country changed between 2011, when the UN declaration was announced, and 2022?

Descriptives and EDA

Plots

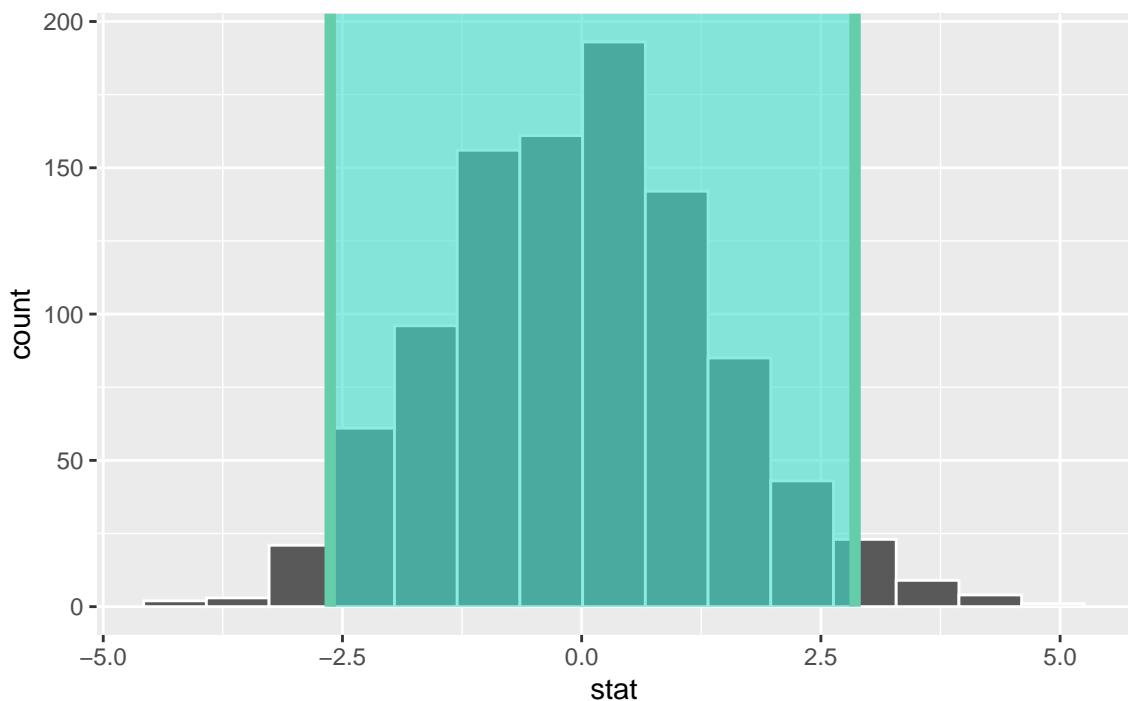


T-test

```
## [1] -9.393962 -3.880547
## attr(,"conf.level")
## [1] 0.95

## # A tibble: 1 x 2
##   lower_ci upper_ci
##       <dbl>    <dbl>
## 1     -2.63     2.86
```

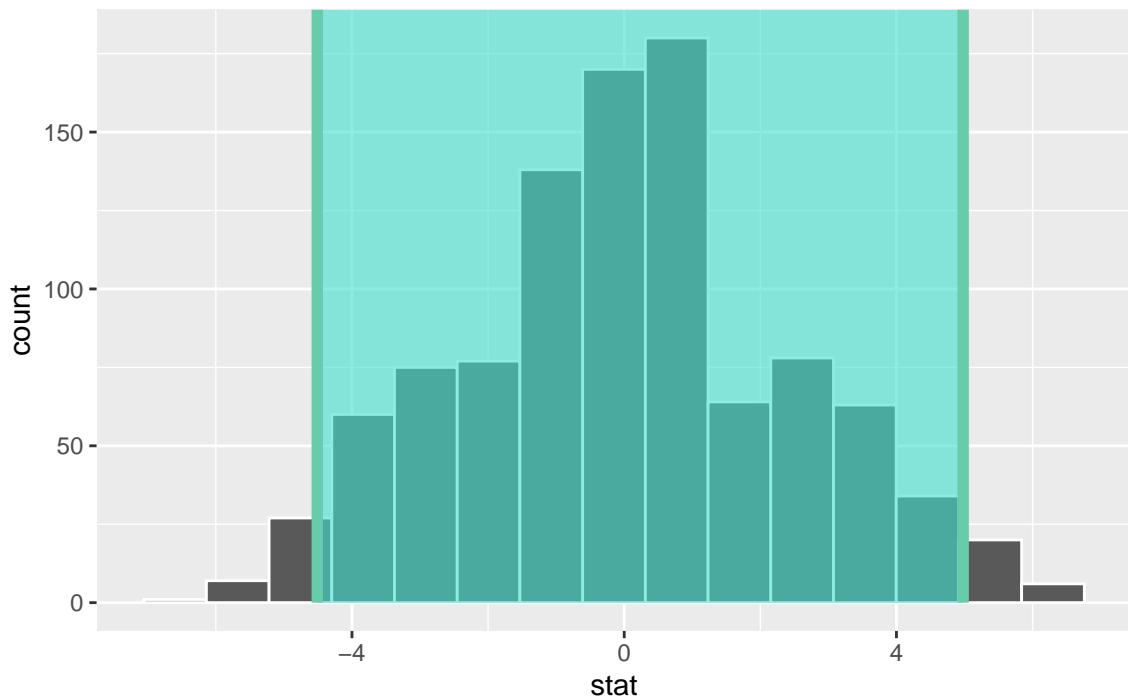
Simulation-Based Null Distribution



Wilcoxin-test

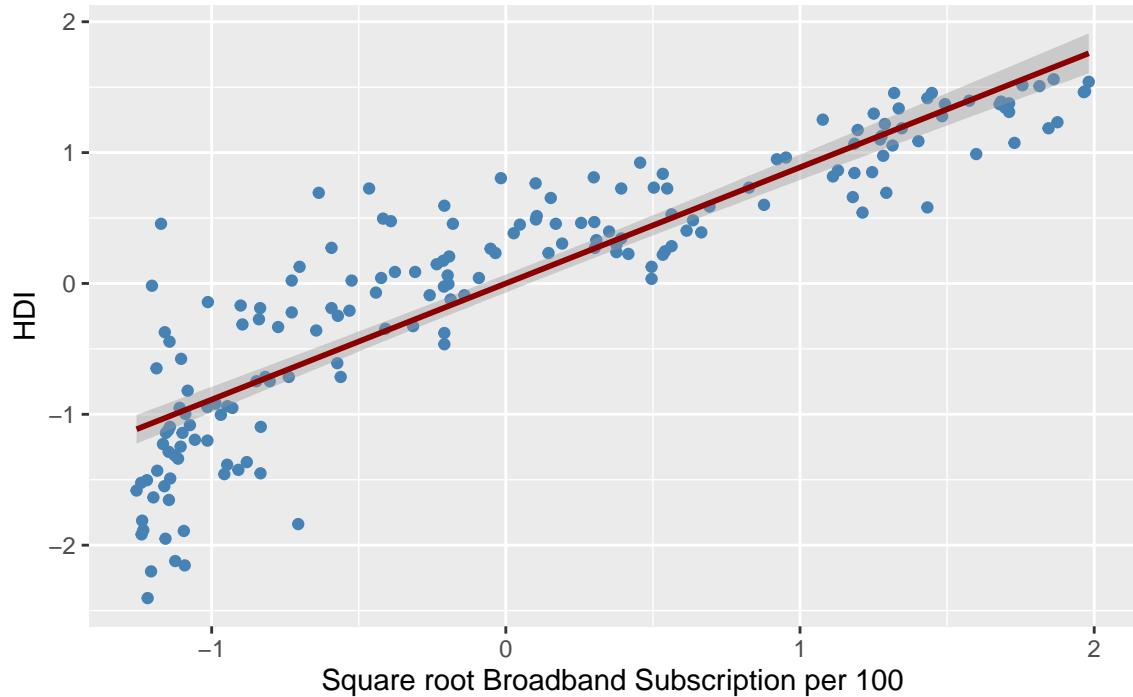
```
##  
##  Wilcoxon rank sum test with continuity correction  
##  
##  data:  data_2011$broadband and data_2022$broadband  
##  W = 12189, p-value = 1.391e-05  
##  alternative hypothesis: true location shift is not equal to 0  
  
##  NULL  
  
## # A tibble: 1 x 2  
##   lower_ci upper_ci  
##     <dbl>    <dbl>  
## 1     -4.51     4.98
```

Simulation-Based Null Distribution



Scatterplot

Scatter Plot with Line of Best Fit of Square root Broadband vs HDI in 201



##

```

## Call:
## lm(formula = hdi ~ sqrt_broadband + log_gdp, data = data_2011_standardized)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.94560 -0.13112 -0.00058  0.15436  1.04002
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 4.379e-16 2.292e-02  0.000     1
## sqrt_broadband 3.406e-01 4.293e-02  7.934 2.49e-13 ***
## log_gdp      6.477e-01 4.293e-02 15.089 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.305 on 174 degrees of freedom
## Multiple R-squared:  0.908, Adjusted R-squared:  0.907
## F-statistic: 859.1 on 2 and 174 DF, p-value: < 2.2e-16

##Outlier country in 2011

## # A tibble: 2 x 9
##   country broadband    hdi     gdp sqrt_broadband log_gdp fitted_hdi residuals
##   <chr>      <dbl>  <dbl>   <dbl>        <dbl>    <dbl>      <dbl>    <dbl>
## 1 Cuba       -0.846  0.456 -0.570      -1.17   -0.285    -0.584    1.04
## 2 Djibouti   -0.745 -1.84  -0.795      -0.706  -1.01     -0.893   -0.946
## # i 1 more variable: std_resid <dbl>

```

Our outlier is 2011 is Cuba

Question ??

Create a multi regression with gdp as the control variable

```

##
## Call:
## lm(formula = hdi ~ sqrt_broadband + log_gdp, data = data_2022_standardized)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.87118 -0.14524  0.02077  0.13574  0.79086
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -6.138e-16 1.926e-02  0.00     1
## sqrt_broadband 2.940e-01 3.869e-02  7.60 1.46e-12 ***
## log_gdp      6.991e-01 3.869e-02 18.07 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2633 on 184 degrees of freedom
## Multiple R-squared:  0.9314, Adjusted R-squared:  0.9307
## F-statistic: 1249 on 2 and 184 DF, p-value: < 2.2e-16

```

Checking assumptions

Lack of Multicollinearity

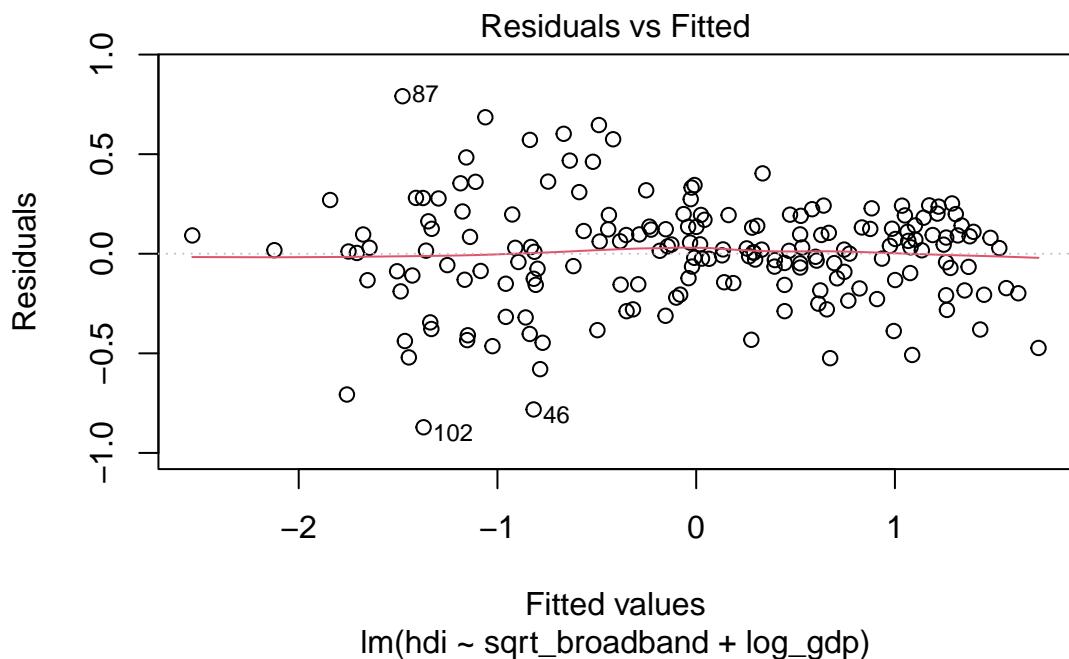
```
## sqrt_broadband      log_gdp
##          4.015438      4.015438
```

The variance inflation factors are 4.01 for sqrt_broadband and 4.01 for log_gdp. This indicates that there is not a strong linear relationship between these factors.

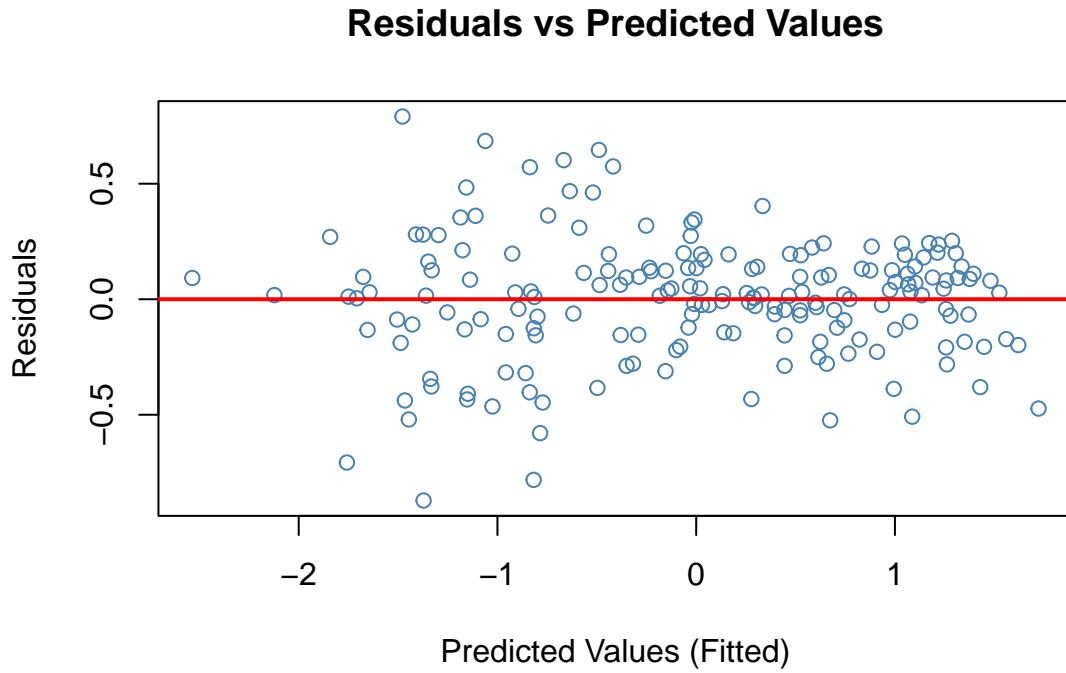
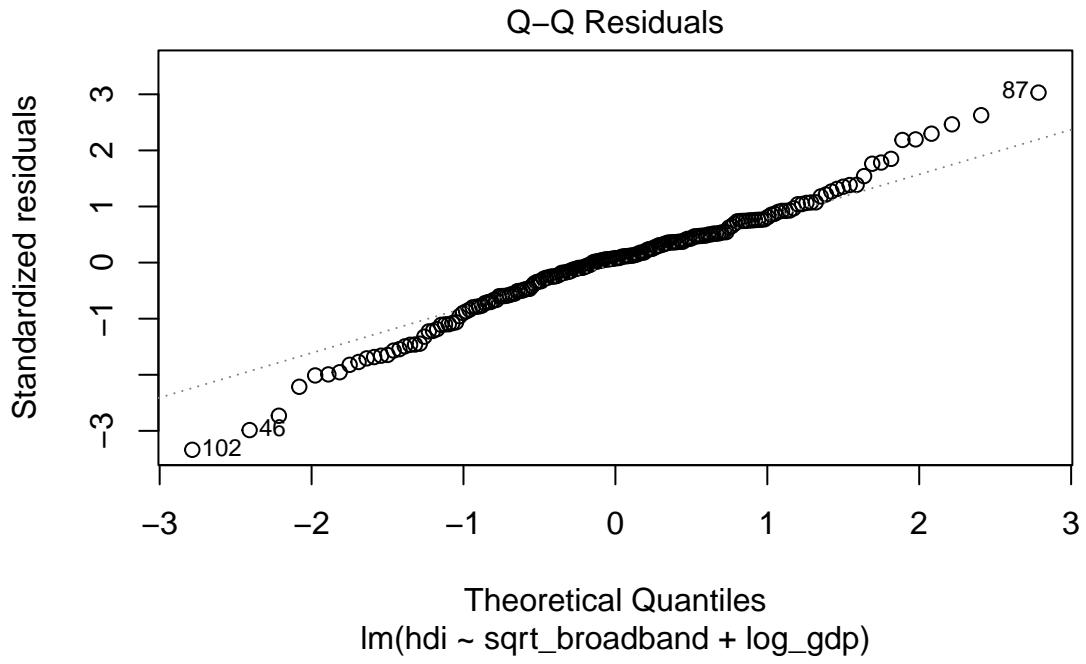
Independence

```
##
## Durbin-Watson test
##
## data: multi_reg
## DW = 1.9102, p-value = 0.2686
## alternative hypothesis: true autocorrelation is greater than 0
??
??
```

Normality of residuals



```
##
## Shapiro-Wilk normality test
##
## data: res_model
## W = 0.98015, p-value = 0.009251
```



```
## integer(0)
```

Homoscedascity Next, let's look for the independence of the residuals.

```

##  

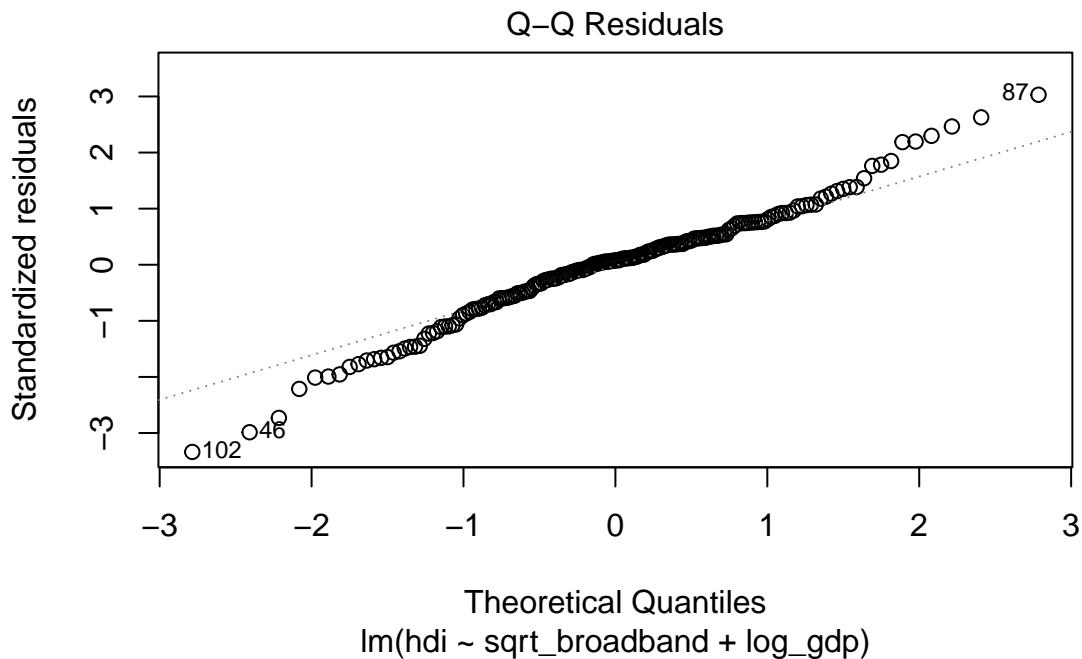
## Shapiro-Wilk normality test  

##  

## data: res_model  

## W = 0.98015, p-value = 0.009251

```



6. Results and Interpretation

Lorem ipsum dolor sit amet, consectetur adipiscing elit. In egestas lobortis porta. Phasellus tincidunt metus sed mollis imperdiet. Aliquam blandit nibh in fermentum consequat. Fusce blandit magna quis nulla ornare, non mattis enim tempor. Nulla et odio dui. Nunc ut elit venenatis, porttitor dui et, placerat tortor. Sed aliquet sodales magna, sit amet porta odio tempor in. CHANGE THIS OF COURSE

7. Discussions

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Appendix

Code

The report was created using *R* (R Core Team 2020) and *R Studio* (RStudio Team 2020) with *R Markdown* (RStudio, n.d.). The main library utilized for this purpose is *Tidyverse* (Wickham et al. 2019). Its used sub-packages include *dplyr* (Wickham et al. 2022) to enable query-like syntax, and *ggplot* (Wickham 2016) to create graphs and charts. Other packages and tools include *janitor* (Firke 2021), *knitr* (Xie 2022), *kableExtra* (Zhu 2021), and *scales* (Wickham and Seidel 2022).

References

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- RStudio Team. 2020. *RStudio: Integrated Development Environment for r.* Boston, MA: RStudio, PBC. <http://www.rstudio.com/>.
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- Wickham, Hadley, Mara Averick, Jennifer Bryan, Winston Chang, Lucy D'Agostino McGowan, Romain François, Garrett Grolemund, et al. 2019. "Welcome to the tidyverse." *Journal of Open Source Software* 4 (43): 1686. <https://doi.org/10.21105/joss.01686>.
- Wickham, Hadley, Romain François, Lionel Henry, and Kirill Müller. 2022. *Dplyr: A Grammar of Data Manipulation.* <https://CRAN.R-project.org/package=dplyr>.
- Wickham, Hadley, and Dana Seidel. 2022. *Scales: Scale Functions for Visualization.* <https://CRAN.R-project.org/package=scales>.
- Xie, Yihui. 2022. *Knitr: A General-Purpose Package for Dynamic Report Generation in r.* <https://yihui.org/knitr/>.
- Zhu, Hao. 2021. *kableExtra: Construct Complex Table with 'Kable' and Pipe Syntax.* <https://CRAN.R-project.org/package=kableExtra>.