
Latent Dirichlet Analysis for Document Topic Modelling

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Abstract

In this project, we studied the topic latent Dirichlet allocation (LDA), a nonparametric Bayesian model for collections of discrete data such as text corpora, which was first proposed by Blei, Ng, and Jordan in 2003 [1]. We followed the original paper to implement LDA using variance inference techniques and an EM algorithm for estimating the Bayes parameters and extracting subtopic from a text corpus. In addition, we also implemented LDA using collapsed Gibbs Sampling following Griffiths and Steyvers (2004). We recreated the document modeling experiment in [1] to extract subtopics on AP dataset. It was found variational inference and Gibbs sampling generated similar perplexities and subtopics. We also compared LDA with simple unigram model (and find that ...).

1 Introduction

Here, describe the problem statement: Given a text document, model the topics of the document. (expand on that more).

1.1 Related Works

Based on Blei, briefly talk about unigram, mixture of unigram, and plsi.

2 Notation

We used similar notation as those denoted in the paper:

N = number of words in total.

z_j = the j -th topic

d_i = the i -th document

w_i = the i -th word in the document

3 LDA

The latent Dirichlet allocation (LDA) model explains the generation of text documents, which can be viewed as samples from a mixture of multinomial distributions over a vocabulary of words. Each multinomial mixture component is called a topic. The general process of the model to write a document is the following:



Figure 1: Graphic model of LDA. The boxes are “plates” representing replicates. The outer plate represents documents, while the inner plate represents the repeated choice of topics and words within a document.

- The number of words N in document $\sim \text{Poisson}(\zeta)$
- The topic mixture θ for the document $\sim \text{Dir}(\alpha)$ (with a fixed set of K topics)
- Then for each word w_i in the document:
 1. Choose a topic t_i based on multinomial distribution with parameter θ from step (2)
 2. Use this topic z_i to generate word itself by using the existing probability for each word in this topic (i.e. $p(w_i|z_i, \beta)$)

This is the generative model for a collection of documents. LDA then tries to backtrack from the (training) documents to find a set of topics that are likely to have generated the collection. Now the question is how does LDA backtrack to find the parameters in this model. Suppose we have a set of documents D , and we set the number of topics to be K . What we want is to use LDA to learn two things 1) the topic representation of each document and 2) the words associated to each topic.

There are two methods to learn these two things: collapsed Gibbs sampling [1] and variational inference [2, 3]. We first discuss Gibbs sampling method here:

3.1 Gibbs Sampling Method

- For each document, randomly assign each word in the document to one of the K topics.
 1. this step gives topic representation of all the documents
 2. this step gives word distributions of all the topics
 3. since randomly assign topics to each word is very naive, so we need to improve it
- For each word w_k in document d_i
 1. For each topic t_j that this word belongs to, compute:
 - (a) $p(z_j|d_i) = \frac{\text{number of words assigned to } z_j \text{ in } d_i}{\text{total number of words in } d_i}$
 - (b) $p(w_k|z_j) = \frac{\text{number of words assigned to } z_j \text{ in } d_i}{\text{number of words assigned to } z_j \text{ for all docs}}$
- we compute the product of i) and ii) above which gives the new topics to assign to this word.
- repeating step 2 over and over until it reaches a steady state where the assignments make good sense.
- Use this model to estimate the topic mixtures of each document and words associated to each topic, which are the two things we want to learn.

3.2 Inference Method

With the same Dirichlet distribution model assumption shown in the previous section, variational parameters (γ and ϕ) are introduced. The way to do this is to place a distribution over hidden variables (θ and Z) with free parameters which are the so called variational parameters. Then, an optimization process can be performed such that the placed distribution is close to the posterior in KL divergence. However, since the KL divergence is intractable, Jensen’s inequality is applied to yield

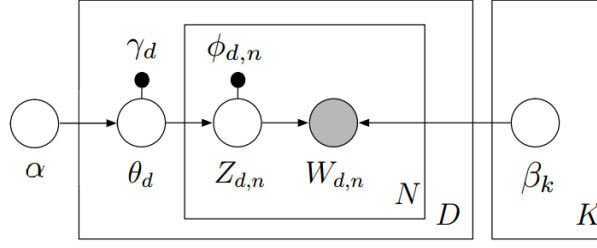


Figure 2: Graphical model representation of the variational distribution used to approximate the posterior in LDA.

an evidence lower bound. Minimizing the KL divergence is equivalent to maximizing the evidence lower bound [5]. The posterior distribution can be obtained with those variational parameters using EM algorithm.

Algorithm 1 Estimation

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procedure
  Initialize:  $\phi_{ni}^0 = 1/K$  for all  $i$  and  $n$ 
  Initialize:  $\gamma_i^0 = \alpha_i + N/K$  for all  $i$ 
  repeat
    for  $n = 1$  to  $N$  do
      for  $i = 1$  to  $K$  do
         $\phi_{ni}^{t+1} := \beta_{i w_n} \exp\{\varphi(\gamma_i^t) - \varphi(\sum_{j=1}^K \gamma_j^t)\}$ 
      end for
    end for
     $\gamma^{t+1} := \alpha + \sum_{n=1}^N \phi_n^{t+1}$ 
     $t \leftarrow t + 1$ 
  until convergence

```

Algorithm 2 Maximization

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procedure
  Update  $\beta$ 
  for  $i = 1$  to  $K$  do
    for  $j = 1$  to  $V$  do
       $\beta_{ij} \propto \sum_{d=1}^D \sum_{n=1}^{N_d} \phi_{dni} w_{dn}^j$ 
    end for
  end for
  repeat
    Calculate gradient  $g(\alpha^t)$  and Hessian  $H(\alpha^t)$ 
     $\alpha^{t+1} = \alpha^t - H^{-1}(\alpha^t)g(\alpha^t)$ 
     $t \leftarrow t + 1$ 
  until convergence

```

4 Evaluations and Empirical Results

4.1 Dataset and Preprocessing

To evaluate our algorithm, we replicated one of the experiments implemented by Blei et al. on document modeling. We used AP dataset which contains 2246 (verify this number) news articles from the associated press [6]. The dataset was partitioned into 80 percent training set and 20 percent test data. In preprocessing of the data, we removed a list of stop words from the text. We further removed words that appear less than 20 times (rare words), as well as words that appear in more than 90 percent of the documents (common words). We ended up with a vocabulary size of 3564.

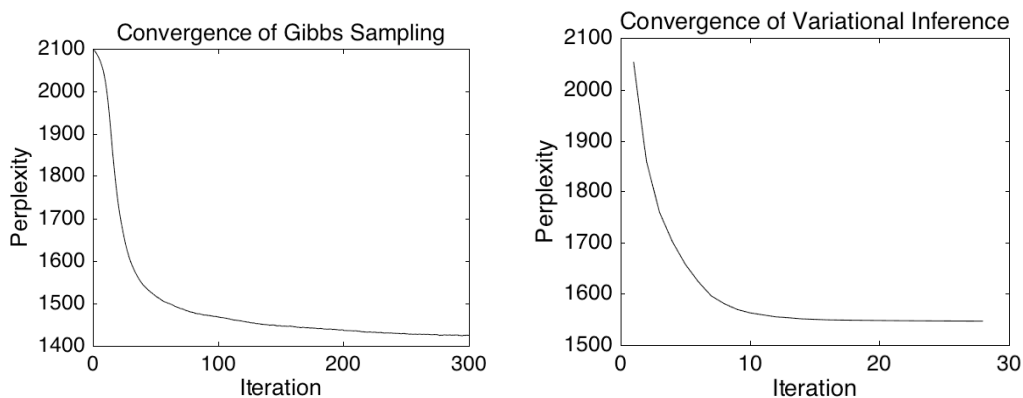


Figure 3: Convergence of LDA using Gibbs Sampling (*left*) and Variational Inference (*right*)

“Law”	“War”	“Trade”	“Politics”	“Company”
court	united	percent	government	million
state	states	market	soviet	year
federal	military	prices	party	billion
case	war	stock	union	company
department	president	dollar	south	new
law	american	trade	gorbachev	workers
attorney	iraq	year	political	based
judge	officials	late	west	last
office	aid	oil	country	corp
former	israel	higher	president	co

Figure 4: List of topics generated by LDA.

4.2 Convergence of Algorithms

In AP dataset, each document is unlabeled. Therefore, here we are doing unsupervised learning with a purpose to estimate the likelihood of the test dataset. In natural language processing, the likelihood of a document is usually called perplexity, which is the inverse of the average per-word log likelihood. The perplexity of on the text corpus is defined by

Describe perplexity here (need help with Yan).

While implementing our algorithms, we first monitors the convergence of the algorithm. This was done by monitoring the perplexity (defined below) of training data, as shown Figure 3. We can see that in both cases the algorithm converges after enough number of iterations, although the numbers of iterations required to reach convergence are very different.

4.3 Extracted Subtopics

We trained a 10-topic LDA model on the training dataset using both Gibbs sampling and variational inference, and 5 of the generated subtopics in shown in Figure 4. For each topic, the 10 words that are most likely to occur is listed. As we expected, LDA automatically generated meaning full subtopics from the AP corpus, with similar words more likely to appear in the same topic.

5 Conclusion

Discuss the subsequent conclusions we gained from this reimplement of LDA. Summarize advantages and disadvantages as well.

Author Contributions

All authors contributed to the overall study of LDA and its implementation. Xiang preprocessed AP dataset in Python to generate input matrices for LDA, and implemented Gibbs Sampling LDA in MATLAB. Zheng implemented variational inference LDA in MATLAB. Sajan implemented the Unigram model in MATLAB. Yan wrote MATLAB functions for calculating perplexity and extracting subtopics from LDA outputs. All authors participated in final data analysis and interpretation, as well as writing of the manuscript.

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- [6]. <http://www.cs.columbia.edu/~blei/lda-c/>. It should be noted that the size of the dataset here is about one eighth of the dataset used by Blei et al. So there might be some discrepancy between our result and those presented in Blei et al.