Context Free Grammar

CONTEXT-FREE GRAMMAR (CFG) describes infinite set of valid trees using a finite set of rules, e.g.:

$$S \rightarrow NP VP$$

PROBABILISTIC CFG assign weights to rules, e.g.:

$$\mathsf{VP} \to \left\{ \begin{array}{ll} \mathsf{V} & 0.1 \\ \mathsf{V} \; \mathsf{NP} & 0.5 \\ \mathsf{V} \; \mathsf{NP} \; \mathsf{NP} & 0.4 \end{array} \right. \tag{1}$$

Generative model for probabilitic CFG:

$$p(\text{tree } T|\text{sentence } s) = \prod_{X \to \alpha \in T} p(\alpha|X) \tag{2}$$