Relation to Noisy Channel

With equal weights and only two features:

- $h_{\mathsf{TM}}(e_1^I, f_1^J) = \log p(f_1^J|e_1^I)$ for the translation model,
- $h_{\mathrm{LM}}(e_1^I,f_1^J) = \log p(e_1^I)$ for the language model,

log-linear model reduces to Noisy Channel:

$$\begin{array}{ll} \hat{e}_{1}^{\hat{I}} &= \operatorname{argmax}_{I,e_{1}^{I}} \exp(\sum_{m=1}^{M} \lambda_{m} h_{m}(e_{1}^{I}, f_{1}^{J})) \\ &= \operatorname{argmax}_{I,e_{1}^{I}} \exp(h_{\mathsf{TM}}(e_{1}^{I}, f_{1}^{J}) + h_{\mathsf{LM}}(e_{1}^{I}, f_{1}^{J})) \\ &= \operatorname{argmax}_{I,e_{1}^{I}} \exp(\log p(f_{1}^{J}|e_{1}^{I}) + \log p(e_{1}^{I})) \\ &= \operatorname{argmax}_{I,e_{1}^{I}} p(f_{1}^{J}|e_{1}^{I}) p(e_{1}^{I}) \end{array}$$