

# Team notebook

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## 1 end\_pos\_set\_for\_suffix\_automata

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```
1 inline int add(int _a, int _b, int md){
2     if(_a < 0){ _a += md; }
3     if(_b < 0){ _b += md; }
4     if(_a + _b >= md){ return _a + _b - md; }
5     return _a + _b;
6 }
7 inline int mul(int _a, int _b, int md){
8     if(_a < 0){ _a += md; }
9     if(_b < 0){ _b += md; }
10    return ((ll)((ll)_a * (ll)_b)) % md;
11 }
12 struct state{
13     int len, link;
14     map <char, int> next;
15 };
16 state st[SZ * 2];
17 int to_state = 0, last, f_occ[SZ * 2], d[2 * SZ], sbtr[2 * SZ], vrtx[2 * SZ];
18 int t = 0;
19 vector <int> adj[2 * SZ];
20 void sa_init(){
21     to_state = 0, st[0].len = 0, st[0].link = -1;
22     to_state++, last = 0;
23 }
24 void sa_extend(char c){
25     int cur = to_state++;
26     st[cur].len = st[last].len + 1, f_occ[cur] = st[cur].len - 1;
27     st[cur].next.clear();
28     int p = last;
29     while(p != -1 && st[p].next.find(c) == st[p].next.end()){
```

```

30     st[p].next[c] = cur;
31     p = st[p].link;
32 }
33 if(p == -1){ st[cur].link = 0; }
34 else{
35     int q = st[p].next[c];
36     if(st[p].len + 1 == st[q].len){ st[cur].link = q; }
37     else{
38         int clone = to_state++;
39         st[clone].len = st[p].len + 1;
40         st[clone].next = st[q].next;
41         st[clone].link = st[q].link;
42         f_occ[clone] = f_occ[q];
43         while(p != -1 && st[p].next[c] == q){
44             st[p].next[c] = clone;
45             p = st[p].link;
46         }
47         st[q].link = st[cur].link = clone;
48     }
49 } last = cur;
50 }
51 int n; ll mx_up, mx_dn;
52 char str[SZ];
53 void build(){
54     int i, j, u, v;
55     sa_init();
56     for0(i, n){ sa_extend(str[i]); }
57     for0(i, to_state){
58         u = i, v = st[i].link;
59         if(v != -1){ adj[v].push_back(u); }
60     }
61 }
62 void input(){
63     int i, j;
64     ss(str), n = strlen(str);
65 }
66 void dfs(int src){
67     int i, j, u;
68     vrtx[t++] = src, d[src] = t - 1, sbtr[src] = 1;
69     for0(i, adj[src].size()){
70         u = adj[src][i];
71         dfs(u), sbtr[src] += sbtr[u];
72     }
73 }
74 set<int> end_pos;
75 inline void update_max(ll up, ll dn){
76     ll g = __gcd(up, dn); up /= g, dn /= g;
77     if(mx_up * dn <= up * mx_dn){
78         mx_up = up, mx_dn = dn;
79     }
80 }
81 inline void update(int src, int pos){
82     ll up, dn;
83     if(end_pos.empty()){ return; }
84     std::set<int>::iterator it;
85     it = end_pos.upper_bound(pos);
86     if(it == end_pos.end()){
87         --it;
88         if(abs(pos - *it) >= st[src].len){
89             up = (ll)abs(pos - *it) + (ll)st[src].len;
90             dn = (ll)abs(pos - *it);

```

```

91     update_max((ll)up, (ll)dn);
92 }
93 return;
94 }
95 if(*it - pos >= st[src].len){
96     up = (ll)abs(*it - pos) + (ll)st[src].len;
97     dn = (ll)abs(*it - pos);
98     update_max((ll)up, (ll)dn);
99 }
100 if(it != end_pos.begin()){
101     --it;
102     if(abs(pos - *it) >= st[src].len){
103         up = (ll)abs(pos - *it) + (ll)st[src].len;
104         dn = (ll)abs(pos - *it);
105         update_max((ll)up, (ll)dn);
106     }
107 }
108 }
109 void dsu(int src, bool keep){
110     int i, j, mx = -1, bg = -1, u, v;
111     for0(i, adj[src].size()){
112         u = adj[src][i];
113         if(sbtr[u] > mx){
114             mx = sbtr[u], bg = u;
115         }
116     }
117     for0(i, adj[src].size()){
118         u = adj[src][i];
119         if(u != bg){
120             dsu(u, false);
121         }
122     }
123     if(bg != -1){ dsu(bg, true); }
124     for0(i, adj[src].size()){
125         u = adj[src][i];
126         if(u != bg){
127             for(j = d[u]; j <= d[u] + sbtr[u] - 1; j++){
128                 v = vrtx[j];
129                 if(f_occ[v] + 1 - st[v].len == 0){
130                     update(src, f_occ[v]);
131                     end_pos.insert(f_occ[v]);
132                 }
133             }
134         }
135     }
136     if(f_occ[src] + 1 - st[src].len == 0){
137         update(src, f_occ[src]), end_pos.insert(f_occ[src]);
138     }
139     // std::set<int>::iterator it;
140     // cout << src << "-->"; nl;
141     // for(it = end_pos.begin(); it != end_pos.end(); ++it){
142     //     pi(*it); sp;
143     // }nl;
144     if(!keep){ end_pos.clear(); }
145 }
146 int h[2][SZ], base[] = {47, 31}, P[2][SZ], mod[] = {MOD, MOD + 2};
147 void make_hash(){
148     int i, j;
149     for0(i, 2){
150         for(j = 1, P[i][0] = 1; j <= SZ - 2; j++){
151             P[i][j] = mul(P[i][j - 1], base[i], mod[i]);

```

```

152     }
153 }
154 for0(i, 2){
155     for(j = n - 1, h[i][n] = 0; j >= 0; j--){
156         h[i][j] = add(str[j] - 'a' + 1, mul(base[i], h[i][j + 1], mod[i]), mod[i]);
157     }
158 }
159 }
160 inline int get_hash(int l, int r, int idx){
161     return add(h[idx][l], -mul(h[idx][r + 1], P[idx][r - l + 1], mod[idx]), mod[idx]);
162 }
163 int lcp(int l1, int r1, int l2, int r2){
164     if(l1 > r1 || l2 > r2){ return 0; }
165     int lo = 0, hi = min(r1 - l1 + 1, r2 - l2 + 1), mid;
166     int f0, f1, g0, g1;
167     while(lo < hi){
168         mid = (lo + hi + 1) >> 1;
169         f0 = get_hash(l1, l1 + mid - 1, 0);
170         f1 = get_hash(l1, l1 + mid - 1, 1);
171         g0 = get_hash(l2, l2 + mid - 1, 0);
172         g1 = get_hash(l2, l2 + mid - 1, 1);
173         if(f0 == g0 && f1 == g1){ lo = mid; }
174         else{ hi = mid - 1; }
175     }
176     return lo;
177 }
178 int lcs(int l1, int r1, int l2, int r2){
179     if(l1 > r1 && l2 > r2){ return 0; }
180     int lo = 0, hi = min(r1 - l1 + 1, r2 - l2 + 1), mid;
181     int f0, f1, g0, g1;
182     while(lo < hi){
183         mid = (lo + hi + 1) >> 1;
184         f0 = get_hash(r1 - mid + 1, r1, 0);
185         f1 = get_hash(r1 - mid + 1, r1, 1);
186         g0 = get_hash(r2 - mid + 1, r2, 0);
187         g1 = get_hash(r2 - mid + 1, r2, 1);
188         if(f0 == g0 && f1 == g1){ lo = mid; }
189         else{ hi = mid - 1; }
190     }
191     return lo;
192 }
193 pair <int, int > vec[SZ];
194 void solve(){
195     int i, j, cnt, k;
196     build();
197     t = 0, dfs(0);
198     mx_up = -INF, mx_dn = 1; dsu(0, false);
199     make_hash();
200     for(i = 1; i <= n; i++){
201         for(j = 0, cnt = 0; j + i - 1 < n; j += i){
202             int h0 = get_hash(j, j + i - 1, 0);
203             int h1 = get_hash(j, j + i - 1, 1);
204             vec[cnt++] = mpr(h0, h1);
205         }
206         for(j = 0; j < cnt; j = k){
207             for(k = j; k < cnt && vec[k] == vec[j]; k++){
208                 int x = lcs(0, j * i - 1, j * i, j * i + i - 1);
209                 int y = lcp(k * i, n - 1, j * i, j * i + i - 1);
210                 ll up = (ll)x + (ll)y + (ll)(k - j) * (ll)i;
211                 ll dn = i;
212                 update_max(up, dn);

```

```

213     }
214 }
215 printf("%lld/%lld\n", mx_up, mx_dn);
216 }
217 int main(){
218 //  freopen("input.txt","r",stdin);
219 //  freopen("output.txt", "w", stdout);
220
221     input();
222     solve();
223 }

```

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## 2 expected\_number\_of\_components

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```

1 //First we consider how to calculate E(X).
2 //
3 //The number of connected components equals to the number of nodes
4 //minus the number of edges and then add the number of rings in it.
5 //So we can calculate the possibility of removing one node,
6 //one edge or one single ring.
7 //
8 //Then we can split the variance, it is equals to  $E(X^2)^2E(X)^2+E(X)^2=E(X^2)E(X)^2$ .
9 //Then we can again to split  $X^2$ .
10 //Let the number nodes equal to a, the number edges equal to b,
11 //the number rings equal to c.
12 //Then  $X^2=(ab+c)^2=a^2+b^2+c^2+2ab+2bc+2ac$ .
13 //We can find there is contribution between a pair of nodes, edges, rings
14 //(the two may be the same) and between a node and an edge,
15 //a node and a ring, an edge and a ring. Then we can calculate the possibility of
16 //such pair that the elements in it remains at the same time.
17 //The answer is the same when the pair is a ring and a node on it,
18 //or when it is a ring and a node not on it,
19 //or an edge with one of its end point ...
20 //If we consider all the situation of intersection and not intersection,
21 //we can get a liner algorithm. But the Time Complexity is  $O(n\log n)$ 
22 //since we need to calculate the multiplicative inverse of modulo.
23 int big_mod(int v, int p){
24     if(p == 0){ return 1; }
25     int ret = big_mod(v, p / 2);
26     if(p % 2 == 0){ return mul(ret, ret); }
27     return mul(ret, mul(ret, v));
28 }
29 int n, m, pwr[2 * SZ], inv_pwr[2 * SZ];
30 vector<int> adj[SZ];
31 bool vis[SZ], is_art[SZ];
32 int Time, low[SZ], dis[SZ], bcc_cnt;
33 vector<int> bcc[SZ], art_vec[SZ];
34 stack<int> S;
35 void pop_bcc(int s, int u){
36     is_art[s] = true;
37     bcc[bcc_cnt].push_back(s);
38     while(true){
39         bcc[bcc_cnt].push_back(S.top());
40         if(S.top() == u){ S.pop(); break; }
41         S.pop();
42     }
43     bcc_cnt++;
44     if(bcc[bcc_cnt - 1].size() <= 2){

```

```

45     bcc[bcc_cnt - 1].clear();
46     bcc_cnt--;
47 }
48 }
49 void find_bcc(int src, int par){
50     S.push(src);
51     int i, u, child = 0; vis[src] = true, Time++, dis[src] = low[src] = Time;
52     for0(i, adj[src].size()){
53         u = adj[src][i];
54         if(!vis[u]){
55             child++, find_bcc(u, src);
56             low[src] = min(low[src], low[u]);
57             if(par != -1 && low[u] >= dis[src]){ pop_bcc(src, u); }
58             else if(par == -1){
59                 if(child > 1){ pop_bcc(src, u); }
60             }
61             } else if(par != u){ low[src] = min(low[src], dis[u]); }
62     } if(par == -1 && child > 1){ is_art[src] = true; }
63 }
64 void process_bcc(){
65     int i, j;
66     bool f;
67     bcc_cnt = 0;
68     for0(i, n){
69         if(!vis[i]){
70             Time = 0;
71             find_bcc(i, -1);
72             f = false;
73             while(!S.empty()){
74                 f = true;
75                 bcc[bcc_cnt].push_back(S.top());
76                 S.pop();
77             } if(f){
78                 bcc_cnt++;
79                 if(bcc[bcc_cnt - 1].size() <= 2){
80                     bcc[bcc_cnt - 1].clear();
81                     bcc_cnt--;
82                 }
83             }
84         }
85     }
86 }
87 void input(){
88     int i, j;
89     sii(n, m);
90     for0(i, m){
91         int u, v;
92         sii(u, v), u--, v--;
93         adj[u].push_back(v), adj[v].push_back(u);
94     }
95 }
96 inline int comb(int a){
97     return mul(a, a - 1);
98 }
99 void solve(){
100     int i, j, sol = 0, sz, baki = 0, sum = 0, sz1;
101     process_bcc();
102     //a
103     int a = mul(n, inv_pwr[1]);
104     //b
105     int b = mul(m, inv_pwr[2]);

```

```

106 //c
107 int c = 0;
108 for0(i, bcc_cnt){
109     sz = bcc[i].size();
110     c = add(c, inv_pwr[sz]);
111 }
112 //a^2;
113 int a_2 = mul(comb(n), inv_pwr[2]);
114 a_2 = add(a_2, mul(n, inv_pwr[1]));
115 //b^2
116 int b_2 = 0;
117 for0(i, n){
118     sz = adj[i].size();
119     b_2 = add(b_2, mul(comb(sz), inv_pwr[3]));
120     b_2 = add(b_2, -mul(comb(sz), inv_pwr[4]));
121 }
122 b_2 = add(b_2, mul(comb(m), inv_pwr[4]));
123 b_2 = add(b_2, mul(m, inv_pwr[2]));
124 //c^2
125 int c_2 = 0;
126 for0(i, bcc_cnt){
127     for0(j, bcc[i].size()){
128         if(is_art[bcc[i][j]]){
129             art_vec[bcc[i][j]].push_back(i);
130         }
131     }
132 }
133 for(i = 0; i < n; i++){
134     for(j = 0, sum = 0; j < art_vec[i].size(); j++){
135         sz = bcc[art_vec[i][j]].size();
136         sum = add(sum, inv_pwr[sz]);
137     }
138     for0(j, art_vec[i].size()){
139         sz = bcc[art_vec[i][j]].size();
140         c_2 = add(c_2, mul(add(sum, -inv_pwr[sz]), inv_pwr[sz - 1]));
141         c_2 = add(c_2, -mul(add(sum, -inv_pwr[sz]), inv_pwr[sz]));
142     }
143 }
144 for(i = 0, sum = 0; i < bcc_cnt; i++){
145     sz = bcc[i].size();
146     sum = add(sum, inv_pwr[sz]);
147 }
148 for0(i, bcc_cnt){
149     sz = bcc[i].size();
150     c_2 = add(c_2, mul(add(sum, -inv_pwr[sz]), inv_pwr[sz]));
151     c_2 = add(c_2, inv_pwr[sz]);
152 }
153 //ab
154 int ab = 0;
155 ab = add(ab, mul(mul(2, m), inv_pwr[2]));
156 ab = add(ab, mul(mul(m, n - 2), inv_pwr[3]));
157 //bc
158 int bc = 0;
159 for0(i, bcc_cnt){
160     sz = bcc[i].size();
161     bc = add(bc, mul(sz, inv_pwr[sz]));
162     bc = add(bc, -mul(sz, inv_pwr[sz + 2]));
163     bc = add(bc, mul(m, inv_pwr[sz + 2]));
164     for0(j, bcc[i].size()){
165         sz1 = adj[bcc[i][j]].size();
166         sz1 = add(sz1, -2);

```

```

167         bc = add(bc, mul(sz1, inv_pwr[sz + 1]));
168         bc = add(bc, -mul(sz1, inv_pwr[sz + 2]));
169     }
170 }
171 //ac
172 int ca = 0;
173 for0(i, bcc_cnt){
174     sz = bcc[i].size();
175     ca = add(ca, mul(sz, inv_pwr[sz]));
176     ca = add(ca, -mul(sz, inv_pwr[sz + 1]));
177     ca = add(ca, mul(n, inv_pwr[sz + 1]));
178 }
179 int e_x = add(a, add(-b, c));
180 sol = 0;
181 sol = add(sol, -mul(e_x, e_x));
182 sol = add(sol, add(a_2, add(b_2, c_2)));
183 sol = add(sol, -mul(2, ab));
184 sol = add(sol, -mul(2, bc));
185 sol = add(sol, mul(2, ca));
186 pi(sol); nl;
187 }
188 void pre_process(){
189     int i, j, inv_2 = big_mod(2, MOD - 2);
190     for(i = 1, pwr[0] = 1, inv_pwr[0] = 1; i < 2 * SZ - 2; i++){
191         pwr[i] = mul(pwr[i - 1], 2);
192         inv_pwr[i] = mul(inv_pwr[i - 1], inv_2);
193     }
194 }
195 int main(){
196     // freopen("input.txt", "r", stdin);
197     // freopen("output.txt", "w", stdout);
198     pre_process();
199     input();
200     solve();
201 }

```

---

### 3 function\_decomposition

```

1  int add(int _a, int _b){
2      _a = (_a + MOD) % MOD;
3      _b = (_b + MOD) % MOD;
4      return (_a + _b) % MOD;
5  }
6  int mul(int _a, int _b){
7      _a = (_a + MOD) % MOD;
8      _b = (_b + MOD) % MOD;
9      return ((ll)((ll)_a * (ll)_b)) % MOD;
10 }
11 int n, ara[SZ], sccCnt = 0, sccRoot[SZ], sccNo[SZ], rootNo[SZ], sbtr[SZ], ht[SZ], q,
    ↪ global[SZ], position[SZ], sol[SZ];
12 const int thresh = 200005;
13 bool inCycle[SZ];
14 vector <int> adj[SZ], rev[SZ], scc[SZ], cum[SZ];
15 vector <int> topo, treeRoot, qlist[SZ], vrtx;
16 pair <ll, int> query[SZ];
17 bool vis[SZ];
18 void input(){
19     int i, j;

```



```

20     si(n);
21     for1(i, n){
22         si(ara[i]);
23         if(ara[i] == i){ inCycle[ara[i]] = true; }
24         adj[ara[i]].push_back(i); rev[i].push_back(ara[i]);
25     }
26 // ppvec(i, j, n + 1, adj);
27 }
28 void dfs0(int src){
29     int i, j; vis[src] = true;
30     for0(i, adj[src].size()){
31         int u = adj[src][i];
32         if(!vis[u]){ dfs0(u); }
33     } topo.push_back(src);
34 }
35 void dfs1(int src){
36     int i, j; vis[src] = true; scc[sccCnt].push_back(src);
37     sccNo[src] = sccCnt;
38     for0(i, rev[src].size()){
39         int u = rev[src][i];
40         if(!vis[u]){ dfs1(u); }
41     }
42 }
43 void dfs2(int src, int rt){
44     int i, j; vis[src] = true; sbtr[src] = 1;
45     rootNo[src] = rt;
46     vrtx.push_back(src);
47     for0(i, adj[src].size()){
48         int u = adj[src][i];
49         if(!vis[u]){ dfs2(u, rt), sbtr[src] += sbtr[u]; }
50     }
51 }
52 void dfs3(int src, int rt, int d, int len, int idx){
53     int i, j; vis[src] = true; ht[src] = d;
54     cum[idx][ht[src]]++;
55     for0(i, adj[src].size()){
56         int u = adj[src][i];
57         if(!vis[u]){
58             if(inCycle[u]){ dfs3(u, u, d + 1, len, idx); }
59             else{ dfs3(u, rt, d + 1, len, idx); }
60         }
61     }
62 }
63
64 void dsu(int src, int par, bool keep){
65     int i, j, u, bg = -1, mx = -1, v;
66     ll d;
67     for0(i, adj[src].size()){
68         u = adj[src][i];
69         if(u != par && u != rootNo[src]){
70             if(sbtr[u] > mx){ mx = sbtr[u], bg = u; }
71         }
72     }
73     for0(i, adj[src].size()){
74         u = adj[src][i];
75         if(u != par && u != rootNo[src] && u != bg){
76             dsu(u, src, false);
77         }
78     }
79     if(mx != -1){ dsu(bg, src, true); }
80     global[ht[src]]++;

```

```

81     for0(i, adj[src].size()){
82         u = adj[src][i];
83         if(u != par && u != rootNo[src] && u != bg){
84             for(j = position[u]; j <= position[u] + sbtr[u] - 1; j++){
85                 v = vrtx[j];
86                 global[ht[v]]++;
87             }
88         }
89     }
90     for0(i, qlist[src].size()){
91         int idx = qlist[src][i];
92         d = query[idx].first;
93         if((ll)ht[src] + d <= (ll)thresh){
94             sol[idx] += global[(ll)ht[src] + d];
95         }
96     }
97     if(!keep){
98         for(j = position[src]; j <= position[src] + sbtr[src] - 1; j++){
99             v = vrtx[j];
100             global[ht[v]]--;
101         }
102     }
103 }
104 void solve(){
105     int i, j, u, len, r, dis, sz;
106     ll d;
107     for(i = 1; i <= n; i++){
108         if(!vis[i]){ dfs0(i); }
109     }
110     // pvec(i, topo);
111     reverse(topo.begin(), topo.end());
112     for(i = 1; i <= n; i++){ vis[i] = false; }
113     for(i = 0; sccCnt = 0; i < topo.size(); i++){
114         if(!vis[topo[i]]){
115             dfs1(topo[i]);
116             sccRoot[sccCnt] = topo[i];
117             sccCnt++;
118         }
119     }
120     for0(i, sccCnt){
121         if(scc[i].size() >= 2){
122             for0(j, scc[i].size()){
123                 inCycle[scc[i][j]] = true;
124             }
125         }
126     }
127     for(i = 1; i <= n; i++){ vis[i] = false; }
128     for(i = 0; i < sccCnt; i++){
129         if(scc[i].size() >= 2 || (scc[i].size() == 1 && inCycle[scc[i][0]])){
130             treeRoot.push_back(sccRoot[i]);
131             dfs2(sccRoot[i], sccRoot[i]);
132         }
133         else if(scc[i].size() == 1 && rev[scc[i][0]].size() == 0){
134             treeRoot.push_back(scc[i][0]);
135             dfs2(scc[i][0], scc[i][0]);
136         }
137     }
138     for0(i, vrtx.size()){
139         u = vrtx[i], position[u] = i;
140     }
141     for(i = 1; i <= n; i++){ vis[i] = false; }

```

```

142     for(i = 0; i < treeRoot.size(); i++){
143         u = treeRoot[i];
144         if(inCycle[u]){
145             cum[u].resize(sbtr[u] + 1);
146             len = scc[sccNo[u]].size();
147             dfs3(u, u, 0, len, u);
148             for(j = 0; j < cum[u].size(); j++){
149                 cum[u][j] = j - len < 0 ? cum[u][j] : cum[u][j] + cum[u][j - len];
150             }
151         }
152     }
153     si(q);
154     for0(i, q){
155         scanf("%lld %d", &query[i].first, &query[i].second);
156         qlist[query[i].second].push_back(i);
157         u = query[i].second; d = query[i].first;
158         // pi(u); nl;
159         if(inCycle[u]){
160             r = rootNo[u];
161             len = scc[sccNo[r]].size();
162             dis = len - ht[u];
163             d -= (1LL)dis; sz = cum[r].size();
164             if(d >= sz){
165                 d = d - ((d - (1LL)sz + (1LL)len) / (1LL)len) * (1LL)len;
166             }
167             if(d < 0){ continue; }
168             sol[i] += cum[r][d];
169         }
170     }
171     for0(i, treeRoot.size()){
172         u = treeRoot[i];
173         dsu(u, -1, false);
174     }
175     for0(i, q){
176         pi(sol[i]); nl;
177     }
178 }
179 int main(){
180     // freopen("input.txt", "r", stdin);
181     // freopen("output.txt", "w", stdout);
182     input();
183     solve();
184 }

```

---

## 4 iterative\_segment\_tree

```

1  const int N = 1e5; // limit for array size
2  int n; // array size
3  int t[2 * N];
4
5  void build() { // build the tree
6      for (int i = n - 1; i > 0; --i) t[i] = t[i<<1] + t[i<<1|1];
7  }
8
9  void modify(int p, int value) { // set value at position p
10     for (t[p += n] = value; p > 1; p >>= 1) t[p>>1] = t[p] + t[p^1];
11 }
12

```

```

13 int query(int l, int r) { // sum on interval [l, r)
14     int res = 0;
15     for (l += n, r += n; l < r; l >>= 1, r >>= 1) {
16         if (l&1) res += t[l++];
17         if (r&1) res += t[--r];
18     }
19     return res;
20 }
21
22 int main() {
23     scanf("%d", &n);
24     for (int i = 0; i < n; ++i) scanf("%d", t + n + i);
25     build();
26     modify(0, 1);
27     printf("%d\n", query(3, 11));
28     return 0;
29 }

```

---

## 5 jumping\_frog\_with\_update

```

1 int n, ara[SZ], q, nxt[SZ], hole[SZ], inside[SZ];
2 int sqn;
3 void input(){
4     int i, j;
5     sii(n, q);
6     for0(i, n){si(ara[i]);}
7     sqn = sqrt(n) + 1;
8 }
9 void solve(){
10    int i, j, ret = 0, last;
11    for(i = 0; i <= n / sqn; i++){
12        for(j = min(n - 1, (i + 1) * sqn - 1); j >= i * sqn; j--){
13            if(j + ara[j] > min(n - 1, (i + 1) * sqn - 1)){
14                nxt[j] = j + ara[j];
15                inside[j] = j;
16                hole[j] = 1;
17            }
18            else{
19                nxt[j] = nxt[j + ara[j]];
20                inside[j] = inside[j + ara[j]];
21                hole[j] = 1 + hole[j + ara[j]];
22            }
23        }
24    }
25    for0(i, q){
26        int t;
27        si(t);
28        if(t == 0){
29            int idx, v;
30            sii(idx, v); idx--;
31            ara[idx] = v;
32            for(j = min(n - 1, ((idx / sqn) + 1) * sqn - 1); j >= (idx / sqn) * sqn; j--){
33                if(j + ara[j] > min(n - 1, ((idx / sqn) + 1) * sqn - 1)){
34                    inside[j] = j;
35                    nxt[j] = j + ara[j];
36                    hole[j] = 1;
37                }
38                else{

```

```

39         nxt[j] = nxt[j + ara[j]];
40         inside[j] = inside[j + ara[j]];
41         hole[j] = 1 + hole[j + ara[j]];
42     }
43 }
44 }
45 else{
46     int idx;
47     si(idx); idx--;
48     for(ret = 0 ;idx < n;){
49         last = inside[idx];
50         ret += hole[idx];
51         idx = nxt[idx];
52     }
53     pii(last + 1, ret);NL;
54 }
55 }
56 }
57 int main(){
58     // freopen("input.txt","r",stdin);
59     input();
60     solve();
61 }

```

---

## 6 mo\_on\_tree

```

1 inline int add(int _a, int _b, int md){
2     if(_a < 0){ _a += md; }
3     if(_b < 0){ _b += md; }
4     if(_a + _b >= md){ return _a + _b - md; }
5     return _a + _b;
6 }
7 inline int mul(int _a, int _b, int md){
8     if(_a < 0){ _a += md; }
9     if(_b < 0){ _b += md; }
10    return ((ll)((ll)_a * (ll)_b)) % md;
11 }
12 struct state{
13     int len, link;
14     map <char, int> next;
15 };
16 state st[SZ * 2];
17 int to_state = 0, last, f_occ[SZ * 2], d[2 * SZ], sbtr[2 * SZ], vrtx[2 * SZ];
18 int t = 0;
19 vector <int> adj[2 * SZ];
20 void sa_init(){
21     to_state = 0, st[0].len = 0, st[0].link = -1;
22     to_state++, last = 0;
23 }
24 void sa_extend(char c){
25     int cur = to_state++;
26     st[cur].len = st[last].len + 1, f_occ[cur] = st[cur].len - 1;
27     st[cur].next.clear();
28     int p = last;
29     while(p != -1 && st[p].next.find(c) == st[p].next.end()){
30         st[p].next[c] = cur;
31         p = st[p].link;
32     }

```

```

33     if(p == -1){ st[cur].link = 0; }
34     else{
35         int q = st[p].next[c];
36         if(st[p].len + 1 == st[q].len){ st[cur].link = q; }
37         else{
38             int clone = to_state++;
39             st[clone].len = st[p].len + 1;
40             st[clone].next = st[q].next;
41             st[clone].link = st[q].link;
42             f_occ[clone] = f_occ[q];
43             while(p != -1 && st[p].next[c] == q){
44                 st[p].next[c] = clone;
45                 p = st[p].link;
46             }
47             st[q].link = st[cur].link = clone;
48         }
49     } last = cur;
50 }
51 int n; ll mx_up, mx_dn;
52 char str[SZ];
53 void build(){
54     int i, j, u, v;
55     sa_init();
56     for0(i, n){ sa_extend(str[i]); }
57     for0(i, to_state){
58         u = i, v = st[i].link;
59         if(v != -1){ adj[v].push_back(u); }
60     }
61 }
62 void input(){
63     int i, j;
64     ss(str), n = strlen(str);
65 }
66 void dfs(int src){
67     int i, j, u;
68     vrtx[t++] = src, d[src] = t - 1, sbtr[src] = 1;
69     for0(i, adj[src].size()){
70         u = adj[src][i];
71         dfs(u), sbtr[src] += sbtr[u];
72     }
73 }
74 set<int> end_pos;
75 inline void update_max(ll up, ll dn){
76     ll g = __gcd(up, dn); up /= g, dn /= g;
77     if(mx_up * dn <= up * mx_dn){
78         mx_up = up, mx_dn = dn;
79     }
80 }
81 inline void update(int src, int pos){
82     ll up, dn;
83     if(end_pos.empty()){ return; }
84     std::set<int>::iterator it;
85     it = end_pos.upper_bound(pos);
86     if(it == end_pos.end()){
87         --it;
88         if(abs(pos - *it) >= st[src].len){
89             up = (ll)abs(pos - *it) + (ll)st[src].len;
90             dn = (ll)abs(pos - *it);
91             update_max((ll)up, (ll)dn);
92         }
93     }

```

```

94     }
95     if(*it - pos >= st[src].len){
96         up = (ll)abs(*it - pos) + (ll)st[src].len;
97         dn = (ll)abs(*it - pos);
98         update_max((ll)up, (ll)dn);
99     }
100     if(it != end_pos.begin()){
101         --it;
102         if(abs(pos - *it) >= st[src].len){
103             up = (ll)abs(pos - *it) + (ll)st[src].len;
104             dn = (ll)abs(pos - *it);
105             update_max((ll)up, (ll)dn);
106         }
107     }
108 }
109 void dsu(int src, bool keep){
110     int i, j, mx = -1, bg = -1, u, v;
111     for0(i, adj[src].size()){
112         u = adj[src][i];
113         if(sbtr[u] > mx){
114             mx = sbtr[u], bg = u;
115         }
116     }
117     for0(i, adj[src].size()){
118         u = adj[src][i];
119         if(u != bg){
120             dsu(u, false);
121         }
122     }
123     if(bg != -1){ dsu(bg, true); }
124     for0(i, adj[src].size()){
125         u = adj[src][i];
126         if(u != bg){
127             for(j = d[u]; j <= d[u] + sbtr[u] - 1; j++){
128                 v = vrtx[j];
129                 if(f_occ[v] + 1 - st[v].len == 0){
130                     update(src, f_occ[v]);
131                     end_pos.insert(f_occ[v]);
132                 }
133             }
134         }
135     }
136     if(f_occ[src] + 1 - st[src].len == 0){
137         update(src, f_occ[src]), end_pos.insert(f_occ[src]);
138     }
139     // std::set<int>::iterator it;
140     // cout << src << "-->"; nl;
141     // for(it = end_pos.begin(); it != end_pos.end(); ++it){
142     //     pi(*it); sp;
143     // }nl;
144     if(!keep){ end_pos.clear(); }
145 }
146 int h[2][SZ], base[] = {47, 31}, P[2][SZ], mod[] = {MOD, MOD + 2};
147 void make_hash(){
148     int i, j;
149     for0(i, 2){
150         for(j = 1, P[i][0] = 1; j <= SZ - 2; j++){
151             P[i][j] = mul(P[i][j - 1], base[i], mod[i]);
152         }
153     }
154     for0(i, 2){

```

```

155     for(j = n - 1, h[i][n] = 0; j >= 0; j--){
156         h[i][j] = add(str[j] - 'a' + 1, mul(base[i], h[i][j + 1], mod[i]), mod[i]);
157     }
158 }
159 }
160 inline int get_hash(int l, int r, int idx){
161     return add(h[idx][l], -mul(h[idx][r + 1], P[idx][r - l + 1], mod[idx]), mod[idx]);
162 }
163 int lcp(int l1, int r1, int l2, int r2){
164     if(l1 > r1 || l2 > r2){ return 0; }
165     int lo = 0, hi = min(r1 - l1 + 1, r2 - l2 + 1), mid;
166     int f0, f1, g0, g1;
167     while(lo < hi){
168         mid = (lo + hi + 1) >> 1;
169         f0 = get_hash(l1, l1 + mid - 1, 0);
170         f1 = get_hash(l1, l1 + mid - 1, 1);
171         g0 = get_hash(l2, l2 + mid - 1, 0);
172         g1 = get_hash(l2, l2 + mid - 1, 1);
173         if(f0 == g0 && f1 == g1){ lo = mid; }
174         else{ hi = mid - 1; }
175     }
176     return lo;
177 }
178 int lcs(int l1, int r1, int l2, int r2){
179     if(l1 > r1 && l2 > r2){ return 0; }
180     int lo = 0, hi = min(r1 - l1 + 1, r2 - l2 + 1), mid;
181     int f0, f1, g0, g1;
182     while(lo < hi){
183         mid = (lo + hi + 1) >> 1;
184         f0 = get_hash(r1 - mid + 1, r1, 0);
185         f1 = get_hash(r1 - mid + 1, r1, 1);
186         g0 = get_hash(r2 - mid + 1, r2, 0);
187         g1 = get_hash(r2 - mid + 1, r2, 1);
188         if(f0 == g0 && f1 == g1){ lo = mid; }
189         else{ hi = mid - 1; }
190     }
191     return lo;
192 }
193 pair <int, int > vec[SZ];
194 void solve(){
195     int i, j, cnt, k;
196     build();
197     t = 0, dfs(0);
198     mx_up = -INF, mx_dn = 1; dsu(0, false);
199     make_hash();
200     for(i = 1; i <= n; i++){
201         for(j = 0, cnt = 0; j + i - 1 < n; j += i){
202             int h0 = get_hash(j, j + i - 1, 0);
203             int h1 = get_hash(j, j + i - 1, 1);
204             vec[cnt++] = mpr(h0, h1);
205         }
206         for(j = 0; j < cnt; j = k){
207             for(k = j; k < cnt && vec[k] == vec[j]; k++){ }
208             int x = lcs(0, j * i - 1, j * i, j * i + i - 1);
209             int y = lcp(k * i, n - 1, j * i, j * i + i - 1);
210             ll up = (ll)x + (ll)y + (ll)(k - j) * (ll)i;
211             ll dn = i;
212             update_max(up, dn);
213         }
214     }
215     printf("%lld/%lld\n", mx_up, mx_dn);

```



```

216 }
217 int main(){
218 // freopen("input.txt","r",stdin);
219 // freopen("output.txt", "w", stdout);
220
221 input();
222 solve();
223 }

```

---

## 7 online\_fft

```

1 int big_mod(int v, int p){
2     if(p == 0){ return 1; }
3     int ret = big_mod(v, p / 2);
4     if(p % 2 == 0){ return mul(ret, ret); }
5     else{ return mul(ret, mul(ret, v)); }
6 }
7 const int N = (1 << 18) + 10, mod = 998244353, g = 3;
8 int rev[N], w[N], inv_n;
9 void prepare(int &n){
10     int sz = 31 - __builtin_clz(n); sz = abs(sz);
11     int r = big_mod(g, (mod - 1) / n);
12     inv_n = big_mod(n, mod - 2);
13     w[0] = w[n] = 1;
14     for(int i = 1; i < n; ++i){ w[i] = (ll)w[i - 1] * r % mod; }
15     for(int i = 1; i < n; ++i){ rev[i] = (rev[i >> 1] >> 1) | ((i & 1) << (sz - 1)); }
16 }
17 void ntt(int *a, int n, int dir){
18     for(int i = 1; i < n - 1; ++i){
19         if(i < rev[i]){ swap(a[i], a[rev[i]]); }
20     }
21     for(int m = 2; m <= n; m <= 1){
22         for(int i = 0; i < n; i += m){
23             for(int j = 0; j < (m >> 1); ++j){
24                 int &u = a[i + j], &v = a[i + j + (m >> 1)];
25                 int t = (ll)v * w[dir ? n - n / m * j : n / m * j] % mod;
26                 v = u - t < 0 ? u - t + mod : u - t;
27                 u = u + t >= mod ? u + t - mod : u + t;
28             }
29         }
30     } if(dir){ for(int i = 0; i < n; ++i){ a[i] = (ll)a[i] * inv_n % mod; } }
31 }
32 int f_a[N], f_b[N];
33 vector<int> multiply(vector<int> a, vector<int> b){
34     int sz = 1, na = (int)(a.size()), nb = (int)(b.size());
35     while(sz < na + nb - 1){ sz <= 1; }
36     prepare(sz);
37     for(int i = 0; i < sz; ++i){ f_a[i] = i < na ? a[i] : 0; }
38     for(int i = 0; i < sz; ++i){ f_b[i] = i < nb ? b[i] : 0; }
39     ntt(f_a, sz, 0), ntt(f_b, sz, 0);
40     for(int i = 0; i < sz; ++i){ f_a[i] = (ll)f_a[i] * f_b[i] % mod; }
41     ntt(f_a, sz, 1); return vector<int> (f_a, f_a + sz);
42 }
43 int n, G[SZ], F[SZ], dp[SZ];
44 bool vis[SZ];
45 void input(){
46     int i, j;
47     si(n);

```

```

48     for0(i, n){ si(G[i]); }
49 }
50 vector<int> segmentation(int l1, int r1, int l2, int r2){
51     int i, j;
52     vector<int> a, b;
53     a.resize(r1 - l1 + 1); b.resize(r2 - l2 + 1);
54     for(i = l1, j = 0; i <= n && i <= r1; i++, j++){
55         a[j] = F[i];
56     }
57     for(i = l2, j = 0; i <= n && i <= r2; i++, j++){
58         b[j] = G[i];
59     }
60     return multiply(a, b);
61 }
62 void contribute(int offst, vector<int> &poly){
63     int i, j;
64     for(j = 0; j < poly.size() && j + offst <= n; j++){
65         F[j + offst] = add(F[j + offst], poly[j]);
66     }
67 }
68 int brute(int x){
69     if(x == 0){ return 1; }
70     if(vis[x]){ return dp[x]; }
71     vis[x] = true;
72     int ret = G[x], i;
73     for(i = 0; i <= x - 1; i++){
74         ret = add(ret, mul(brute(i), G[x - i]));
75     }
76     return dp[x] = ret;
77 }
78 void solve(){
79     int i, j, l, ret;
80     F[0] = 1;
81     for(i = 0; i <= n; i++){ F[i] = G[i]; }
82     for(i = 0; i <= n; i++){
83         for(j = 0; (1 << j) <= i + 1; j++){
84             if((i + 1) % (1 << j) == 0){
85                 vector<int> a = segmentation(i - (1 << j) + 1, i, 1 << j, (1 << j) + (1 <<
86                     ↪ j) - 1);
87                 int offst = (1 << j) * (i / (1 << j) + 1);
88                 contribute(offst, a);
89                 cout << "i-->" << i << " " << "j-->" << j << " " << offst; nl;
90                 para(l, 0, n, F);
91             }
92         } nl;
93         dp[0] = 1;
94         for(i = 0; i <= n; i++){
95             ret = brute(i);
96         }
97         para(i, 0, n, dp);
98         para(i, 0, n, F);
99     }
100 int main(){
101     input();
102     solve();
103 }

```

---

## 8 sum\_of\_kth\_power\_of\_all\_possible\_subgraph\_in\_the\_tree

---

```

1  int add(int _a, int _b){
2      _a = (_a + MOD) % MOD;
3      _b = (_b + MOD) % MOD;
4      return (_a + _b) % MOD;
5  }
6  int mul(int _a, int _b){
7      _a = (_a + MOD) % MOD;
8      _b = (_b + MOD) % MOD;
9      return ((ll)((ll)_a * (ll)_b)) % MOD;
10 }
11 int n, k, sbtr[SZ], sum[210], dif[SZ][210], sol = 0, fac[SZ], inv[SZ], h[SZ][210],
    ↪ f[210][210];
12 vector<int> adj[SZ];
13 void input(){
14     int i, j;
15     sii(n, k);
16     for(i = 0; i < n - 1; i++){
17         int u, v; sii(u, v), u--, v--;
18         adj[u].push_back(v), adj[v].push_back(u);
19     }
20 }
21 int bigMod(int v, int p){
22     if(p == 0){ return 1; }
23     int ret = bigMod(v, p / 2);
24     if(p % 2 == 0){ return mul(ret, ret); }
25     else{ return mul(ret, mul(ret, v)); }
26 }
27 void factorial(){
28     int i, j;
29     for(i = 1, fac[0] = inv[0] = 1; i < SZ - 1; i++){
30         fac[i] = mul(fac[i - 1], i);
31         inv[i] = mul(inv[i - 1], bigMod(i, MOD - 2));
32     }
33 }
34 void H(int src){
35     int sz = adj[src].size(), i, j, l, u, x;
36     for(i = sz - 1; i >= 0; i--){
37         for(u = adj[src][i], j = 0; j <= min(k, sbtr[src] - 1); j++){
38             if(i == sz - 1){
39                 if(j == 0){ h[i][j] = add(1, dif[u][j]); }
40                 else{ h[i][j] = add(dif[u][j], mul(j, dif[u][j - 1])); }
41                 continue;
42             }
43             for(l = 0, h[i][j] = 0; l <= min(sbtr[u], j); l++){
44                 x = mul(fac[j], mul(inv[l], inv[j - l]));
45                 if(l == 0){ x = mul(x, add(1, dif[u][0])); }
46                 else{ x = mul(x, add(dif[u][l], mul(l, dif[u][l - 1]))); }
47                 x = mul(x, h[i + 1][j - l]);
48                 h[i][j] = add(h[i][j], x);
49             }
50         }
51     }
52 }
53 int F(int u, int v){
54     int ret = 0;
55     if(v > u){ return 0; }
56     if(v == 0){ return 0; }
57     if(u == 1){ return 1; }

```

```

58     if(f[u][v] != -1){ return f[u][v]; }
59     ret = add(mul(v, F(u - 1, v)), F(u - 1, v - 1));
60     return f[u][v] = ret;
61 }
62 bool cmp(int lhs, int rhs){ return sbtr[lhs] < sbtr[rhs]; }
63 void dfs(int src, int par){
64     int i, j, idx = -1, mns, ret, u, x; sbtr[src] = 1, ret = 0;
65     for(i = 0; i < adj[src].size(); i++){
66         u = adj[src][i];
67         if(u == par){ idx = i; break; }
68     }
69     if(idx != -1){ adj[src].erase(adj[src].begin() + idx); }
70     for(i = 0, dif[src][0] = 2, mns = 0; i < adj[src].size(); i++){
71         u = adj[src][i];
72         dfs(u, src);
73         sbtr[src] += sbtr[u];
74         dif[src][0] = mul(dif[src][0], add(1, dif[u][0]));
75     }
76     sort(adj[src].begin(), adj[src].end(), cmp);
77     dif[src][0] = add(dif[src][0], -1);
78     for(j = 0; j <= k; j++){
79         for(i = 0, sum[j] = 0; i < adj[src].size(); i++){
80             int u = adj[src][i];
81             sum[j] = add(sum[j], dif[u][j]);
82         }
83     }
84     H(src);
85     for(i = 1; i <= min(k, sbtr[src] - 1); i++){
86         u = adj[src][0];
87         x = mul(2, h[0][i]);
88         dif[src][i] = x;
89         x = add(x, -sum[i]);
90         x = add(x, -(mul(i, sum[i - 1]))); //check korte hbe
91         x = mul(x, F(k, i));
92         ret = add(ret, x);
93     }
94     sol = add(sol, ret);
95 }
96 void solve(){
97     int i, j;
98     mem(f, -1); factorial();
99     dfs(0, -1);
100    pi(sol); nl;
101 }
102 int main(){
103     // freopen("input.txt", "r", stdin);
104     // int ret = F(3, 3);
105     // pi(ret); nl;
106     // freopen("output.txt", "w", stdout);
107     input();
108     solve();
109 }

```

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