

Assignment

Data set:-

x	y
Weight	Price
2	35
4	60
5	20
3	50
6	50
5	55
7	60

Formulae, $y = mx + c = \text{predict output}$

Here,
$$m = \frac{N \sum(xy) - (\sum x)(\sum y)}{N \sum(x^2) - (\sum x)^2}$$

$$\therefore \sum(xy) = (2 \times 35) + (4 \times 60) + (5 \times 20) + (3 \times 50) + (6 \times 50) \\ + (5 \times 55) + (7 \times 60)$$

$$= 1405$$

$$\sum x = 2 + 4 + 5 + 3 + 6 + 5 + 7 = 32$$

$$\sum y = 35 + 60 + 20 + 50 + 50 + 55 + 60 = 330$$

$$\sum(x^2) = 4 + 16 + 25 + 9 + 36 + 25 + 49 = 164$$

$$(\sum x)^2 = 32^2 = 1024$$

$$n = 7$$

$$\therefore m = \frac{1405 - (32 \times 330)}{164 - (32)^2}$$

$$\therefore m = \frac{7 \times 1555 - 32 \times 330}{7 \times 164 - (32)^2}$$

$$= \frac{325}{124} = 2.62$$

and $c = \frac{\sum y - m \sum x}{n}$

$$= \frac{330 - 2.62 \times 32}{7}$$

$$= 35.16$$

1. Task - 1:

predict value for 6 = $2.62 \times 6 + 35.16$

$$= 50.88 \text{ (Ans:-)}$$

2. Task - 2:

residual = original (price) - predict (price)

$$= 35 - 40.4 = -5.4$$

residual
-5.40
14.35
-28.26
6.97
-0.88
6.73
6.49

Task: 3

We know, $MSE = \frac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2$

$$\begin{aligned}
 \therefore (Y_i - \hat{Y}_i)^2 &= (-5.40)^2 + (14.35)^2 + (-28.26)^2 + (6.97)^2 \\
 &\quad + (-0.88)^2 + (6.73)^2 + (6.49)^2 \\
 &= 29.16 + 205.92 + 798.63 + 48.58 + 0.77 \\
 &\quad + 45.29 + 20.16 \\
 &= 1148.51
 \end{aligned}$$

$$\therefore MSE = \frac{1148.51}{7} = 164.07$$

$$\therefore MAE = \frac{1}{n} \sum_{i=1}^n |Y_i - \hat{Y}_i|$$

$$= \frac{5.40 + 14.35 + 28.26 + 6.97 + 0.88 + 6.73}{7} + 49$$

$$= 9.87 \text{ (Ans:-)}$$