# EE 511 - Homework 01

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# Part 1: Signal with no harmonics

#### 1a) Draw the following waveform:

```
\left\{egin{array}{ll} 6sin(\omega t+\pi/3) & t<0.1 \ 10sin(\omega t+\pi/3) & t\geq0.1 \end{array}
ight.
```

Given that, f = 60 Hz, and sampling frequency is 12 samples per cycle.

```
In [1]: ## IMPORT PACKAGES
  import matplotlib.pyplot as plt
  import numpy as np
  import math
```

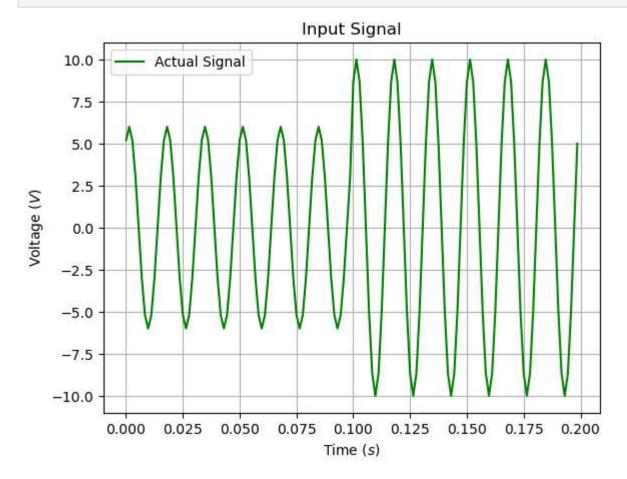
### Plotting the input signal:

```
In [3]: ## PLOTTING INPUT SIGNAL
    Time = np.arange(StartTime,EndTime,dT)
    Voltage1 = []

for t in range(0,len(Time)):
        if Time[t] < 0.1:
            v = A1 * np.sin(w * Time[t] + np.pi/3) # first signal
        else:
            v = A2 * np.sin(w * Time[t] + np.pi/3) # second signal

        Voltage1.append(v)

plt.plot(Time,Voltage1,'green')
    plt.title("Input Signal")
    plt.xlabel("Time $(s)$")
    plt.ylabel("Voltage $(V)$")
    plt.legend(["Actual Signal"])</pre>
```



### 1b) Estimate the amplitude of the signal using Mann&Morrison algorithm

In Mann & Morrison algorithm, it is assumed that the signal can be represented as a pure sinusoid whose amplitude as well as frequency is constant during the period under consideration [1].

So for a signal  $V=V_p sin(\omega_0 t + heta)$ :

$$V_p=\sqrt{(V_p sin heta)^2+(V_p cos heta)^2}=\sqrt{(V_0)^2+(rac{V_{+1}-V_{-1}}{2\omega_0\Delta t})^2}$$

Here, sine component,  $V_p sin heta=V_0$  and cosine component  $V_p cos heta=rac{V_{+1}-V_{-1}}{2\omega_0\Delta t}$ 

## **Mann & Morrison Algorithm Function:**

```
In [4]: # MANN & MORRISON ALGORITHM

def MannMorrison(StartTime,EndTime,sample,frequency,voltage):

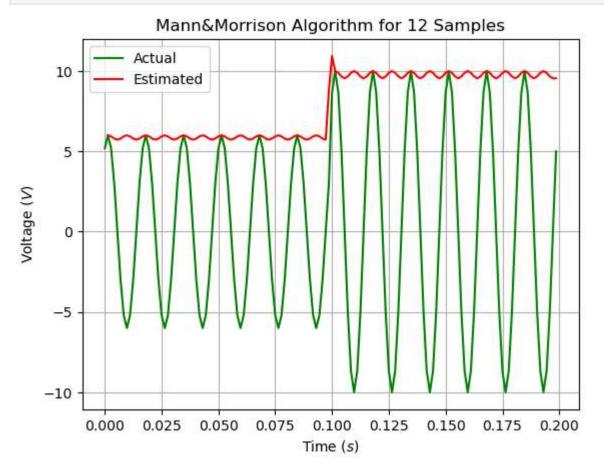
    f0 = frequency # fundamental frequency
    n = sample

    T = 1/f0
    dT = T/n
    w0 = 2 * np.pi * f0
    time = np.arange(StartTime,EndTime,dT)
```

```
Vp = []
for t in range(1, len(time)-1):
    sine_component = voltage[t]
    cosine_component = (voltage[t+1] - voltage[t-1])/(2 * w0 * dT)
    vp_temp = np.sqrt(sine_component**2 + cosine_component**2)
    Vp.append(vp_temp)
Vp.append(vp_temp)
# PLOT
plt.plot(time, voltage, 'green')
plt.plot(time[1:len(time)], Vp, 'r-')
plt.title("Mann&Morrison Algorithm for " + str(n) + " Samples")
plt.xlabel("Time $(s)$")
plt.ylabel("Voltage $(V)$")
plt.legend(["Actual", "Estimated"])
plt.grid()
plt.show()
```

### **Applying Mann & Morrison algorithm on input signal:**

In [5]: MannMorrison(StartTime,EndTime,n,f,Voltage1)



#### 1c) Estimate the amplitude of the signal using Prodar algorithm

The basic difference between Mann&Morrison and Prodar algorithm is, in Prodar algorithm, the sine component is taken from second derivative [1]. In this way, if there is a DC component in the input signal it can be handled.

```
So for a signal V=V_psin(\omega_0t+\theta): V_p=\sqrt{(V_psin\theta)^2+(V_pcos\theta)^2} Where, sine component, V_psin\theta=\frac{V_{+1}-2V_0+V_{-1}}{(\omega_0\Delta t)^2} and cosine component V_pcos\theta=\frac{V_{+1}-V_{-1}}{2\omega_0\Delta t}
```

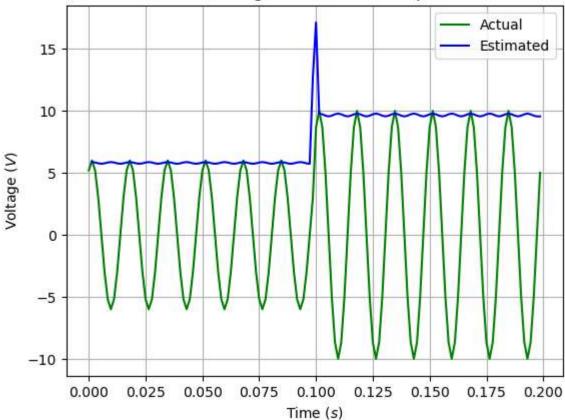
#### **Prodar Algorithm Function:**

```
# PRODAR ALGORITHM
In [6]:
        def Prodar(StartTime,EndTime,sample,frequency,voltage):
            f0 = frequency # fundamental frequency
            n = sample
            T = 1/f0
            dT = T/n
            w0 = 2 * np.pi * f0
            time = np.arange(StartTime,EndTime,dT)
            Vp = []
            for t in range(1, len(time)-1):
                 sine\_component = (voltage[t+1] - 2 * voltage[t] + voltage[t-1])/((w0 * dT)**2)
                 cosine_component = (voltage[t+1] - voltage[t-1])/(2 * w0 * dT)
                 vp_temp = np.sqrt(sine_component**2 + cosine_component**2)
                Vp.append(vp_temp)
            Vp.append(vp_temp)
            # PLOT
            plt.plot(time, voltage, 'green')
             plt.plot(time[1:len(time)], Vp, 'b-')
            plt.title("Prodar Algorithm for " + str(n) + " Samples")
            plt.xlabel("Time $(s)$")
            plt.ylabel("Voltage $(V)$")
            plt.legend(["Actual", "Estimated"])
            plt.grid()
             plt.show()
```

#### **Applying Prodar algorithm on input signal:**

```
In [7]: Prodar(StartTime,EndTime,n,f,Voltage1)
```

## Prodar Algorithm for 12 Samples



# Part 2: Signal with harmonics

2a) Add second harmonic to the signal which means the signal becomes as follows:

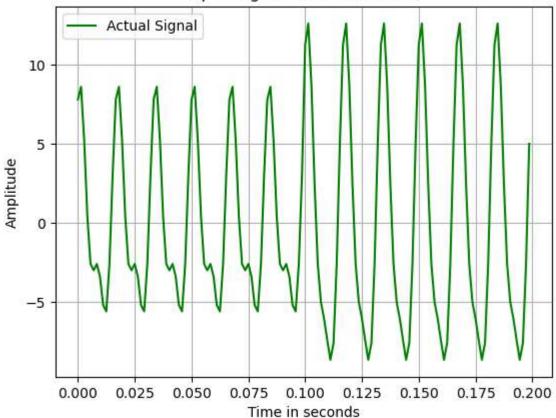
$$\left\{ egin{aligned} 6 sin(\omega t + \pi/3) + 3 sin(2\omega t + \pi/3) & t < 0.1 \ 10 sin(\omega t + \pi/3) + 3 sin(2\omega t + \pi/3) & t \geq 0.1 \end{aligned} 
ight.$$

Given that, f = 60 Hz, and sampling frequency is 12 samples per cycle.

## Plotting the input signal:

```
plt.title("Input Signal with Harmonics")
plt.xlabel("Time in seconds")
plt.ylabel("Amplitude")
plt.legend(["Actual Signal"])
plt.grid()
plt.show()
```

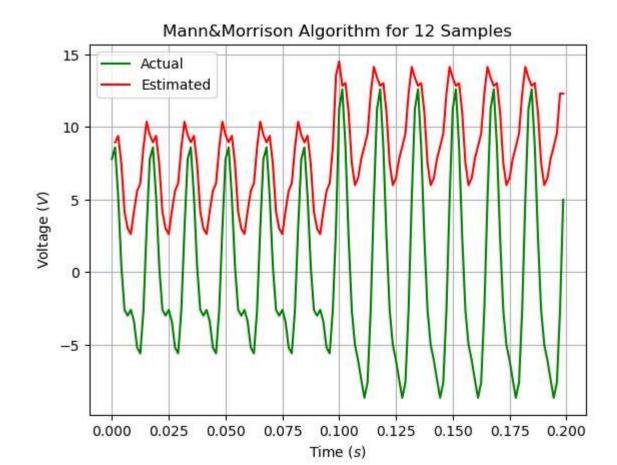
# Input Signal with Harmonics



2b) Estimate the amplitude of the signal using Mann&Morrison algorithm

### **Applying Mann & Morrison algorithm on input signal:**

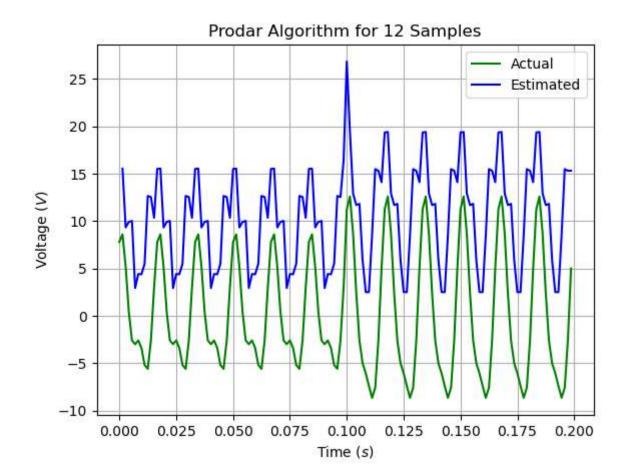
```
In [9]: # MANN & MORRISON ALGORITHM
    MannMorrison(StartTime,EndTime,n,f,Voltage2)
```



## 2c) Estimate the amplitude of the signal using Prodar algorithm

## **Applying Prodar algorithm on input signal:**

In [10]: Prodar(StartTime,EndTime,n,f,Voltage2)



# References

[1] S. R. Bhide, Digital Power System Protection, Delhi, 2014.