# **Self-Driving Car Engineer Nanodegree**

# **Deep Learning**

# **Project: Build a Traffic Sign Recognition Classifier**

In this notebook, a template is provided for you to implement your functionality in stages, which is required to successfully complete this project. If additional code is required that cannot be included in the notebook, be sure that the Python code is successfully imported and included in your submission if necessary.

**Note**: Once you have completed all of the code implementations, you need to finalize your work by exporting the iPython Notebook as an HTML document. Before exporting the notebook to html, all of the code cells need to have been run so that reviewers can see the final implementation and output. You can then export the notebook by using the menu above and navigating to \n", "**File -> Download as -> HTML (.html)**. Include the finished document along with this notebook as your submission.

In addition to implementing code, there is a writeup to complete. The writeup should be completed in a separate file, which can be either a markdown file or a pdf document. There is a <u>write up template</u> (<a href="https://github.com/udacity/CarND-Traffic-Sign-Classifier-Project/blob/master/writeup\_template.md">https://github.com/udacity/CarND-Traffic-Sign-Classifier-Project/blob/master/writeup\_template.md</a>) that can be used to guide the writing process. Completing the code template and writeup template will cover all of the rubric points (https://review.udacity.com/#!/rubrics/481/view) for this project.

The <u>rubric (https://review.udacity.com/#!/rubrics/481/view)</u> contains "Stand Out Suggestions" for enhancing the project beyond the minimum requirements. The stand out suggestions are optional. If you decide to pursue the "stand out suggestions", you can include the code in this lpython notebook and also discuss the results in the writeup file.

**Note:** Code and Markdown cells can be executed using the **Shift + Enter** keyboard shortcut. In addition, Markdown cells can be edited by typically double-clicking the cell to enter edit mode.

# Step 0: Load The Data

```
# Load pickled data
In [1]:
        import pickle
        # TODO: Fill this in based on where you saved the training and testing
        data
        training file = "traffic-signs-data/train.p"
        validation file="traffic-signs-data/valid.p"
        testing_file = "traffic-signs-data/test.p"
        with open(training file, mode='rb') as f:
            train = pickle.load(f)
        with open(validation file, mode='rb') as f:
            valid = pickle.load(f)
        with open(testing file, mode='rb') as f:
            test = pickle.load(f)
        X train, y train = train['features'], train['labels']
        X_valid, y_valid = valid['features'], valid['labels']
        X_test, y_test = test['features'], test['labels']
```

# **Step 1: Dataset Summary & Exploration**

The pickled data is a dictionary with 4 key/value pairs:

- 'features' is a 4D array containing raw pixel data of the traffic sign images, (num examples, width, height, channels).
- 'labels' is a 1D array containing the label/class id of the traffic sign. The file signnames.csv contains id -> name mappings for each id.
- 'sizes' is a list containing tuples, (width, height) representing the original width and height the image.
- 'coords' is a list containing tuples, (x1, y1, x2, y2) representing coordinates of a bounding box around the sign in the image. THESE COORDINATES ASSUME THE ORIGINAL IMAGE. THE PICKLED DATA CONTAINS RESIZED VERSIONS (32 by 32) OF THESE IMAGES

Complete the basic data summary below. Use python, numpy and/or pandas methods to calculate the data summary rather than hard coding the results. For example, the <u>pandas shape method</u> (<a href="http://pandas.pydata.org/pandas-docs/stable/generated/pandas.DataFrame.shape.html">http://pandas.pydata.org/pandas-docs/stable/generated/pandas.DataFrame.shape.html</a>) might be useful for calculating some of the summary results.

Provide a Basic Summary of the Data Set Using Python, Numpy and/or Pandas

```
In [2]: ### Replace each question mark with the appropriate value.
        ### Use python, pandas or numpy methods rather than hard coding the re
        sults
        import numpy as np
        # TODO: Number of training examples
        n train = len(X train)
        # TODO: Number of validation examples
        n validation = len(X valid)
        # TODO: Number of testing examples.
        n \text{ test} = len(X \text{ test})
        # TODO: What's the shape of an traffic sign image?
        image shape = X train[0].shape
        # TODO: How many unique classes/labels there are in the dataset.
        n classes = len(np.unique(y train))
        print("Number of training examples =", n train)
        print("Number of validation examples =", n validation)
        print("Number of testing examples =", n test)
        print("Image data shape =", image shape)
        print("Number of classes =", n classes)
        Number of training examples = 34799
        Number of validation examples = 4410
        Number of testing examples = 12630
        Image data shape = (32, 32, 3)
        Number of classes = 43
```

### Include an exploratory visualization of the dataset

Visualize the German Traffic Signs Dataset using the pickled file(s). This is open ended, suggestions include: plotting traffic sign images, plotting the count of each sign, etc.

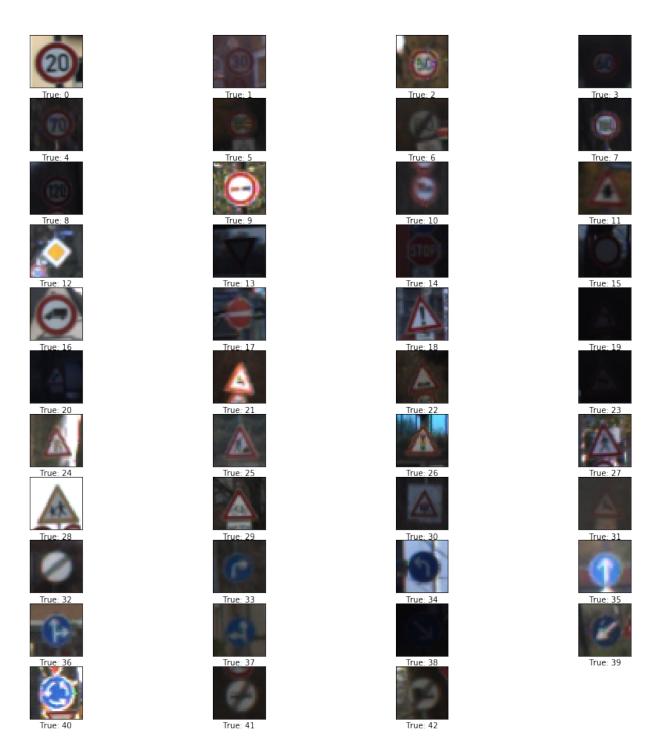
The <u>Matplotlib (http://matplotlib.org/) examples (http://matplotlib.org/examples/index.html)</u> and <u>gallery (http://matplotlib.org/gallery.html)</u> pages are a great resource for doing visualizations in Python.

**NOTE:** It's recommended you start with something simple first. If you wish to do more, come back to it after you've completed the rest of the sections. It can be interesting to look at the distribution of classes in the training, validation and test set. Is the distribution the same? Are there more examples of some classes than others?

```
In [3]: ### Data exploration visualization code goes here.
        ### Feel free to use as many code cells as needed.
        import math
        import matplotlib.pyplot as plt
        %matplotlib inline
        def plot images (images, class true, class pred):
            assert len(images) == len(class true)
            n cols = 4
            n rows = math.ceil(len(images)/4)
            fig = plt.figure(figsize=(16, 16))
            for i in range(len(images)):
                ax = fig.add subplot(n rows, n cols, i+1)
                plt.imshow(images[i])
                if class pred is None:
                      xlabel = "True: {0}".format(class_true[i])
                else:
                     xlabel = "True: {0}, Pred: {1}".format(class true[i], cla
        ss pred[i])
                ax.set xlabel(xlabel)
                #Remove ticks from the plot.
                ax.set xticks([])
                ax.set yticks([])
```

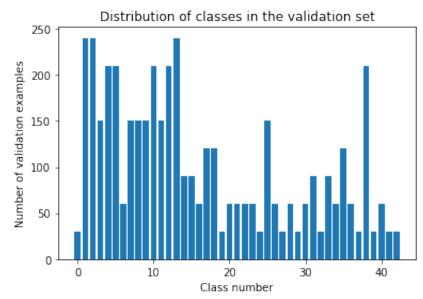
```
In [4]: images = []
    true_class = np.unique(y_train)
    for i in range(len(true_class)):
        X_temp = X_train[y_train == i]
        images.append(X_temp[0])

plot_images(images=images, class_true=true_class, class_pred = None)
    plt.savefig('Examples/Visualization_1')
```



```
In [5]: ## Checking the distribution of the classes in the training set and va
        lidation set
        dict num class = dict(zip(np.unique(y_train),np.zeros(len(np.unique(y_
        train)))))
        for i in y train:
            dict num class[i]+=1
        plt.bar(list(dict num class.keys()), list(dict num class.values()))
        plt.title("Distribution of classes in the training set")
        plt.xlabel("Class number")
        plt.ylabel("Number of training examples")
        plt.show()
        dict num class valid = dict(zip(np.unique(y valid),np.zeros(len(np.uni
        que(y valid)))))
        for i in y_valid:
            dict num class valid[i]+=1
        plt.bar(list(dict_num_class_valid.keys()), list(dict num class valid.v
        alues()))
        plt.title("Distribution of classes in the validation set")
        plt.xlabel("Class number")
        plt.ylabel("Number of validation examples")
        plt.show()
```





# Step 2: Design and Test a Model Architecture

Design and implement a deep learning model that learns to recognize traffic signs. Train and test your model on the German Traffic Sign Dataset (http://benchmark.ini.rub.de/?section=gtsrb&subsection=dataset).

The LeNet-5 implementation shown in the <a href="classroom">classroom</a>. <a href="(https://classroom.udacity.com/nanodegrees/nd013/parts/fbf77062-5703-404e-b60c-95b78b2f3f9e/modules/6df7ae49-c61c-4bb2-a23e-6527e69209ec/lessons/601ae704-1035-4287-8b11-e2c2716217ad/concepts/d4aca031-508f-4e0b-b493-e7b706120f81)</a> at the end of the CNN lesson is a solid starting point. You'll have to change the number of classes and possibly the preprocessing, but aside from that it's plug and play!

With the LeNet-5 solution from the lecture, you should expect a validation set accuracy of about 0.89. To meet specifications, the validation set accuracy will need to be at least 0.93. It is possible to get an even higher accuracy, but 0.93 is the minimum for a successful project submission.

There are various aspects to consider when thinking about this problem:

- Neural network architecture (is the network over or underfitting?)
- Play around preprocessing techniques (normalization, rgb to grayscale, etc)
- Number of examples per label (some have more than others).
- · Generate fake data.

Here is an example of a <u>published baseline model on this problem</u> (<a href="http://yann.lecun.com/exdb/publis/pdf/sermanet-ijcnn-11.pdf">http://yann.lecun.com/exdb/publis/pdf/sermanet-ijcnn-11.pdf</a>). It's not required to be familiar with the approach used in the paper but, it's good practice to try to read papers like these.

### Pre-process the Data Set (normalization, grayscale, etc.)

Minimally, the image data should be normalized so that the data has mean zero and equal variance. For image data, (pixel - 128) / 128 is a quick way to approximately normalize the data and can be used in this project.

Other pre-processing steps are optional. You can try different techniques to see if it improves performance.

Use the code cell (or multiple code cells, if necessary) to implement the first step of your project.

```
In [6]: ### Preprocess the data here. It is required to normalize the data. Ot
her preprocessing steps could include
### converting to grayscale, etc.
### Feel free to use as many code cells as needed.
```

```
In [7]: import cv2
        def slicing(image):
            return image[3:29,3:29,:]
        def blur(image):
            image new = cv2.GaussianBlur(image,(7,7),10)
            return cv2.addWeighted(image, 2.3, image new, -1, 0)
        def translate(image):
            M = np.float32([[1,0,3],[0,1,2]])
            return cv2.warpAffine(image,M,(image.shape[1],image.shape[0]))
        def rotate(image):
            M = cv2.getRotationMatrix2D((image.shape[1]/2,image.shape[0]/2),np
        .random.rand(1)*10,1)
            return cv2.warpAffine(image,M,(image.shape[1],image.shape[0]))
        def distort(image):
            image1 = slicing(image)
            image2 = blur(image1)
            image3 = rotate(image2)
            return image3
```

```
In [8]: ### Showing the difference between the raw image and the preprocessed
        image
        example image = 4900
        image_processed = blur(slicing(X_train[example_image]))
        plt.figure(figsize=(6, 4))
        plt.subplot(121)
        plt.xlabel('Raw Image')
        plt.xticks(())
        plt.yticks(())
        plt.imshow(X_train[example_image])
        plt.subplot(122)
        plt.xlabel('Processed Image')
        plt.xticks(())
        plt.yticks(())
        plt.imshow(image_processed)
        plt.savefig('Examples/Raw-and-processed-Images')
```





Raw Image

Processed Image

```
In [9]: X train new = []
        y train new = []
        for i in range(n train):
            X train new.append(blur(slicing(X train[i])))
            y train new.append(y train[i])
        for i in range(n validation):
            X train new.append(blur(slicing(X valid[i])))
            y train new.append(y valid[i])
        desired length = 1500
        for i in range(n classes):
                cnt = 0
                X train less = X train[y train == i]
                current length = len(X train less)
                add_length = desired_length - current_length
                while (cnt <= add length):</pre>
                     ind = np.random.randint(0,current length-1)
                     X train new.append(distort(X train less[ind]))
                     y train new.append(i)
                     cnt = cnt + 1
```

```
In [10]: from sklearn.model_selection import train_test_split
X_train_p, X_valid_p, y_train_p, y_valid_p = train_test_split(X_train_new, y_train_new, test_size = 0.15,random_state=0)
```

```
In [11]: X_train_p[0].shape
len(X_train_p)
```

Out[11]: 61051

### **Model Architecture**

```
In [12]: ### Define your architecture here.
import tensorflow as tf
from tensorflow.contrib.layers import flatten

keep_prob = tf.placeholder(tf.float32) # probability to keep units

def LeNet(x):
    # Arguments used for tf.truncated_normal, randomly defines variable es for the weights and biases for each layer
    mu = 0
    sigma = 0.01
```

```
# TODO: Layer 1: Convolutional. Input = 26x26x3. Output = 22x22x6.
   W layer 1 = tf.Variable(tf.random normal([5, 5, 3, 6], mu, sigma))
    Bias layer 1 = tf.Variable(tf.random normal([6],mu,sigma))
    conv layer 1 = tf.nn.bias add(tf.nn.conv2d(x, W layer 1, strides=[
1, 1, 1, 1], padding='VALID'), Bias layer 1)
    # TODO: Activation.
    conv layer 1 = tf.nn.relu(conv layer 1)
    # TODO: Pooling. Input = 22x22x6. Output = 11x11x6.
    layer 1 = tf.nn.max pool(conv layer 1, ksize=[1, 2, 2, 1], strides
=[1, 2, 2, 1],padding='SAME')
    # TODO: Layer 2: Convolutional. Output = 7x7x16.
    W layer 2 = tf.Variable(tf.random normal([5, 5, 6, 16],mu,sigma))
    Bias layer 2 = tf.Variable(tf.random normal([16],mu,sigma))
    conv_layer_2 = tf.nn.bias_add(tf.nn.conv2d(layer_1, W_layer_2, str
ides=[1, 1, 1, 1], padding='VALID'), Bias layer 2)
    # TODO: Activation.
    conv layer 2 = tf.nn.relu(conv layer 2)
    # TODO: Pooling. Input = 7x7x16. Output = 4x4x16.
    layer 2 = tf.nn.max pool(conv layer 2, ksize=[1, 2, 2, 1], strides
=[1, 2, 2, 1],padding='SAME')
    # TODO: Flatten. Input = 4x4x16. Output = 256.
    layer 2 = flatten(layer 2)
    # TODO: Layer 3: Fully Connected. Input = 256. Output = 120.
   W layer 3 = tf.Variable(tf.random normal([256,120],mu,sigma))
    Bias layer 3 = tf.Variable(tf.random normal([120],mu,sigma)),
    layer 3 = tf.add(tf.matmul(layer 2,W layer 3),Bias layer 3)
    # TODO: Activation.
    layer 3 = tf.nn.relu(layer 3)
    layer 3= tf.nn.dropout(layer 3, keep prob)
    # TODO: Layer 4: Fully Connected. Input = 120. Output = 84.
   W layer 4 = tf.Variable(tf.random normal([120,84],mu,sigma))
    Bias layer 4 = tf.Variable(tf.random normal([84],mu,sigma)),
    layer 4 = tf.add(tf.matmul(layer 3,W layer 4),Bias layer 4)
    # TODO: Activation.
    layer 4 = tf.nn.relu(layer 4)
    layer 4= tf.nn.dropout(layer 4, keep prob)
    # TODO: Layer 5: Fully Connected. Input = 84. Output = 43.
    W layer 5 = tf.Variable(tf.random normal([84,43],mu,sigma))
```

```
Bias_layer_5 = tf.Variable(tf.random_normal([43],mu,sigma)),
logits = tf.add(tf.matmul(layer_4,W_layer_5),Bias_layer_5)

return logits
### Feel free to use as many code cells as needed.
```

```
In [13]: x = tf.placeholder(tf.float32, (None, 26, 26, 3))
y = tf.placeholder(tf.int32, (None))
one_hot_y = tf.one_hot(y, 43)
```

### Train, Validate and Test the Model

A validation set can be used to assess how well the model is performing. A low accuracy on the training and validation sets imply underfitting. A high accuracy on the training set but low accuracy on the validation set implies overfitting.

```
In [15]: ### Train your model here.
### Calculate and report the accuracy on the training and validation s
et.
### Once a final model architecture is selected,
### the accuracy on the test set should be calculated and reported as
well.
### Feel free to use as many code cells as needed.
```

```
In [16]: correct_prediction = tf.equal(tf.argmax(logits, 1), tf.argmax(one_hot_y, 1))
    accuracy_operation = tf.reduce_mean(tf.cast(correct_prediction, tf.flo at32))
    saver = tf.train.Saver()

def evaluate(X_data, y_data):
    num_examples = len(X_data)
    total_accuracy = 0
    sess = tf.get_default_session()
    for offset in range(0, num_examples, BATCH_SIZE):
        batch_x, batch_y = X_data[offset:offset+BATCH_SIZE], y_data[of fset:offset+BATCH_SIZE]
        accuracy = sess.run(accuracy_operation, feed_dict={x: batch_x, y: batch_y, keep_prob:1})
        total_accuracy += (accuracy * len(batch_x))
    return total_accuracy / num_examples
```

```
In [17]:
         from sklearn.utils import shuffle
         EPOCHS = 15
         BATCH SIZE = 128
         with tf.Session() as sess:
             sess.run(tf.global variables initializer())
             num examples = len(X train p)
             print("Training...")
             print()
             for i in range(EPOCHS):
                 print("EPOCH {} ...".format(i+1))
                 X train p, y train p = shuffle(X train p, y train p)
                 for offset in range(0, num examples, BATCH SIZE):
                     end = offset + BATCH SIZE
                     batch x, batch y = X train p[offset:end], y train p[offset
         :end]
                     sess.run(training operation, feed dict={x: batch x, y: bat
         ch y, keep prob: 0.6})
                     if (offset% 25600 == 0):
                         training accuracy = evaluate(batch_x, batch_y)
                         print("Training Accuracy = {:.3f}".format(training acc
         uracy), "offset = {}".format(offset))
                 validation accuracy = evaluate(X valid p, y valid p)
                 print("Validation Accuracy = {:.3f}".format(validation accurac
         y))
                 print()
             saver.save(sess, './lenet')
             print("Model saved")
         Training...
         EPOCH 1 ...
         Training Accuracy = 0.031 offset = 0
         Training Accuracy = 0.195 offset = 25600
         Training Accuracy = 0.523 offset = 51200
         Validation Accuracy = 0.585
         EPOCH 2 ...
         Training Accuracy = 0.602 offset = 0
         Training Accuracy = 0.750 offset = 25600
         Training Accuracy = 0.914 offset = 51200
         Validation Accuracy = 0.873
         EPOCH 3 ...
         Training Accuracy = 0.844 offset = 0
```

> Training Accuracy = 0.945 offset = 25600 Training Accuracy = 0.914 offset = 51200 Validation Accuracy = 0.938

### EPOCH 4 ...

Training Accuracy = 0.961 offset = 0 Training Accuracy = 0.906 offset = 25600 Training Accuracy = 0.977 offset = 51200 Validation Accuracy = 0.957

#### EPOCH 5 ...

Training Accuracy = 0.969 offset = 0 Training Accuracy = 0.953 offset = 25600 Training Accuracy = 0.969 offset = 51200 Validation Accuracy = 0.961

#### EPOCH 6 ...

Training Accuracy = 0.984 offset = 0 Training Accuracy = 0.945 offset = 25600 Training Accuracy = 0.961 offset = 51200 Validation Accuracy = 0.971

#### EPOCH 7 ...

Training Accuracy = 0.992 offset = 0 Training Accuracy = 0.984 offset = 25600 Training Accuracy = 0.992 offset = 51200 Validation Accuracy = 0.974

#### EPOCH 8 ...

Training Accuracy = 0.984 offset = 0 Training Accuracy = 1.000 offset = 25600 Training Accuracy = 0.992 offset = 51200 Validation Accuracy = 0.974

### EPOCH 9 ...

Training Accuracy = 0.992 offset = 0 Training Accuracy = 0.984 offset = 25600 Training Accuracy = 0.992 offset = 51200 Validation Accuracy = 0.973

### EPOCH 10 ...

Training Accuracy = 0.961 offset = 0 Training Accuracy = 0.961 offset = 25600 Training Accuracy = 0.992 offset = 51200 Validation Accuracy = 0.978

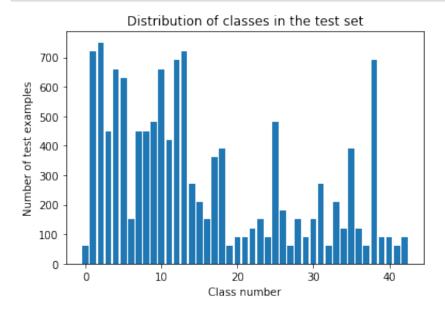
### EPOCH 11 ...

Training Accuracy = 0.992 offset = 0 Training Accuracy = 1.000 offset = 25600 Training Accuracy = 0.984 offset = 51200

```
Validation Accuracy = 0.978
EPOCH 12 ...
Training Accuracy = 0.984 offset = 0
Training Accuracy = 0.961 offset = 25600
Training Accuracy = 0.992 offset = 51200
Validation Accuracy = 0.980
EPOCH 13 ...
Training Accuracy = 1.000 offset = 0
Training Accuracy = 1.000 offset = 25600
Training Accuracy = 0.984 offset = 51200
Validation Accuracy = 0.979
EPOCH 14 ...
Training Accuracy = 0.984 offset = 0
Training Accuracy = 1.000 offset = 25600
Training Accuracy = 0.992 offset = 51200
Validation Accuracy = 0.982
EPOCH 15 ...
Training Accuracy = 0.992 offset = 0
Training Accuracy = 0.969 offset = 25600
Training Accuracy = 0.984 offset = 51200
Validation Accuracy = 0.981
```

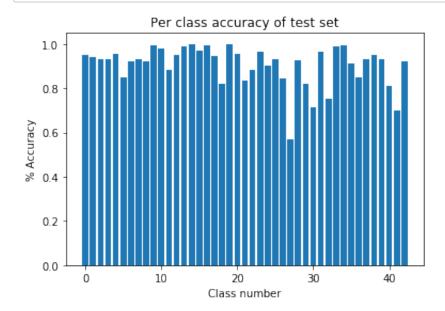
Model saved

### Accuracy on the given test set



Test Accuracy = 0.928

```
In [20]:
         ## Plotting accuracy for each of the classes:
         dict class accuracy = dict(zip(np.unique(y test),np.zeros(len(np.uniqu
         e(y test)))))
         X_test_alt_np = np.asarray(X_test_alt)
         with tf.Session() as sess:
             saver.restore(sess, tf.train.latest checkpoint('.'))
             for i in range(n classes):
                 X particular class = X test alt np[y test == i]
                 y_particular_class = i*np.ones(len(X_particular_class))
                 dict_class_accuracy[i] = evaluate(X_particular_class, y_partic
         ular class)
         plt.bar(list(dict class accuracy.keys()), list(dict_class_accuracy.val
         ues()))
         plt.title("Per class accuracy of test set")
         plt.xlabel("Class number")
         plt.ylabel("% Accuracy")
         plt.show()
```



# Step 3: Test a Model on New Images

To give yourself more insight into how your model is working, download at least five pictures of German traffic signs from the web and use your model to predict the traffic sign type.

You may find signnames.csv useful as it contains mappings from the class id (integer) to the actual signname.

### **Load and Output the Images**

```
In [21]:
         ### Load the images and plot them here.
         ### Feel free to use as many code cells as needed.
         import os
         def mylistdir(directory):
              """A specialized version of os.listdir() that ignores files that
              start with a leading period."""
              filelist = os.listdir(directory)
              return [x for x in filelist
                      if not (x.startswith('.'))]
         list images = mylistdir("New Test images/")
         len list images = len(list images)
         #os.mkdir('test images output')
         X_{test_raw} = []
         y \text{ test raw} = [3,9,35,13,14]
         for i,im in zip(range(len list images), list images):
              image = plt.imread(os.path.join("New Test images/",im))
              image = cv2.resize(image, (32, 32))
              X test raw.append(image)
```

```
In [22]: # Processing images
X_test_new = []
y_test_new = [3,9,35,13,14]
for i in range(len(X_test_raw)):
    image_in = blur(slicing(X_test_raw[i]))
    X_test_new.append(image_in)
    plt.axis('off')
    image_out = plt.imshow(image_in)
    plt.savefig('examples/Test_'+str(i+1))
```



## **Predict the Sign Type for Each Image**

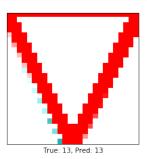
```
In [23]: ### Run the predictions here and use the model to output the predictio
n for each image.
### Make sure to pre-process the images with the same pre-processing p
ipeline used earlier.
### Feel free to use as many code cells as needed.
with tf.Session() as sess:
    saver.restore(sess, tf.train.latest_checkpoint('.'))
    predictions = sess.run(tf.argmax(logits,1), feed_dict={x: X_test_n
ew, keep_prob:1})
print("Class predictions={}".format(predictions))
```

Class predictions=[ 3 9 35 13 14]











### **Analyze Performance**

```
In [25]: ### Calculate the accuracy for these 5 new images.
    ### For example, if the model predicted 1 out of 5 signs correctly, it
    's 20% accurate on these new images.
    with tf.Session() as sess:
        saver.restore(sess, tf.train.latest_checkpoint('.'))

    test_new_accuracy = evaluate(X_test_new, y_test_new)
    print("Test Accuracy on the new images = {:.3f}".format(test_new_accuracy))
```

Test Accuracy on the new images = 1.000

### Output Top 5 Softmax Probabilities For Each Image Found on the Web

```
In [26]: ### Print out the top five softmax probabilities for the predictions o
         n the German traffic sign images found on the web.
         ### Feel free to use as many code cells as needed.
         with tf.Session() as sess:
             saver.restore(sess, tf.train.latest checkpoint('.'))
             probabilities = sess.run(tf.nn.softmax(logits), feed dict={x: X te
         st new, keep prob:1})
             top k vals = sess.run(tf.nn.top k(tf.constant(probabilities), k=5)
         top k vals
Out[26]: TopKV2(values=array([[ 9.98250186e-01,
                                                  1.17269345e-03,
                                                                     5.249806
         56e-04,
                                     1.97974214e-06],
                   4.50356129e-05,
                 9.99998808e-01,
                                     1.17700267e-06,
                                                       1.26837456e-08,
                  7.27348581e-09,
                                     1.36813416e-09],
                7.11053848e-01,
                                     1.26245901e-01,
                                                      1.11906268e-01,
                   3.01445890e-02,
                                    1.38063980e-021,
                [ 1.0000000e+00,
                                     5.69038506e-21,
                                                      2.80684414e-26,
                   4.01137850e-27,
                                     5.21360380e-31],
                [ 9.99998093e-01,
                                     1.00458021e-06,
                                                      3.57222575e-07,
                   2.46024541e-07,
                                     2.01043505e-07]], dtype=float32), indice
         s=array([[ 3, 5, 2, 16, 32],
                [ 9, 10, 13, 16, 41],
                [35, 34, 36, 28, 25],
                [13, 14, 10, 9, 1],
                [14, 17, 2, 13, 1]], dtype=int32))
```