

ENGR101 TUTORIAL 8

CORE 1

$$f(x) = \frac{1}{\sqrt{2\pi}} e^{-\frac{(x)^2}{2}}$$
$$= 0.05399096651$$
$$= 0.05$$

CORE 2

Because there is no possible way the probability can add to 1 when you are adding the probability of an infinite set of finite numbers.

CORE 3

Since the probability of getting the +ve value and the -ve value is the same, over time the probability will therefore become zero. The amplitude of the noise is at approx 0.14, the red graph.

COMPLETION 1

If you keep averaging over time the noise will average to zero and the signal would average to about the signal.

COMPLETION 2

TRIALS	Avg mag of noise
1	0.8
10	0.25
100	0.082
1000	0.026
10,000	0.0079
100,000	0.0026

If you average n samples of the noise, the magnitude decreases by \sqrt{n} .
The \pm for a mag decreases by \sqrt{n} for n measurements.

COMPLETION 3

- Specification—How accurately do you need to measure the voltage?
 - How long can you afford to take to average the data?
 - Can't take so long that the signal changes significantly during measurement.
- Specs suggest a sample rate, but what is your budget?
- Can you change the measurement or hardware to reduce noise before averaging.

FOR AVC:

- Avoid wiggling camera
- Better light conditions
- Bigger camera.
- Tradeoff between image res and frame rate.

CHALLENGE

$$\begin{aligned}\overline{|x|} &= \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} |x| e^{-\frac{x^2}{2}} dx \\ u &= x^2 \\ du &= 2x dx \\ &= \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} e^{-\frac{x^2}{2}} \underbrace{x dx}_{\frac{du}{2}} \\ &= \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} e^{-\frac{u}{2}} \frac{du}{2} \\ &= \frac{1}{2\sqrt{2\pi}} \left[e^{-\frac{u}{2}} \right]_{-\infty}^{\infty} \\ &= \left[\frac{1}{\sqrt{2\pi}} \frac{e^{-\frac{u}{2}}}{-\frac{1}{2}} \right]_{-\infty}^{\infty}\end{aligned}$$