

## **Tensor Transposition**

- Transpose of scalar is itself, e.g.:  $x^{T} = x$
- Transpose of vector, seen earlier, converts column to row (and vice versa)
- Scalar and vector transposition are special cases of **matrix transposition**:
  - Flip of axes over main diagonal such that:

$$\left(\boldsymbol{X}^{\mathrm{T}}\right)_{i,j} = \boldsymbol{X}_{j,i}$$

Hands-on code demo
$$\begin{bmatrix}
\chi_{1,1} & \chi_{1,2} \\
\chi_{2,1} & \chi_{2,2} \\
\chi_{3,1} & \chi_{3,2}
\end{bmatrix} = \begin{bmatrix}
\chi_{1,1} & \chi_{2,1} & \chi_{3,1} \\
\chi_{1,2} & \chi_{2,2} & \chi_{3,2}
\end{bmatrix}$$

#### ML Foundations Series

#### Intro to Linear Algebra is foundational for:

- 1. Intro to Linear Algebra
- 2. Linear Algebra II: Matrix Operations
- 3. Calculus I: Limits & Derivatives
- 4. Calculus II: Partial Derivatives & Integrals
- 5. Probability & Information Theory
- 6. Intro to Statistics
- 7. Algorithms & Data Structures
- 8. Optimization

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## Exercises

1. What is the transpose of this vector?

2. Using algebraic notation, what are the dimensions of this matrix *Y*?

$$y = \begin{bmatrix} 42 & 4 & 7 & 99 \\ -99 & -3 & 17 & 22 \end{bmatrix}$$

3. Using algebraic notation, what is the position of the element in this matrix *Y* with the value of 17?

# Segment 1: Data Structures for Algebra

- What Linear Algebra Is
- A Brief History of Algebra
- Tensors
- Scalars
- Vectors and Vector Transposition
- Norms and Unit Vectors
- Basis, Orthogonal, and Orthonormal Vectors
- Arrays in NumPy
- Matrices
- Tensors in TensorFlow and PyTorch