

Ridge Regression part-4

5 key understanding under Ridge.

As we know that, in Ridge

$$L = \sum_{i=1}^n (y_i - \hat{y}_i)^2 + \lambda \|w\|^2$$

regularization term
or
shrinkage Co-eff

$$= \lambda (w_1^2 + w_2^2 + \dots + w_n^2)$$

↳ all features
get same shrinkage
Co-eff.

Q1. How the Co-eff gets affected?

As $\lambda \uparrow \rightarrow$ Co-eff \downarrow towards zero but never become zero.

Q2. Higher values are impacted more?

Let's say for example

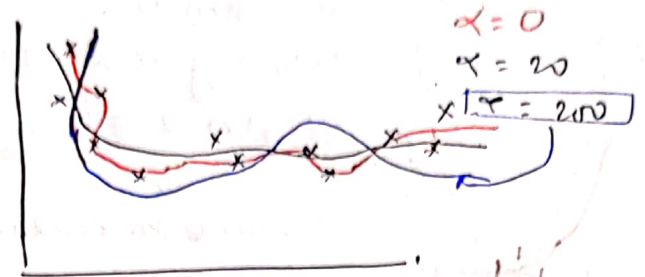
x_1	x_2	x_3	y
\downarrow	\downarrow	\downarrow	
w_0	w_2	w_3	
$= 1000$	$= 10$	$= 1$	

→ here are Co-eff of features we got after applying reg

As the time $\lambda = 1 \rightarrow \infty$ increasing its value 1 to ∞ , How w_0, w_2, w_3 will get affected?

On increasing λ -value, the Co-eff which is as bigger will decrease (or penalize) as fast ^{comparision.} ~~to~~ to smaller Co-eff.

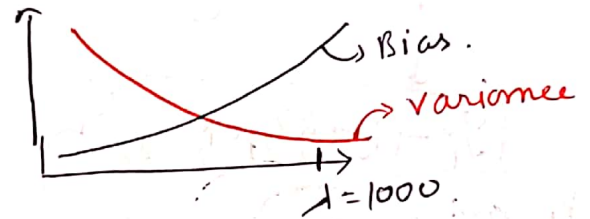
Q3. Bias Variance Tradeoff



for $\alpha = 0 \rightarrow$ regg. line tries to touch each data point \rightarrow ~~high~~ Low bias

$\alpha = 20 \rightarrow$ regg. line becoming smooth \rightarrow ~~high~~ Low bias
 \rightarrow ~~high~~ Low variance.

• $\alpha \uparrow \Rightarrow$ bias \uparrow variance \downarrow



Q4. Effect of regularization on loss function.

As we know that

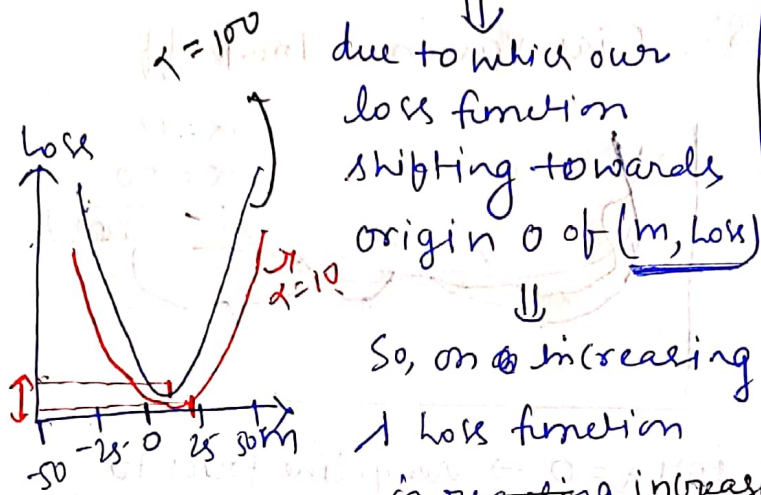
$$L = \sum_{i=1}^n (y_i - \hat{y}_i)^2 + \lambda \|w\|^2$$

Let's assume b is constant only m is varying due to regularization. Then eqⁿ of Loss would be

$$L = \sum_{i=1}^n (y_i - mx_i)^2 + \lambda m^2$$



$\lambda \uparrow \rightarrow \text{Co-eff} \downarrow \rightarrow \text{tends } 0$



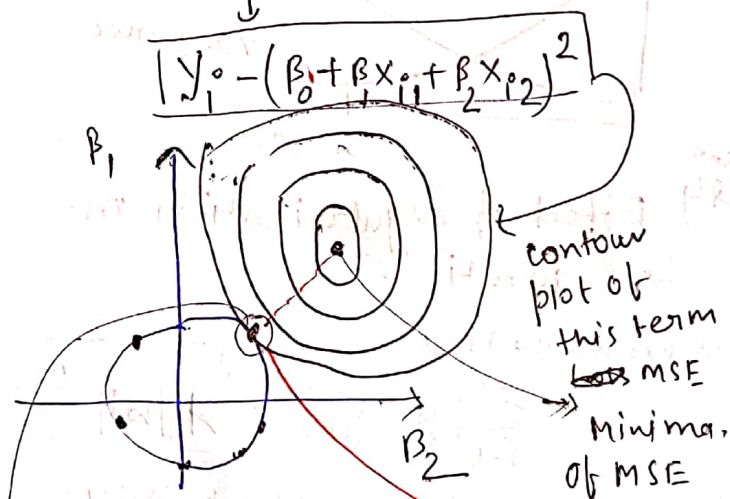
due to which our loss function shifting towards origin 0 of (m, Loss)

So, on increasing λ loss function is ~~increasing~~ increasing but m is decreasing.

* why Ridge is called Ridge.

As we know that in Ridge

$$\text{Loss} = \text{MSE} + \lambda \|W\|^2$$



$$\lambda (B_1^2 + B_2^2)$$

this is point from where MSE minima is nearest to point bound on periphery of Extra term $\lambda (B_1^2 + B_2^2)$

So, always ~~common~~ common point (β_1, β_2) lie on periphery (Ridge)

\therefore its called as Ridge estimation.

that's why

~~this is~~ called as ridge estimation