

# Find Smallest Letter Greater than target

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11:20 PM

## 1. The Goal

We need to find the smallest character in a sorted list that is strictly larger than the target.

- Input: Sorted list ['c', 'f', 'j'], Target 'a'
- Constraints: If no letter is larger than the target, return the very first letter.

## 2. The Approach: Modified Binary Search

Since the i/p letters is sorted, we should immediately think of Binary Search ( $O(\log n)$ ) instead of scanning every element ( $O(n)$ ).

### The "Wrap Around" Trick.

Before we even start searching, we handle the edge case:

- Problem: What if target is 'z' and our list only goes upto 'j'?
- Solution: We initialize our result variable to letters[0].
  - If we find a valid answer during the search, we update result.
  - If the search finishes and we found nothing bigger, result remains letters[0], automatically solving the wrap-around requirement.

## 3. The Logic

We are looking for the upper Bound (first value  $>$  Target)

The Decision at mid: When we look at letters[mid], we have two possibilities:

CASE A: letters[mid]  $>$  target (Potential Ans)

- Observation: This letter is valid! It is bigger than the target
- Action 1: Store it in result (it might be the best answer we find).
- Action 2: Move left (end = mid - 1)
- Why Left? We want the smaller greater letter. Even though mid is valid, there might be an even smaller valid letter to its left.

CASE B: letters[mid]  $\leq$  target (Not Valid)

- Observation: This letter is either too small or exactly equal to the target. We need strictly greater.
- Action: move Right (start = mid + 1)
- Why Right? All numbers to the left are even smaller. We must look to the right for bigger numbers.

## 4. Dry Run Example

List: ['c', 'f', 'j'] | Target: 'a'

- Default result 'c'

Iteration 1:

- mid point to 'f'
- Is 'f'  $>$  'a'? Yes
- Update: result = 'f'
- move: end moves left

Iteration 2:

- mid point to 'c'
- Is 'c'  $>$  'a'? Yes
- Update: result = 'c'
- move: end moves left (past start)

Loop Ends: Return 'c'

TIME COMPLEXITY:  $O(\log n)$  - very efficient

SPACE COMPLEXITY:  $O(1)$  - No extra lists used