

1. The Goal

Find the contiguous subarray within a list of numbers that produces the largest sum.

2. The Core Intuition

- "Don't carry dead weight."
- If a subarray sum becomes negative, it is useless for the future. Why? Because adding a negative number to the next number will always result in a smaller total than just starting fresh.
- The Rule: If your current running sum drops below 0, reset it to 0 immediately.

3. The Logic Flow (Pseudocode)

We iterate through the array once. At every number, we do three things:

1. ADD: Add the current number to "current-sum".
2. CHECK RECORD: Is "current-sum" > "max-sum"? If yes, update "max-sum".
3. RESET: Is "current-sum" < 0? If yes, reset "current-sum" to 0.

4. Visual Trace

Input: [-2, 1, -3, 4, -1, 2, 1, -5, 4]

<u>Step</u>	<u>Number</u>	<u>Current-Sum</u>	<u>max-sum</u>	<u>Notes</u>
0		0	0	Start
1	-2	-2 → 0	0	Neg? Reset to 0
2	1	1	1	New Record!
3	-3	-2 → 0	1	Neg? Reset to 0
4	4	4	4	New Record!
5	-1	3	4	Decreased, but still +
6	2	5	5	New Record!
7	1	6	6	Max found
8	-5	1	6	dropped, but > 0
9	4	5	6	End.

5. Complexity Cheat sheet

- Time Complexity: $O(n)$
 - Why? We visit every number exactly once (linear time)
- Space Complexity: $O(1)$
 - Why? We only use two variables (max-sum and current-sum). We do not create a new array.