Lecture 3 : Exploratory Data Analysis

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Motivation

Understand the market conditions for hotels in Vienna, using prices.

- ► How should you start the analysis itself?
- How to describe the data and present the key features?
- ► How to explore the data and check whether it is clean enough for (further) analysis?

Exploratory data analysis (EDA) - describing variables

5 reason to do EDA!

- 1. To check data cleaning (part of iterative process)
- 2. To guide subsequent analysis (for further analysis)
- 3. To give context of the results of subsequent analysis (for interpretation)
- 4. To ask additional questions (for specifying the (research) question)
- 5. Offer simple, but possibly important answers to questions.

Key tasks: describe variables

Look at key variables

- what values they can take and
- how often they take each of those values.
- are there extreme values

Describe what you see

Descriptive statistics - key features
 summarized



- ► to understand variables you work with
- ► to make comparisons

Frequency of values

- ► The *frequency* or more precisely, *absolute frequency* or *count*, of a value of a variable is simply the number of observations with that particular value.
- ► The *relative frequency* is the frequency expressed in relative, or percentage, terms: the *proportion* of observations with that particular value among all observations.
- Practical Note on Missing Values: When calculating proportions, decide whether to include all observations or just those with non-missing values. The latter is commonly preferred.

The distribution and the histogram

A key part of EDA is to look at the (empirical) distribution of the most important variables.

- ► All variables have a distribution.
- ► The distribution of a variable gives the frequency of each value of the variable in the data.
- ▶ May be expressed in terms of absolute frequencies (number of observations) or relative frequencies (percent of observations).
- ► The distribution of a variable completely describes the variable as it occurs in the data.
- ► Each variable's distribution is analyzed *independently*, not influenced by other variables' distributions.

Histograms

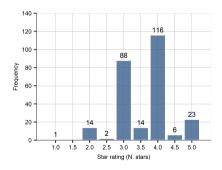
Histogram reveals important properties of a distribution.

- Number and location of *modes*: these are the peaks in the distribution that stand out from their immediate neighborhood.
- Approximate regions for center and tails
- ► Symmetric or not asymmetric distributions have a long left tail or a long right tail
- Extreme values: values that are very different from the rest. Extreme values are at the far end of the tails of histograms.

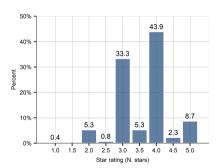
Extreme values

- ▶ Some variables have extreme values: substantially larger or smaller values for one or a handful of observations than the values for the rest of the observations.
- Need conscious decision.
 - ► Is this an error? (drop or replace)
 - ▶ Is this not an error but not part of what we want to talk about? (drop)
 - ▶ Is this an integral feature of the data? (keep)

(a) Absolute frequency (count)

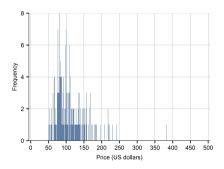


(b) Relative frequency (percent)

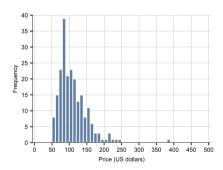


Source: hotels-vienna dataset. Vienna, Hotels only, for a 2017 November weekday

(a) Histogram: individual values

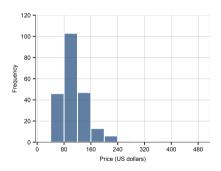


(b) Histogram: 20\$ bins

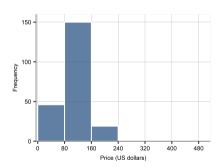


Note: Panel (a) just shows individual values - help see where most values are. Panel (b) is a histogram with 20\$ bins - more useful to capture frequencies. Source: hotels-vienna dataset. Vienna, 3-4 stars hotels only, for a 2017 November weekday

(a) Histogram: 40\$ bins



(b) Histogram: 80\$ bins

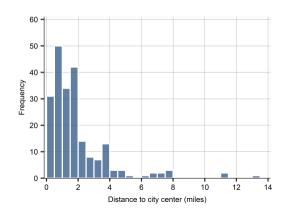


Note: Bin size matters. Wider bins suggest a more gradual decline in frequency.

Hotel density plot

- ▶ Vienna all hotels, 3-4 stars
- Use absolute frequency (count)
- ► For this histogram we use 0.5-mile-wide bins. This way we can see the extreme values in more detail
- Dropped very far likely not Vienna

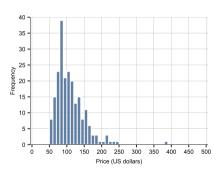
Figure: Histogram of distance to the city center.



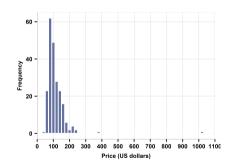
Hotel prices

- ▶ Vienna all hotels. 3-4 stars
- Use absolute frequency (count)
- ► We go back to prices
- ▶ How to decide what to include? -> check observation!

(a) Histogram: 20\$ bins as seen



(b) Histogram: including extreme value above 1000\$



Source: hotels-vienna dataset. Vienna, 3-4 stars hotels only, for a 2017 November weekday

Summary statistics

- For any given variable, a *statistic* is a meaningful number that we can compute from a dataset.
- Basic summary statistics describe the most important features of distributions of variables.
- ► Many of you know this. I briefly cover it

Summary statistics: Sample mean

The most used statistic is the *mean*:

$$\bar{x} = \frac{\sum x_i}{p} \tag{1}$$

where x_i is the value of variable x for observation i in the dataset that has n observations in total. Two key features

$$\overline{x+a} = \overline{x} + a \tag{2}$$

$$\overline{x \cdot b} = \overline{x} \cdot b \tag{3}$$

The Expected value

- ► The expected value is the value that one can expect for a randomly chosen observation
- ▶ The notation for the expected value is E[x].
- For a quantitative variable, the expected value is the mean
- For a qualitative variable, it can only be determined if transformed to a number

Summary statistics: The median and other quantiles

- ▶ Quantiles: a quantile is a value that divides the observations in a dataset into two or more groups in specific proportions.
- ► The *median* is the middle value of the distribution half the observations have lower value and the other half have higher value.
- ► Percentiles are values that divide a dataset into 100 equal parts, each representing a percentage of data points that fall below it
- Quartiles are a type of quantiles which divide the number of data points into four parts, or quarters, of more-or-less equal size.

Summary statistics: The mode

- ▶ The *mode* is the value with the highest frequency in the data.
- ▶ Some distributions are unimodal, others have multiple modes.
- ► Multiple modes can be observed, each distinct within its own 'neighborhood' of values, yet they may exhibit differing frequencies

Summary statistics: central tendency

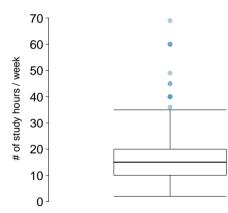
- ► The mean, median and mode are different statistics for the *central value* of the distribution
- ► Central tendency.
 - ► The mode is the most frequent value
 - ► The median is the middle value
 - ▶ The mean is the value that one can expect for a randomly chosen observation.

Summary Statistics: Spread of Distributions

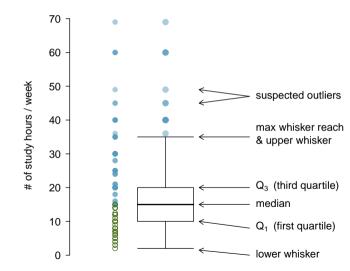
- ▶ Analyzing the *spread of distributions* is crucial for understanding data variability.
- ▶ Key statistics for measuring distribution spread include:
 - ▶ Range: The difference between the maximum and minimum values in a dataset.
 - ► Inter-Quartile Range (IQR): The difference between the third quartile (75th percentile) and the first quartile (25th percentile), showing the spread of the middle 50% of the data.
 - ▶ 90-10 Percentile Range: The difference between the 90th and 10th percentiles, highlighting the spread of the central 80% of the data.
 - ► Standard Deviation and Variance: Measures that quantify the dispersion of data points around the mean.
- ► These statistics provide insights into the distribution's overall variability and identify potential outliers.

Box Plot

The box in a box plot represents the middle 50% of the data, and the thick line in the box is the median.



Anatomy of a box plot



Whiskers and Outliers

- \blacktriangleright Whiskers of a box plot can extend up to $1.5 \times IQR$ away from the quartiles.
- ▶ The maximum upper whisker reach is calculated as $Q3 + 1.5 \times IQR$, and the maximum lower whisker reach is $Q1 1.5 \times IQR$.
- ▶ For example, if the IQR (Interquartile Range) is 20 10 = 10, then:
 - ▶ The maximum upper whisker reach would be $20 + 1.5 \times 10 = 35$.
 - ▶ The maximum lower whisker reach would be $10 1.5 \times 10 = -5$.
- ▶ A potential *outlier* is defined as an observation beyond the maximum reach of the whiskers. It is an observation that appears extreme relative to the rest of the data.

Summary statistics: standard deviation

- ► The most widely used measure of spread is the *standard deviation*. Its square is the *variance*.
- ▶ Variance is the average squared difference of each observed value from the mean.
- ► The standard deviation captures the typical difference between a randomly chosen observation and the mean.
- ► The variance is a less intuitive measure. At the same time, the variance is easier to work with, because it is a mean value itself.

$$Var[x] = \frac{\sum (x_i - \overline{x})^2}{n} \tag{4}$$

$$Std[x] = \sqrt{\frac{\sum (x_i - \overline{x})^2}{n}}$$
 (5)

Summary statistics: skewness

- ► A distribution is *skewed* if it isn't symmetric.
- ▶ It may be skewed in two ways, having a long left tail or having a long right tail.
- Example: hotel price distributions having a long right tail such as in hotel price distribution.
- ▶ Skewness and the prevalence of extreme values are related. With distributions with long tails, values far away from all other values are more likely.
- When extreme values are important for the analysis, skewness of distributions is important, too.

Summary statistics: skewness measure

Simplest measure is *mean-median measure of skewness*.

$$Skewness = \frac{(\overline{x} - median(x))}{Std[x]}$$
 (6)

- ▶ When the distribution is symmetric its mean and median are the same.
- ▶ When it is skewed with a long right tail the mean is larger than the median: the few very large values in the right tail tilt the mean further to the right.
- ▶ When a distribution is skewed with a long left tail the mean is smaller than the median
- ► To make this measure comparable across various distributions use a standardized measure
- ▶ If multiplied by 3, and then it's called *Pearson's second measure of skewness*.

Vienna vs London

- ► Compare two cities, how hotel markets vary
- ► Vienna, London
- ▶ 3-4 star hotels, only "Hotels" (no apartments), below 1000 dollars.
- ► Focus on actual city=Vienna and actual city=London (exclude nearby related villages).
- ▶ Use hotels-europe dataset.
- ▶ N=207 for Vienna, N=435 for London

London vs Vienna

Figure: Vienna Austria

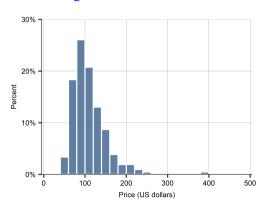
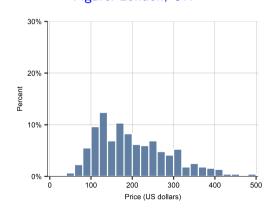


Figure: London, UK

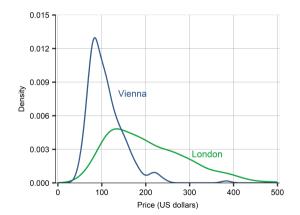


Density plots

- ▶ Density plots also called kernel density estimates
- ▶ Alternative to histograms instead of bars density plots show continuous curves.
- ▶ We may think of them as curves that wrap around the corresponding histograms.
- ▶ Density plots complementing histograms some believe density plots allow for easier comparison of distributions across groups in the data.

The density plot

- Density plot
- Less reliable than histogram
- ► But easy to read the key points
- ► Easy for comparison



Case study hotels: descriptive statistics

Table: Descriptive statistics for hotel prices in two cities.

| City | N | Mean | Median | Min | Max | Std | Skew |
|--------|-----|--------|--------|-----|-----|-------|-------|
| London | 435 | 202.36 | 186 | 49 | 491 | 88.13 | 0.186 |
| Vienna | 207 | 109.98 | 100 | 50 | 383 | 42.22 | 0.236 |

Source: hotels-europe dataset. Vienna and London, weekday, November 2017

Theoretical distributions

Theoretical distributions are distributions of variables with idealized properties.

- ▶ Show frequencies for theoretical distributions and not for empirical ones.
- ► The likelihood of each value in a more abstract setting hypothetical "dataset" or "population," or the abstract space of the possible realizations of events.
- ► Theoretical distributions are fully captured by few *parameters*: these are statistics determine the whole distributions

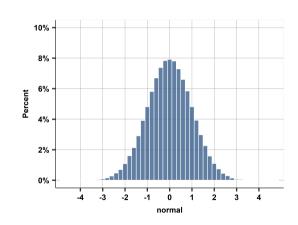
Theoretical Distributions

Theoretical distributions provide valuable insights into data analysis due to their well-defined properties.

- ► Well-Known Properties: Theoretical distributions have specific, well-understood characteristics.
- ► Approximation of Real Data: When a variable in our dataset closely matches a theoretical distribution, we can infer the distribution's properties for our variable. This helps in understanding the behaviour and underlying patterns of the data.
- ► Common in Real Life: Many real-life variables align closely with theoretical distributions, often more than initially expected.
- ▶ Utility in Generalization: Recognizing these patterns is crucial for making broader inferences from our data, as will be discussed in more detail in Chapter 5/Lecture 6 (to be confirmed).

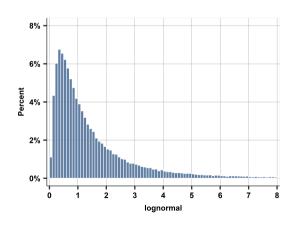
The Normal distribution

- ► Histogram is bell-shaped
- Outcome (event), can take any value
- Distribution is captured by two parameters
 - $\blacktriangleright \mu$ is the mean
 - $\triangleright \sigma$ the standard deviation
- ➤ Symmetric = median, mean (and mode) are the same.
- Example: height of people, IQs, ect.



The log-normal distribution

- Asymmetrically distributed with long right tails.
- start from a normally distributed RV (x), transform it: (e^x) and the resulting variable is distributed log-normal.
- ► Always non-negative
- Example distributions of income, or firm size.



Insights on Normal and Log-Normal Distributions

- ▶ Prevalence of Normal Distribution: A significant number of variables in real life approximate a normal distribution, especially those that result from the sum of many elementary factors.
- Limitations of Normal Distribution: However, the normal distribution might not be a good fit in situations where:
 - There is asymmetry in the data.
 - Extreme values play a crucial role and cannot be ignored.
- ▶ Log-Normal Distribution: Variables resulting from multiplicative processes often fit a log-normal distribution, as the log transformation turns multiplication into addition, aligning more with a normal distribution.

Income and log-income

Figure: income

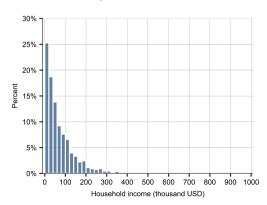
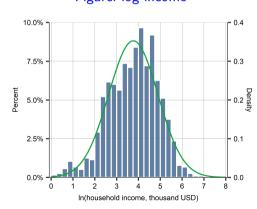
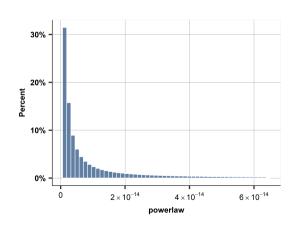


Figure: log income



The power law distribution

- ► Also called as Pareto distribution
- Very large extreme values well approximated
- Relative frequency of close-by values are the same along large and small values
- ► Real world: many examples, but often not the whole distribution
- ► Example: frequency of words, city population, wealth



Data visualization

- ▶ We shall make conscious decisions and not let default settings guide us.
- ► We break our preferences into four layers:
 - usage what you want to show and to whom deciding on purpose, focus, and audience
 - 2. encoding key elements of the graphs showing how you want to present the message
 - 3. scaffolding how you want to present elements that support understanding such as axis and legends
 - 4. annotation adding anything else you want to emphasize

This is a very brief overview, more in Chapter 03 of Gabor Data Analysis Book

Data visualization: usage

- ▶ What message do you want to convey and to whom?
- As a general principle, one graph should convey one message.
- ▶ Be explicit about the purpose of the graph and the target audience: general audience vs specialist
- For a specialist audience, more complicated graphs are okay.

Data visualization: encoding

- ► How to show what you want to show.
- ▶ Picking the type of graph, additional features to it, and colors.
- ► Type of graph: bar chart, scatterplot, etc.
- How to denote information (dots, lines, bars)
- ► Have an additional encoding to help comparison: bar chart for separate groups encoded with colors.
- ▶ One information, one encoding use size or color but not both.

Data visualization: scaffolding

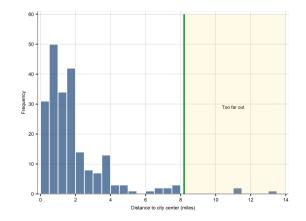
- ▶ How to present elements that support understanding.
- ► Make sure that a graph has
 - ► Title
 - Axis title and labels
 - Legend
- ► Content as well as format, such as font type and size.

Data visualization: annotations

- ▶ If there is something else we want to emphasize?
 - Additional information can help put the graph into context or emphasize some part of it
- ► Colored area, circled observations, arrow+text, etc

Data visualization: example

- Usage: to show distribution for general audience
- ► Encoding is bars (histogram), bin size set at 20
- ► Axes labelled with title + grid
- ► annotation: far away hotels



Summary

- ► Always check your key variables
- ► Look at summary statistics, understand key features such as central tendency, spread and skewness
- ► Look at histograms to get a broader picture of the distribution, see if multiple modes or extreme values.
- ► EDA helps describe the data, and plan the analysis
- ▶ Data vizualization matters, makes sense to do it carefully.